

『理論屋さん, 正直なところどうなんですか? その2』

Precision measurement で探る新物理

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updated:
Moriond 2021,
FNAL muon g-2

高エネルギー将来計画委員会: 第9回 勉強会
2021年4月22日, オンライン



本日のテーマ：

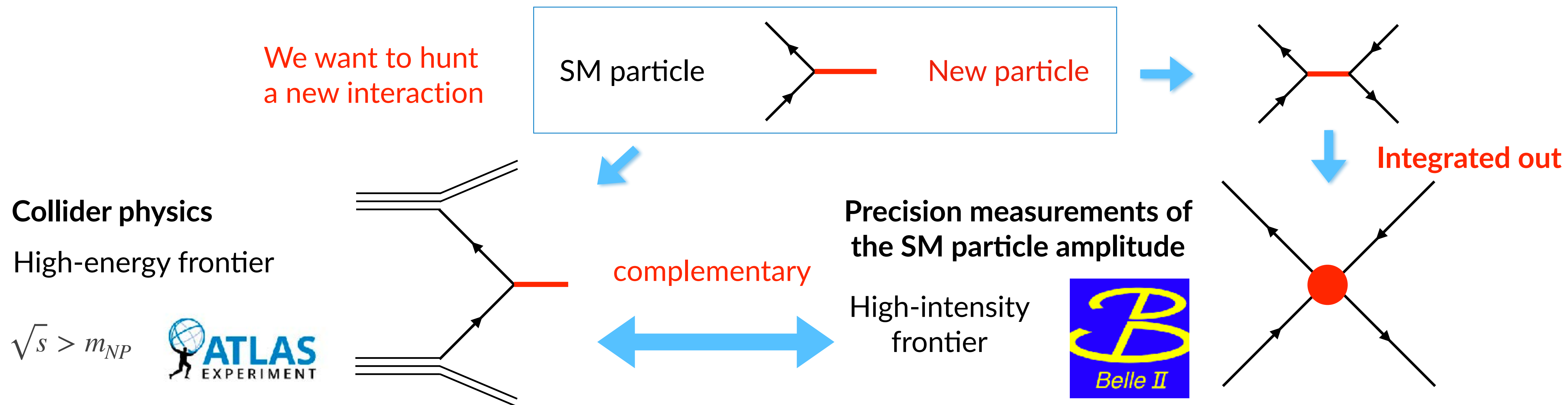
1, メジャーなアノマリーの紹介

2, 示唆される新物理の紹介

updated:
Moriond 2021,
FNAL muon g-2

Introduction (1/3)

- ◆ The Standard Model (SM) is known to be an incomplete model that can not explain matter–antimatter asymmetry, dark matter, gauge hierarchy, quark mass hierarchy, neutrino mass, etc.
- ◆ Beyond the standard model (New Physics/NP) is, therefore, **required**

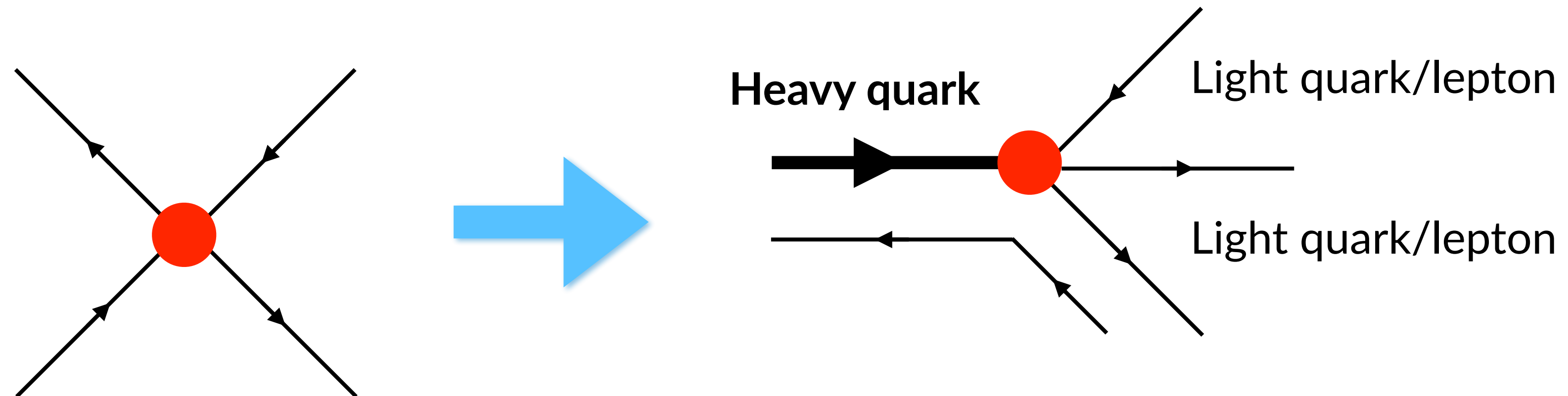


3-point amplitudes



Precision measurements of leptons

4-point amplitudes

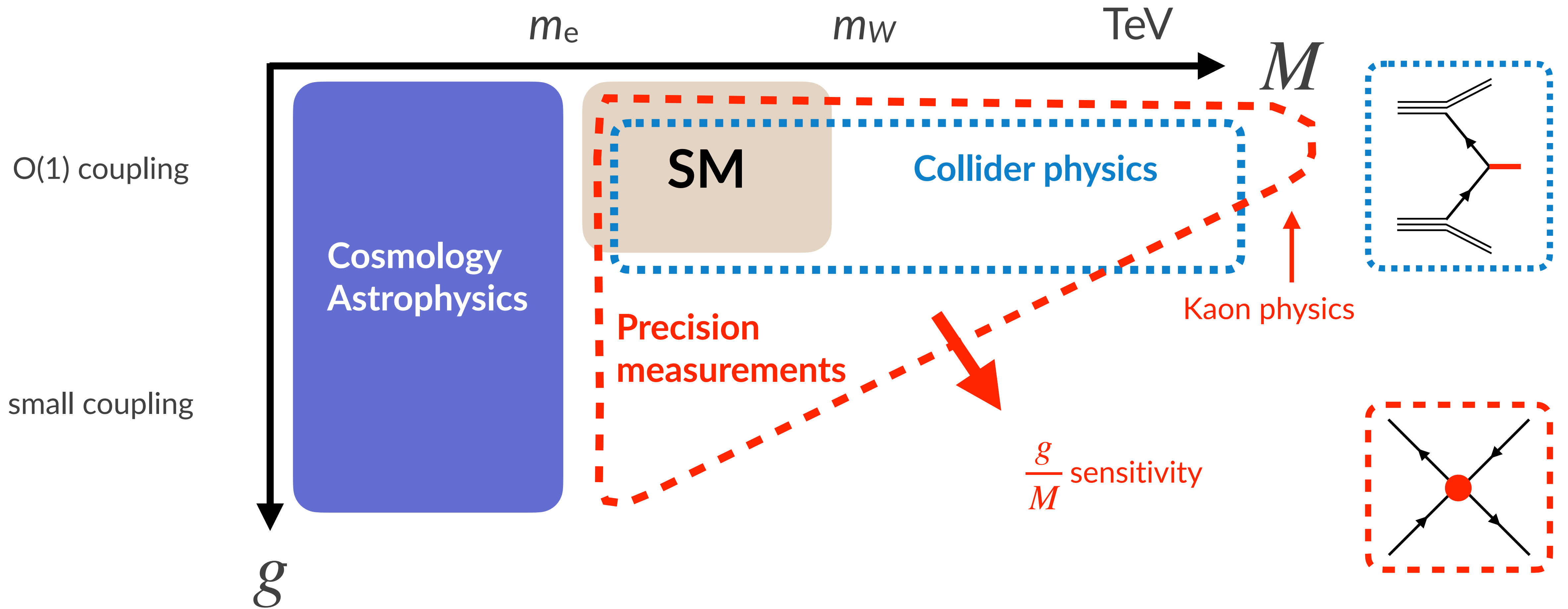


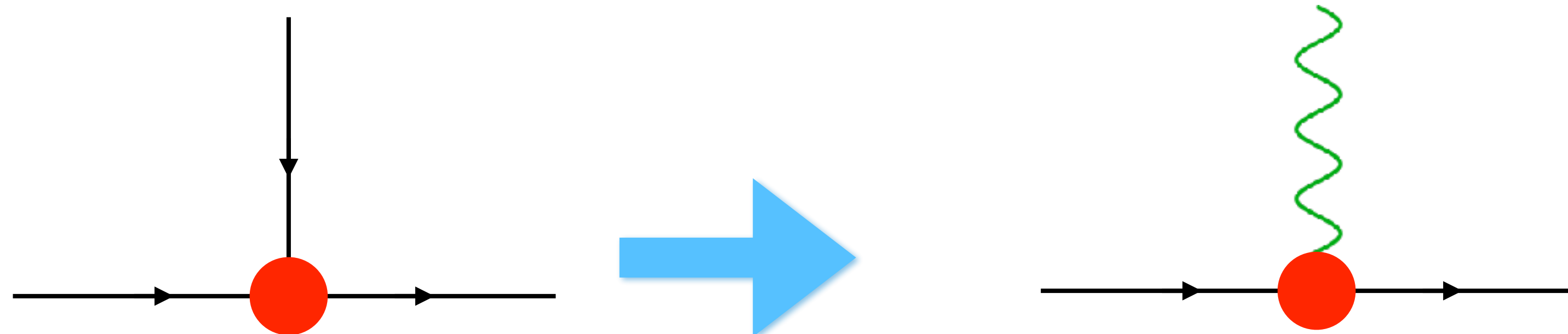
Precision measurements of flavor physics

Advantages:

Precise SM prediction (thanks to small QCD uncertainty, lattice QCD simulation, NN...LO calculations) provides great sensitivity to new physics

Introduction (3/3)





Precision measurements of leptons

Muon g-2

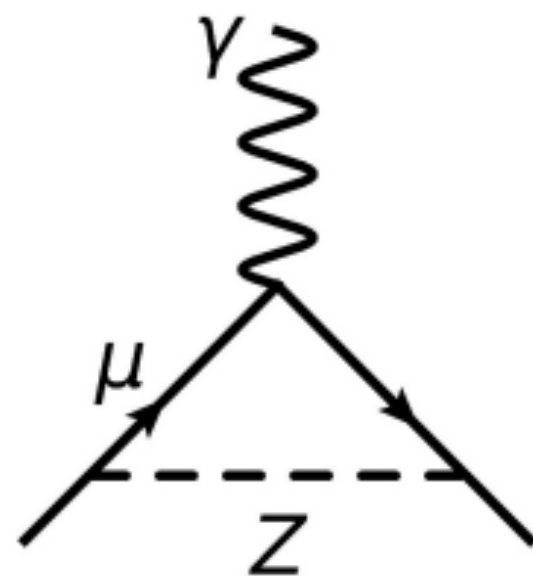
詳細は高エネ将来計画委員会: 第10回 勉強会
 ミューオンで超える標準模型の壁 (三部さん)

Theory



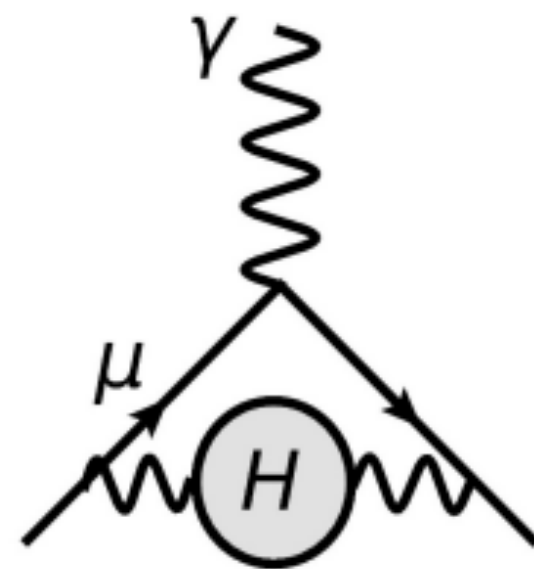
QED

Analytic



EW

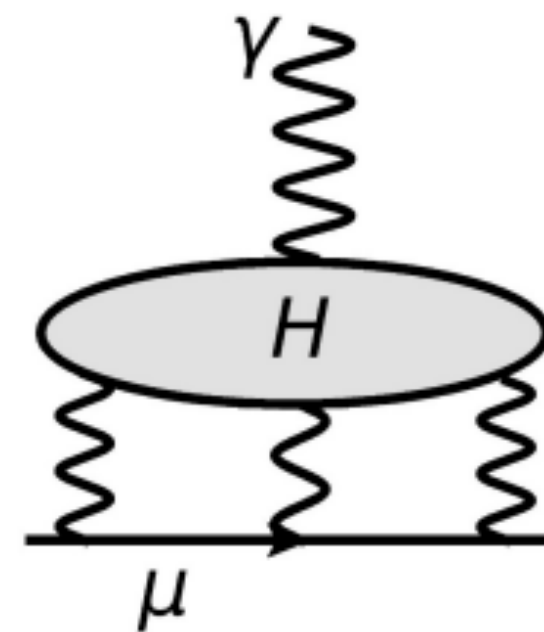
Analytic



Hadronic vacuum
polarization (HVP)

Phenomenological

Lattice



Hadronic light-
by-light (HLbL)

Pheno.

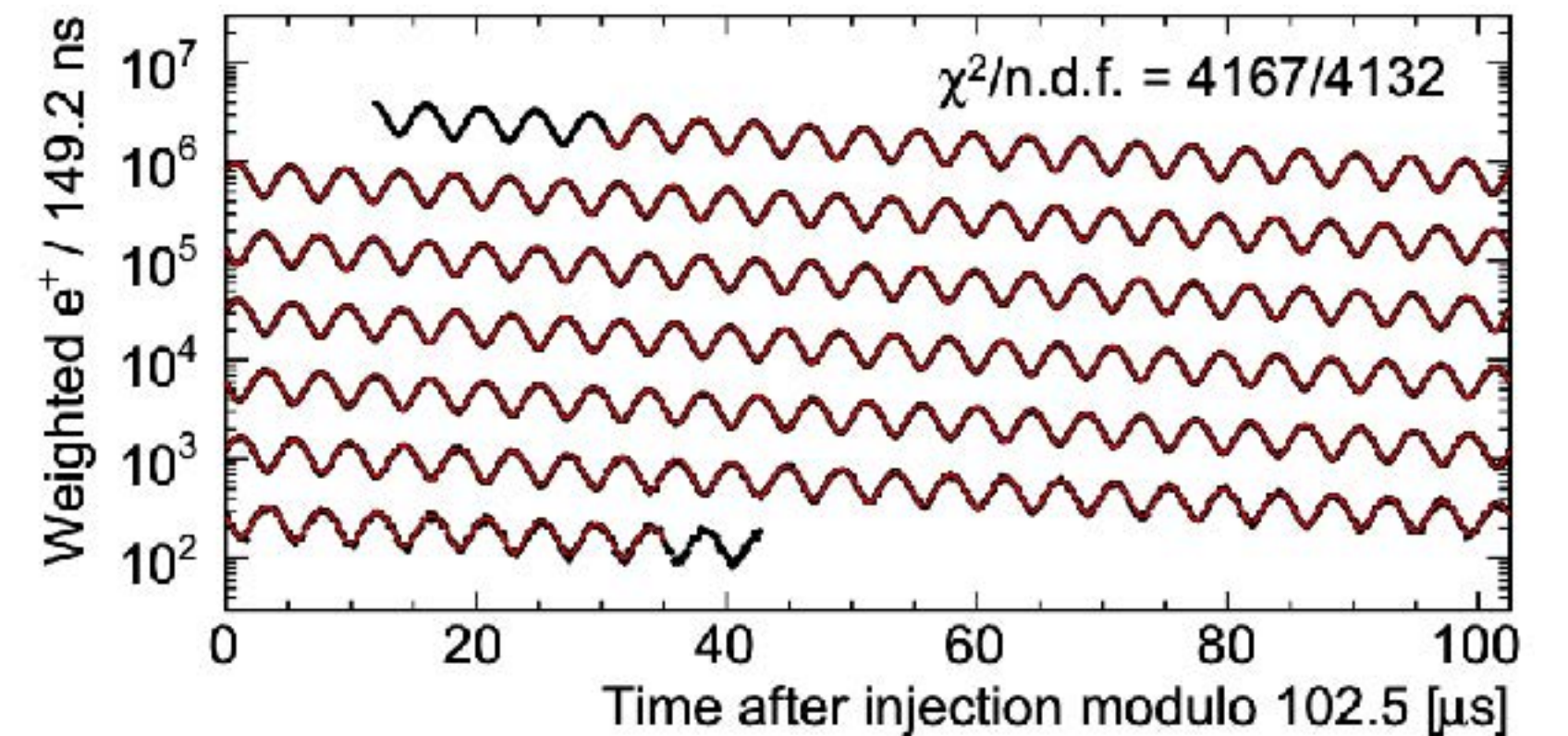
Lattice

Exp.

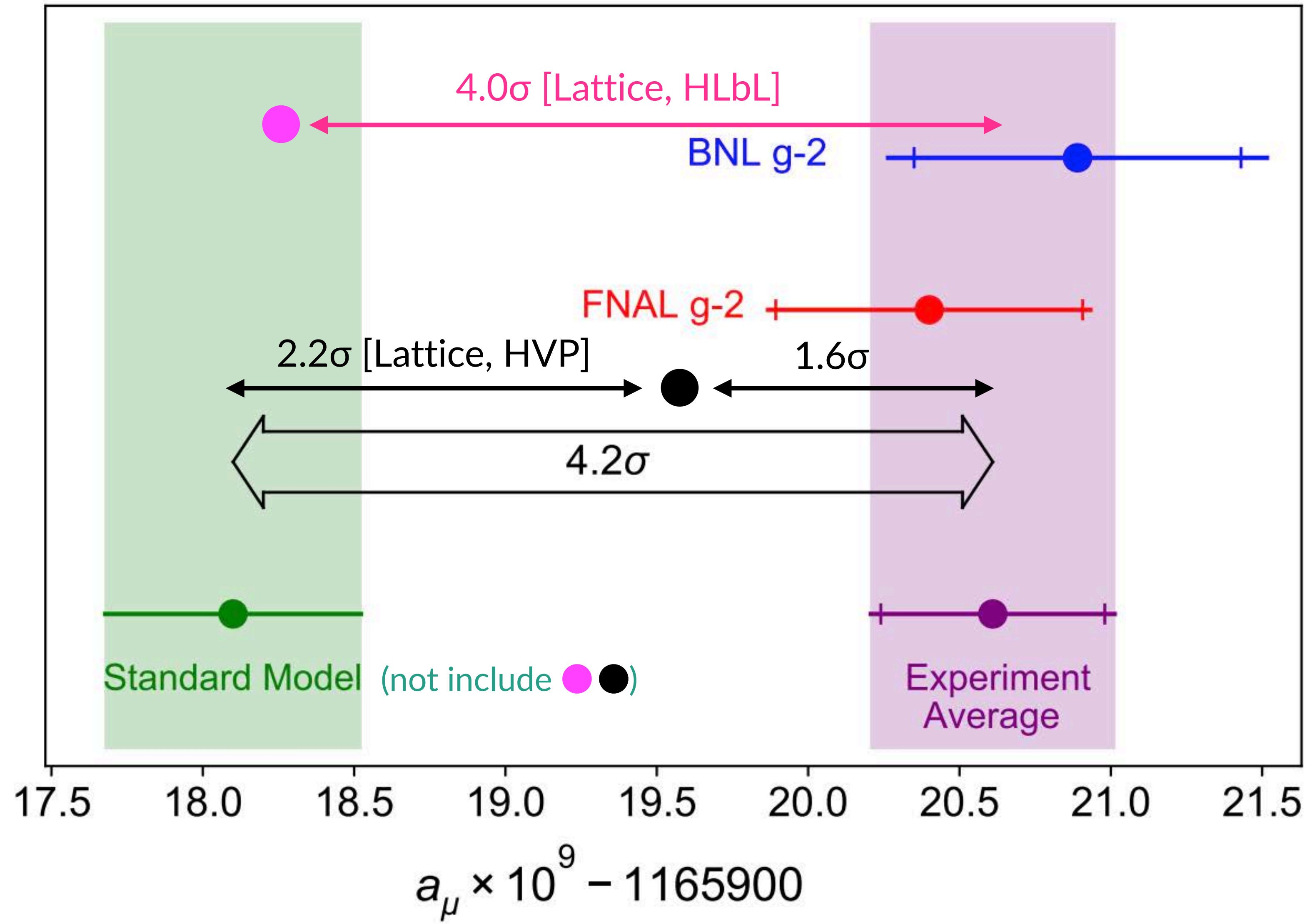
BNL '97-'01

FNAL ongoing

J-PARC
near future



Based on [FNAL Muon g-2, PRL2021]



comments

Stat error dominated

Almost no correlation between BNL and FNAL syst errors

The latest lattice result for HLbL slightly reduces tension [Mainz group, 2104.02632]




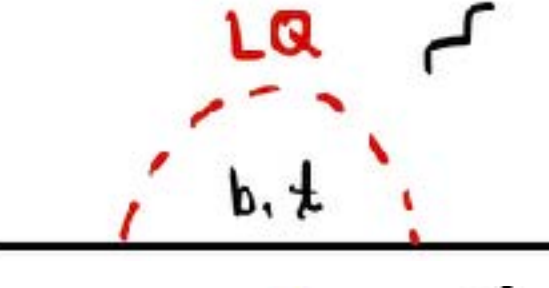


The latest lattice result for HVP significantly reduces tension [BMW, Nature '21]

Several analyses show that EW fit could be no problem, but there is additional tension in $e^+e^- \rightarrow 2\pi$ data, see e.g., [Colangelo et al, 2010.07943]

MUonE exp. will probe HVP [MUonE, 2004.13663]

New physics interpretations

[Refs: Athron et al, 2104.03691; Buen-Abad et al, 2104.03267; Krnjaic et al, 1902.07715; Dermisek et al, 2103.05645]

NP type	diagrams	mass range	probe
Supersymmetry		200~500 GeV	$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \rightarrow (h \tilde{\chi}_1^0) (W^\pm \tilde{\chi}_1^0)$ $pp \rightarrow \gamma\gamma \rightarrow \tilde{l} \tilde{l}^*$
Scalar extensions		20~100 GeV, 150~250 GeV	$Z \rightarrow \tau^+ \tau^-$ $h \rightarrow AA$
Axion-like particle		40 MeV~6 GeV	$e^+ e^- \rightarrow \gamma a, a \rightarrow \gamma\gamma$
Leptoquark		1.5~2 TeV	$pp \rightarrow LQ \bar{L} \bar{Q}$
U(1) μ - τ		10~200 MeV	$e^+ e^- \rightarrow \mu^+ \mu^- Z'$ $K^- \rightarrow \mu^- \bar{\nu} Z'$
Vector-like lepton		< 7 TeV	$h, Z \rightarrow \mu^+ \mu^-$

SUSY example

[Endo, Hamaguchi, Iwamoto, TK, 2104.03217]

$$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \rightarrow (h \tilde{\chi}_1^0) (W^\pm \tilde{\chi}_1^0)$$

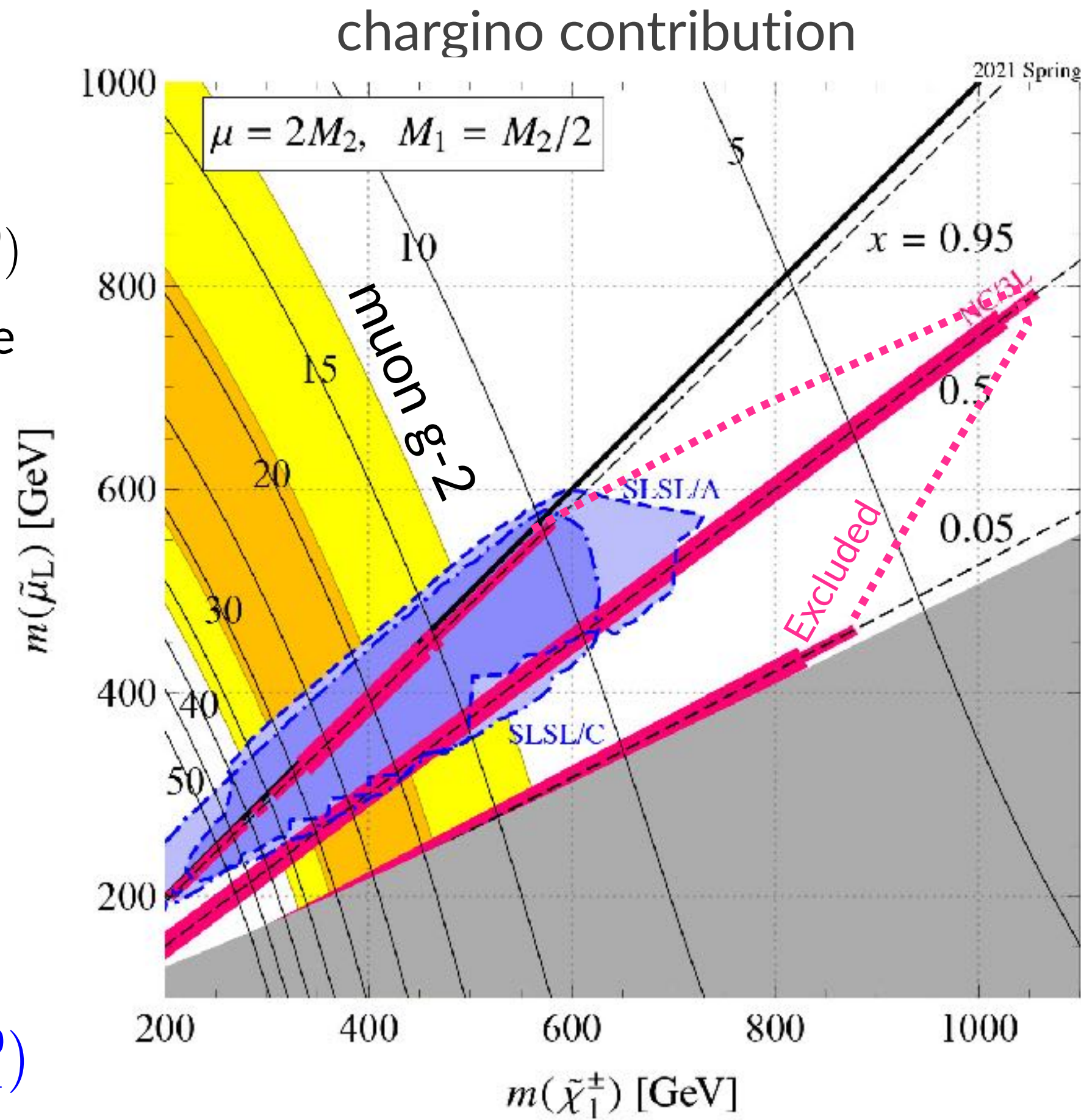
will be able to probe

Point: \tilde{W}^0 decays into h not Z

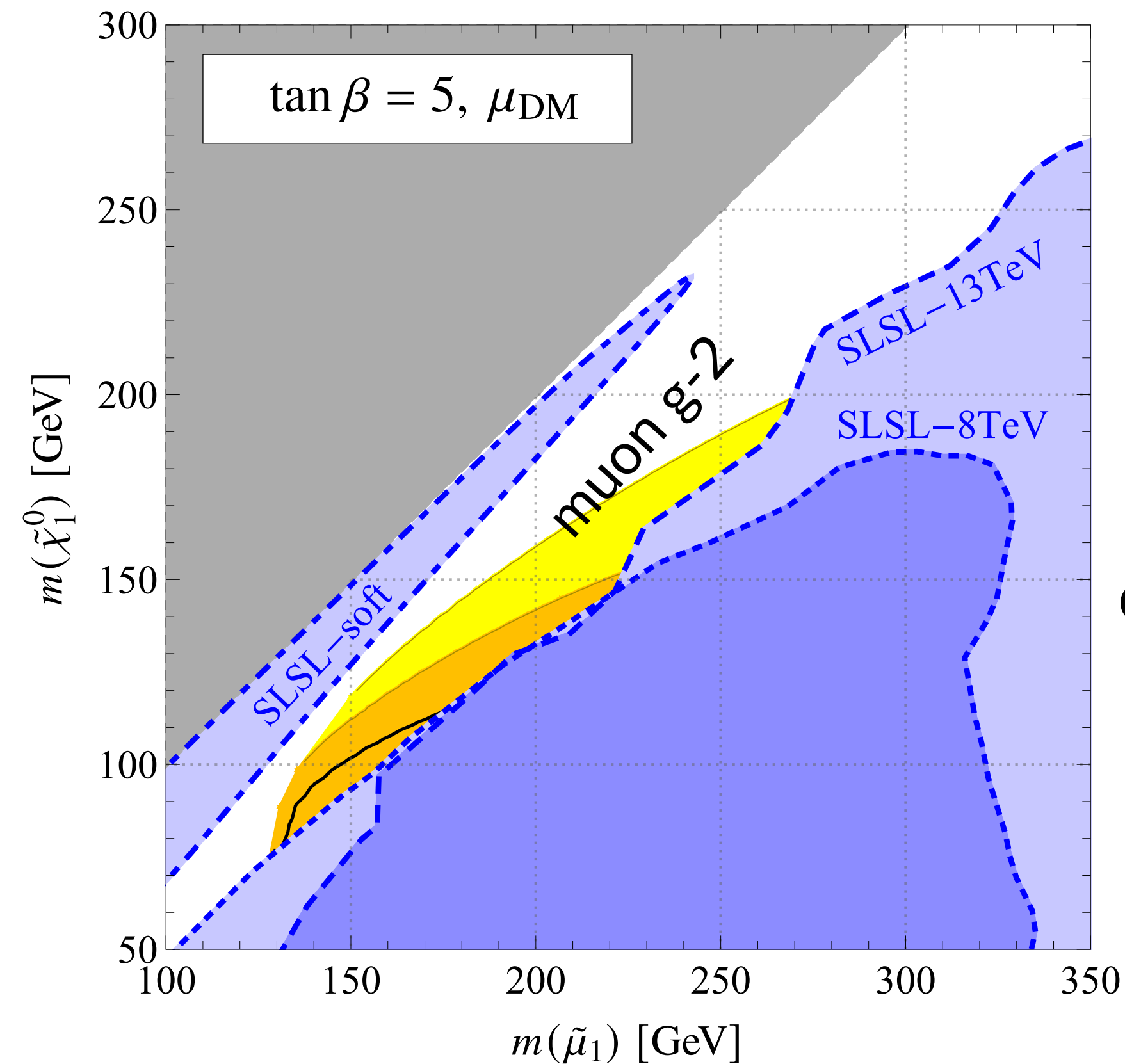
strong bound from:

$$\tilde{l}_L \tilde{l}_L^* \rightarrow (l \tilde{\chi}_1^0) (\bar{l} \tilde{\chi}_1^0)$$

$$\tilde{\chi}_2^0 \tilde{\chi}_1^\pm \rightarrow (\tilde{l}_L) (\nu \tilde{l}_L) \rightarrow (ll \tilde{\chi}_1^0) (\nu l \tilde{\chi}_1^0)$$



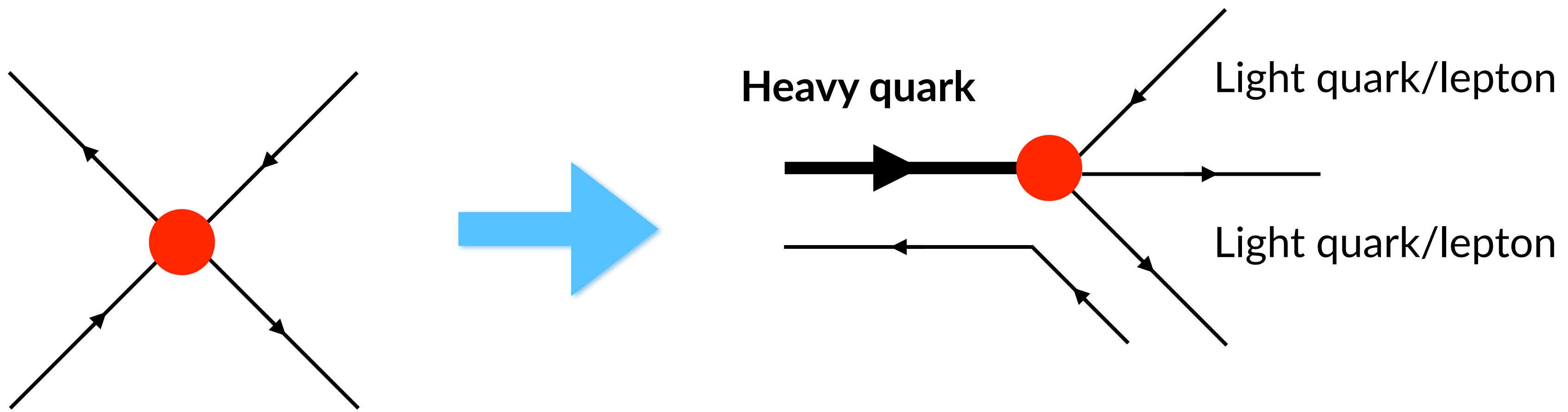
pure-bino contribution with correct Ω_{DM}



Low $\tan \beta$ is preferred(!)

