

MIXING-INDUCED CP VIOLATION IN B_s DECAYS



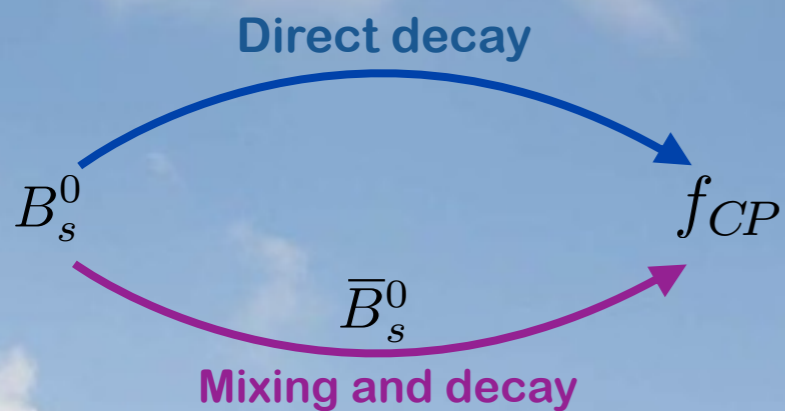
FPCP 2015

Flavor Physics & CP Violation
University of Nagoya, Japan
25-29 May 2015

Simon Akar

on behalf of the LHCb collaboration,
including results from other collaborations

OUTLINE



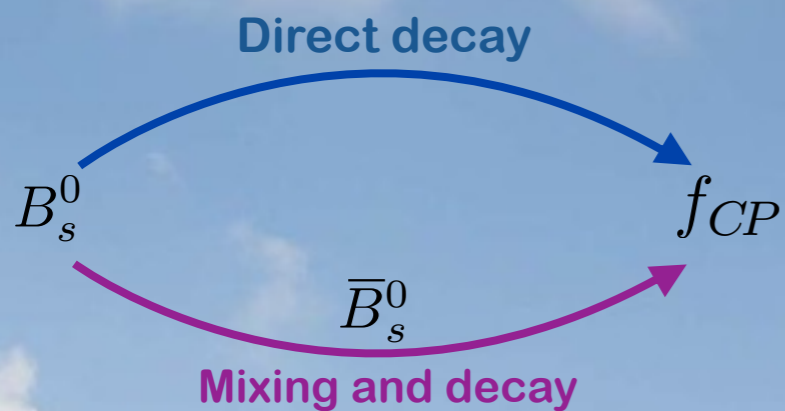
1 Physics motivation

2 Measurement ingredients

3 Measurement of ϕ_s

4 Constraining penguins in ϕ_s

OUTLINE



1 Physics motivation

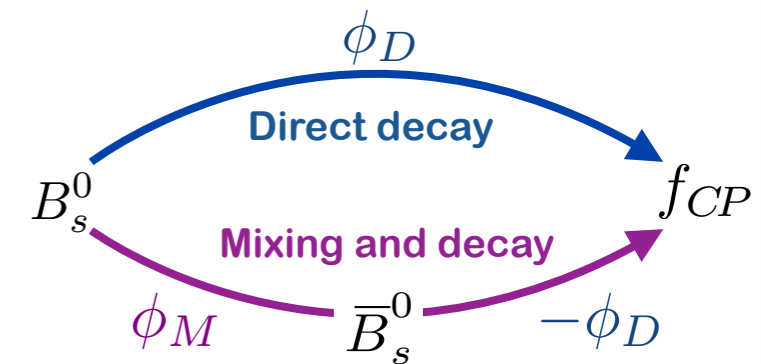
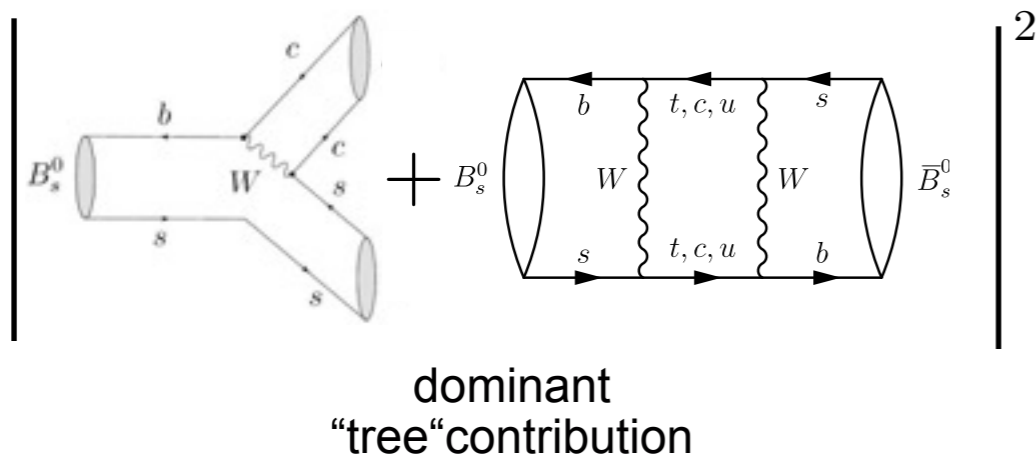
2 Measurement ingredients