Good target for ILC

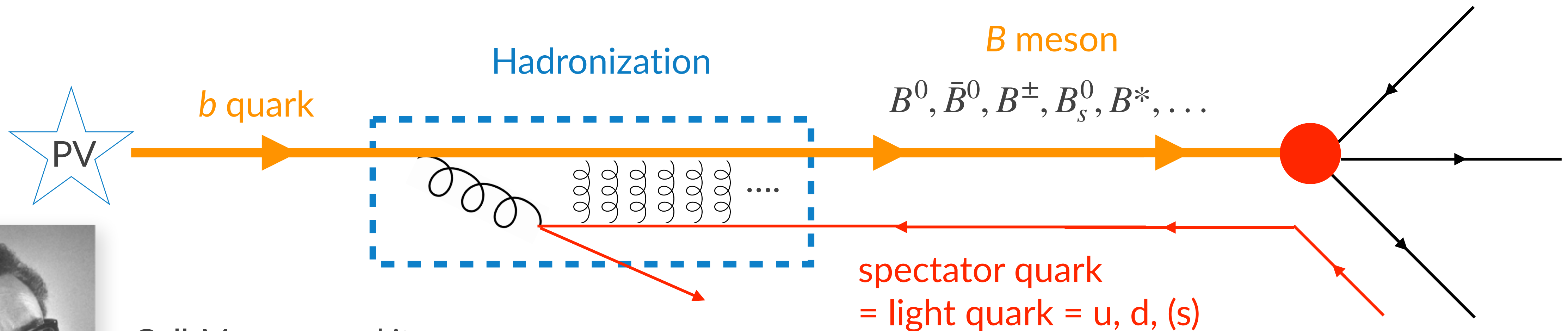
Photon collision $pp \rightarrow \gamma\gamma \rightarrow \tilde{l}\tilde{l}^* \rightarrow (l \tilde{\chi}_1^0) (\bar{l} \tilde{\chi}_1^0)$ will be able to probe [Beresford, Liu, PRL '19]



Precision measurements of flavor physics

What is flavor physics?

- ◆ Quarks can not become asymptotic field, but must be contained in hadron=meson or baryon
 $b \dots B$ meson, $c \dots D$ meson, $s \dots K$ meson, or heavy baryons.



Gell-Mann named it “flavor” at an ice-cream store, just as ice-cream has both color and quark (cheese) flavor

Quark flavor physics means physics of meson/baryon transition;

$$B \rightarrow K + X (b \rightarrow s), D \rightarrow \pi + X (c \rightarrow u), K \rightarrow \pi + X (s \rightarrow d), \text{ etc.}$$



B physics

- ◆ Main stream of the flavor physics. There are three big experiments for B physics.
- ◆ Rich phenomenology; CKM, FCNC, CP violation, tau lepton, LFU, Hadron spectroscopy, dark sector



BaBar experiment @ **SLAC**, physics run was finished at 2008

$$e^+e^- \rightarrow \Upsilon \rightarrow B\bar{B} \quad 10^8 B\bar{B} \text{ per year}$$



Belle and Belle II experiments @ **KEK**, Belle II started at 2019

$$e^+e^- \rightarrow \Upsilon \rightarrow B\bar{B} \quad 10^{10} B\bar{B} \text{ per year}$$



LHCb experiment @ **CERN**, Run 1 and 2 were done, Run 3 will start at 2022

$$pp \rightarrow b\bar{b} \rightarrow B\bar{B} \quad 10^{12} b\bar{b} \text{ per year}$$

CKM matrix

- ◆ CKM matrix arises the relative misalignment between the Yukawa matrices and gauge interactions:

$$\mathcal{L} \supset -\frac{g}{\sqrt{2}} \bar{u}_L^i \gamma^\mu d_L^j W_\mu^+ \xrightarrow{\text{mass-eigenbasis}} -\frac{g}{\sqrt{2}} \bar{u}_L^i \gamma^\mu (U_u^\dagger U_d)^{ij} d_L^j W_\mu^+ \\ = -\frac{g}{\sqrt{2}} \bar{u}_L^i \gamma^\mu V_{\text{CKM}}^{ij} d_L^j W_\mu^+$$

- ◆ Wolfenstein parametrization

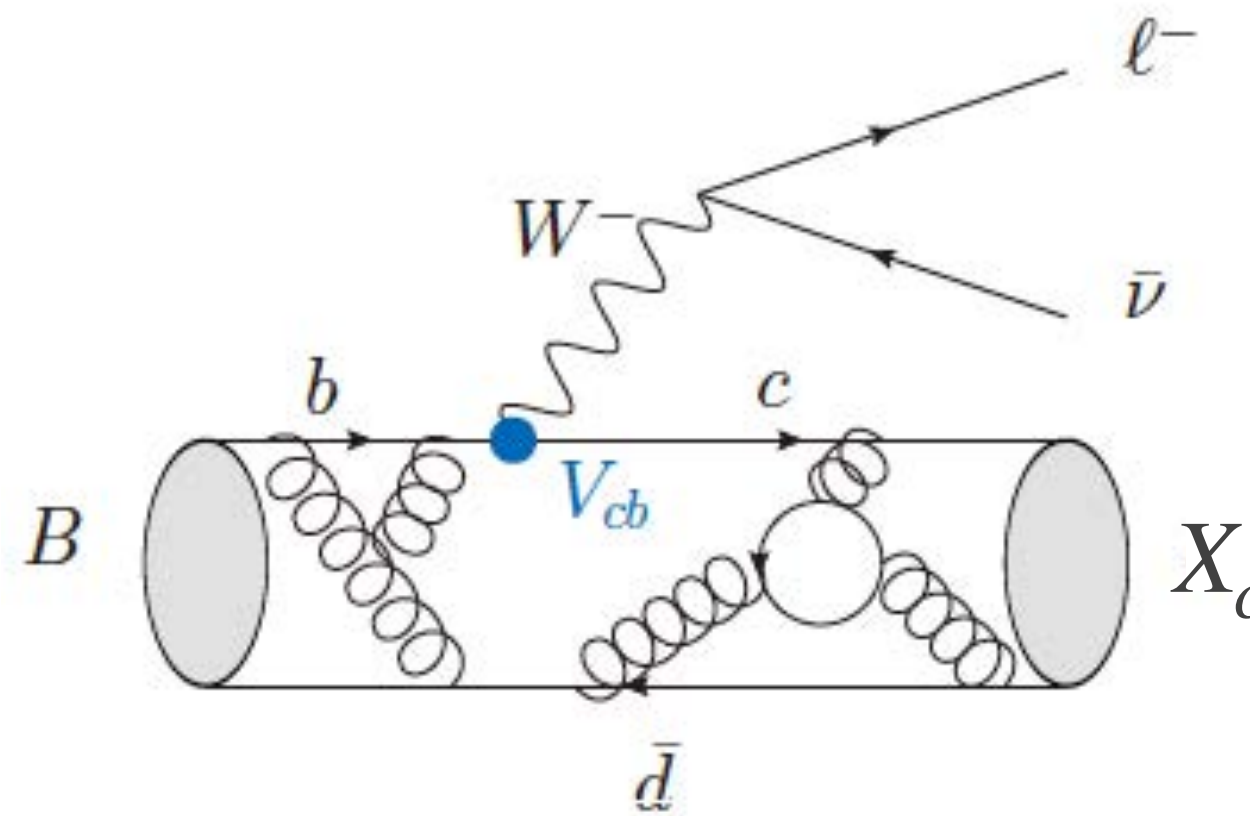
$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{matrix} K \text{ physics} & B \text{ physics} & \\ & & \end{matrix} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$



- ◆ Parameter A is determined by B physics

Measurements of $|V_{cb}|$

- ◆ For determination of $|V_{cb}|$, one measures branching ratios of B -meson semileptonic decay modes, and compare TH



Semileptonic mode $\ell = e, \mu$

Hadron states $X_c (=D^{**}, D^*, D, D\pi, D\pi\pi\dots)$

- ◆ Inclusive decays: $B \rightarrow X_c \ell \nu$

- ◆ It corresponds to quark level decay rate $(b \rightarrow c \ell \nu) + \alpha_s, \Lambda_{\text{QCD}}/m_b$ corrections

- ◆ Last data in 2010 \rightarrow Belle II result coming soon; No lattice \rightarrow the first lattice study [Gambino, Hashimoto, PRL '20]

- ◆ Exclusive decays: $B \rightarrow D \ell \nu, B \rightarrow D^* \ell \nu$

- ◆ Many data with different schemes. One can use lattice simulations.

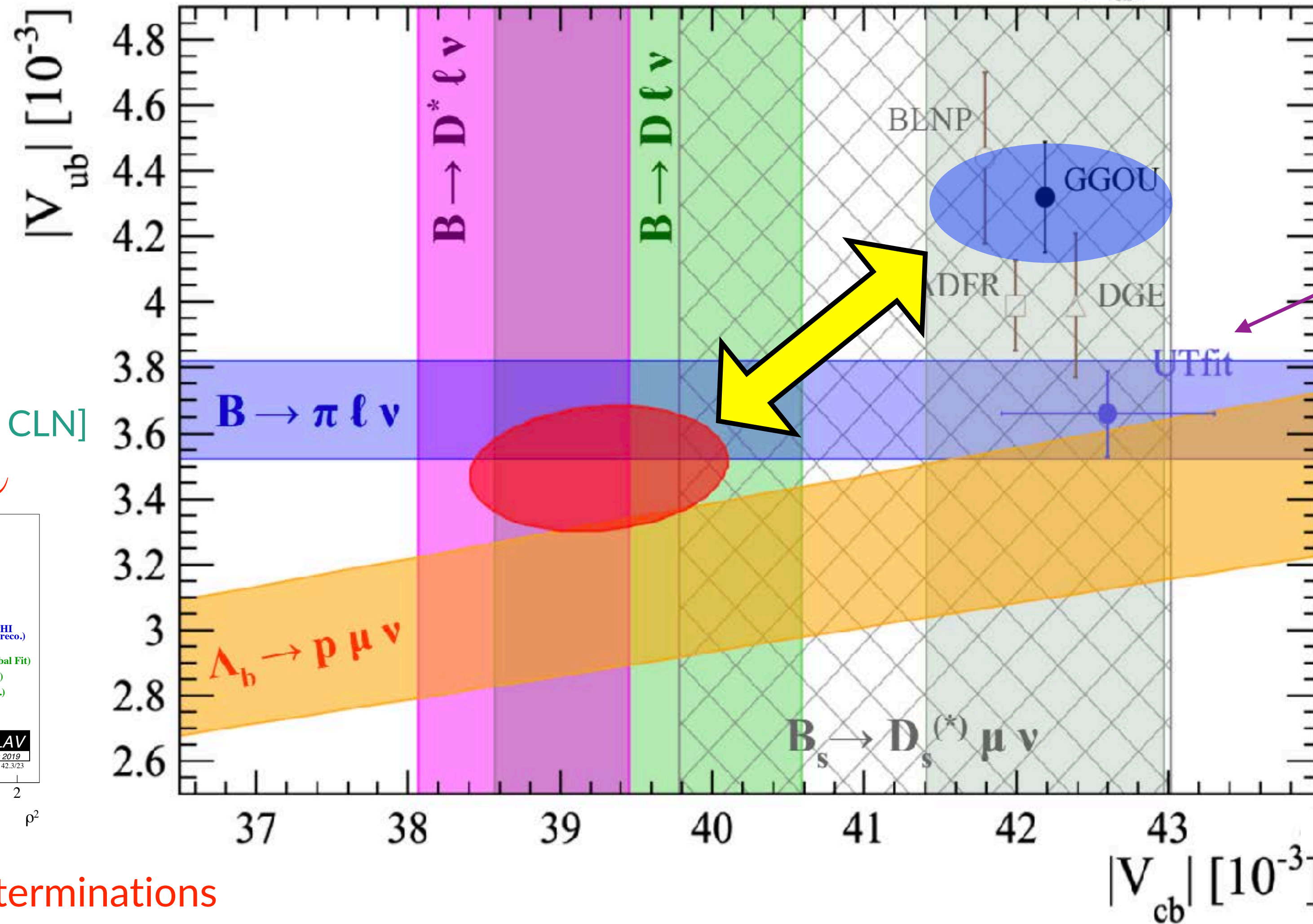
Average of the inclusive determinations

[Ricciardi, Rotondo, 1912.09562]

~3σ tension between inclusive vs. exclusive determinations of V_{cb} and V_{ub}

NP interpretation is difficult [Iguro, Watanabe, 2004.10208]

[HFLAV averages 2019, based on CLN]



CKM unitarity

Kaon physics prefers inclusive V_{cb} (→ page 36)

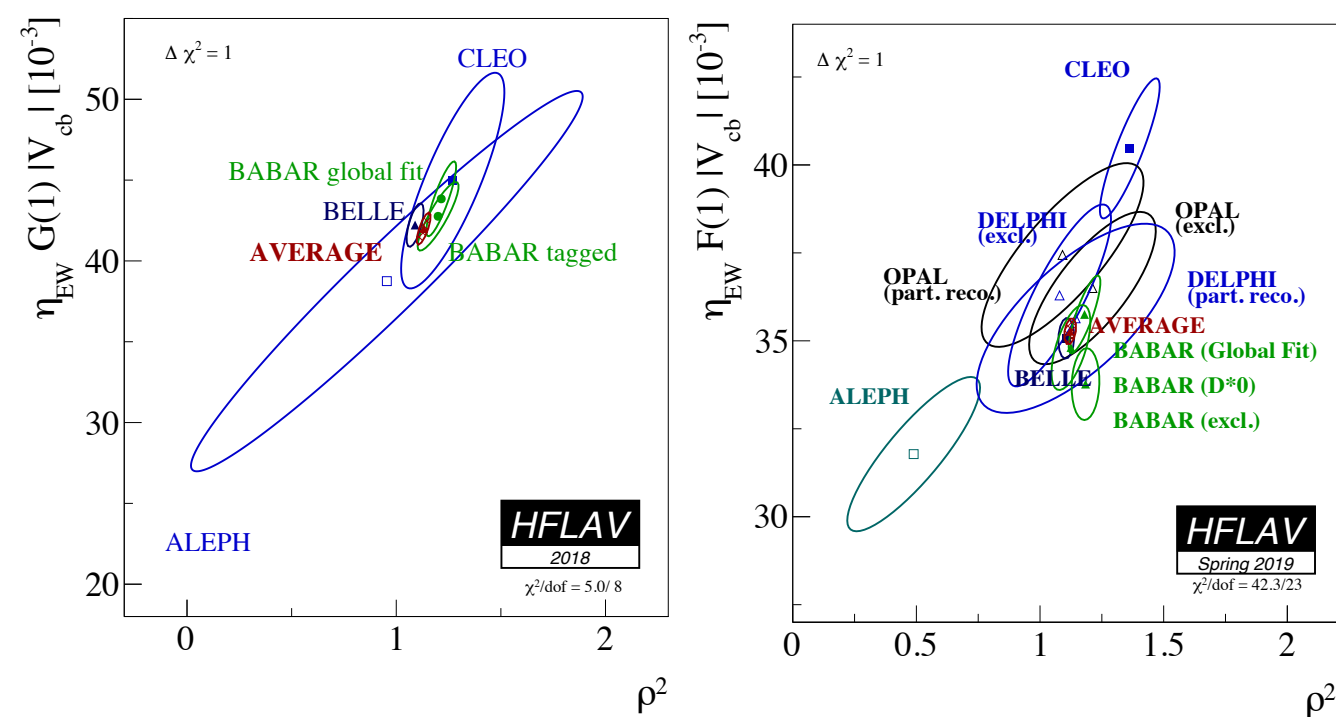
Belle II preliminary result [Moriond2021]

Inclusive V_{cb} = 41.7 (12) $\times 10^{-3}$

Average of the exclusive determinations

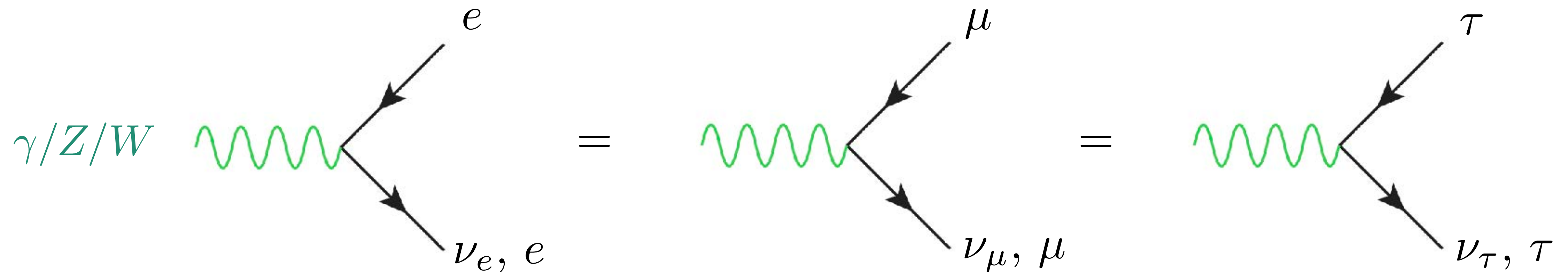
$B \rightarrow D \ell \nu$

$B \rightarrow D^* \ell \nu$



Lepton flavor universality (LFU)

- ◆ Gauge symmetry predicts lepton flavor universal phenomena

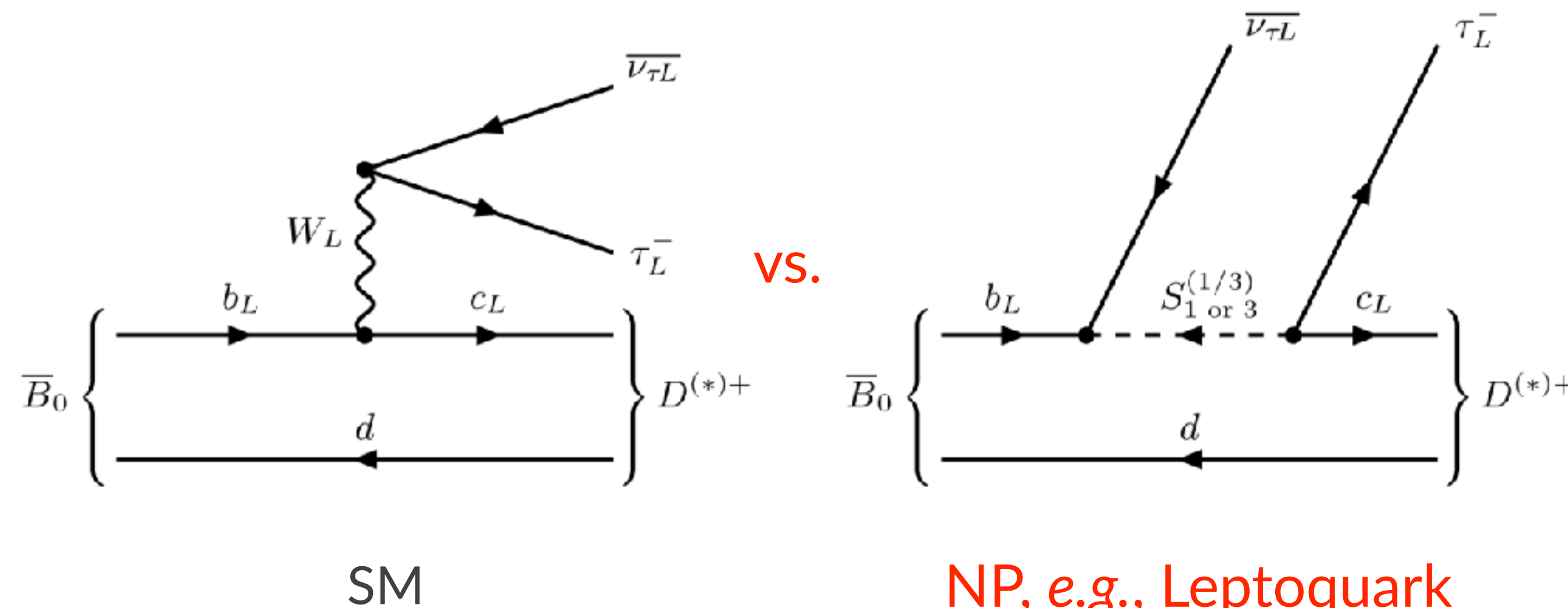


- ◆ Charged lepton mass changes kinematics and modifies scalar form factors in the hadronization, which eventually violates the lepton flavor universality
- ◆ Long-distance QED correction (beyond PHOTOS) could violate the lepton flavor universality [de Boer, TK, Nisandzic, PRL '18; Isidori, Nabeebaccus, Zwicky, '20]

LFU observable $R(D)$

$$R(D^{(*)}) = \frac{\text{BR}(B \rightarrow D^{(*)} \bar{\tau} \nu_{\tau})}{\text{BR}(B \rightarrow D^{(*)} \bar{\ell} \nu_{\ell})}$$

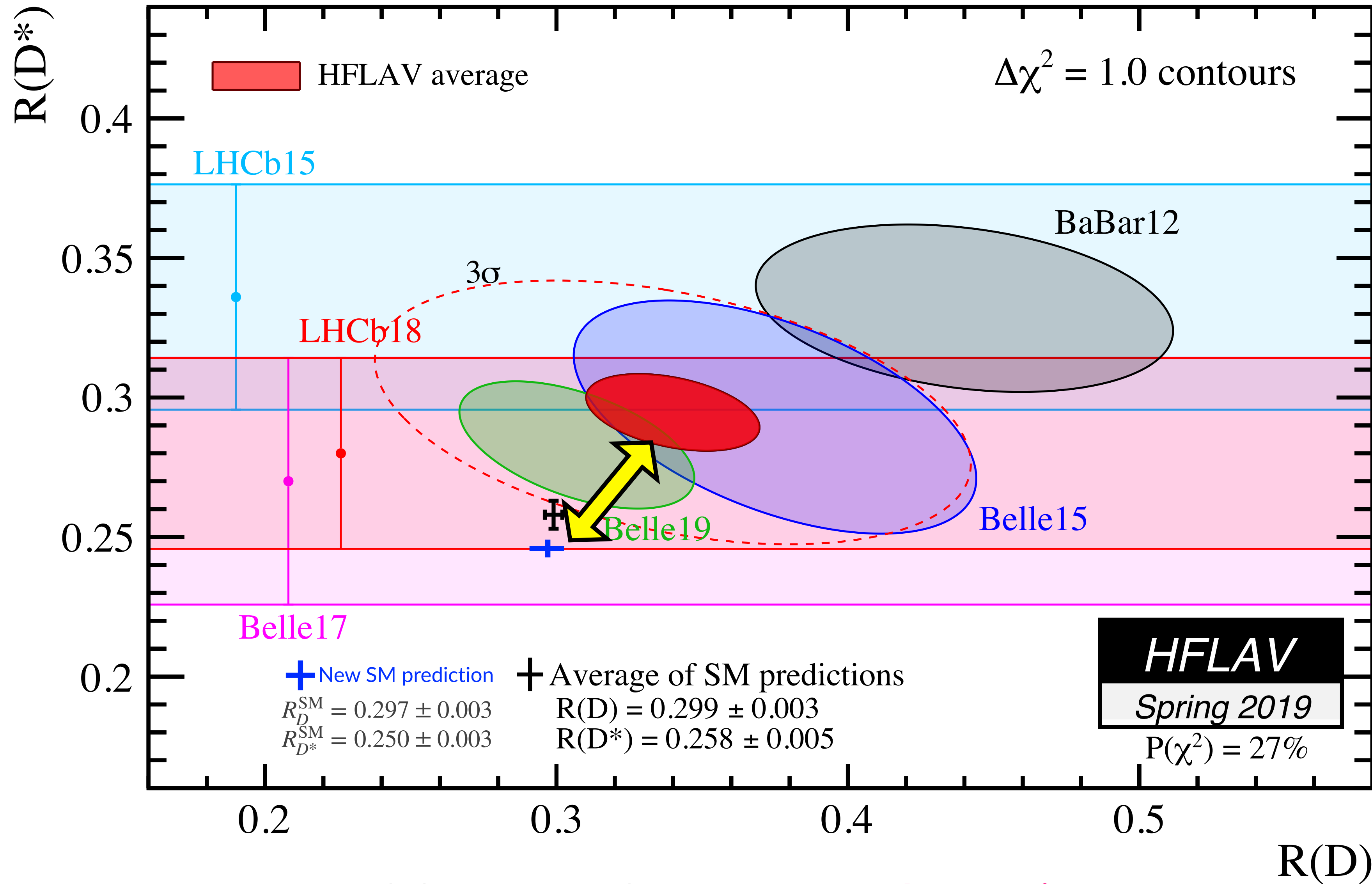
V_{cb} dependence
is dropped



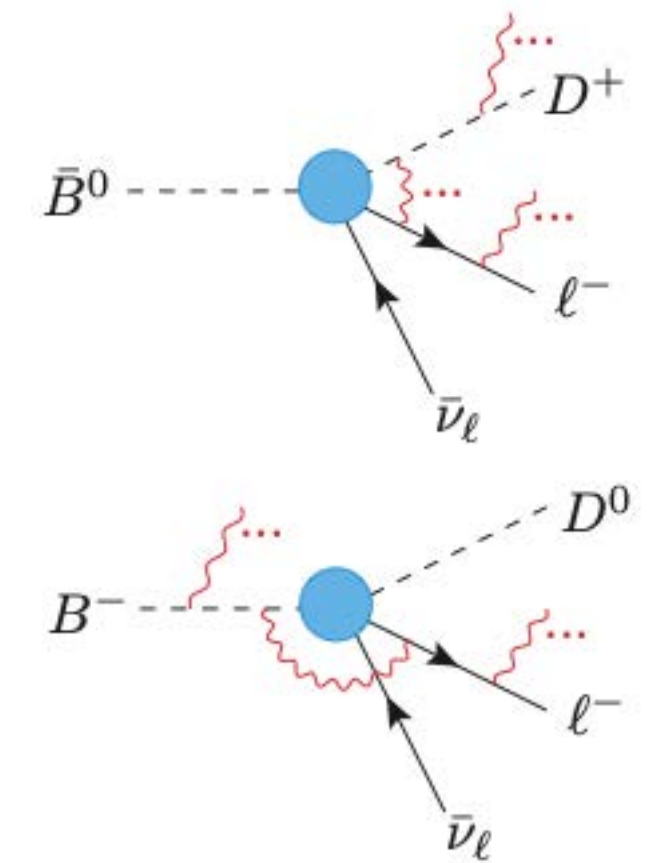
$$\mathcal{B}(B \rightarrow D \ell \nu) = 2\%, \quad \mathcal{B}(B \rightarrow D^* \ell \nu) = 5\%,$$

[HFLAV averages 2019]

Average of the experimental data



Soft-photon QED corrections could change these tensions



It was shown that the QED correction violates LFU at a few % level

[de Boer, TK, Nisandzic, PRL '18]

3.8 σ $\rightarrow\rightarrow\rightarrow$ 3.1 σ $\rightarrow\rightarrow\rightarrow$ $\sim 4 \sigma$ tension

New Belle data '19

New SM '20

[Bordone, Jung, van Dyk, '20; Iguro Watanabe, '20]

EFT global fit [Blanke, Crivellin, TK, Moscati, Nierste, Nisandzic, '19]

◆ Relevant effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = 2\sqrt{2}G_F V_{cb} [(1 + C_V^L)O_V^L + C_S^R O_S^R + C_S^L O_S^L + C_T O_T],$$

$$O_V^L = (\bar{c}\gamma^\mu P_L b) (\bar{\tau}\gamma_\mu P_L \nu_\tau)$$

$$O_S^R = (\bar{c}P_R b) (\bar{\tau}P_L \nu_\tau)$$

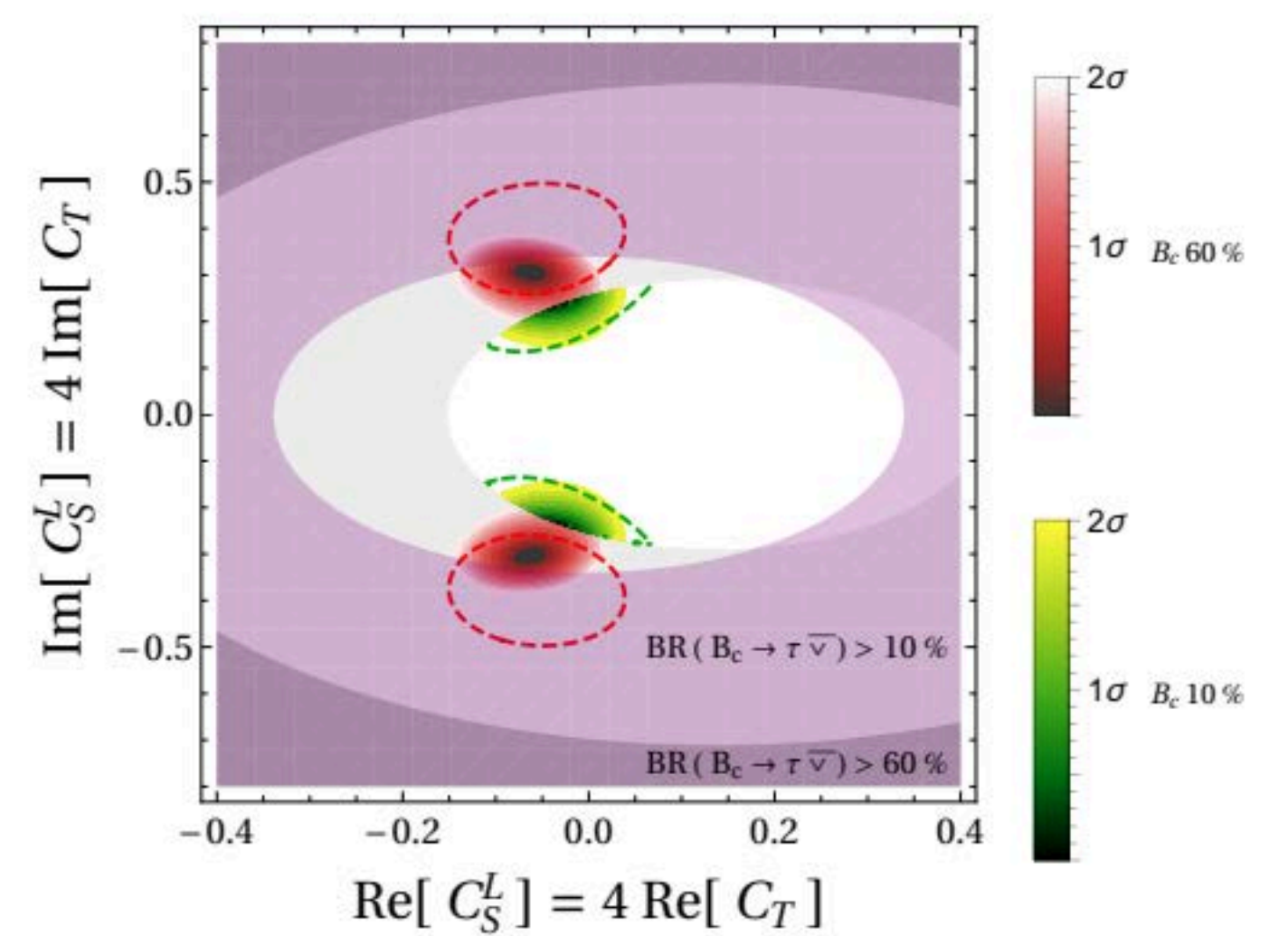
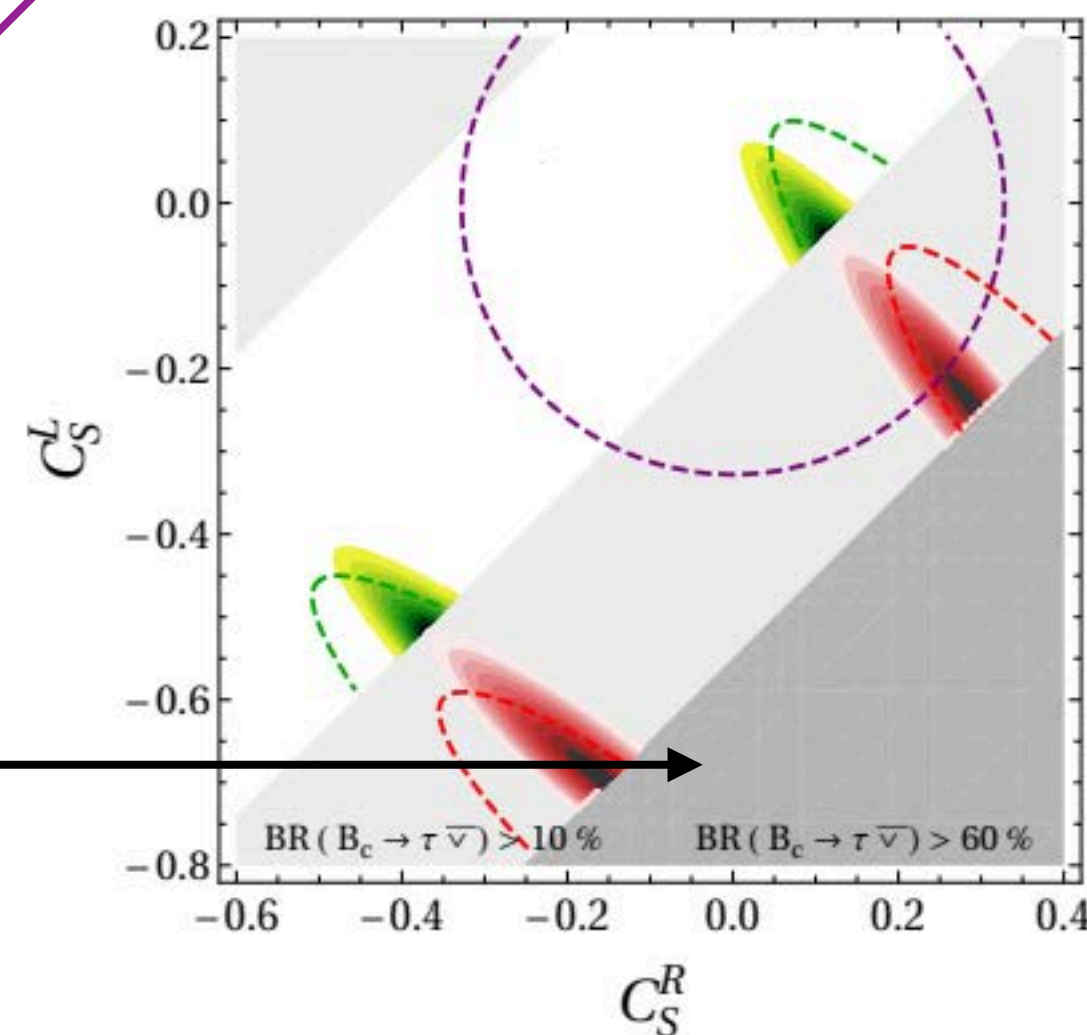
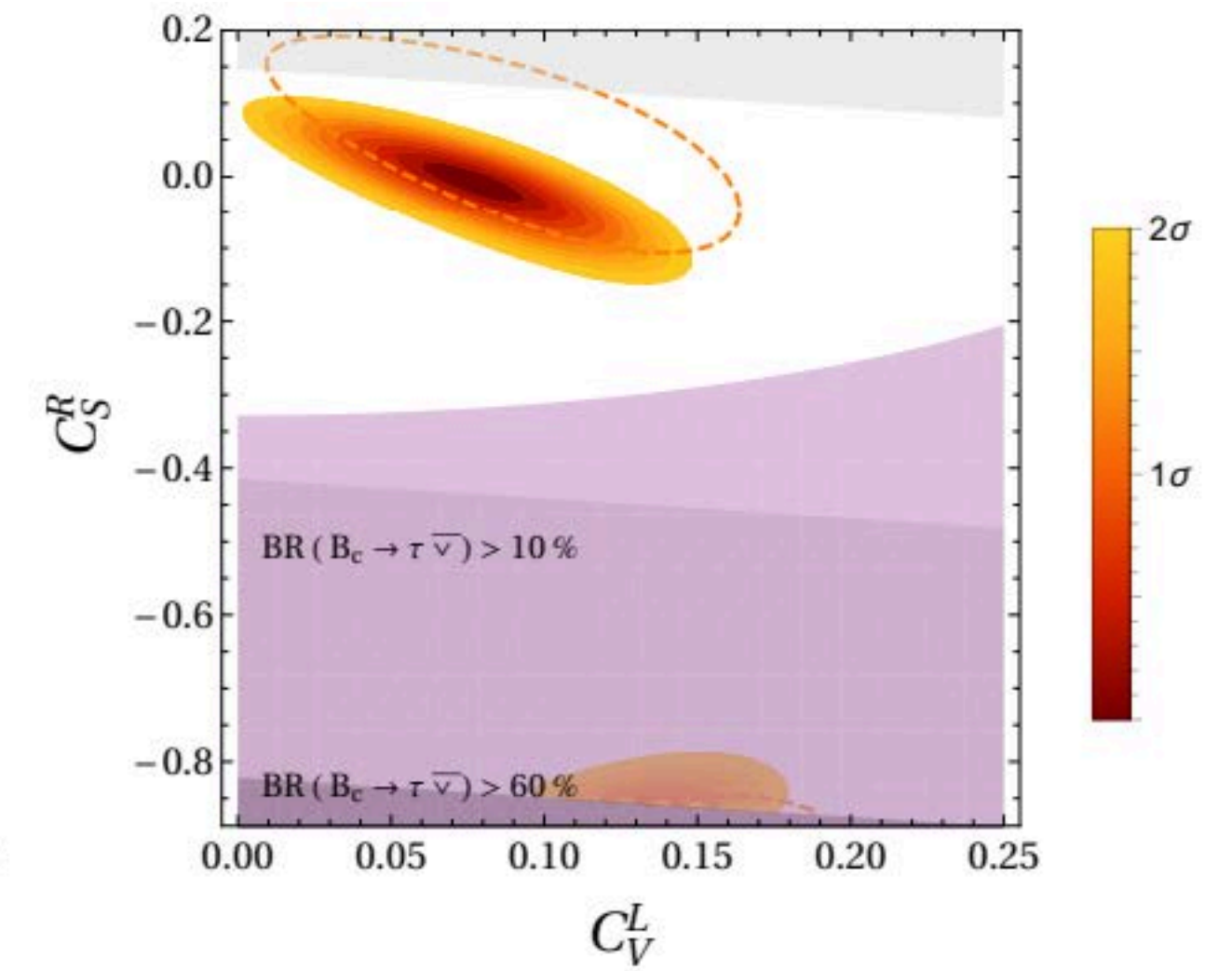
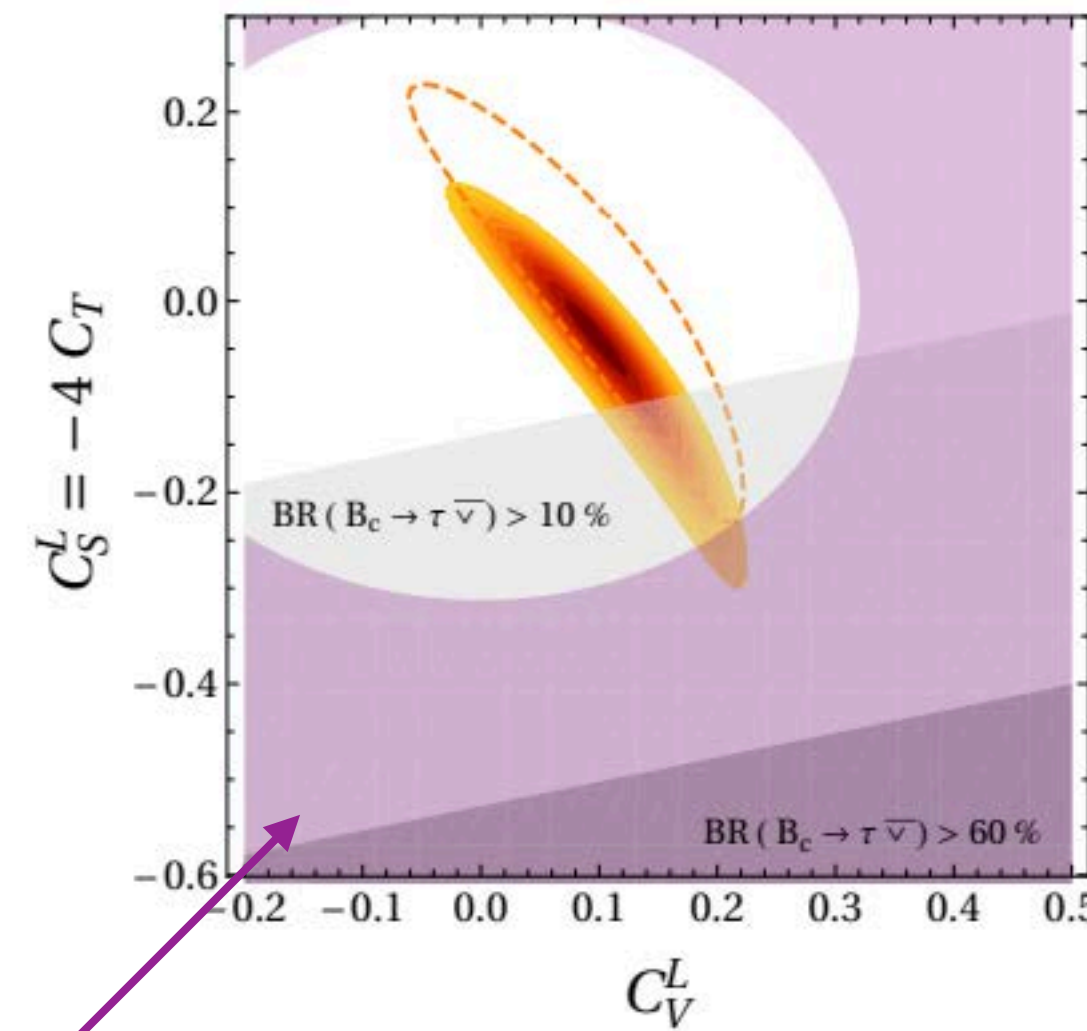
$$O_S^L = (\bar{c}P_L b) (\bar{\tau}P_L \nu_\tau)$$

$$O_T = (\bar{c}\sigma^{\mu\nu} P_L b) (\bar{\tau}\sigma_{\mu\nu} P_L \nu_\tau)$$

◆ Collider bound (→page 26)

◆ Bound from $\text{BR}(B_c^+ \rightarrow \tau^+ \nu) < 60\%$

10% bound is too stringent



“Single particle” interpretations

◆ One WC scenarios

C_V^L W' ,
SU(2)_L-singlet vector LQ,
SU(2)_L-triplet and/or -singlet scalar LQ

C_S^R Charged Higgs,
SU(2)_L-doublet vector LQ (V_2)

C_S^L Charged Higgs with generic flavour
structure

$C_S^L = 4C_T$ scalar SU(2)_L-doublet LQ (R_2)
 (“4” is modified by RG evolution)

◆ Two WCs scenarios

$(C_V^L, C_S^L = -4C_T)$ SU(2)_L-singlet scalar LQ (S_1)

(C_V^L, C_S^R) SU(2)_L-singlet vector LQ (U_1)

(C_S^R, C_S^L) Charged Higgs with generic flavour
structure

$(\text{Re}[C_S^L = 4C_T],$
 $\text{Im}[C_S^L = 4C_T])$ scalar SU(2)_L-doublet LQ (R_2)

◆ There are so many detailed studies for **each** single particle scenarios

◆ There are also “two LQs” scenarios

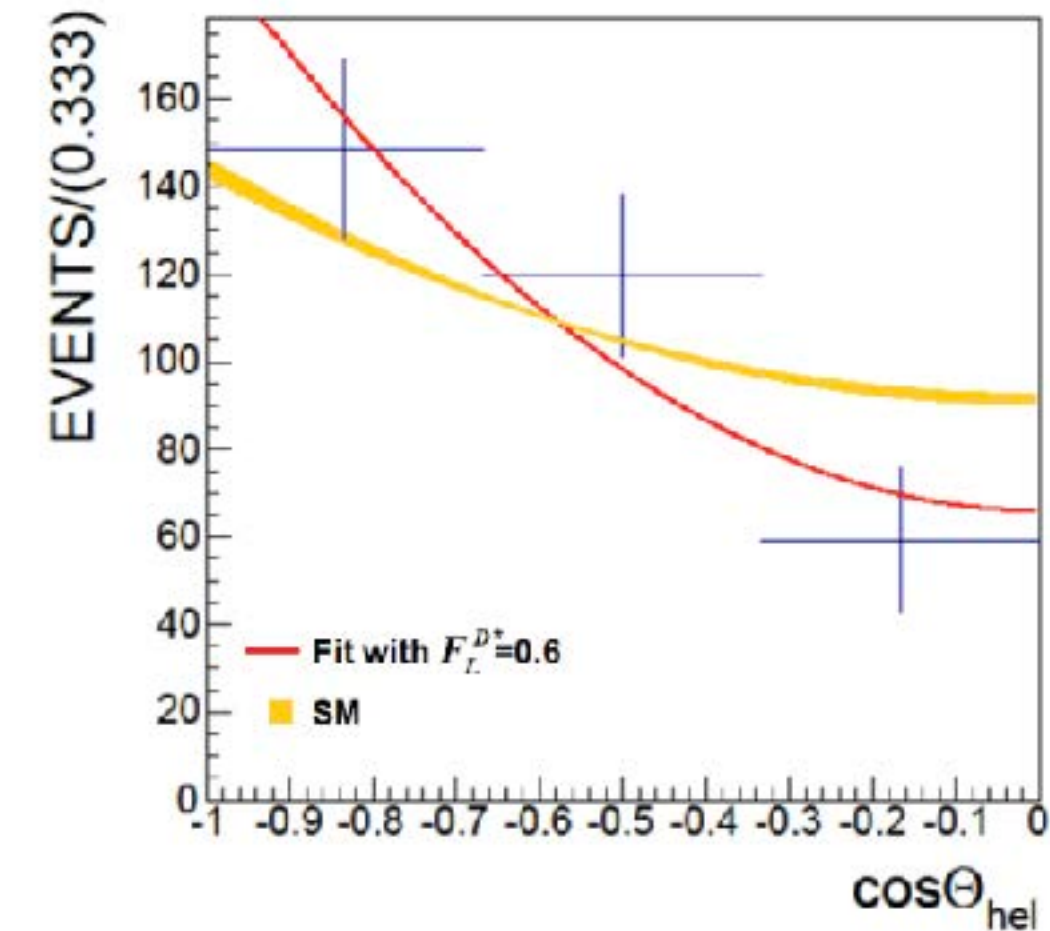
Polarization observables in $b \rightarrow c\tau\nu$

- ◆ The following two polarization observables could be important to confirm/distinguish new physics

- ◆ Longitudinal D^* polarization ($D^* \rightarrow D\pi$)

$$F_L(D^*) = \frac{\Gamma(B \rightarrow D_L^* \tau \nu)}{\Gamma(B \rightarrow D^* \tau \nu)}$$

θ_{hel} is the angle
between D and B in the
 D^* rest frame



[Belle, 1903.03102]

1.4 σ consistent

- ◆ τ polarization asymmetry along the longitudinal directions of τ ($\tau \rightarrow \pi\nu, \rho\nu$) [Tanaka, ZPC '95]

$$P_\tau(D^{(*)}) = \frac{\Gamma(B \rightarrow D^{(*)} \tau^{\lambda=+1/2} \nu) - \Gamma(B \rightarrow D^{(*)} \tau^{\lambda=-1/2} \nu)}{\Gamma(B \rightarrow D^{(*)} \tau \nu)}$$

Fit of angle dependence:
between π, ρ and $W^*(\tau\nu)$
in τ rest frame

Predicted ranges of polarization observables

- ◆ Full parameter searches of each LQ model, including LHC mono- τ bound and $\text{BR}(B_c^+ \rightarrow \tau^+ \nu) < 30\%$

[Greljo, Martin Camalich, Ruiz-Alvarez, PRL '19; Alonso, Grinstein, Martin Camalich, PRL '17]

[Iguro, TK, Omura, Watanabe, Yamamoto, '19, **UPDATED**]

[Predicted ranges]

(50 ab⁻¹)

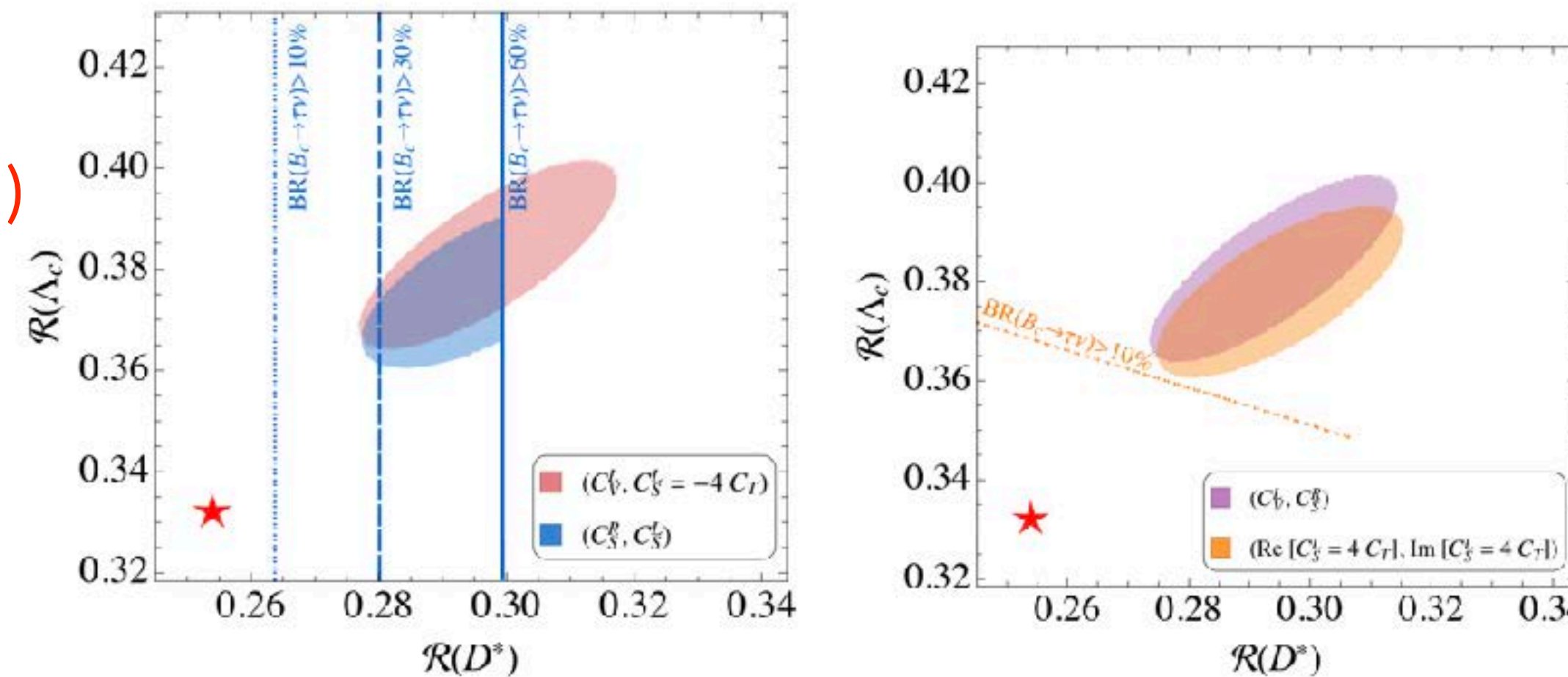
	F_L^{D*}	P_τ^D	P_τ^{D*}	R_D	R_{D*}
R ₂ LQ	[0.442, 0.447]	[0.336, 0.456]	[-0.464, -0.424]	1 σ data	1 σ data
S ₁ LQ	[0.436, 0.481]	[-0.006, 0.489]	[-0.512, -0.450]	1 σ data	1 σ data
U ₁ LQ	[0.440, 0.459]	[0.156, 0.422]	[-0.542, -0.488]	1 σ data	1 σ data
SM	0.46(4)	0.325(9)	-0.497(13)	0.299(3)	0.258(5)
data	0.60(9)	-	-0.38(55)	0.340(30)	0.295(14)
Belle II	0.04	3%	0.07	3%	2%

- ◆ $P_\tau(D)$ can discriminate the new physics
- ◆ LHC mono- τ search gives more severe bound than $\text{BR}(B_c^+ \rightarrow \tau^+ \nu) < 30\%$

Model-independent prediction: $R(\Lambda_c)$

- ◆ Baryonic counterpart: $\mathcal{R}(\Lambda_c) = \frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \ell^- \bar{\nu}_\ell)}$ @ LHCb [Bernlochner, Liegt, Robinson, Sutcliffe, PRL '18]

SU(2)_L-singlet scalar LQ (S_1)
Charged Higgs



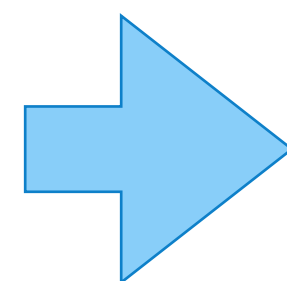
SU(2)_L-singlet vector LQ (U_1)
SU(2)_L-doublet scalar LQ (R_2)

Similar ellipses!

- ◆ Sum rule for $R(\Lambda_c)$ prediction from the form factor analysis

Model-independent sum rule
(also valid for RH neutrino scenarios) $\frac{R(\Lambda_c)}{R(\Lambda_c)_{SM}} \simeq 0.26 \frac{R(D)}{R(D)_{SM}} + 0.74 \frac{R(D^*)}{R(D^*)_{SM}}$

Crosscheck of $R(D^{(*)})$ anomaly is possible by $R(\Lambda_c)$



$$R(\Lambda_c) = 0.38 \pm 0.01_{R(D^{(*)})} \pm 0.01_{FF}$$

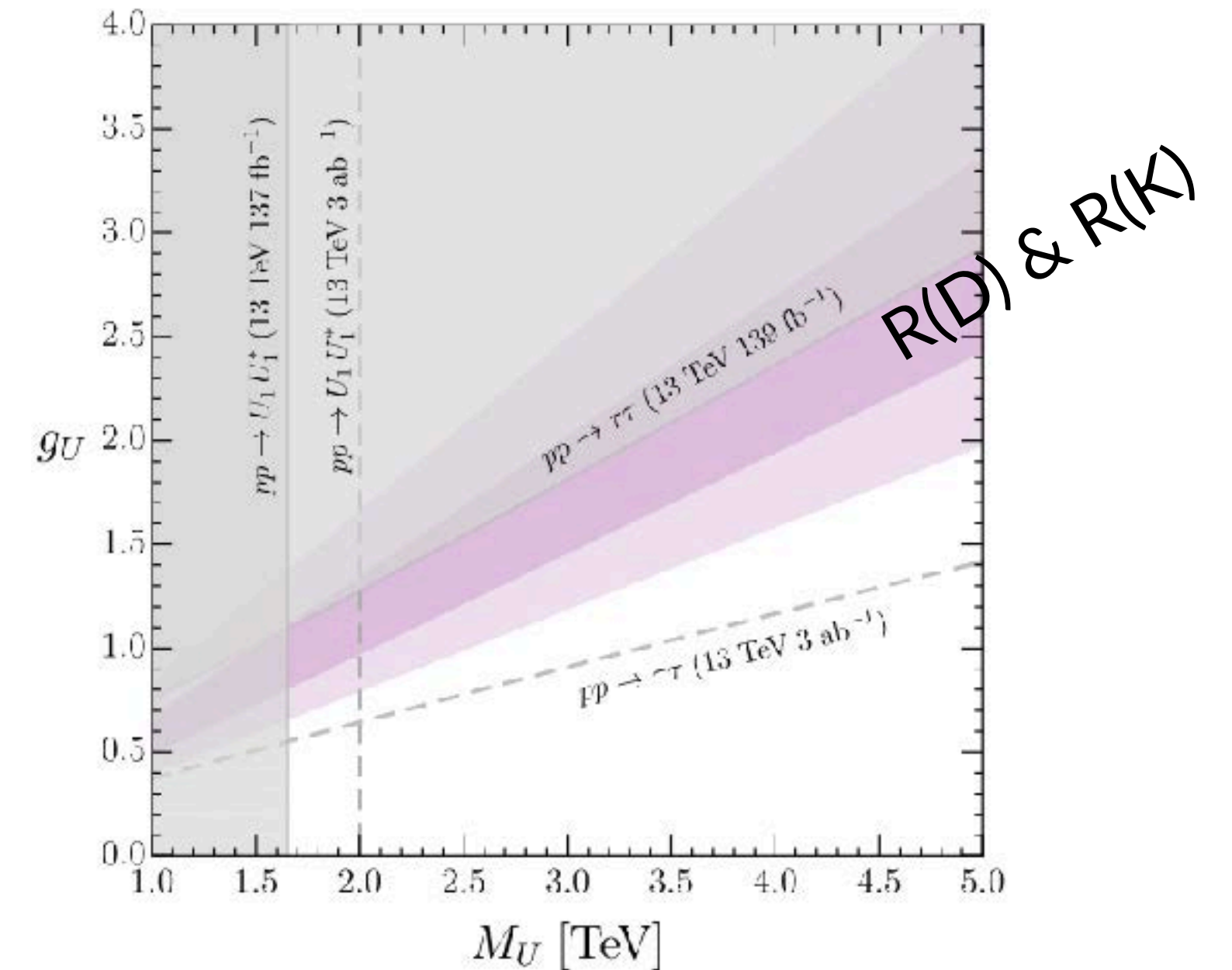
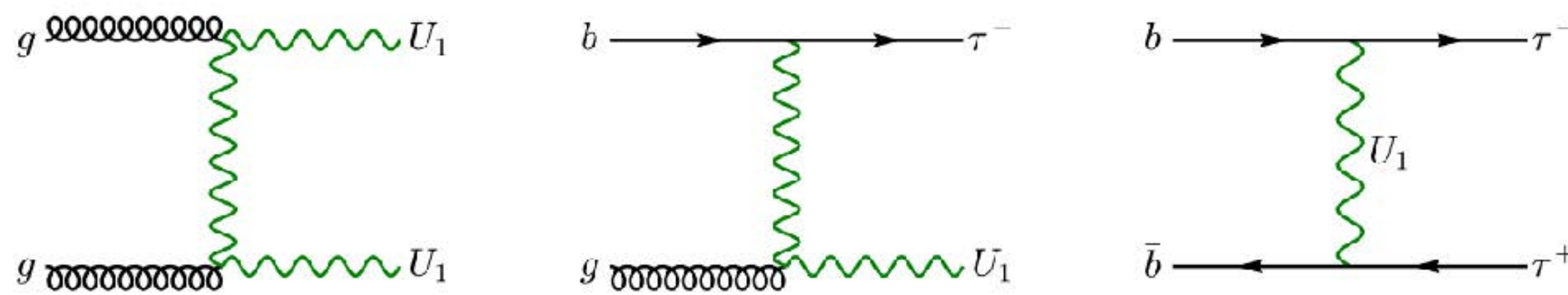
There is no data yet, but soon?

$$R(\Lambda_c)_{SM} = 0.324 \pm 0.004 \quad [\text{Blanke, Crivellin, TK, Moscati, Nierste, Nisandzic, '19}]$$