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4 Constraining penguins in ϕ_s

PHYSICS MOTIVATION

◆ CPV in interference between mixing and decay:

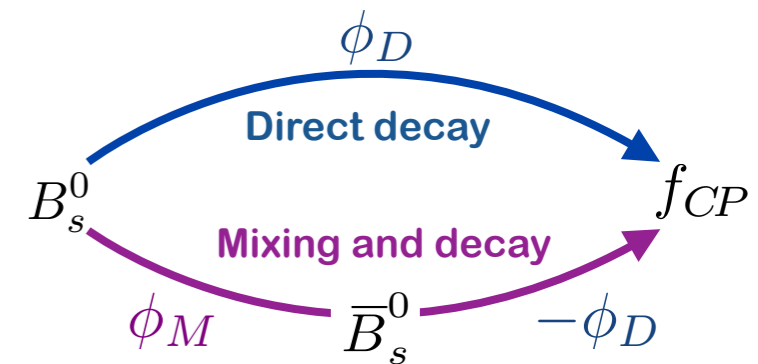
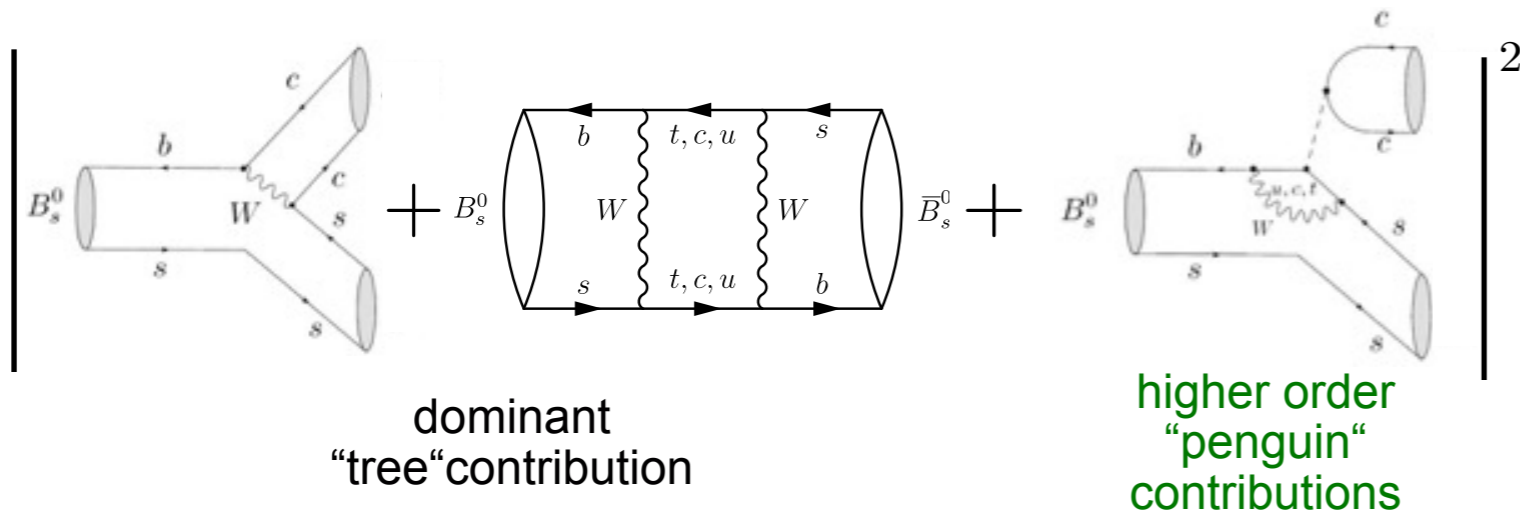