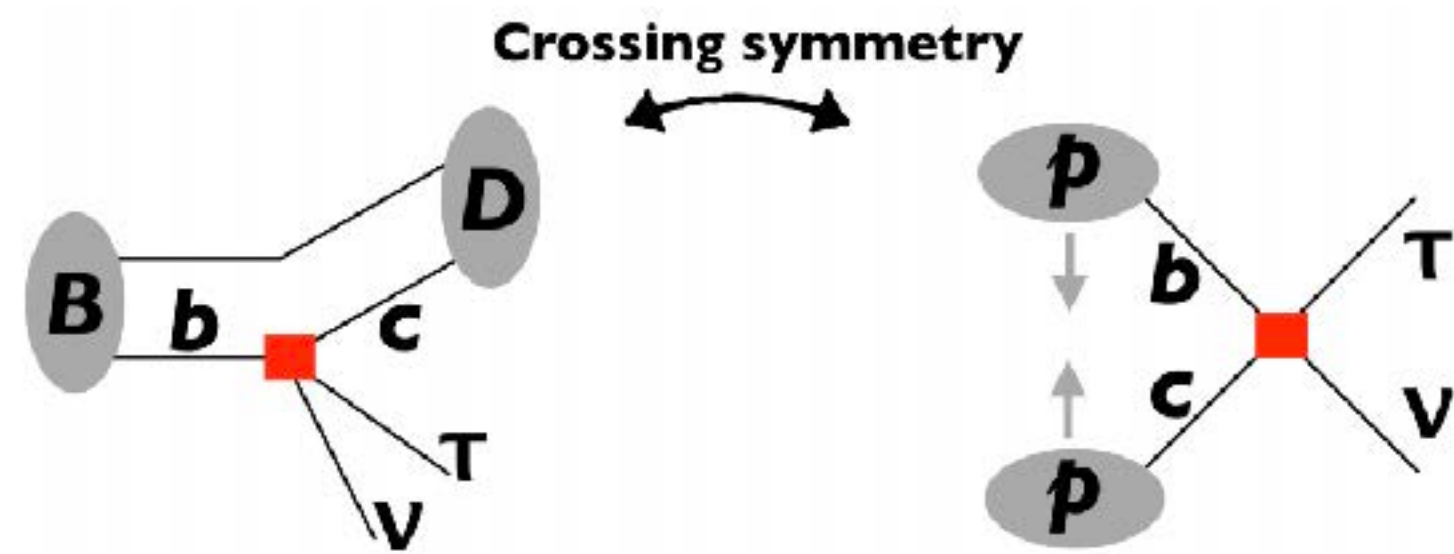
LQ vs LHC

- LQ can be probed by LHC directly and **indirectly**

Vector leptoquark scenario [Cornella et al, 2103.16558]



- The direct bound comes from high- p_T tails in mono- τ searches



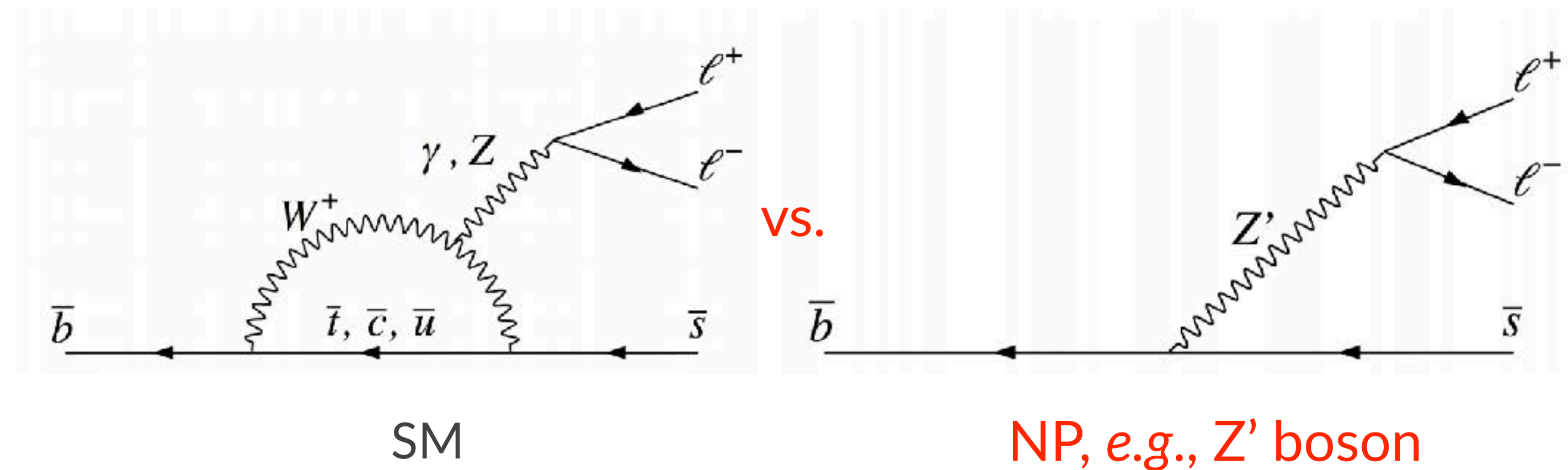
[Greljo, Camalich, Ruiz-Alvarez PRL '19; Marzocca, Min, Son, '20; Iguro, Takeuchi, Watanabe 2011.02486]

Current bounds:

$$\begin{aligned} \text{EFT:} \quad & |C_V^L| < 0.32, \quad |C_S^{L(R)}| < 0.55, \quad |C_T| < 0.17 \\ \text{2TeV LQ:} \quad & |C_V^L| < 0.42, \quad |C_S^{L(R)}| < 0.8, \quad |C_T| < 0.35 \end{aligned}$$

LFU observable $R(K)$

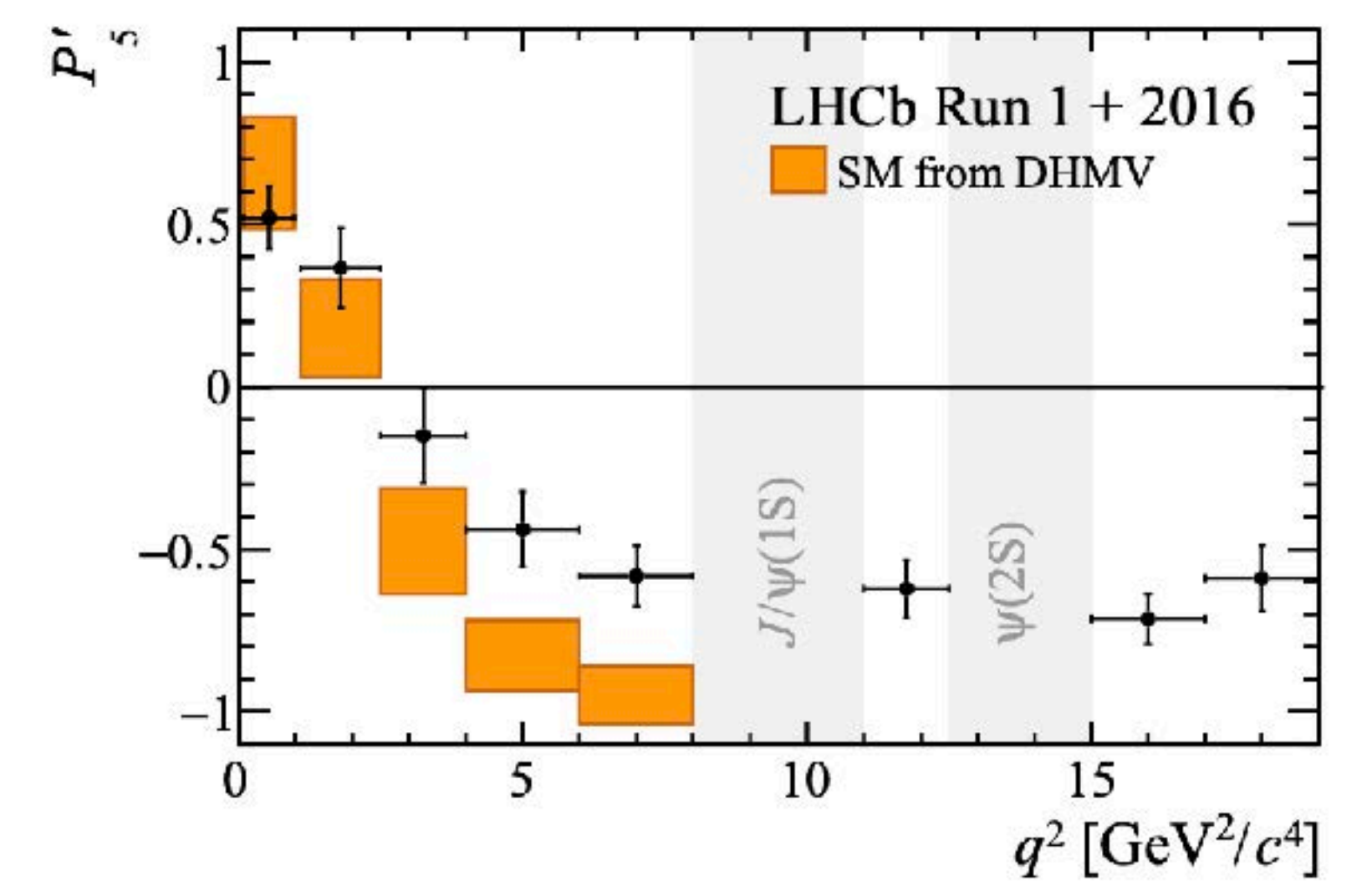
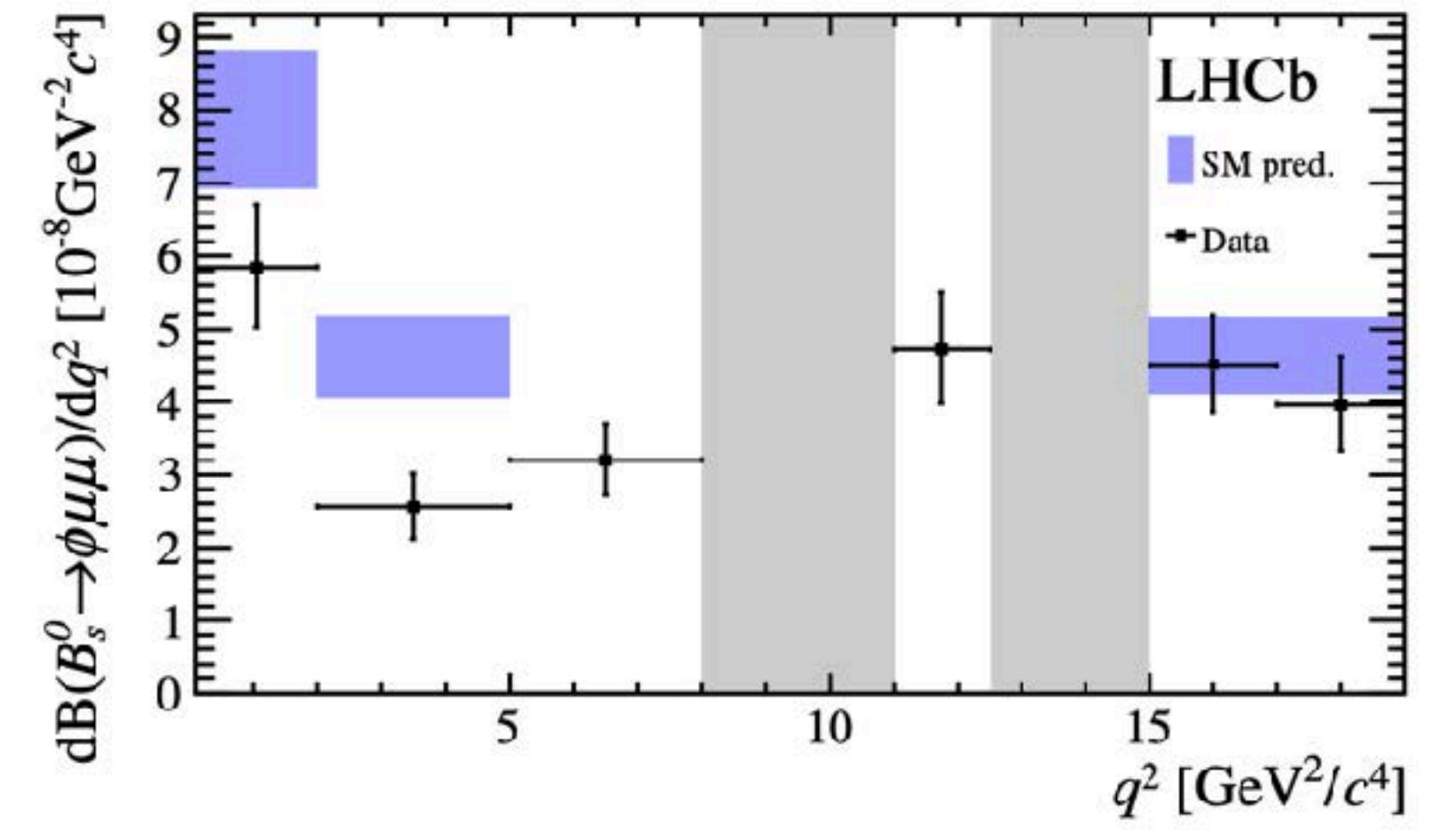
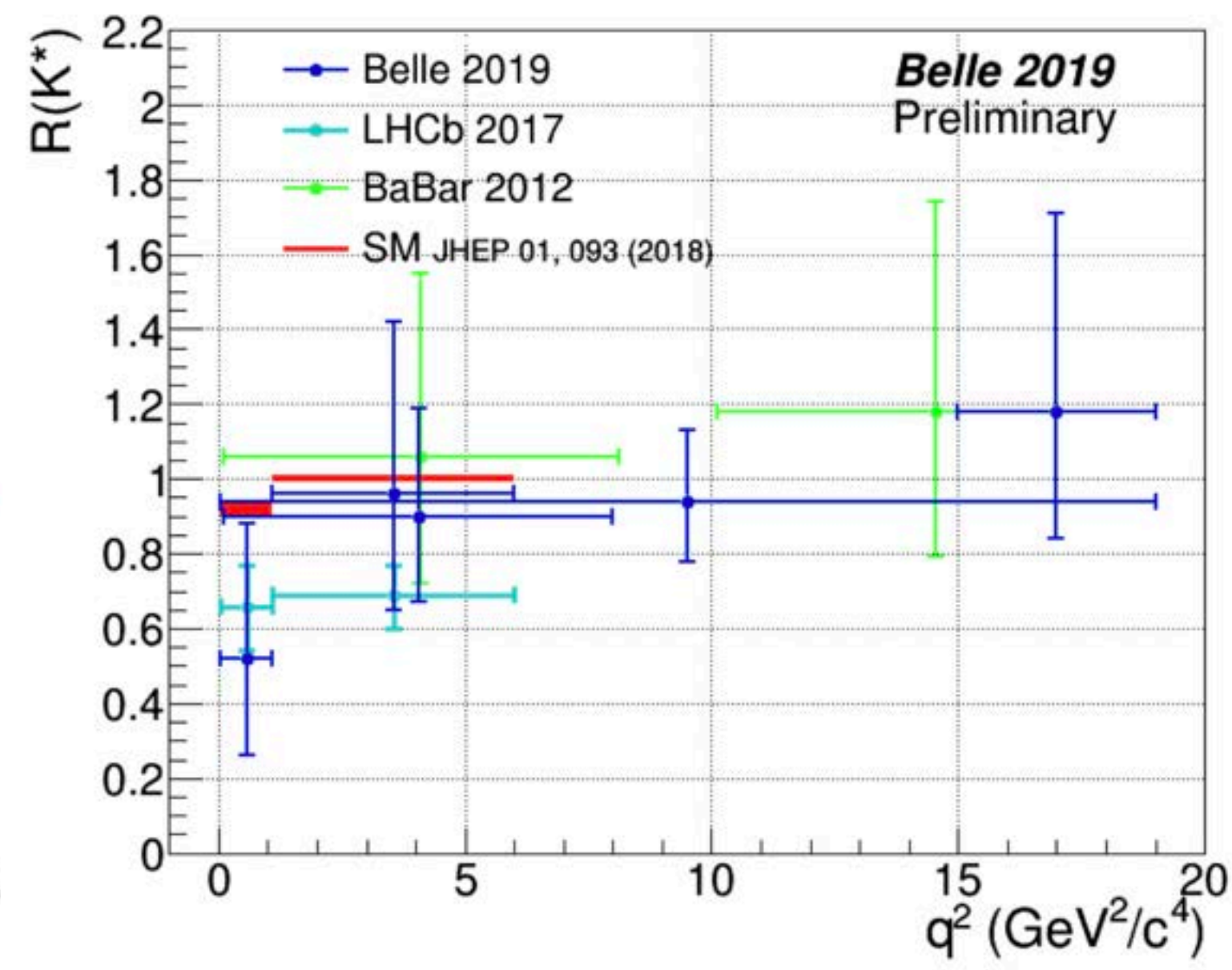
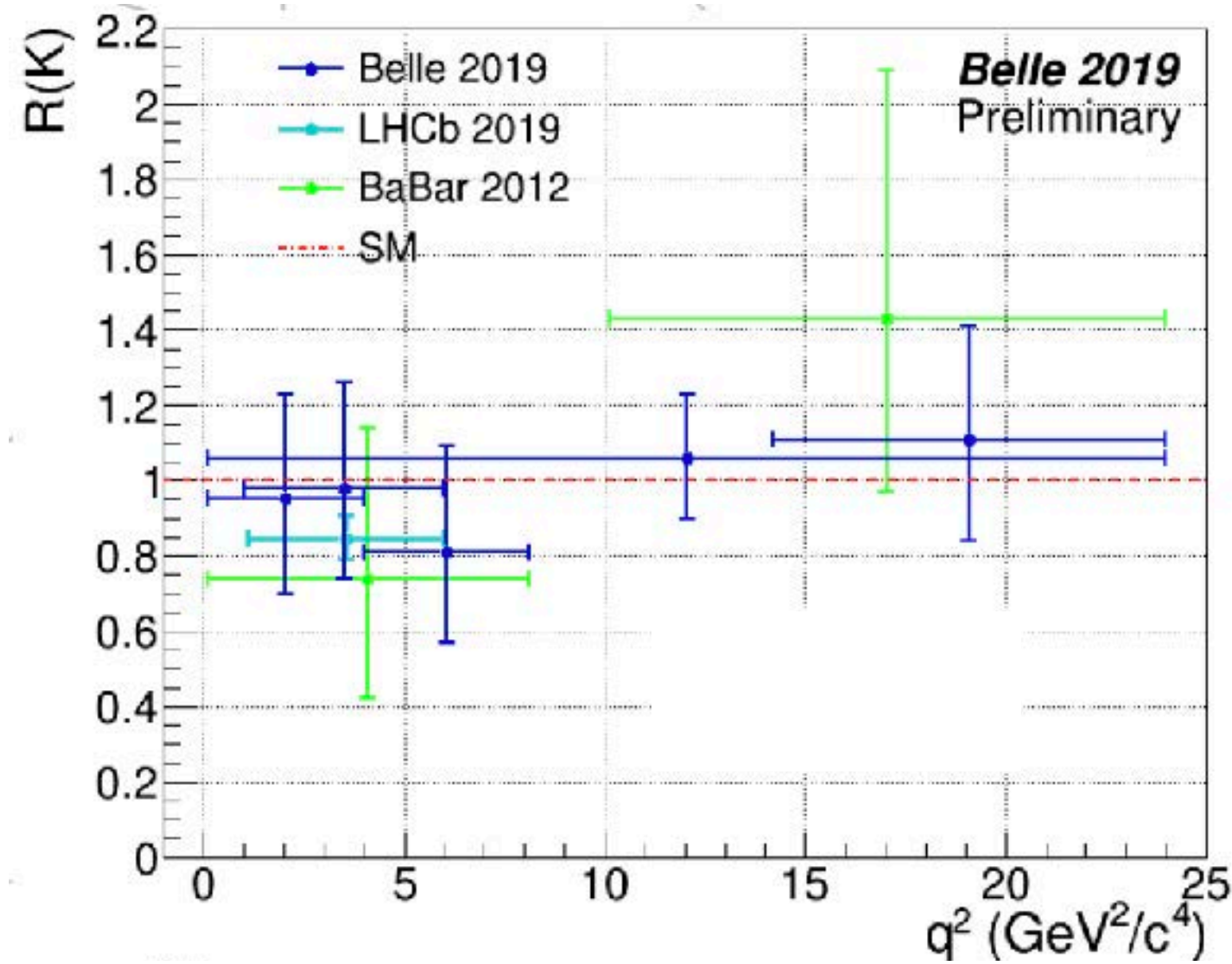
$$R(K^{(*)}) = \frac{\text{BR}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\text{BR}(B \rightarrow K^{(*)} e^+ e^-)}$$



$$\mathcal{B}(B \rightarrow K \ell^+ \ell^-) = \mathcal{O}(10^{-7}), \quad \mathcal{B}(B \rightarrow K^* \ell^+ \ell^-) = \mathcal{O}(10^{-6})$$

$b \rightarrow s\mu^+\mu^-$ anomalies

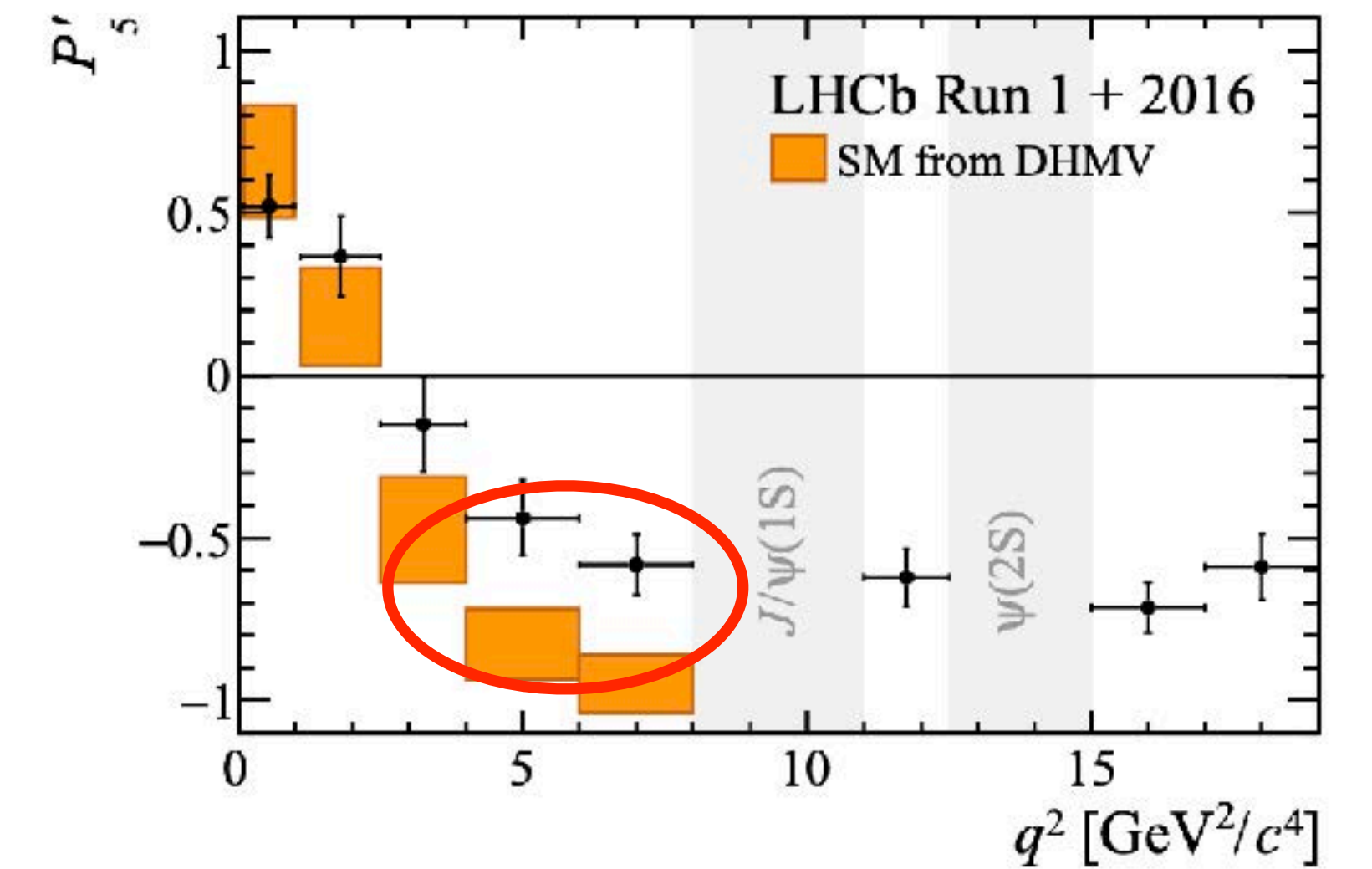
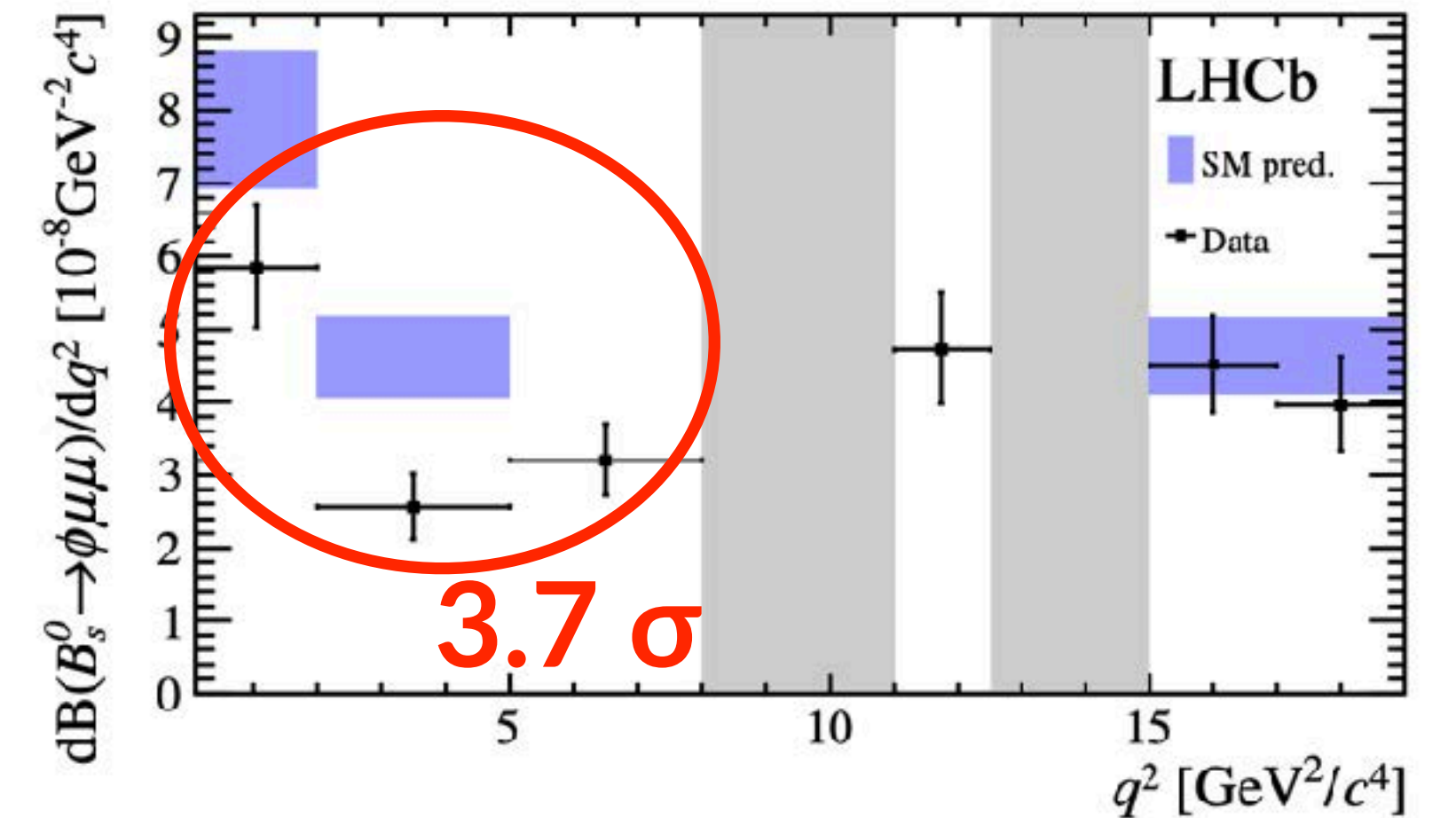
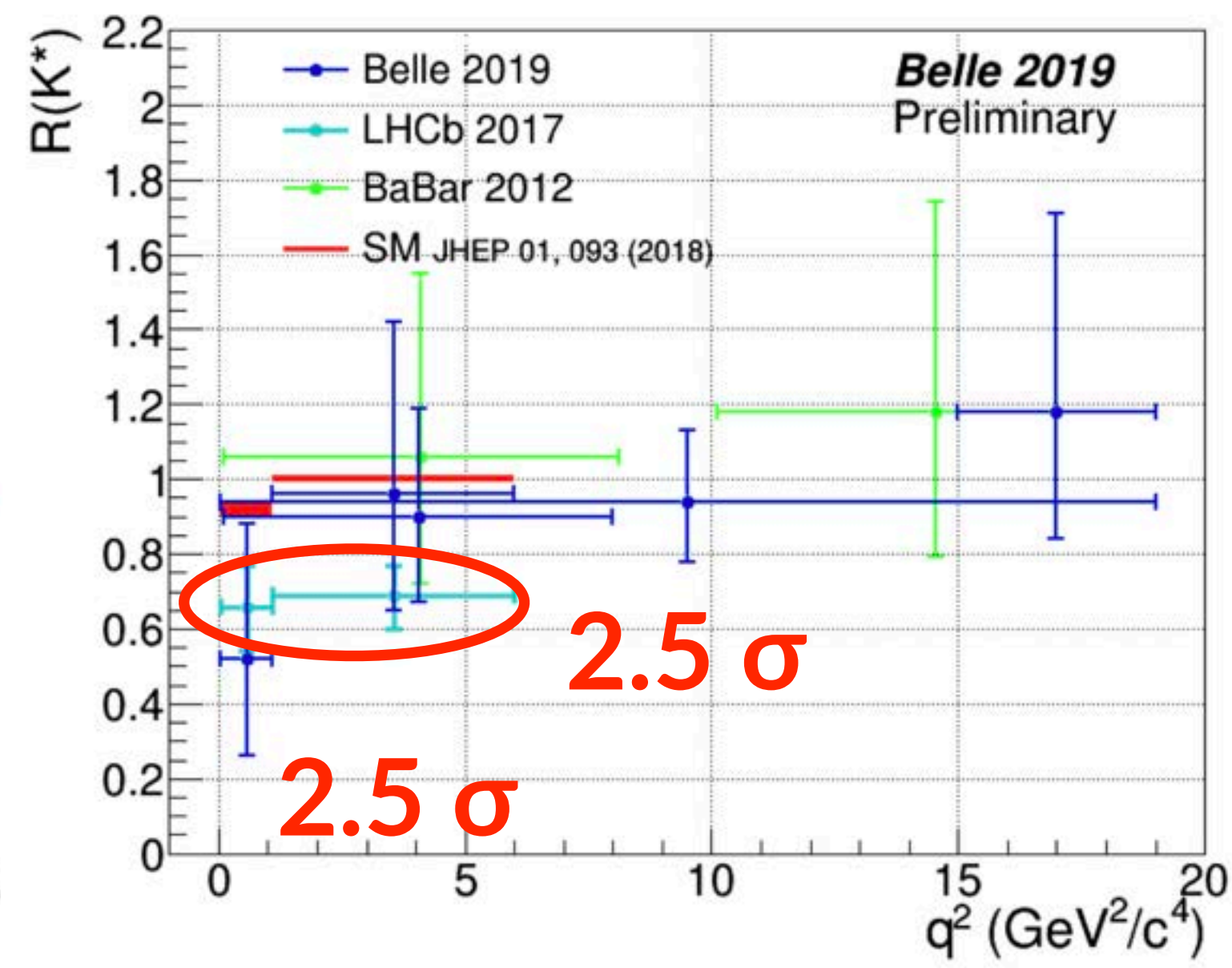
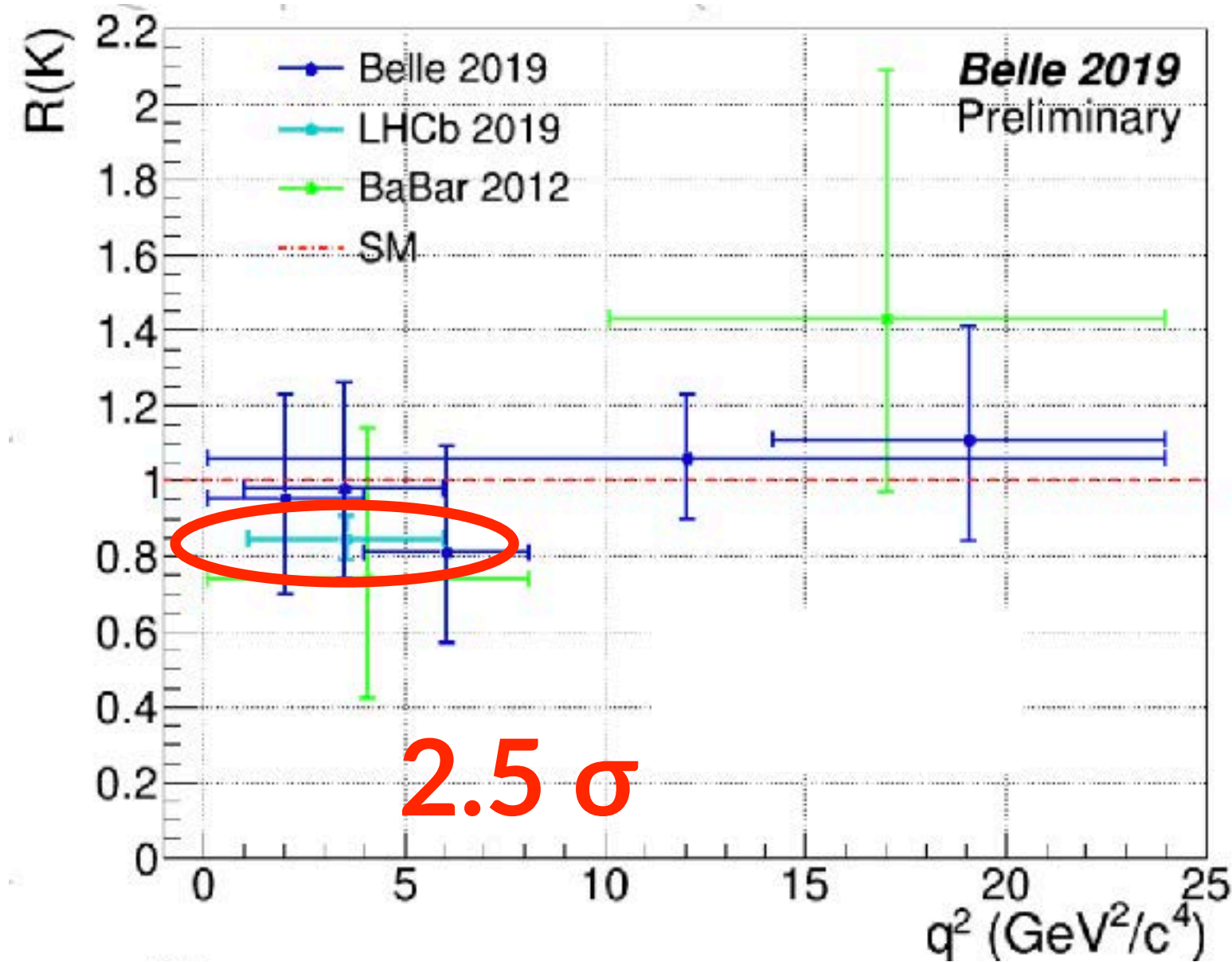
- ◆ In 2019 and 2020, LHCb and Belle presented new results



[LHCb, 2003.04831]

$b \rightarrow s \mu^+ \mu^-$ anomalies

- ◆ In 2019 and 2020, LHCb and Belle presented new results



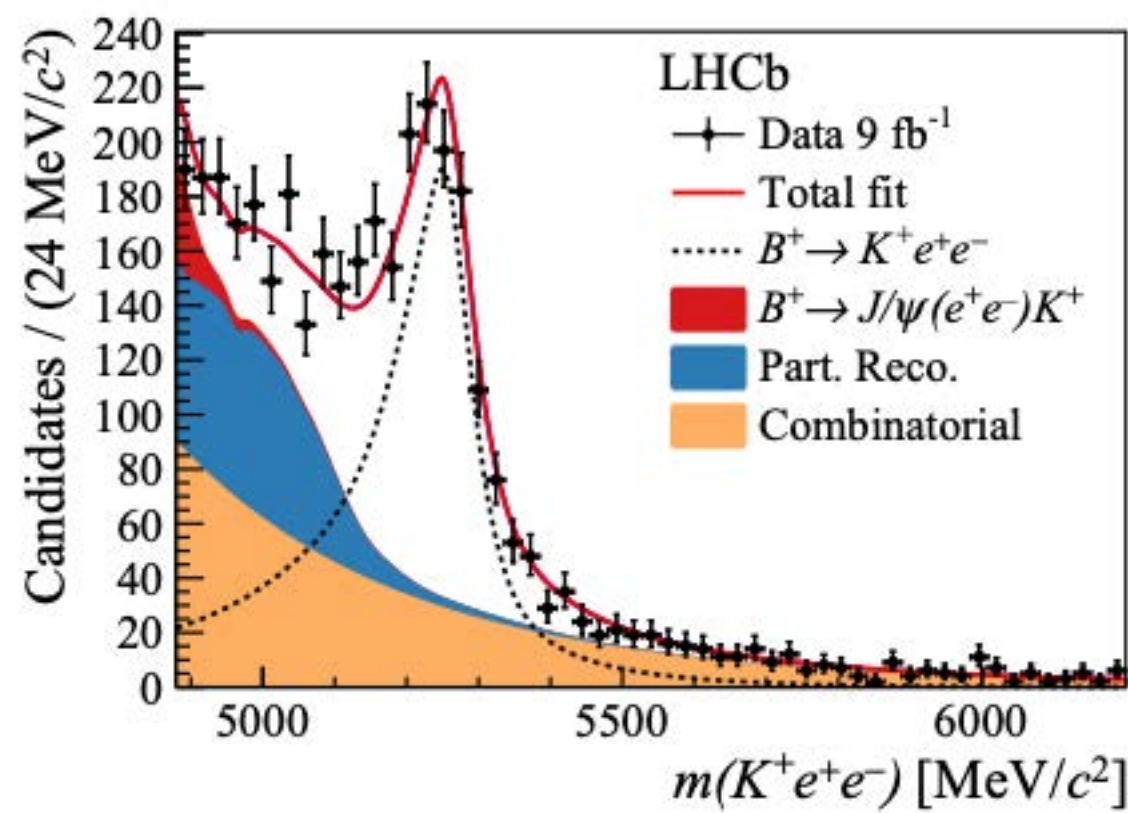
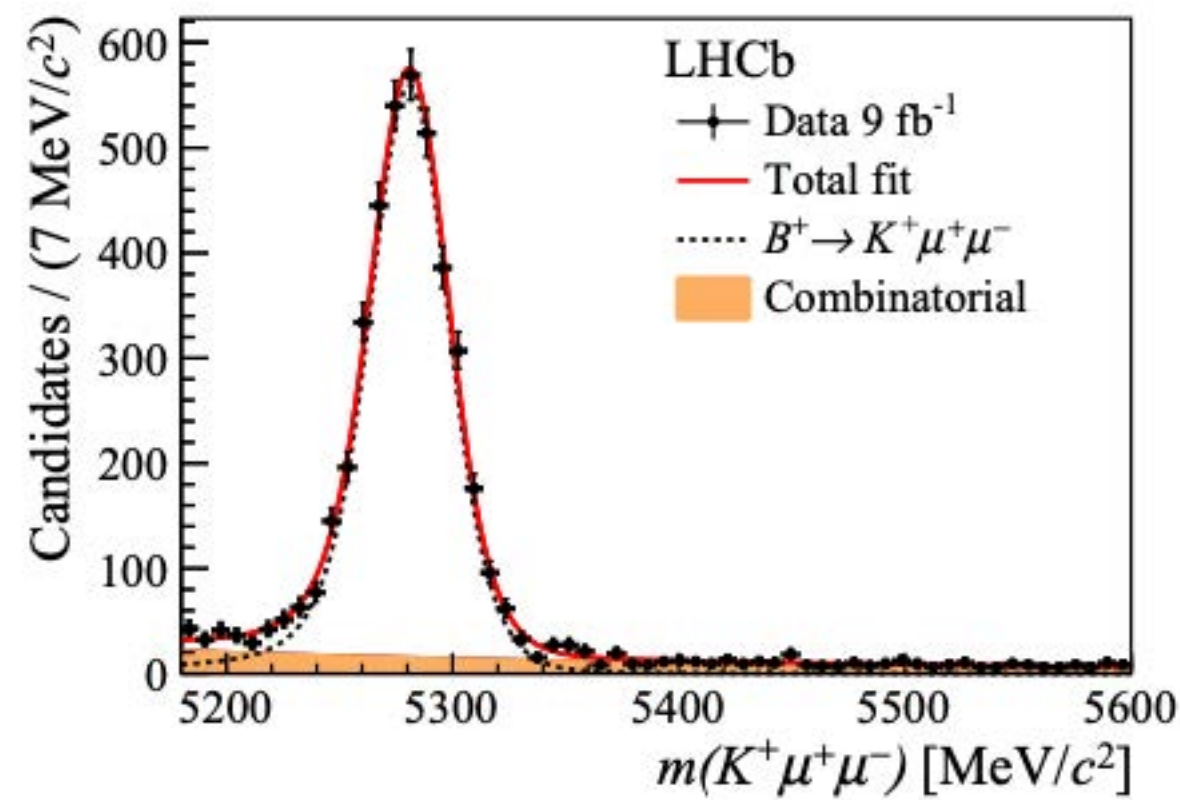
- ◆ Angular distribution of $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ [K_6] is also deviated
at 2.6σ [LHCb, 1808.00264]

[LHCb, 2003.04831]

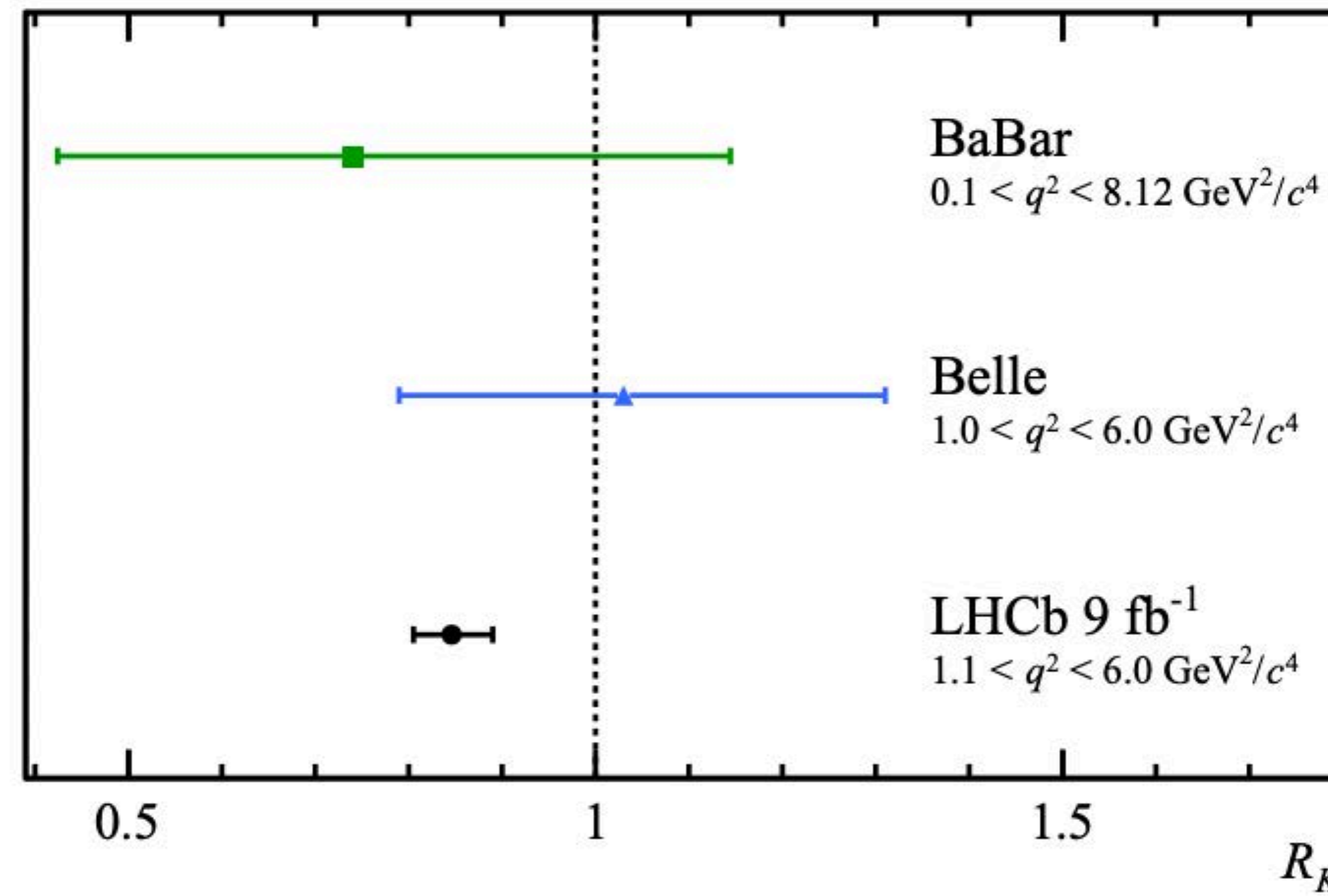
$2.5 \sigma, 2.9 \sigma$

R(K) in Moriond2021

- ◆ Last month, R(K) was confirmed by using full Run 2 data [LHCb Moriond2021, 2103.11769]



$$R_K = 0.846^{+0.042}_{-0.039} \text{ (stat.) } ^{+0.013}_{-0.012} \text{ (syst.)}$$



R(K) only
2.5 σ \rightarrow **3.1 σ**

Including the *look-elsewhere effect* and conservative theoretical error from charm loops, **the global significance of $b \rightarrow s \ell^+ \ell^-$ is 3.9 σ**

[Lancierini, Isidori, Owen, Serra, 2104.05631]

SMEFT global fit

[Geng et al, 2103.12738;
Altmannshofer et al, 2103.13370;
Cornella et al, 2103.16558;
Alguero et al, 2104.08921;
Hurth et al, 2104.10058]

◆ Relevant effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_i C_i \mathcal{O}_i$$

$$\mathcal{O}_7 = (\bar{s}\sigma_{\mu\nu}P_R b) F^{\mu\nu}$$

$$\mathcal{O}_9 = (\bar{s}\gamma_\mu P_L b) (\bar{\ell}\gamma^\mu \ell)$$

$$\mathcal{O}_{10} = (\bar{s}\gamma_\mu P_L b) (\bar{\ell}\gamma^\mu \gamma_5 \ell)$$

$$C_9^{\text{SM}} = 4.1 \quad C_{10}^{\text{SM}} = -4.3$$

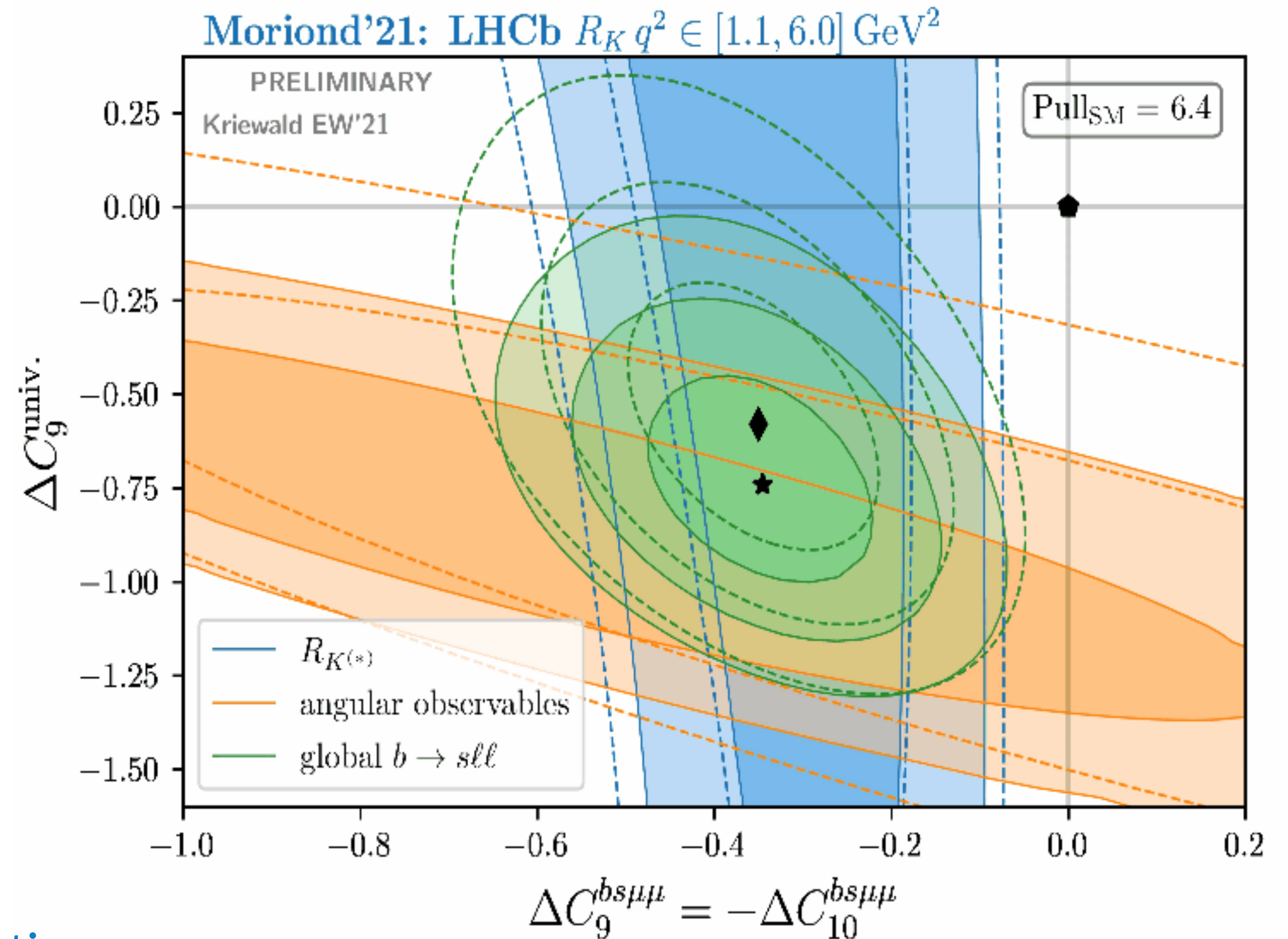
Current best fit: Pull_{SM} = -6.4σ

$$C_9 = -C_{10} = -0.34, C_9^{\text{univ.}} = -0.74$$

➡ $\Lambda_{\text{NP}} = \mathcal{O}(10)\text{TeV}$

All deviations in $b \rightarrow s\mu^+\mu^-$ are the same direction

[Kriewald, Hat, Orloff, Teixeira, 2104.00015]

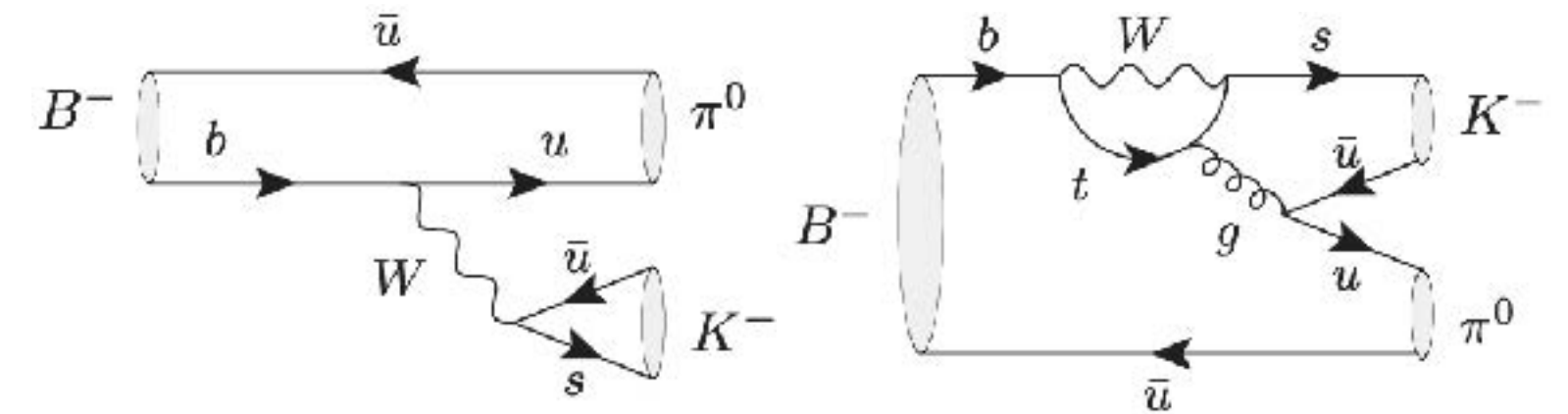


“ $K\pi$ puzzle”: Direct CPV in $B \rightarrow K\pi$ modes

- ◆ Direct CP asymmetry is obtained by

$$A_{CP} = \frac{\Gamma(\bar{B} \rightarrow \bar{f}) - \Gamma(B \rightarrow f)}{\Gamma(\bar{B} \rightarrow \bar{f}) + \Gamma(B \rightarrow f)}$$

- ◆ The difference between two direct CP asymmetries [note that $\mathcal{B}(B \rightarrow K\pi) = \mathcal{O}(10^{-5})$]



$$\Delta A_{CP}(K\pi) = A_{CP}(B^+ \rightarrow \pi^0 K^+) - A_{CP}(B^0 \rightarrow \pi^- K^+) = 0 \text{ @ SM leading order}$$

All data are **in agreement with** each other

$$\Delta A_{CP}|_{\text{SM}}(K\pi) = (1.8_{-3.2}^{+4.1}) \%$$

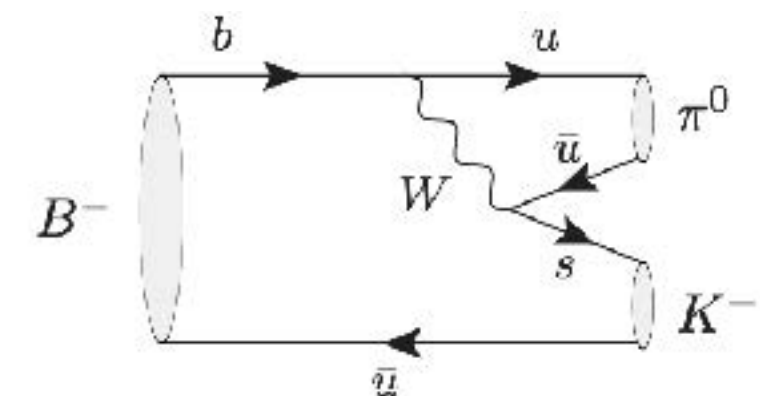
[Hofer, Scherer, Vernazza, JHEP '11;
Crivellin, Gross, Pokorski, Vernazza, PRD '20]

2.2 σ tension



$$\Delta A_{CP}|_{\text{exp}}(K\pi) = (11.5 \pm 1.4) \% \quad [\text{Moriond 2021 average}]$$

SM explanation can be possible, if this HME is bigger than the NLO prediction by a factor of 2
[Li, Mishima, PRD '11; Beaudry, Datta, London, Rashed, Roux, JHEP '18]



$$A_{CP}|_{\text{BaBar}}(B^+ \rightarrow \pi^0 K^+) = (3.0 \pm 3.9 \pm 1.0) \%$$

$$A_{CP}|_{\text{Belle}}(B^+ \rightarrow \pi^0 K^+) = (4.3 \pm 2.4 \pm 0.2) \%$$

New! $A_{CP}|_{\text{LHCb}}(B^+ \rightarrow \pi^0 K^+) = (2.4 \pm 1.5 \pm 0.7) \%$

$$A_{CP}|_{\text{BaBar}}(B^0 \rightarrow \pi^- K^+) = (-10.7 \pm 1.6_{-0.4}^{+0.6}) \%$$

$$A_{CP}|_{\text{Belle}}(B^0 \rightarrow \pi^- K^+) = (-6.9 \pm 1.4 \pm 0.7) \%$$

$$A_{CP}|_{\text{CDF}}(B^0 \rightarrow \pi^- K^+) = (-8.3 \pm 1.3 \pm 0.4) \%$$

$$A_{CP}|_{\text{LHCb}}(B^0 \rightarrow \pi^- K^+) = (-8.4 \pm 0.4 \pm 0.3) \%$$



V_{us} vs unitarity

$$K_L \rightarrow \pi^- \ell^+ \nu$$
$$K^+ \rightarrow \ell^+ \nu$$

ϵ_K and ϵ'

RBC-UKQCD

$$K_L \rightarrow \pi\pi$$



B physics

CORRELATION

FCNC and/or CPV

$$K^0 \rightarrow \mu^+ \mu^-$$



Understanding of ChPT

$$K_S \rightarrow \pi^0 \mu^+ \mu^-$$
$$K_S \rightarrow \mu^+ \mu^- \gamma$$
$$K_S \rightarrow 4\ell$$
$$K_S \rightarrow \pi^+ \pi^- e^+ e^-$$



Reduce the error

$$K \rightarrow \pi \nu \bar{\nu}$$



$$K_L \rightarrow \pi^0 \ell^+ \ell^-$$

$$K \rightarrow \pi X$$

Direct CP violation in $K_L \rightarrow \pi\pi$

- ◆ Precise measurements of Kaon to two pions have discovered the two type of CP violations:

indirect CPV ε_K & direct CPV ε'

$$A(K_L \rightarrow \pi^+\pi^-) \propto \varepsilon_K + \varepsilon' \quad \text{with } \varepsilon_K = \mathcal{O}(10^{-3}) \neq 0 \quad [\text{Christenson, Cronin, Fitch, Turlay, PRL '64}]$$

$$A(K_L \rightarrow \pi^0\pi^0) \propto \varepsilon_K - 2\varepsilon' \quad \varepsilon' = \mathcal{O}(10^{-6}) \neq 0 \quad [\text{NA48/CERN and KTeV/FNAL '99}]$$

Isospin decomposition $I=0$ $I=2$

$$\text{Re} \left[\frac{\varepsilon'_K}{\varepsilon_K} \right] \simeq \frac{1}{6} \frac{|\eta_{+-}|^2 - |\eta_{00}|^2}{|\eta_{+-}|^2} = \frac{1}{6} \left(1 - \frac{\frac{\text{Br}(K_L \rightarrow \pi^0\pi^0)}{\text{Br}(K_S \rightarrow \pi^0\pi^0)}}{\frac{\text{Br}(K_L \rightarrow \pi^+\pi^-)}{\text{Br}(K_S \rightarrow \pi^+\pi^-)}} \right) \begin{array}{l} \text{data} \\ \text{PDG average} \end{array} = (16.6 \pm 2.3) \times 10^{-4}$$

$\text{Re}(\varepsilon'/\varepsilon_K)$ has been measured very precisely using the double ratio of branching ratios

On the other hand, theoretical estimation is difficult due to non-perturbative QCD

$$\eta_{00} \equiv \frac{\mathcal{A}(K_L \rightarrow \pi^0\pi^0)}{\mathcal{A}(K_S \rightarrow \pi^0\pi^0)}$$

$$\eta_{+-} \equiv \frac{\mathcal{A}(K_L \rightarrow \pi^+\pi^-)}{\mathcal{A}(K_S \rightarrow \pi^+\pi^-)}$$

ε_K discrepancy?