$$\begin{aligned}\phi_s &= \phi_M - 2\phi_D \\ &= -2\beta_s\end{aligned}$$

$$\beta_s = \arg\left(-\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}\right)$$

PHYSICS MOTIVATION

◆ CPV in interference between mixing and decay:

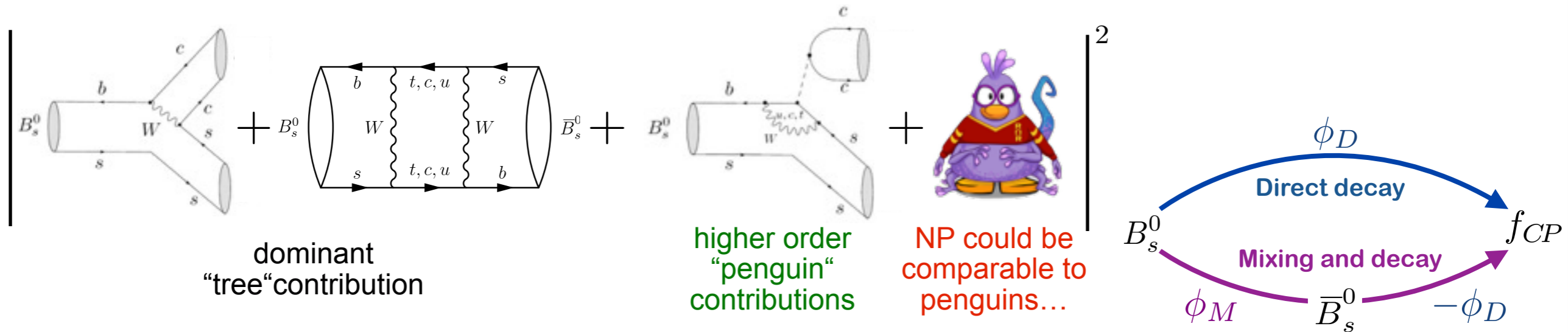


$$\begin{aligned} \phi_s &= \phi_M - 2\phi_D \\ &= -2\beta_s + \Delta\phi_s^{\text{Peng.}} \end{aligned}$$

$$\beta_s = \arg \left(-\frac{V_{ts} V_{tb}^*}{V_{cs} V_{cb}^*} \right)$$

PHYSICS MOTIVATION

◆ CPV in interference between mixing and decay:



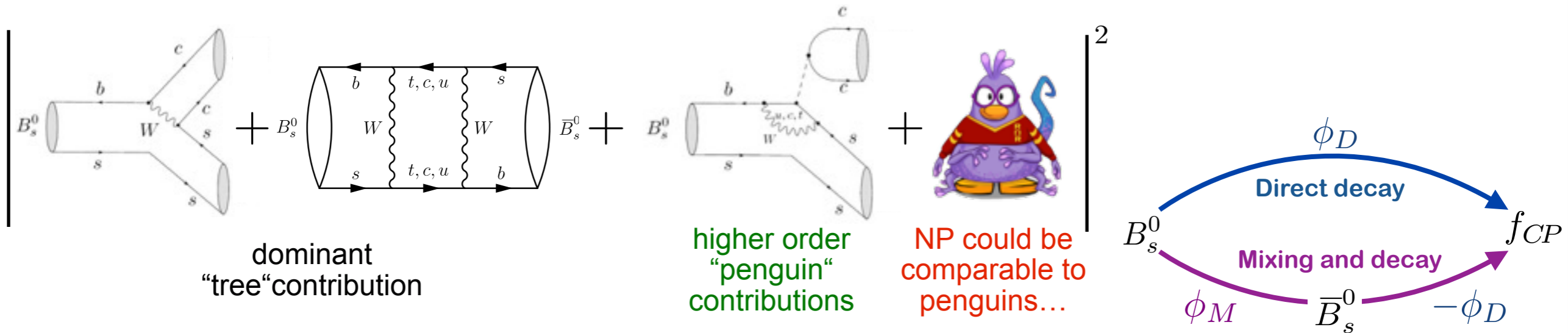
$$\phi_s = \phi_M - 2\phi_D$$

$$= -2\beta_s + \Delta\phi_s^{\text{Peng.}} + \delta^{\text{NP}}$$

$$\beta_s = \arg\left(-\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}\right)$$