- ◆ SM prediction of the indirect CP violation ε_K is sensitive to $|V_{cb}|$

$$\varepsilon_K = \varepsilon_K(\text{SD}) + \varepsilon_K(\text{LD})$$

$$\varepsilon_K(\text{LD}) = -3.6(2.0)\% \times \varepsilon_K(\text{SD})_{\text{SM}}$$

[Buras, Guadagnoli, Isidori, '10]

[Brod, Gorbahn, PRL '12]

$$\varepsilon_K(\text{SD}) \propto \text{Im}\lambda_t [-\text{Re}\lambda_t \eta_{tt} S_0(x_t) + (\text{Re}\lambda_t - \text{Re}\lambda_c) \eta_{ct} S_0(x_c, x_t) + \text{Re}\lambda_c \eta_{cc} S_0(x_c)]$$

$$\simeq \bar{\eta} \lambda^2 |V_{cb}|^2 [|V_{cb}|^2 (1 - \bar{\rho}) \eta_{tt} S_0(x_t) + \eta_{ct} S_0(x_c, x_t) - \eta_{cc} S_0(x_c)]$$

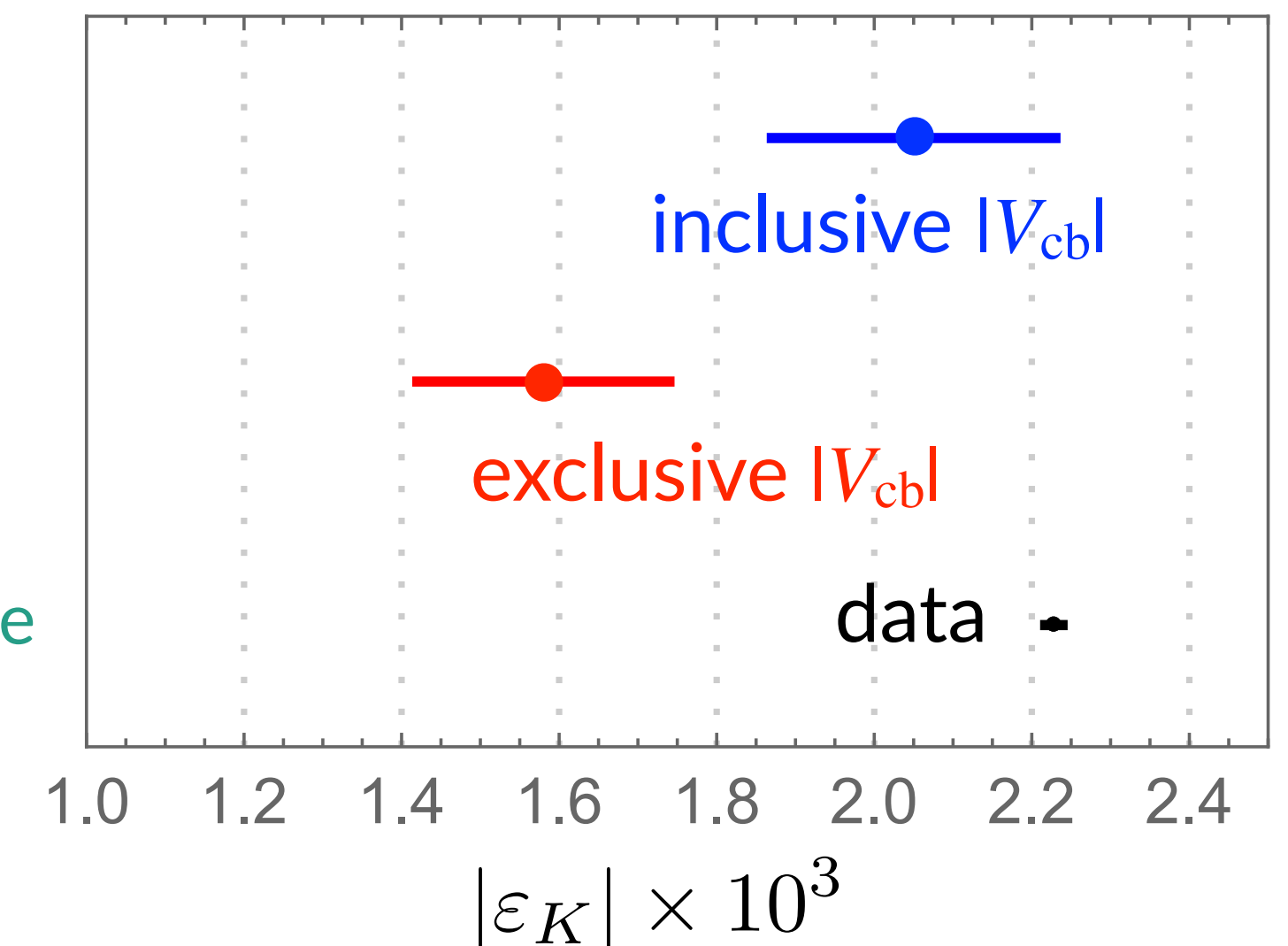
errors are dominated by V_{cb} ,
 $\bar{\eta}$, η_{ct} , η_{cc}

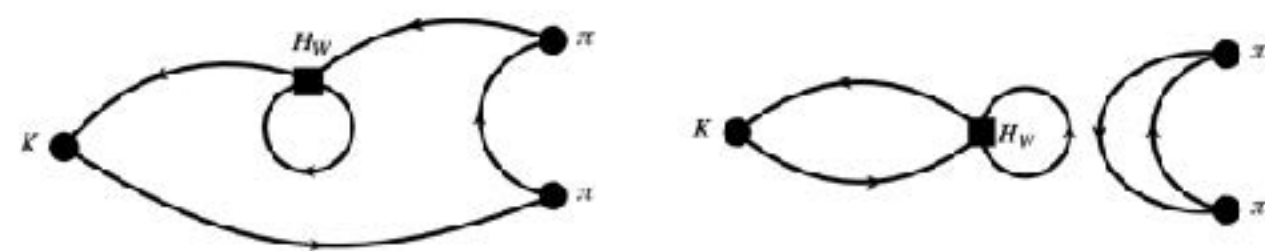
Leading contribution is proportional to $|V_{cb}|^4$

~4.2 σ tension in exclusive $|V_{cb}|$ case

[LANL-SWME, 1912.03024, Wolfenstein parameters are determined by the angle-only fit]

Kaon physics prefers the inclusive V_{cb}





The latest situation of ϵ'/ϵ anomaly

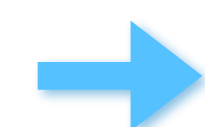
RBC-UKQCD (Lattice) '15

RBC-UKQCD 2004.09440

Data

$$(\epsilon'/\epsilon_K)_{\text{SM}} = (1.4 \pm 5.2 \pm 4.6) \times 10^{-4}$$

stat. sys.



$$(\epsilon'/\epsilon_K)_{\text{SM}} = (21.7 \pm 2.6 \pm 6.2 \pm 5.0) \times 10^{-4}$$

stat. sys. IB-sys.

$$(\epsilon'/\epsilon_K)_{\text{exp}} = (16.6 \pm 2.3) \times 10^{-4}$$

2.9 σ shift

Underestimated the sys. error

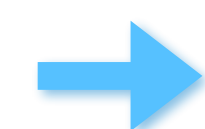
Buras, Gérard 2005.08976

$$(\epsilon'/\epsilon_K)_{\text{SM}} = (13.9 \pm 5.2) \times 10^{-4}$$

+NNLO, η'

$I=0$ $\pi\pi$ phase shift

$$\delta_0(m_K) = (23.8 \pm 4.9 \pm 1.2)^\circ$$



$$\delta_0(E_{\pi\pi}^{\text{lat}} = 479 \text{ MeV}) = (32.3 \pm 1.0 \pm 1.8)^\circ$$

$$\delta_{0,\text{disp.}} = 35.9^\circ$$

1.7 σ shift

$\Delta I = 1/2$ rule

$$\text{Re}(A_0)/\text{Re}(A_2) = 31.0 \pm 11.1$$



$$\text{Re}(A_0)/\text{Re}(A_2) = 19.9 \pm 2.3 \pm 4.4$$

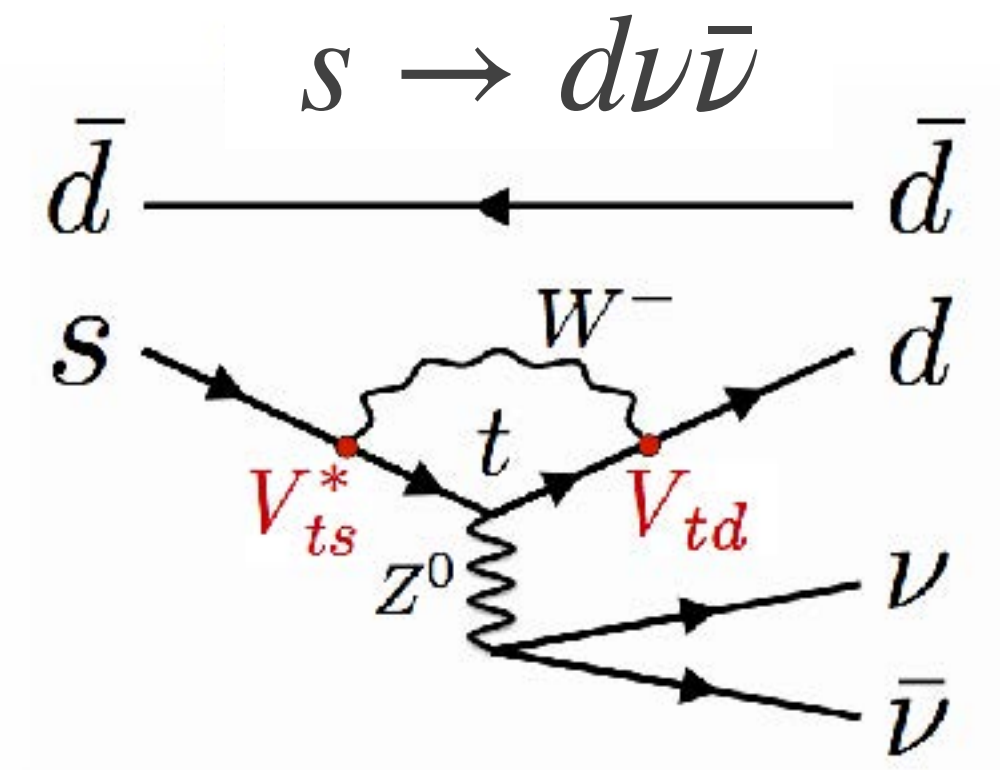
$$\text{Re}(A_0)/\text{Re}(A_2) = 22.45 \pm 0.06$$

1.0 σ shift

Now, all lattice results are consistent with data

$K_L \rightarrow \pi^0 \nu \bar{\nu}$ and $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

- ◆ Both channels are theoretical clean and significantly sensitive to short-distance contributions, **especially $K_L \rightarrow \pi^0 \nu \bar{\nu}$ is purely CPV decay**
(almost) CP-odd \rightarrow CP-even in SM, see [Buchalla, Isidor, PLB '98]
- ◆ **Sensitive to CPV in NP sector**
- ◆ **SM predictions:** [Buras, Buttazzo, Girrbach-Noe, Kneijens, JHEP '15]



loop, GIM, and small CKM

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})_{\text{SM}} = (8.4 \pm 1.0) \times 10^{-11}, \quad \text{c.f.} \quad \mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.65 \pm 0.23) \times 10^{-9}$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})_{\text{SM}} = (3.4 \pm 0.6) \times 10^{-11}. \quad \mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)_{\text{SM}} = (1.06 \pm 0.09) \times 10^{-10}$$

- ◆ On-going experiments:



K_L
@J-PARC

SM event is expected
in ~2024

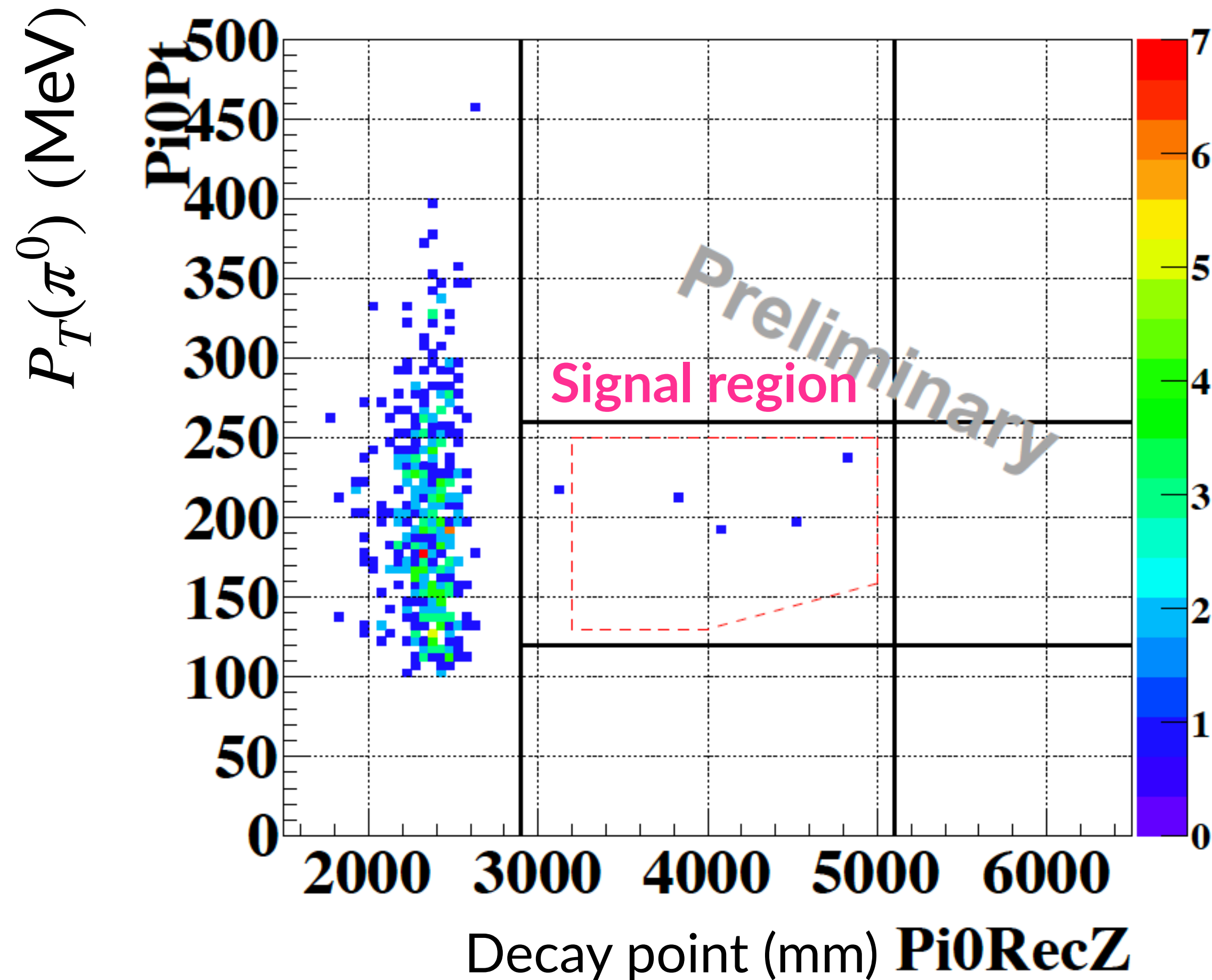


K^+
@CERN

20 SM events are
expected in 2016-18 runs

KOTO@KAON2019

[KOTO, KAON2019; 2016-18 data]



[KOTO, 1810.09655; 2015 data]

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 3.0 \times 10^{-9} \text{ at } 90\% \text{CL}$$

# of events	4 (3)
Single event sensitivity	6.9×10^{-10}
Expected BG	0.05±0.02
Expected SM	0.05±0.01

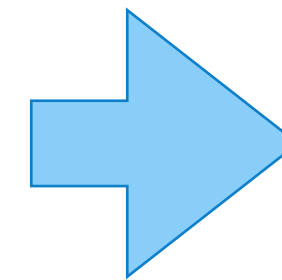
1 in 4 events is suspected that a peak selection was **mistaken** due to a wrong parameter

KOTO was planning to re-evaluate other BG sources, especially K^+ (special run for BG in May–Jun) **[done]**

KOTO@ICHEP2020 + JPS2020Fall + PRL '21

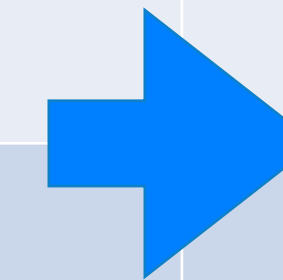
[KOTO, KAON2019]

# of events	4 (3)
Single event sensitivity	6.9×10^{-10}
Expected BG	0.05 ± 0.02
Expected SM	0.05 ± 0.01



[KOTO, ICHEP2020]

3	
7.1×10^{-10}	
0.39 ± 0.10	1.05 ± 0.28
0.05 ± 0.01	

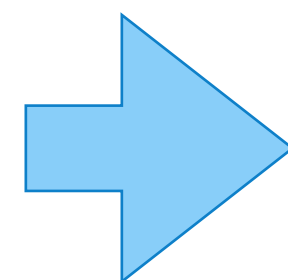


×8 [New K^+ BG]

Based on MC simulation of K^+ before the special run

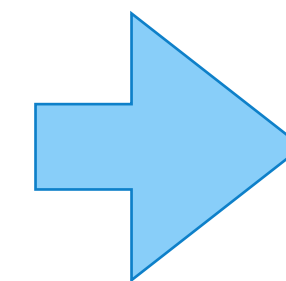
×3 [calibrate K^+ flux]
Based on the special run for K^+

[KOTO, JPS2020Fall]



3
7.2×10^{-10}
1.21 ± 0.25
0.05 ± 0.01

[New halo $K_L \rightarrow 2\gamma$ BG] added



[KOTO, PRL '21]

3
7.2×10^{-10}
1.22 ± 0.26
0.05 ± 0.01

“observed events is statistically consistent with the background expectation”

CONGRATULATIONS!

Cabibbo angle anomaly

- ◆ Kaon measurements can determine the Cabibbo angle: $|V_{us}| \equiv \lambda$

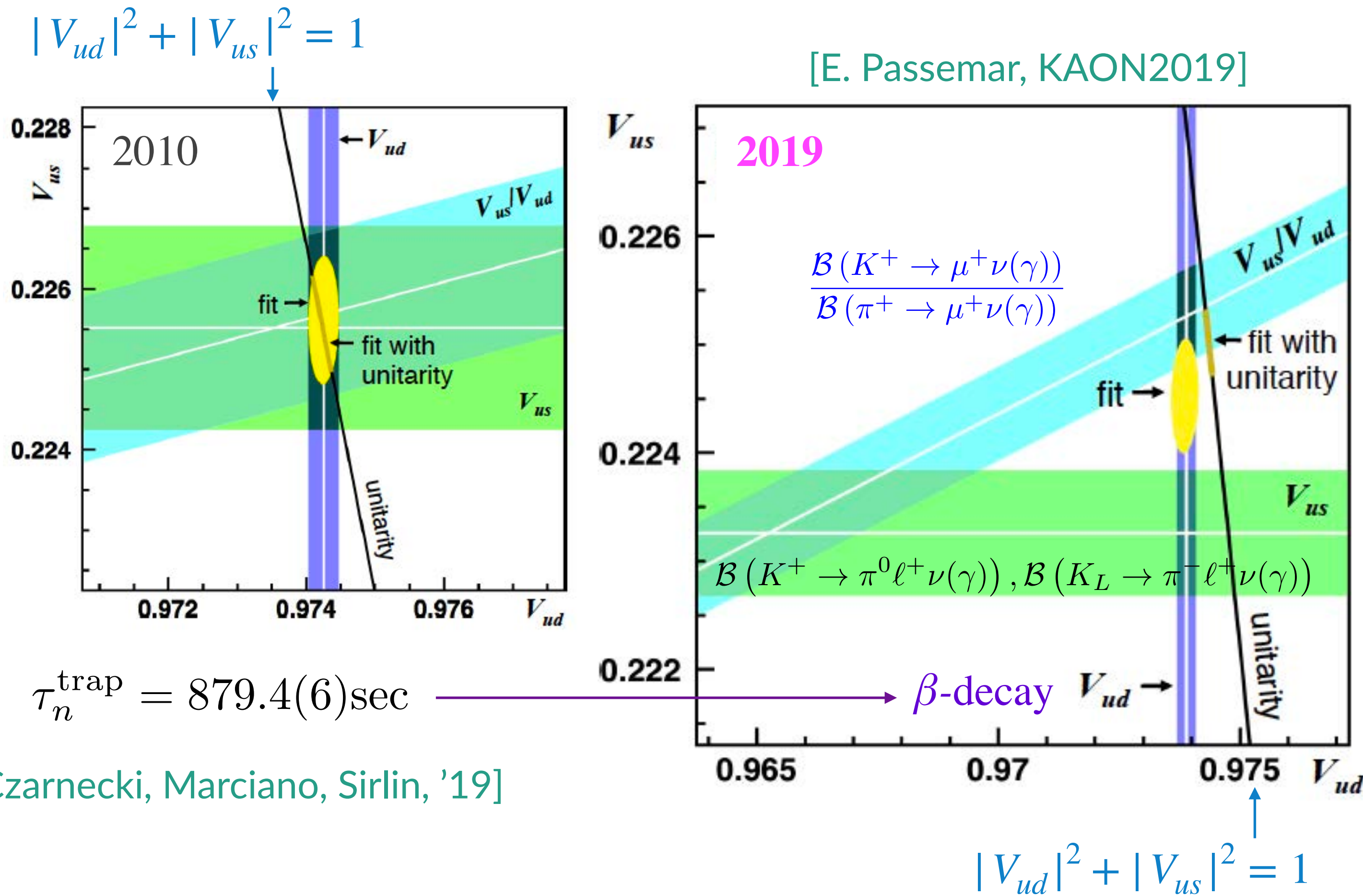
$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

K physics B physics



- ◆ CKM unitarity: $V^\dagger V = 1 \rightarrow |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1 \rightarrow |V_{ud}|^2 + |V_{us}|^2 = 1$
 $\sim 1.4 \times 10^{-5}$
- ◆ Now, one can check this equality from precision data

Cabibbo angle anomaly: V_{ud} , V_{us} vs. CKM unitarity (1/2)



$$\tau_n^{\text{trap}} = 879.4(6)\text{sec}$$

[Czarnecki, Marciano, Sirlin, '19]

[Grossman, Passemar, Schacht, JHEP '20]

quantifies this situation:

CKM unitarity is **rejected at 3.0σ** , and new physics is favored over the SM **at 3.6σ level**.

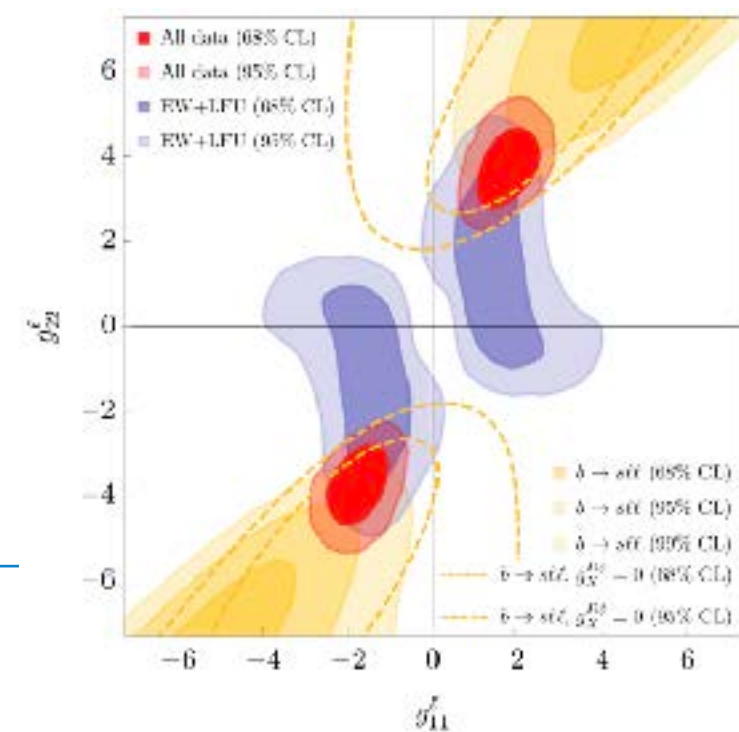
New physics interpretations:

$(\bar{L}\gamma^\mu\tau^I L)(H^\dagger \overset{\leftrightarrow}{D}_\mu^I H)$ [Coutinho, Crivellin, Manzari, PRL '20]

Vector-like leptons (2TeV) [Endo, Mishima, '20]

Heavy $SU(2)_L$ (10TeV) [Capdevila et al, '20]

Cabbie angle anomaly
 $b \rightarrow s\ell\ell$ anomaly



Cabibbo angle anomaly: V_{ud} , V_{us} vs. CKM unitarity (1/2)

◆ What's happened in the last ten years?

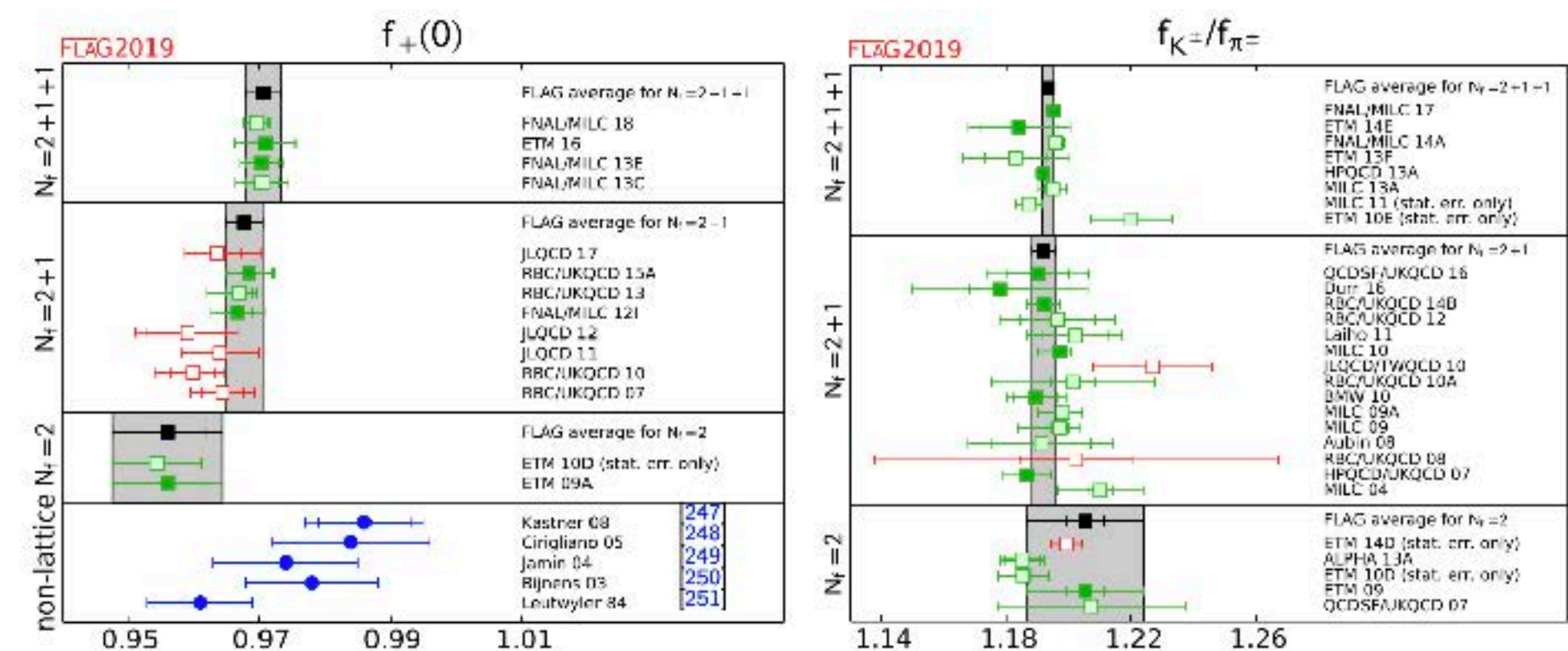
◆ Lattice results [FLAG, 1902.08191]

◆ New data [NA48/2, 1808.09041; OKA, 1708.09587]

◆ Isospin breaking corrections are improved [Cirigliano, Neufeld, PLB '11; Bijmans, Ecker, ARNPS '14]

◆ QED corrections to β decay are improved [Czarnecki, Marciano, Sirlin, PRD '19; Seng, Gorchtein, Ramsey-Musolf, PRD '19]

◆ QCD+QED lattice [Sachrajda, et al, PRL '18; PRD '19]: the result is consistent with one which was obtained analytically and the error is reduced (chiral expansion error vs. lattice error)



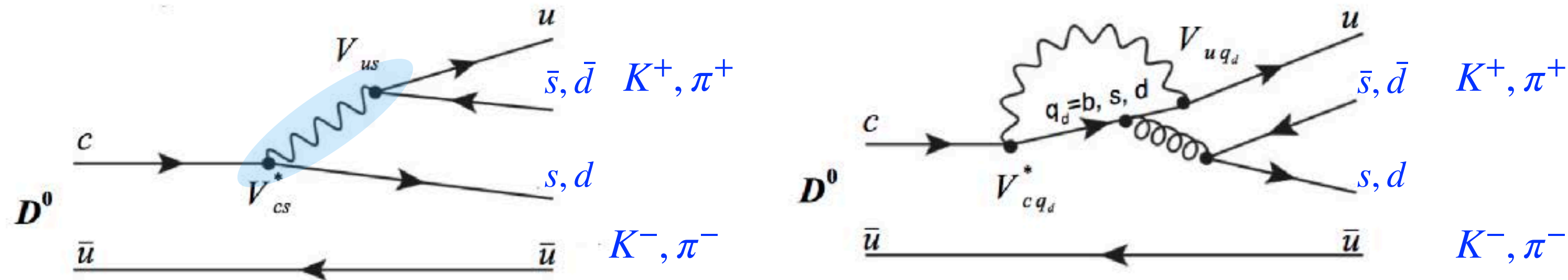


The first observation of CPV in D -meson

- ◆ Difference of Difference of $D^0 \rightarrow h^- h^+$ and $\bar{D}^0 \rightarrow h^- h^+$

Direct CPV $A_{CP}(D^0 \rightarrow K^- K^+) \equiv \frac{\#(D^0(t=0) \rightarrow K^- K^+) - \#(\bar{D}^0(t=0) \rightarrow K^- K^+)}{\#(D^0(t=0) \rightarrow K^- K^+) + \#(\bar{D}^0(t=0) \rightarrow K^- K^+)}$

Observable $\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^- K^+) - A_{CP}(D^0 \rightarrow \pi^- \pi^+)$



The Direct CPV is *amplified* in the difference! $V_{cd} : V_{us} \simeq -1 : 1$

Detection asymmetry and final-state independent uncertainty are completely dropped!

Direct CP violation in D

Latest result [LHCb, 1903.08726]

$$\Delta a_{CP}^{dir} = (-15.7 \pm 2.9) \times 10^{-4} \quad 5.3\sigma \text{ discovery of CPV!}$$

but, need confirmation by Belle II

A reliable SM prediction [QCD sum rule]

$$|\Delta a_{CP}^{dir}| < (2.0 \pm 0.3) \times 10^{-4} \quad [\text{Khodjamirian, Petrov, '17}]$$

Smaller than the data by a factor of 7; 4.7 σ tension

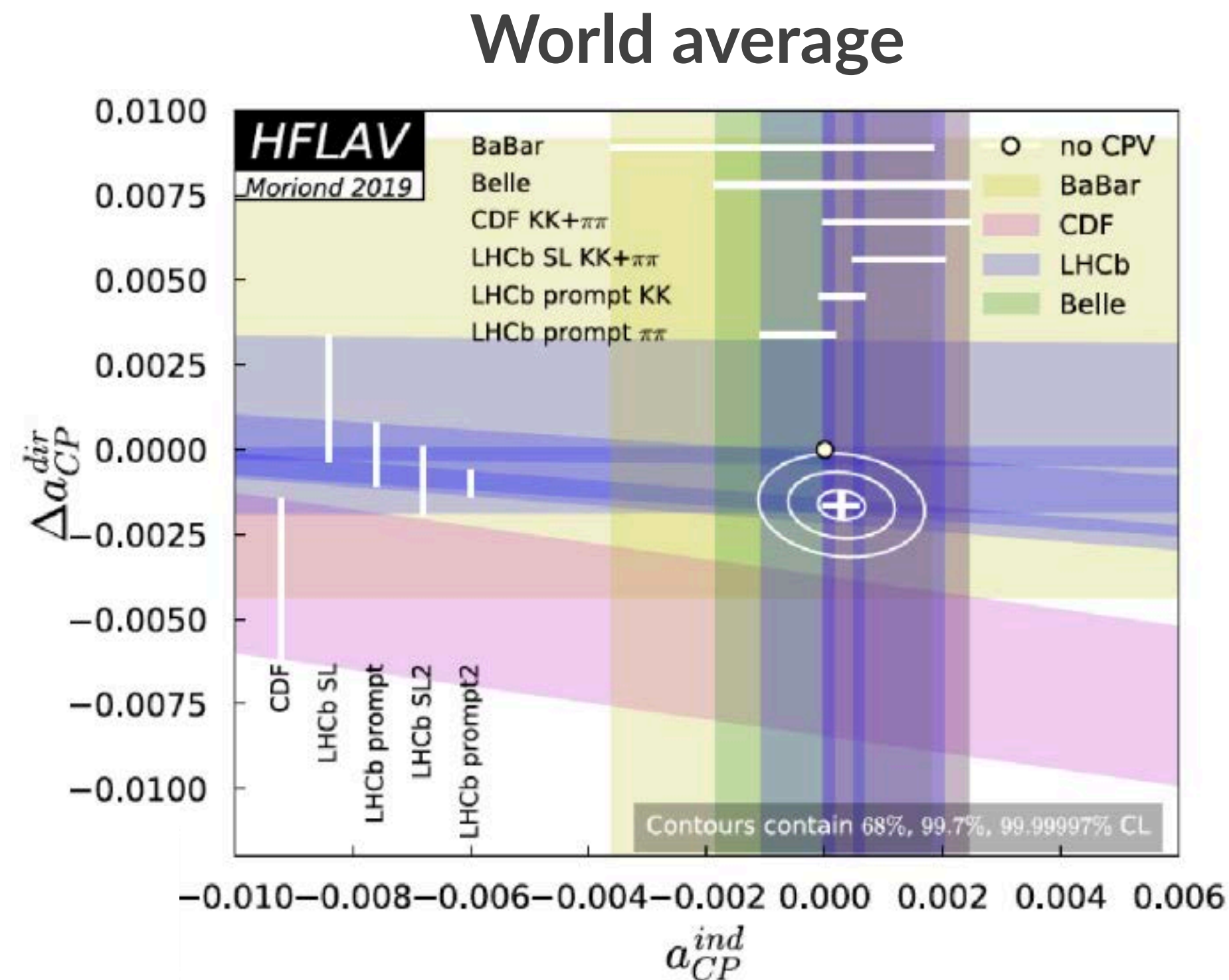
(QCD sum rule works well in B physics)

SM explanation could be possible by QCD re scattering

$$D^0 \rightarrow \pi\pi \rightarrow K^-K^+ \quad [\text{Grossman, FPCP2020}]$$

New physics implications; 2HDM, MSSM, vector-like quark

[Dery, Nir, '19]



B anomaly + muon $g-2$ anomaly = ?

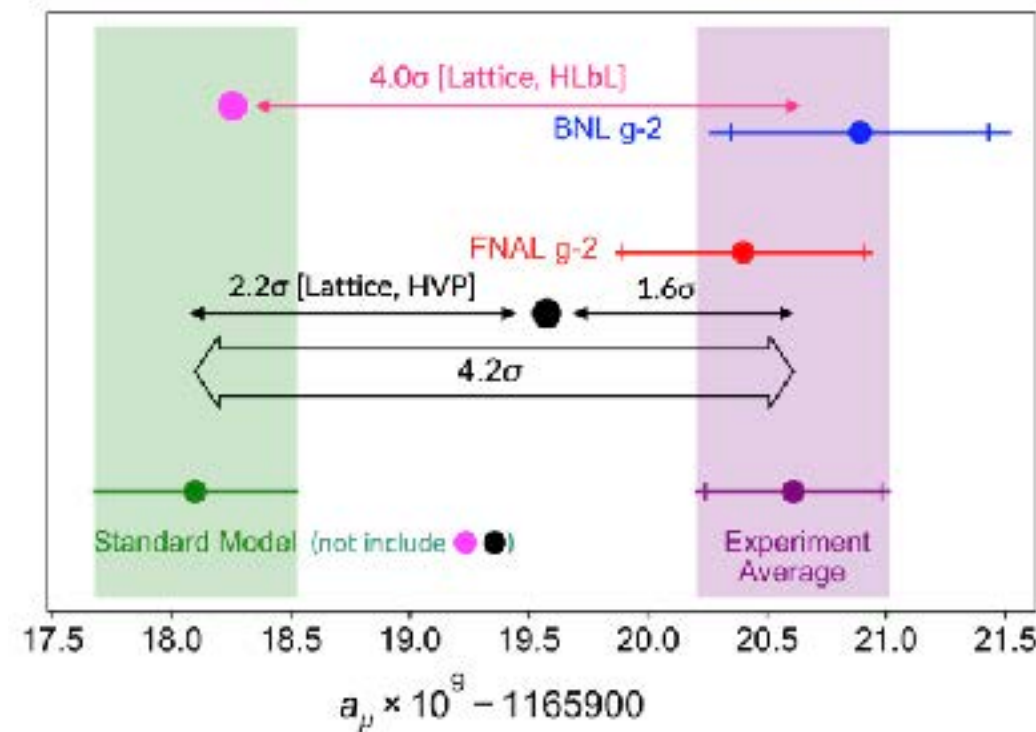
($B + \text{muon } g-2$) anomaly =?

◆ I found 5 scenarios (6 papers)

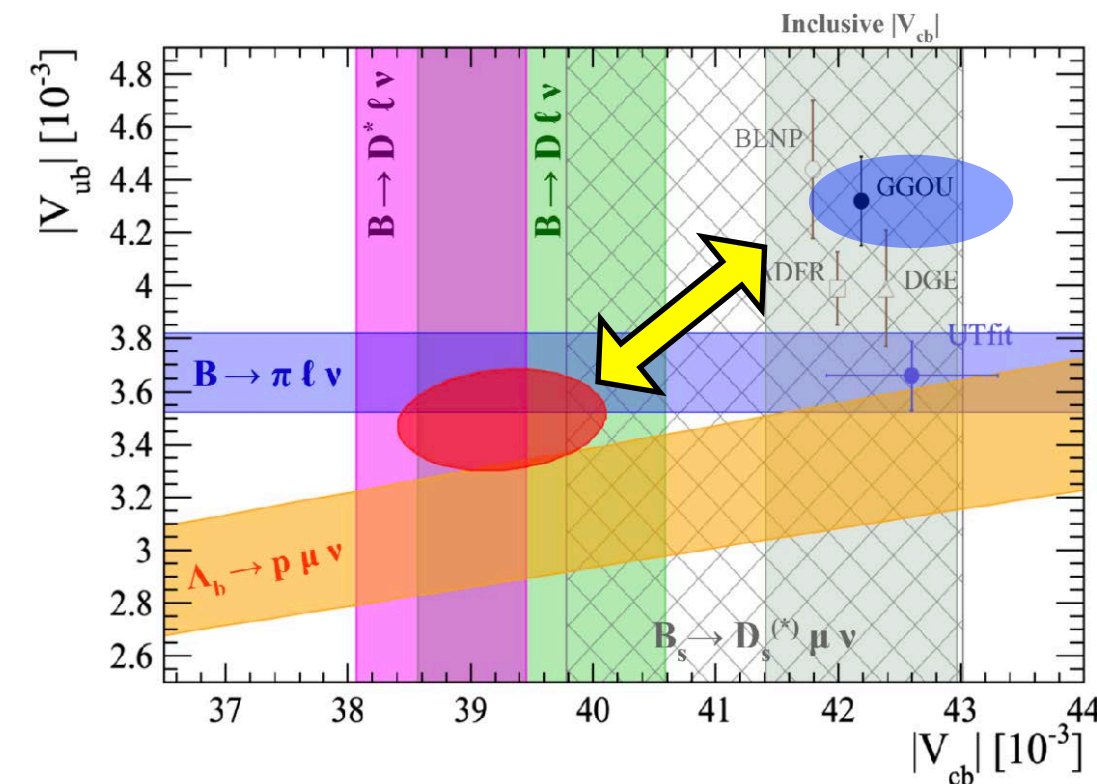
Refs	particles	solve	mass scale
Arcadi et al, 2104.03228	Vector-like fermion + scalars	muon $g-2$, $R(K)$, DM	0.1~1 TeV VL
Nomura, Okada 2104.03248	Scalar LQs	muon $g-2$, $R(K)$, m_ν	~5 TeV LQ
Bhattacharya et al, 2104.03947	ALP	muon $g-2$, $K\pi$ puzzle	~140 MeV ALP
Marzocca, Trifinopoulos, 2104.05730	Scalar LQ + scalar	muon $g-2$, $R(K)$, $R(D)$, CAA	~5 TeV LQ
Du et al, 2104.05685; Ban et al, 2104.06656	Vector LQ	muon $g-2$, $R(K)$, $R(D)$	~2 TeV LQ

Summary of anomalies –which is the truth?–

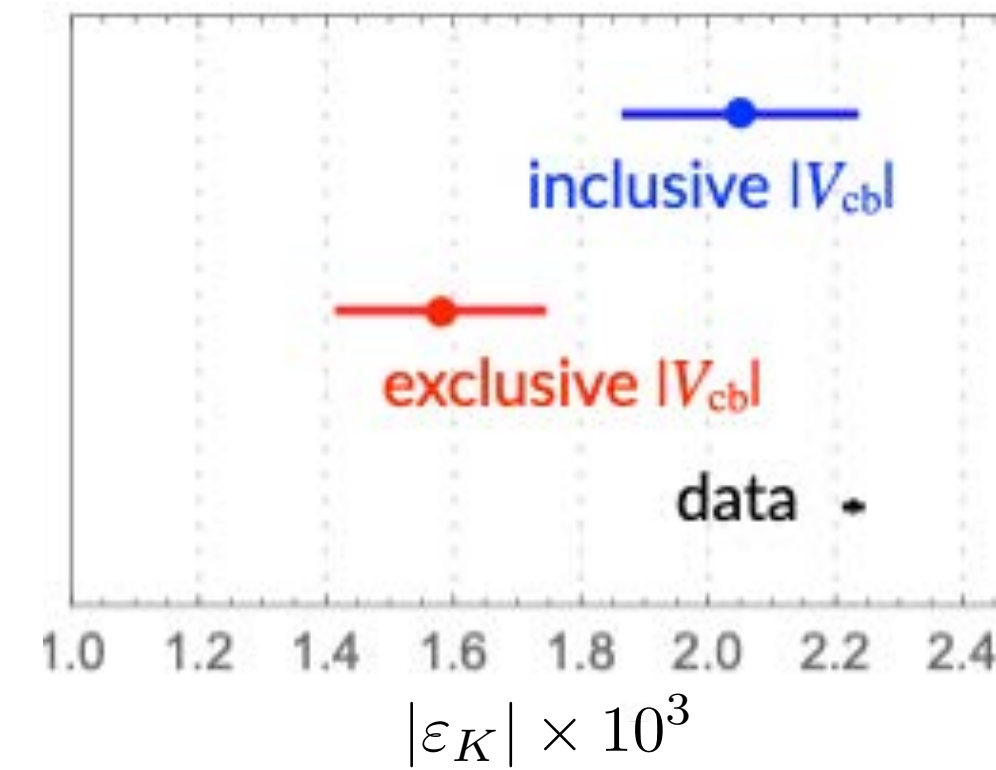
4.2 σ ?



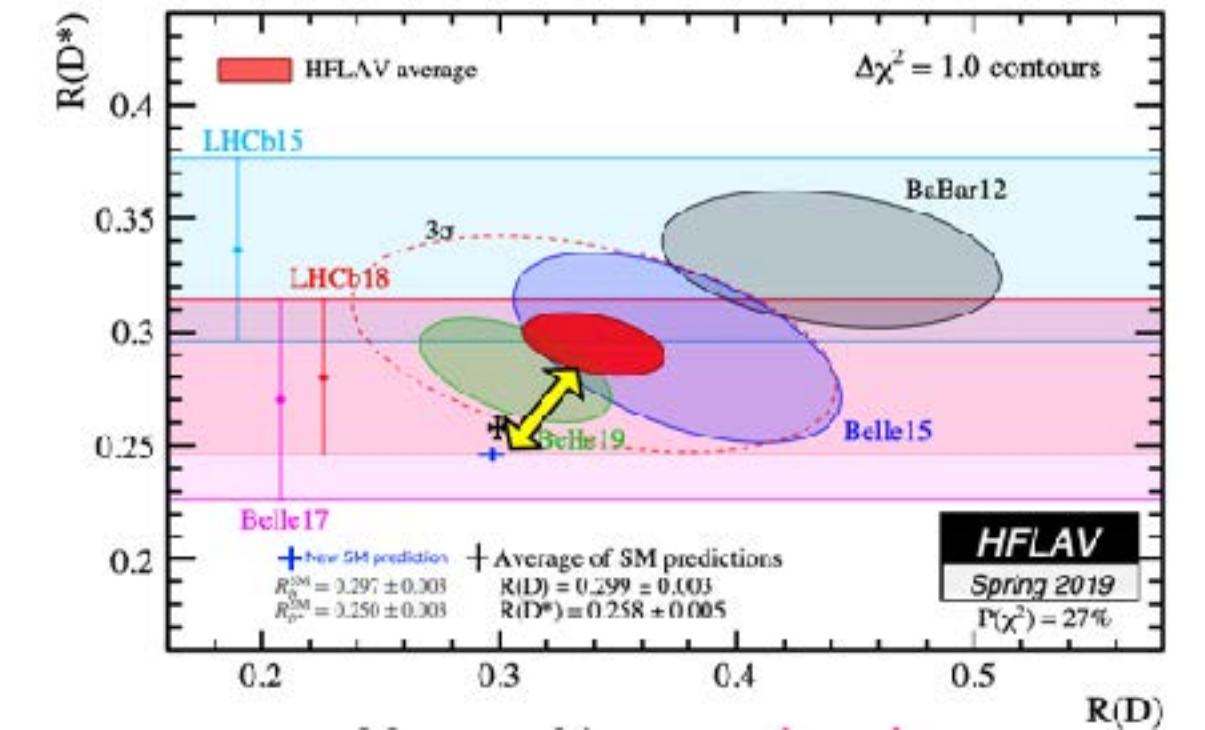
$\sim 3\sigma$



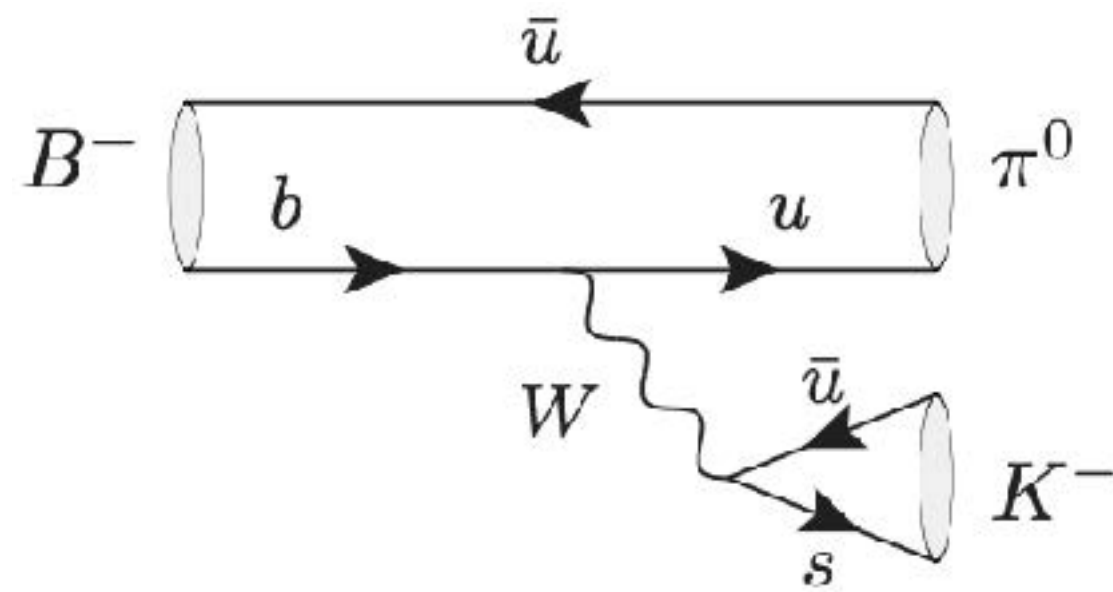
4.2 σ ?



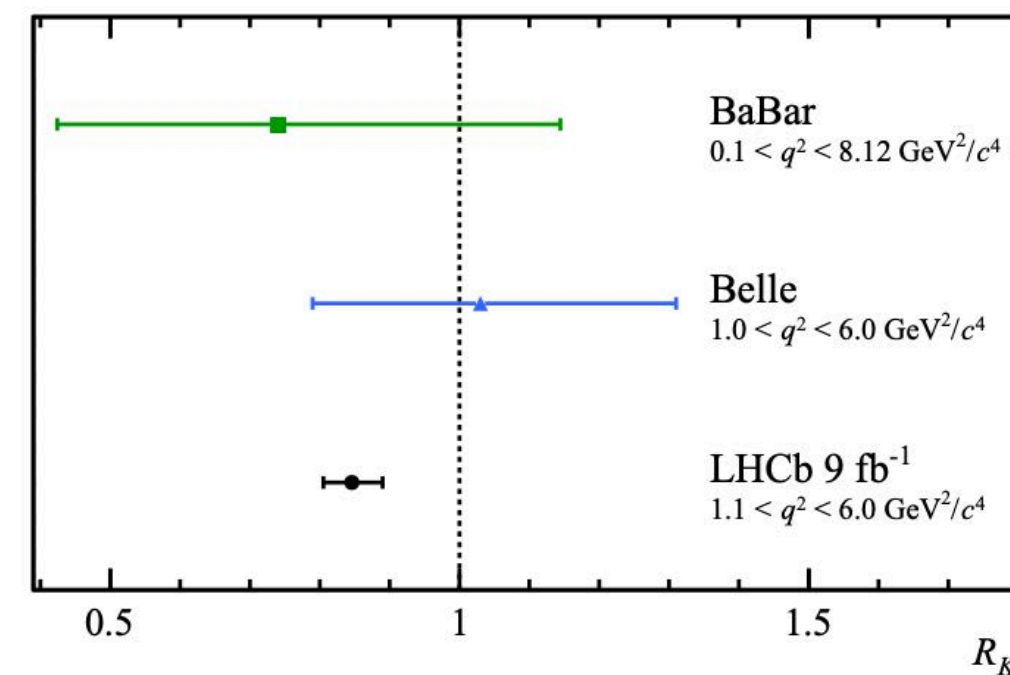
$\sim 4\sigma$



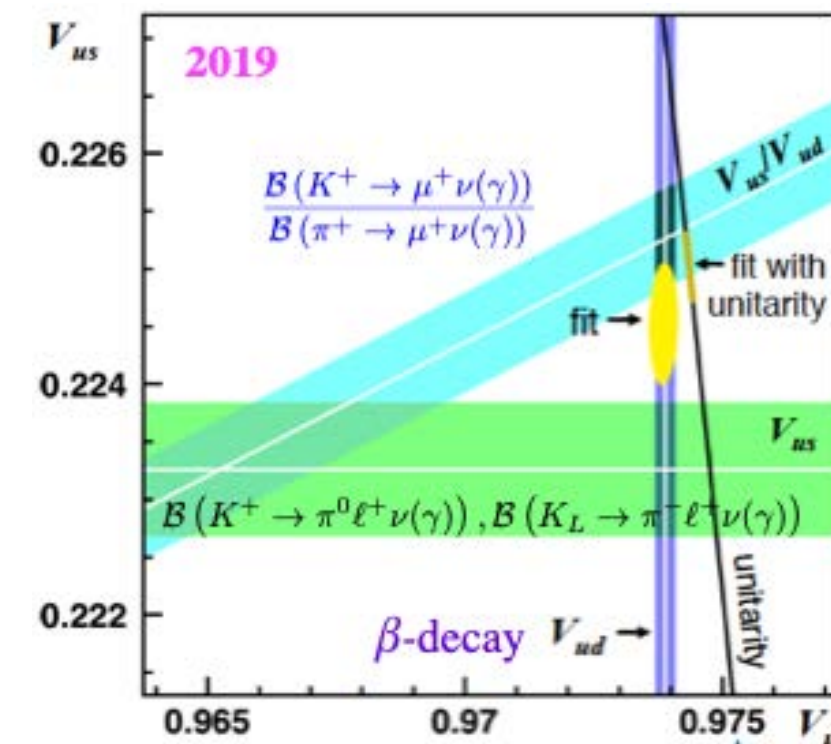
2.2 σ ?



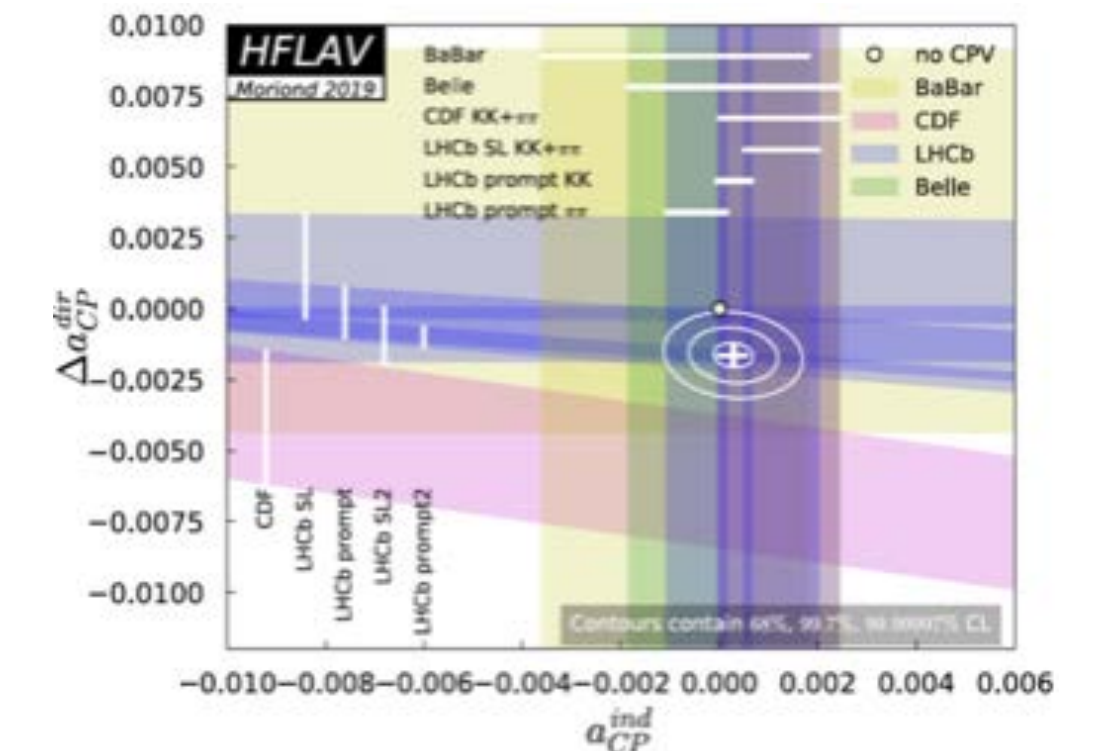
3.9 σ



3-4 σ



4.7 σ ?



SUSY? LQ? ALP? Z'? VL?

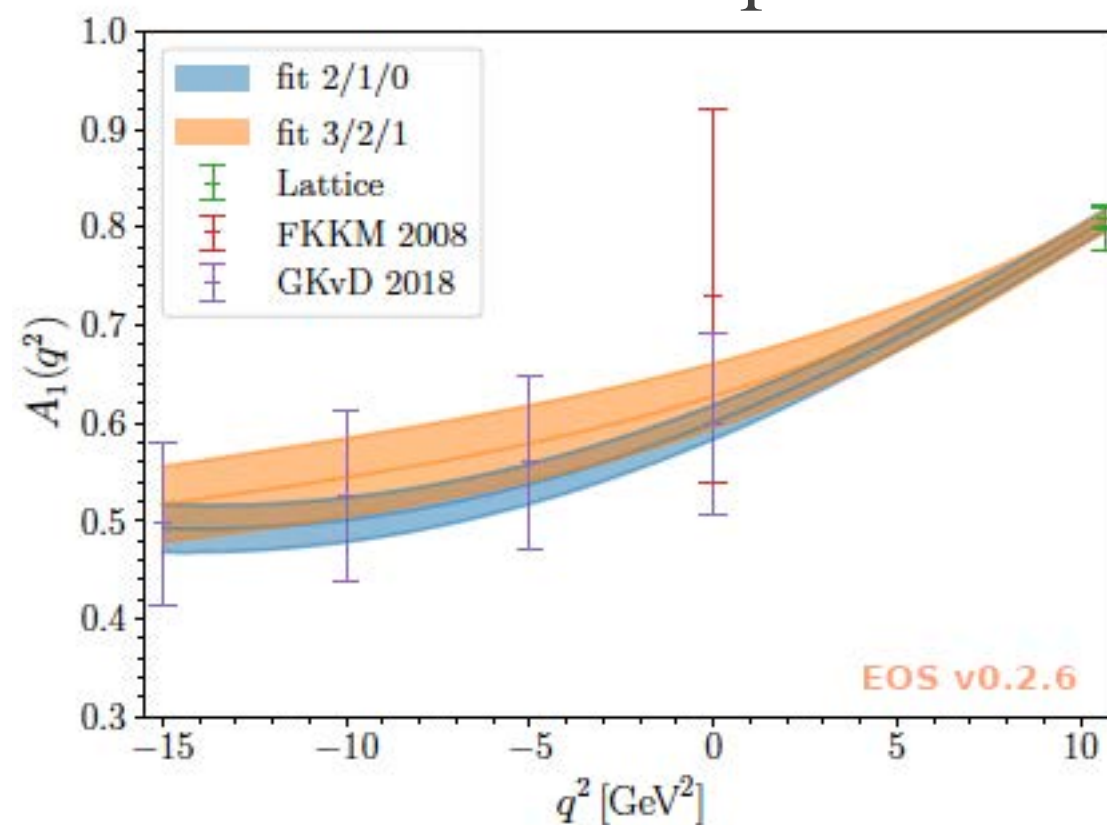
Backup

Latest SM predictions of $R(D)$ and $R(D^*)$

- ◆ All $\mathcal{O}(1/m_c^2)$ corrections in the heavy quark expansion are included and fit all form factors

[Bordone, Jung, van Dyk, EPJC '20; Iguro Watanabe, 2004.10208]

example: A_1 FF



- ◆ All lattice data, QCDSR, and the latest LCSR result [Gubernari, Kokulu, van Dyk, JHEP '19]
 - @ $q^2 = q_{\max}^2$
 - @ $q^2 \leq 0$

$$R(D)_{\text{SM}} = 0.298 \pm 0.003$$

$$R(D^*)_{\text{SM}} = 0.247 \pm 0.006$$

- ◆ + Angular distributions from Belle data [Belle, 1510.03657; 1702.01521; 1809.03290]

$$R(D)_{\text{SM}} = 0.297 \pm 0.003$$

$$R(D^*)_{\text{SM}} = 0.250 \pm 0.003 \quad [\text{BJD}]$$

$$R(D)_{\text{SM}} = 0.297 \pm 0.006$$

$$R(D^*)_{\text{SM}} = 0.245 \pm 0.004 \quad [\text{IW}]$$

2/1/0: $\mathcal{O}(1/m_c^2)$ corrections are just constants

3/2/1: ω dependence in $\mathcal{O}(1/m_c^2)$ is included

$$w = (m_B^2 + m_D^{(*)2} - q^2) / 2m_B m_D^{(*)}$$

$$R(D): 1.4 \rightarrow 1.4, 1.4 \sigma$$

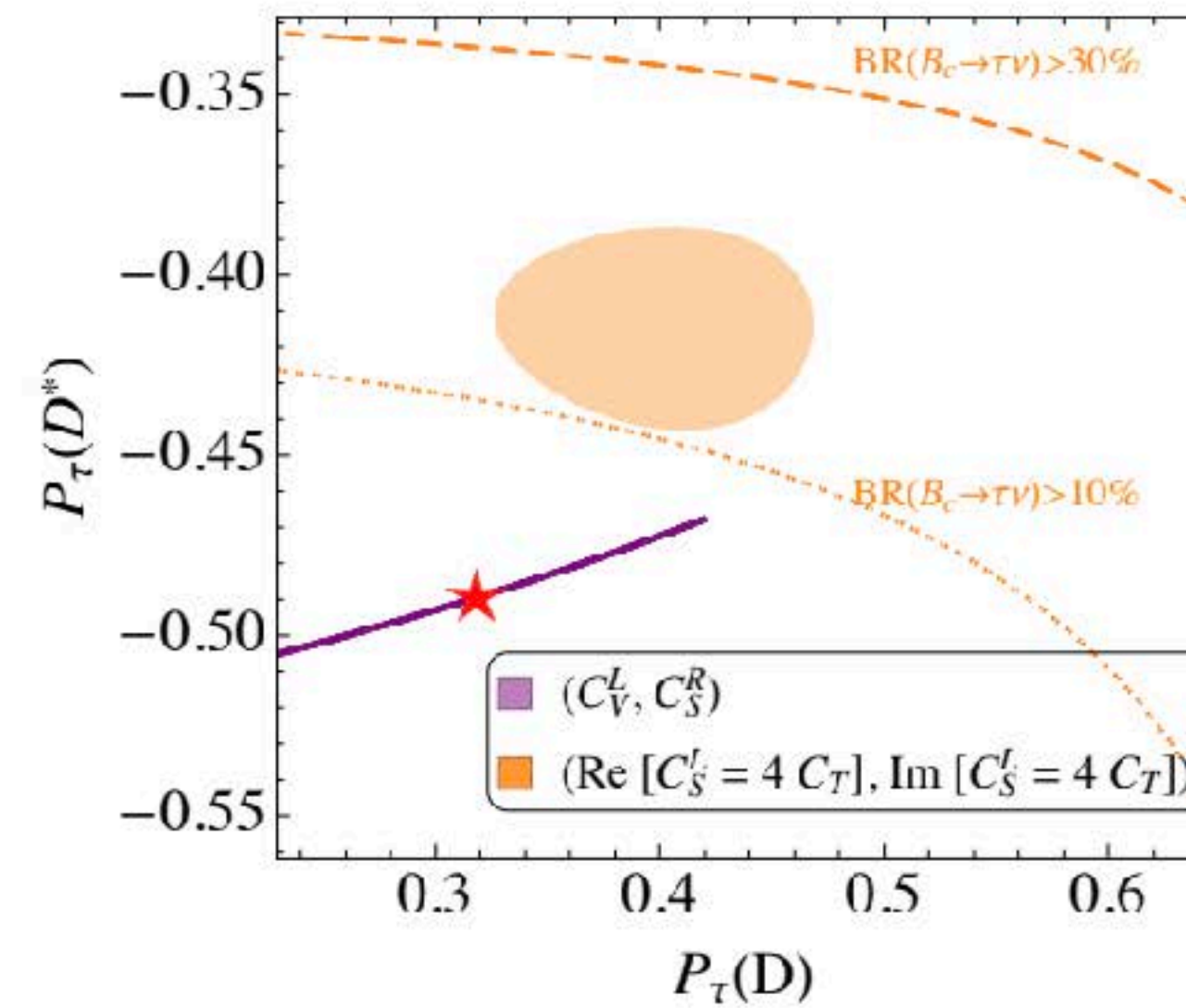
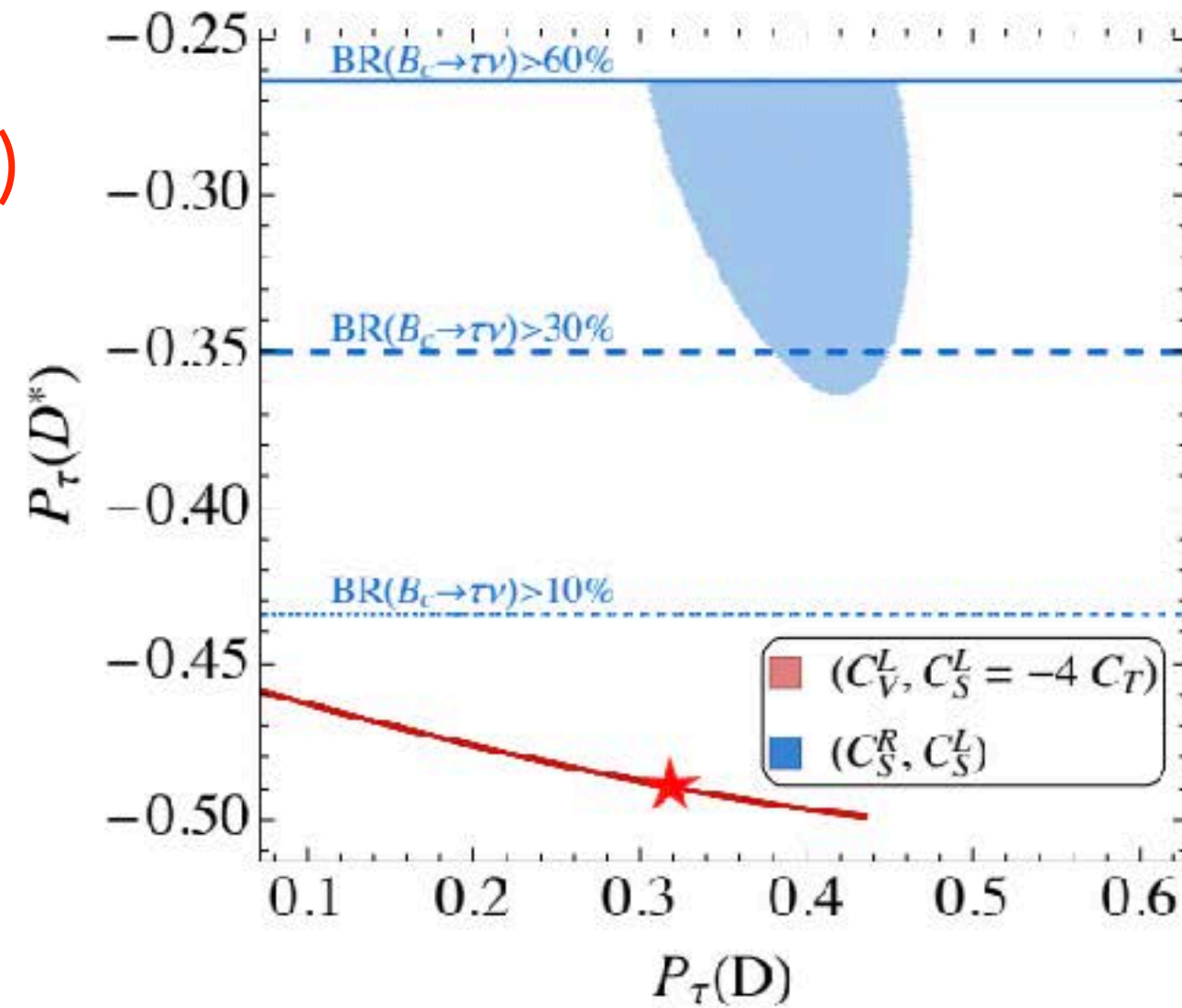
$$R(D^*): 2.5 \rightarrow 3.2, 3.5 \sigma$$

$$\text{combine: } 3.1 \rightarrow 3.9, 4.1 \sigma \quad (\text{my personal analysis})$$