PHYSICS MOTIVATION

◆ CPV in interference between mixing and decay:



$$\begin{aligned} \phi_s &= \phi_M - 2\phi_D \\ &= -2\beta_s + \Delta\phi_s^{\text{Peng.}} + \delta^{\text{NP}} \end{aligned}$$

$$\beta_s = \arg \left(-\frac{V_{ts} V_{tb}^*}{V_{cs} V_{cb}^*} \right)$$

- ϕ_s determination via global fit to experimental results ignores contributions from penguin diagrams:

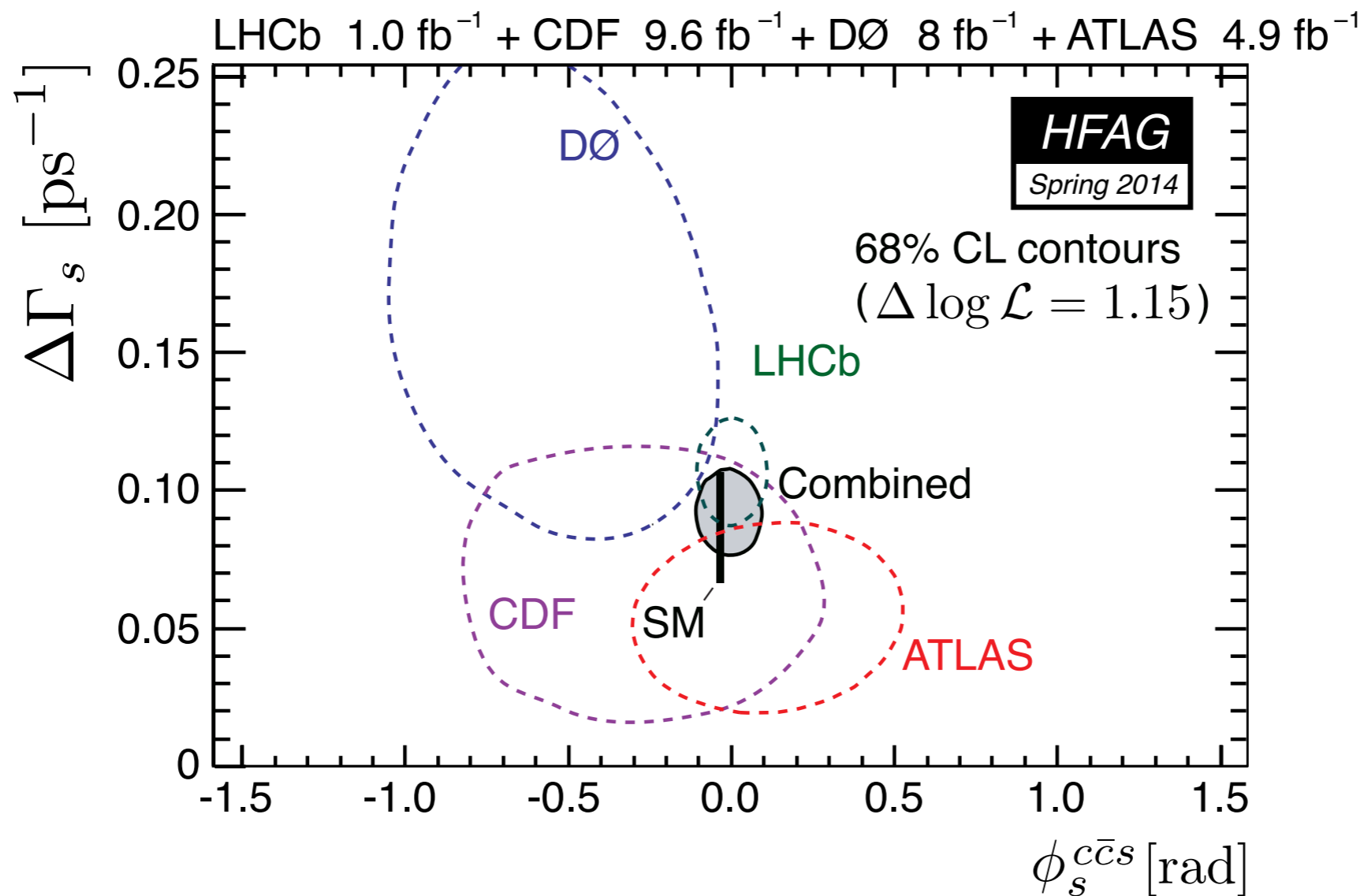
$$\phi_s^{\text{SM no Peng}} = -2\beta_s = -0.0365_{-0.0012}^{+0.0013}$$