SU(2)_L-singlet scalar LQ (S_1)

Charged Higgs

$P_\tau(D)$ vs. $P_\tau(D^*)$

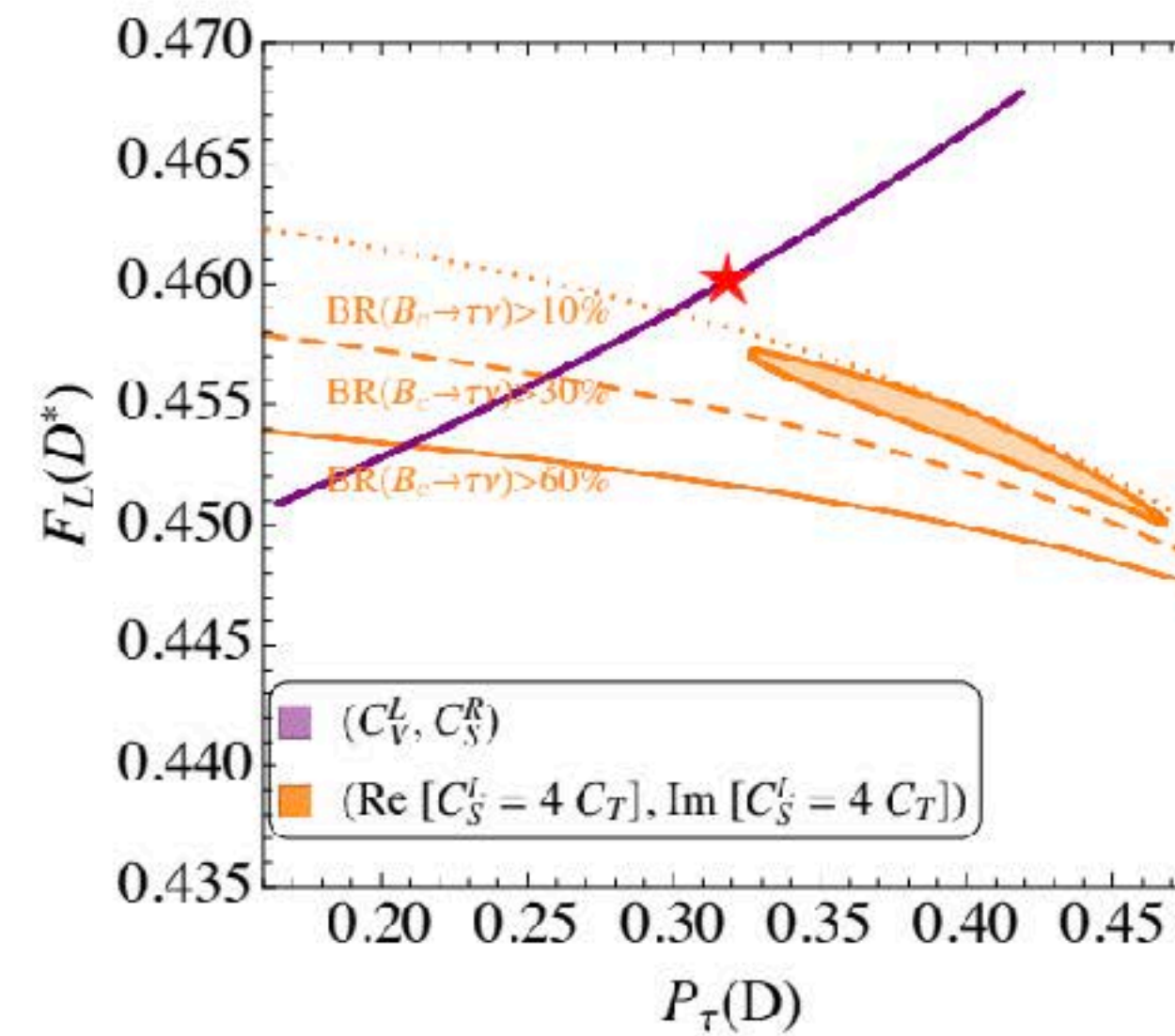
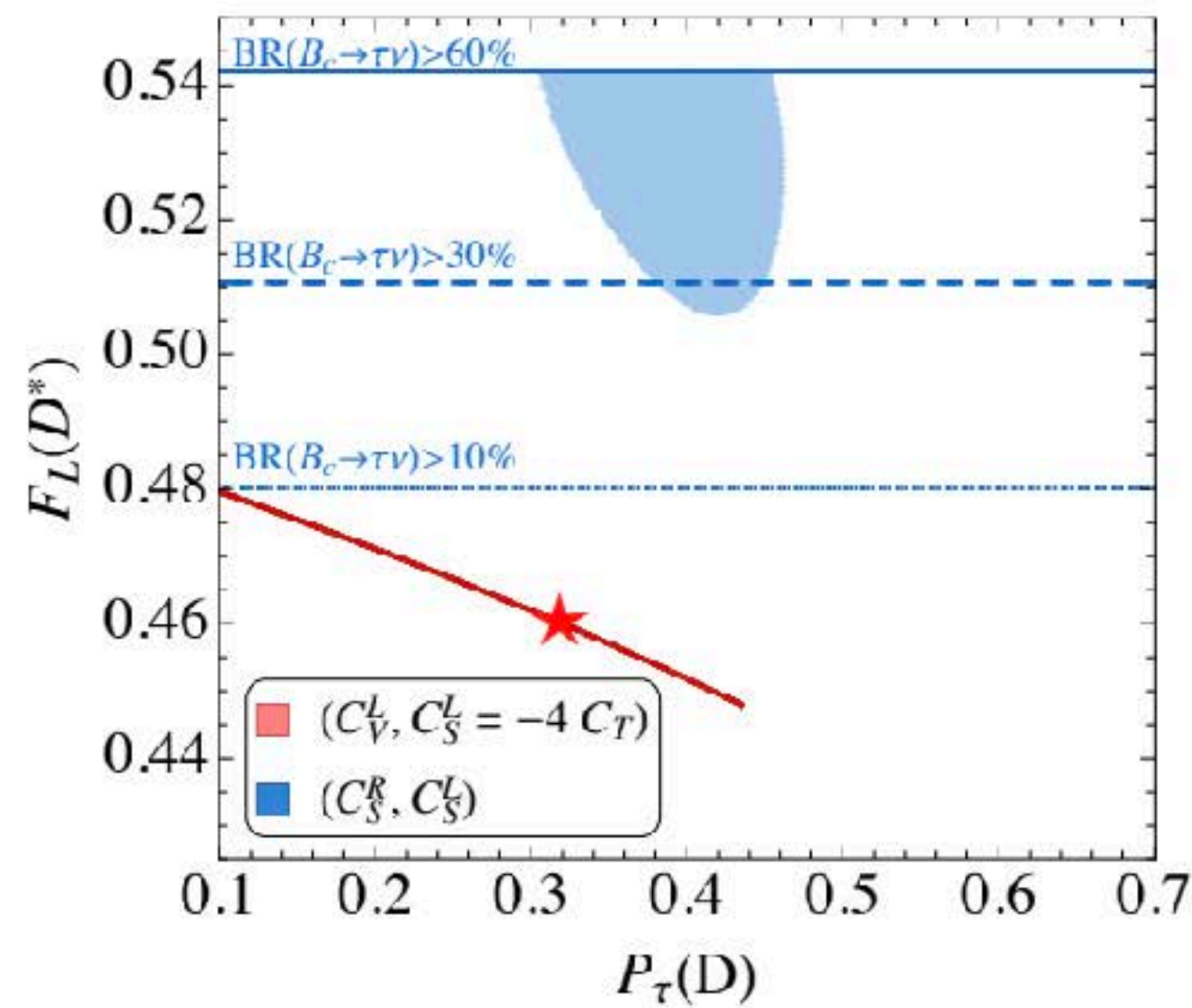


SU(2)_L-singlet vector LQ (U_1)

SU(2)_L-doublet scalar LQ (R_2)

$P_\tau(D)$ can discriminate the new physics

$P_\tau(D)$ vs. $F_L(D^*)$



$P_\tau(D^*)$ could discriminate the new physics

$F_L(D^*)$ is difficult to discriminate them

Tensor operator vs. $F_L(D^*)$

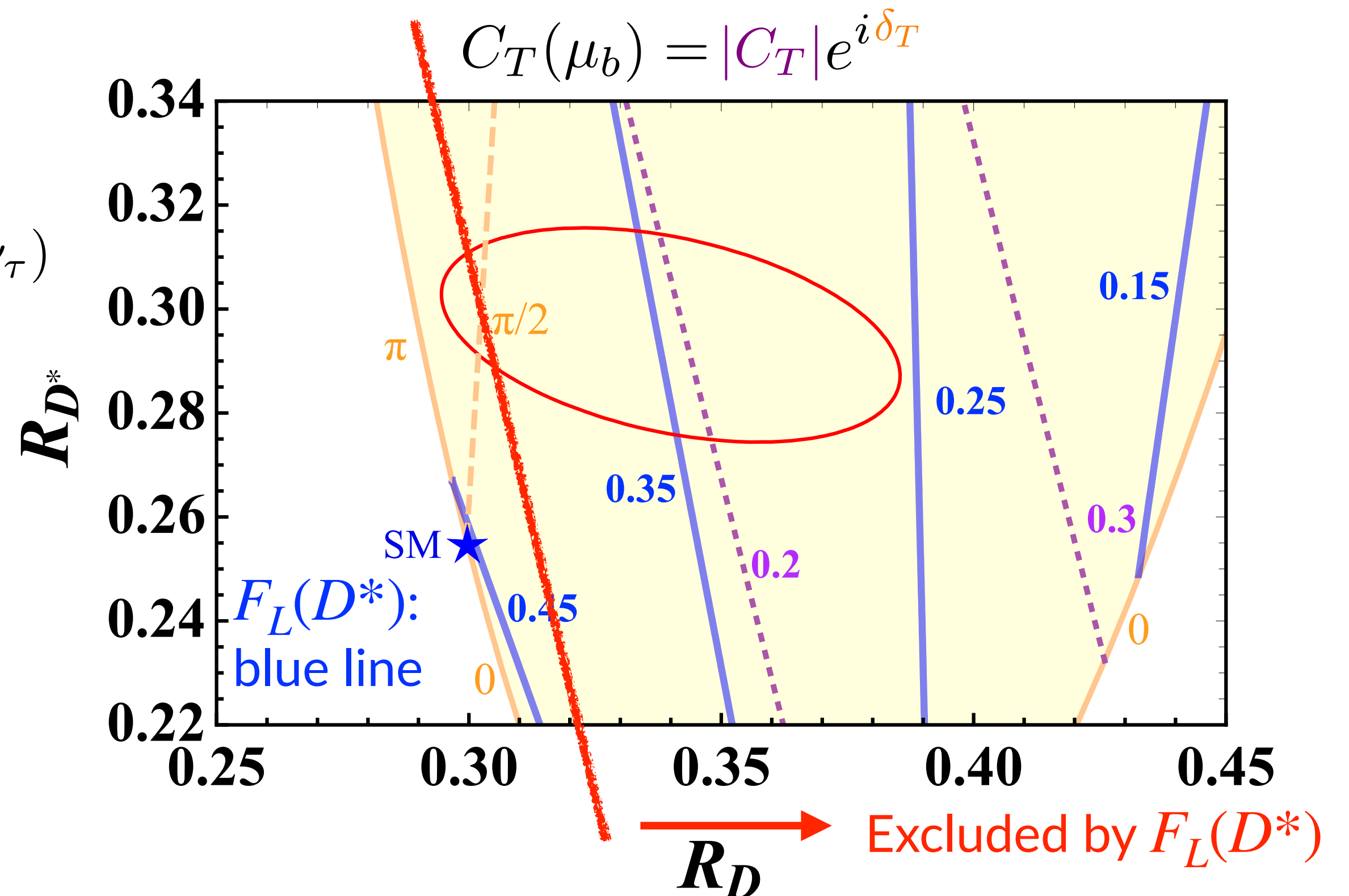
- ◆ Tensor operator in new physics scenario is significantly constrained by $F_L(D^*)$
 [Iguro, TK, Omura, Watanabe, Yamamoto, '19, UPDATED]

$$\mathcal{H}_{\text{eff}} = 2\sqrt{2}G_F V_{cb} C_T(\mu) (\bar{c}\sigma^{\mu\nu} P_L b) (\bar{\tau}\sigma_{\mu\nu} P_L \nu_\tau)$$

$$C_{T, \text{SM}} = 0$$

$$F_L(D^*) = 0.60 \pm 0.08 \pm 0.04$$

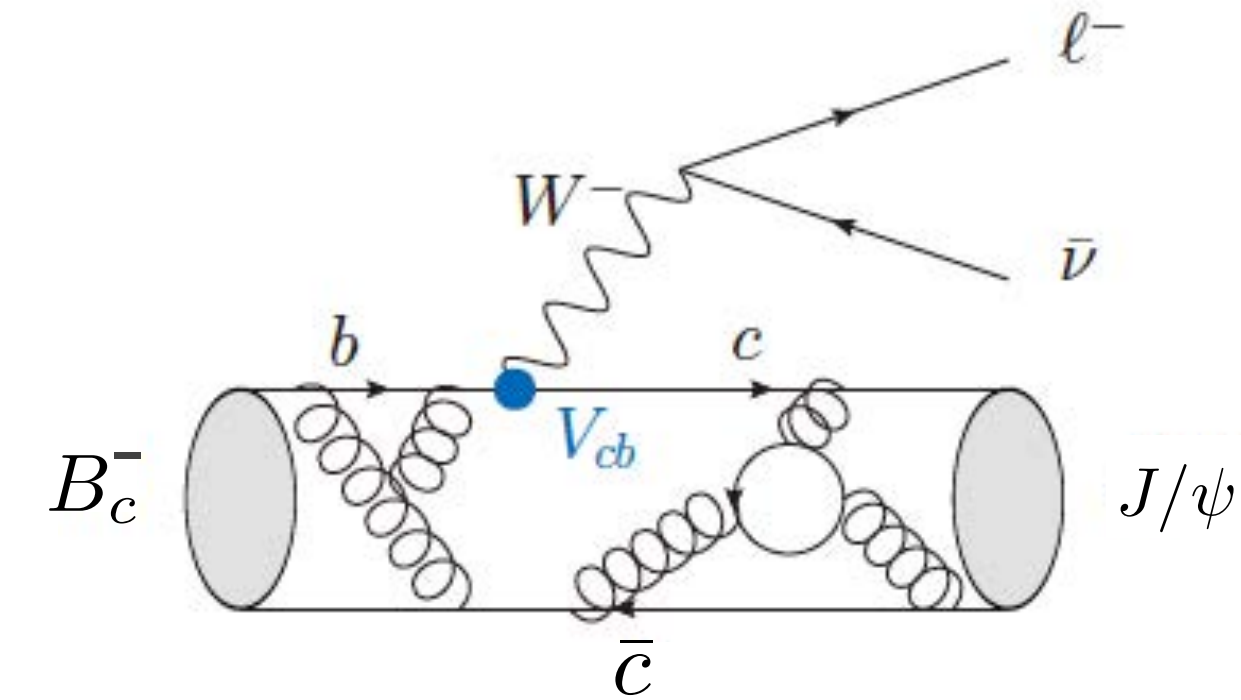
[Belle, 1903.03102]



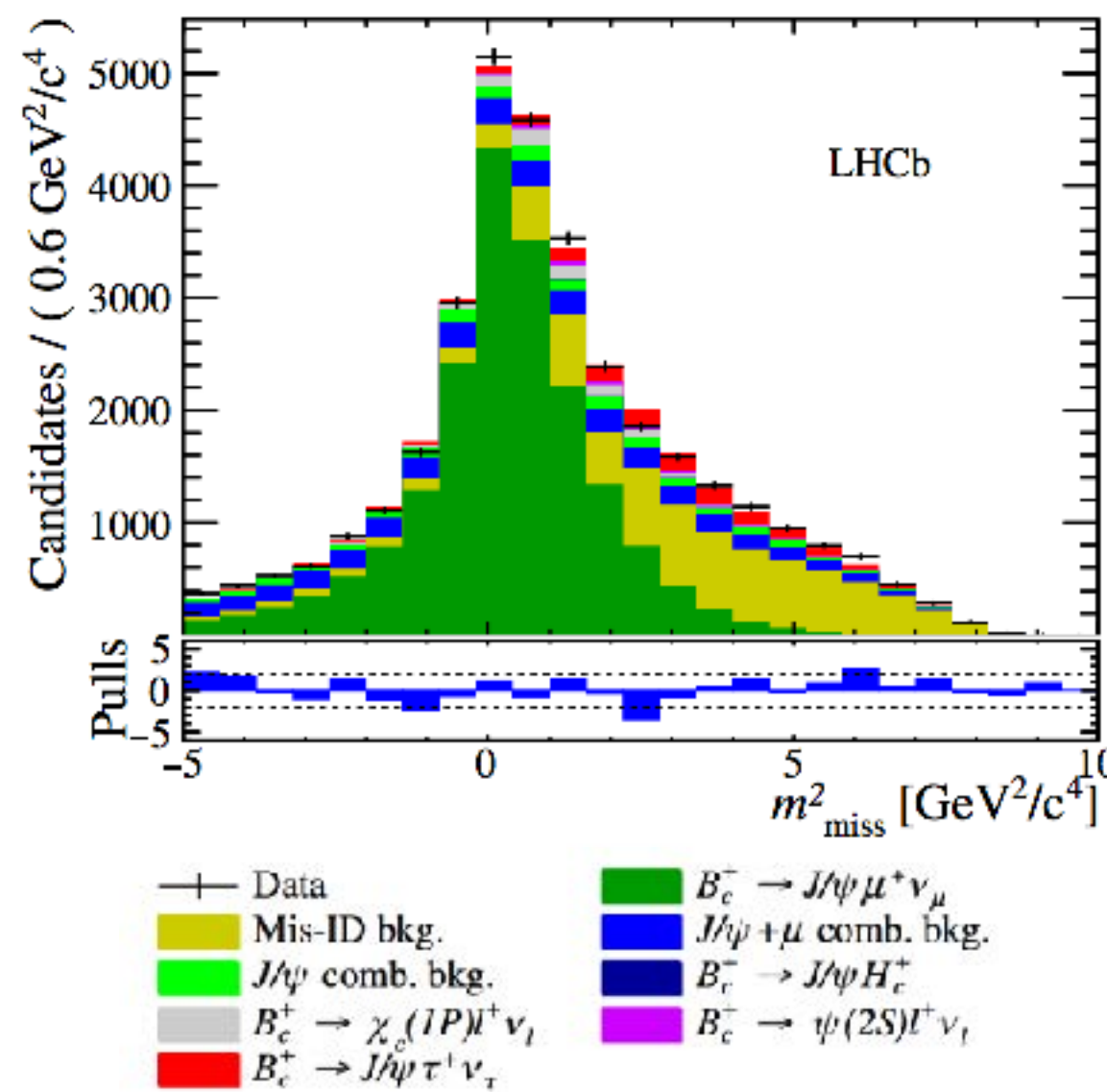
Another channel: $R(J/\psi)$

- The LFU violation was measured in $B_c^- \rightarrow J/\psi$ transitions

$$\mathcal{R}(J/\psi) = \frac{\mathcal{B}(B_c^- \rightarrow J/\psi \tau^- \bar{\nu}_\tau)}{\mathcal{B}(B_c^- \rightarrow J/\psi \ell^- \bar{\nu}_\ell)}$$



[LHCb, 1711.05623]



$$R(J/\psi)_{\text{exp}} = 0.71 \pm 0.17_{\text{stat}} \pm 0.18_{\text{syst}}$$

First lattice result [HPQCD, 2007.06956]

$$R(J/\psi)_{\text{SM}} \sim 0.25-0.28 \quad \rightarrow \rightarrow \rightarrow \rightarrow$$

$$R(J/\psi)_{\text{SM}} = 0.2601 \pm 0.0036$$

1.8 σ consistent

Same-direction as $R(D)$ and $R(D^*)$ tensions.

using $N_f=2+1+1$, with “HISQ” c and heavy quark b

But, the form factors are poorly known

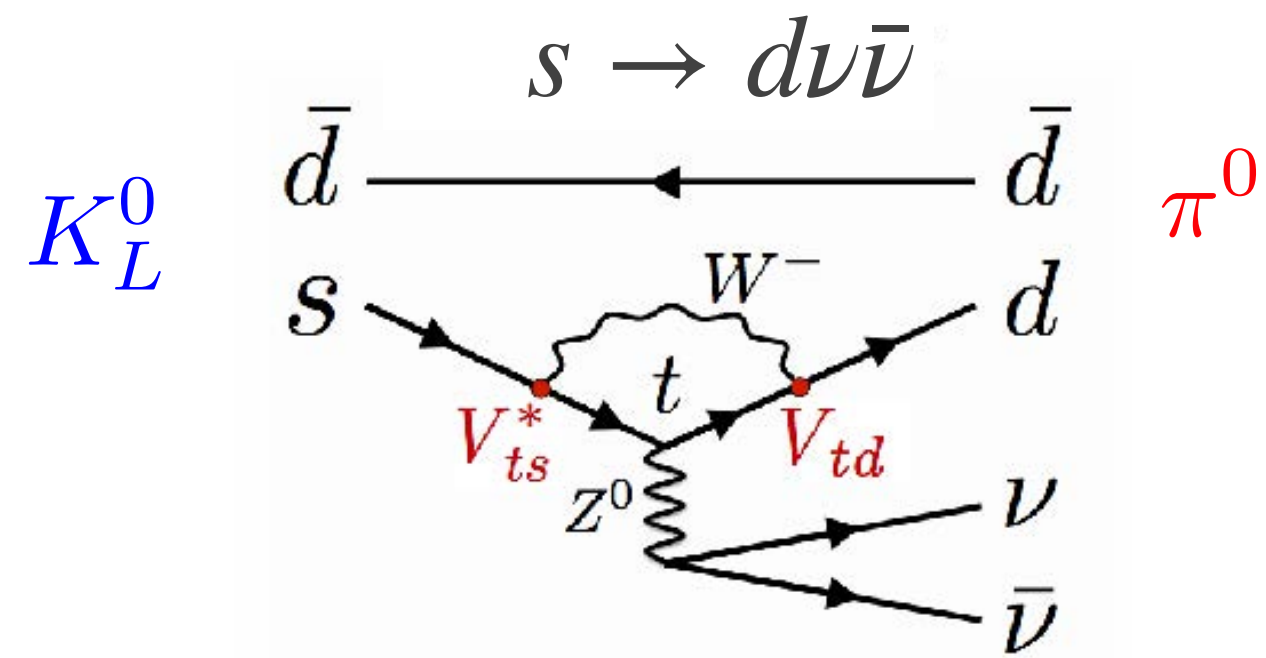
because heavy quark expansion is broken

Early new physics study, e.g., [Watanabe, PLB '18;

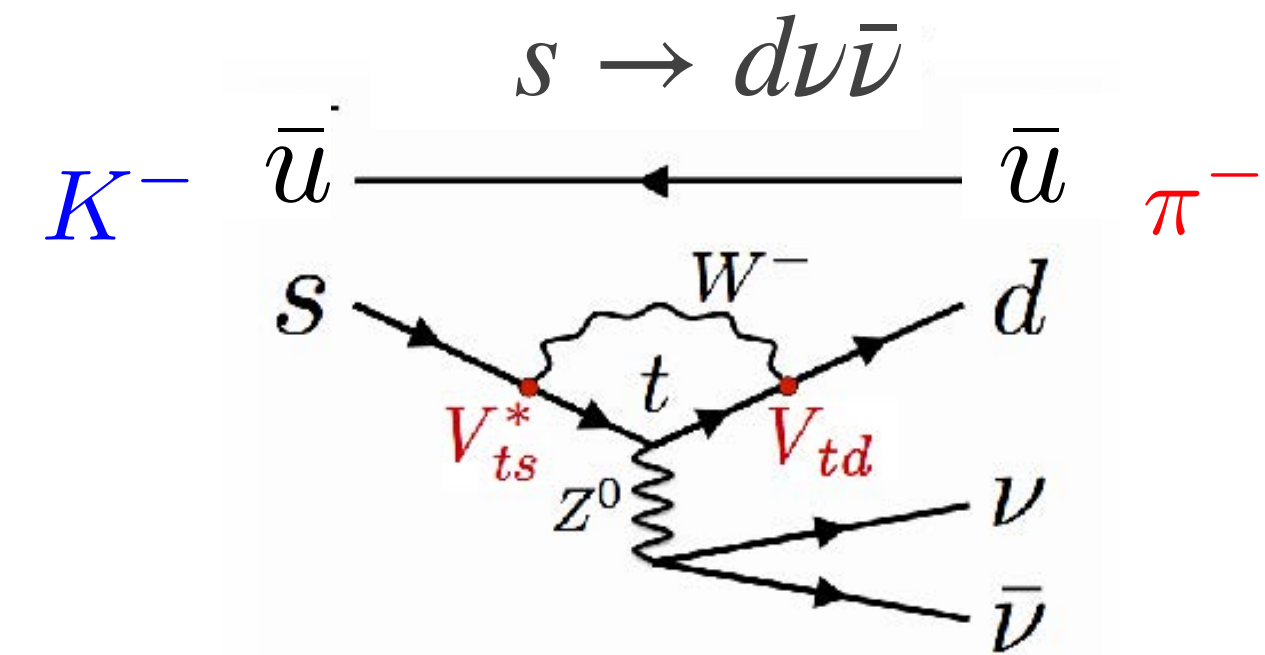
by m_c (spectator quark here)

Alok, Kumar, Kumar, Kumbhakar, Sankar, JHEP '18]

Grossman-Nir bound (theoretical relation)



Same diagram
in quark level



$$\left(\begin{aligned} \frac{\Gamma(K_L \rightarrow \pi^0 \nu \bar{\nu})}{\Gamma(K^+ \rightarrow \pi^+ \nu \bar{\nu})} &= \frac{|pA_{\pi^0 \nu \bar{\nu}} - q\bar{A}_{\pi^0 \nu \bar{\nu}}|^2}{|\sqrt{2}A_{\pi^0 \nu \bar{\nu}}|^2} = \frac{1}{4} |1 - \lambda_{\pi \nu \bar{\nu}}|^2 \\ &= \frac{1}{4} (1 + |\lambda_{\pi \nu \bar{\nu}}|^2 - 2\text{Re}\lambda_{\pi \nu \bar{\nu}}) \simeq \frac{1}{2} (1 - \text{Re}\lambda_{\pi \nu \bar{\nu}}) = \sin^2 \left[\frac{\text{Arg}(\lambda_{\pi \nu \bar{\nu}})}{2} \right] \end{aligned} \right)$$

$$K_L \propto pK^0 - q\bar{K}^0$$

$$A_{\pi^0 \nu \bar{\nu}} = \langle \pi^0 \nu \bar{\nu} | \mathcal{H} | K^0 \rangle,$$

$$\bar{A}_{\pi^0 \nu \bar{\nu}} = \langle \pi^0 \nu \bar{\nu} | \mathcal{H} | \bar{K}^0 \rangle,$$

$$\lambda_{\pi \nu \bar{\nu}} = \left(\frac{q}{p} \right)_K \frac{\bar{A}_{\pi^0 \nu \bar{\nu}}}{A_{\pi^0 \nu \bar{\nu}}}$$

- ◆ Grossman-Nir bound for general NP models (including $\nu_i \bar{\nu}_j$) [Grossman, Nir, PLB '97]

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = \left(\frac{\tau_L}{\tau^+} + \Delta_{\text{IB, EM}} \right) \sin^2 \theta \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) \leq 4.32 \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$