[CKMFitter]

PHYSICS MOTIVATION

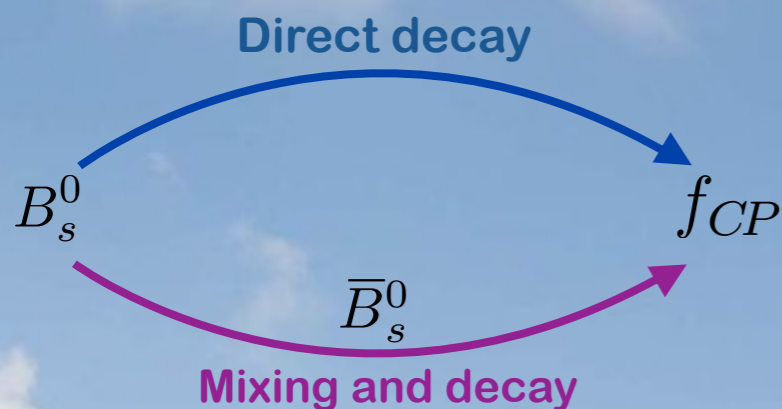
◆ Toward a precise measurement of ϕ_s :

State of the art
at FPCP 2014



- ϕ_s measurement is an excellent probe for the presence of NP...
- ...but it is now mandatory to constrain penguin contributions!

OUTLINE



1 Physics motivation

2 Measurement ingredients

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4 Constraining penguins in ϕ_s

MEASUREMENT INGREDIENTS

◆ Time-dependent CP asymmetry:

$$A_{CP}(t) = \frac{(\bar{B}_s^0(t) \rightarrow f) - (B_s^0(t) \rightarrow f)}{(\bar{B}_s^0(t) \rightarrow f) + (B_s^0(t) \rightarrow f)} = \frac{\mathcal{S}_f \sin(\Delta m t) - \mathcal{C}_f \cos(\Delta m t)}{\cosh\left(\frac{\Delta\Gamma t}{2}\right) + \mathcal{A}_{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma t}{2}\right)}$$

▶ Mixing parameters:

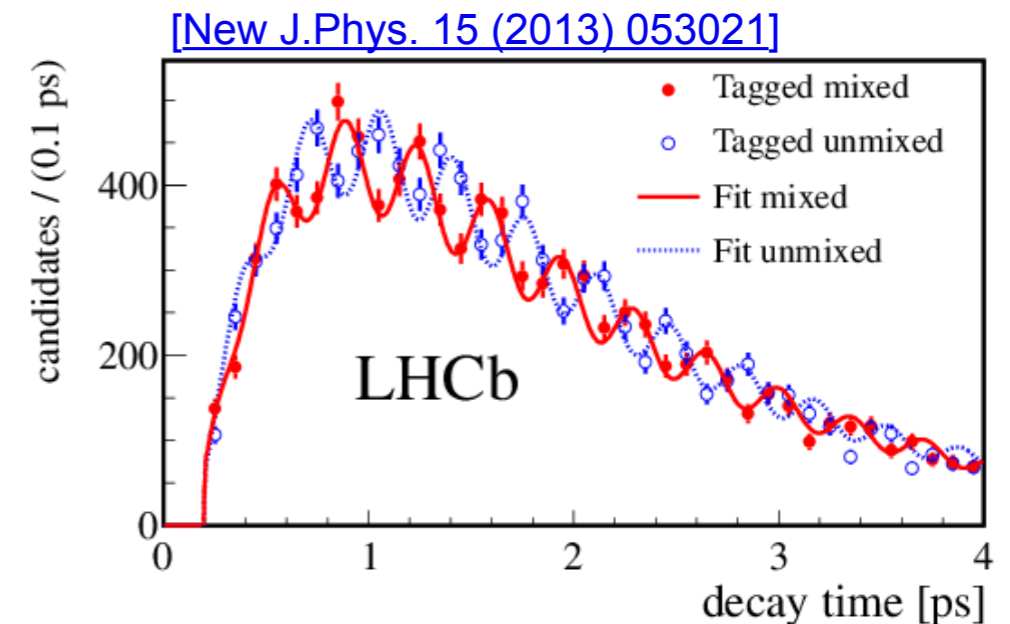
$$\Delta m = m_H - m_L \quad \Delta\Gamma = \Gamma_L - \Gamma_H$$

▶ CP observables:

$$\mathcal{S}_f = \frac{2\Im(\lambda_f)}{1 + |\lambda_f|^2}, \quad \mathcal{C}_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}, \quad \mathcal{A}_{\Delta\Gamma} = -\frac{2\Re(\lambda_f)}{1 + |\lambda_f|^2}$$

$$\lambda_f = \eta_f \frac{q}{p} \frac{A(\bar{B}_s^0(t) \rightarrow f)}{A(B_s^0(t) \rightarrow f)} = \eta_f |\lambda_f| e^{i\phi_s}$$

$$\mathcal{S}_f = -\eta_f \frac{2|\lambda_f| \sin(\phi_s)}{1 + |\lambda_f|^2}, \quad \mathcal{A}_{\Delta\Gamma} = \eta_f \frac{2|\lambda_f| \cos(\phi_s)}{1 + |\lambda_f|^2}$$



MEASUREMENT INGREDIENTS

◆ Tagging, resolution and other nuisance effects:

$$A_{\text{meas}}(t) = A_{CP}(t) \times D_{\text{res}} \times D_{\text{tag}} \pm A_{\text{det/prod}}$$

► Decay time resolution:

$$D_{\text{res}} = e^{-\frac{\Delta m^2 \sigma_t^2}{2}}$$

► Tagging dilution:

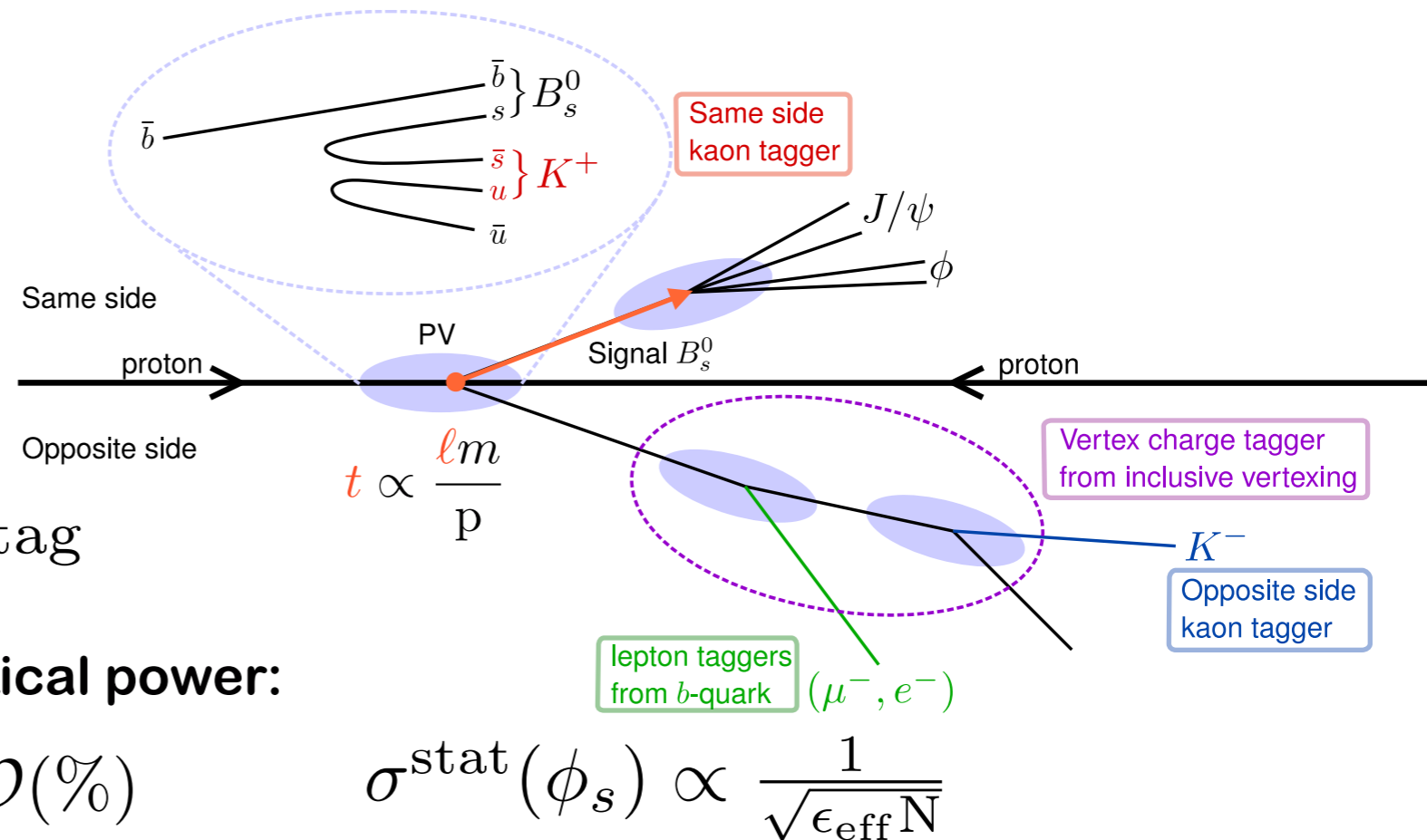
$$D_{\text{tag}} = (1 - 2\omega)$$

- Initial B flavor efficiency: ϵ_{tag}
- Wrong tag rate: ω
- Effective reduction in statistical power:

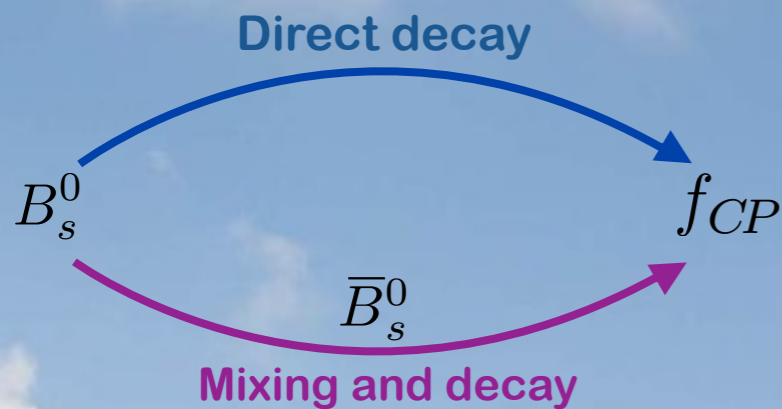
$$\epsilon_{\text{eff}} = \epsilon_{\text{tag}}(1 - 2\omega)^2 \sim \mathcal{O}(\%)$$

$$\sigma^{\text{stat}}(\phi_s) \propto \frac{1}{\sqrt{\epsilon_{\text{eff}} N}}$$

- Also need to account for detection/production asymmetries, acceptance effects on time and angular variables, ...



OUTLINE



1 Physics motivation

2 Measurement ingredients

3 Measurement of ϕ_s :

- ▶ $B_s \rightarrow J/\psi K^+ K^-$
- ▶ $B_s \rightarrow J/\psi \pi^+ \pi^-$
- ▶ $B_s \rightarrow D_s^+ D_s^-$
- ▶ $B_s \rightarrow J/\psi K_S^0$



4 Constraining penguins in ϕ_s :

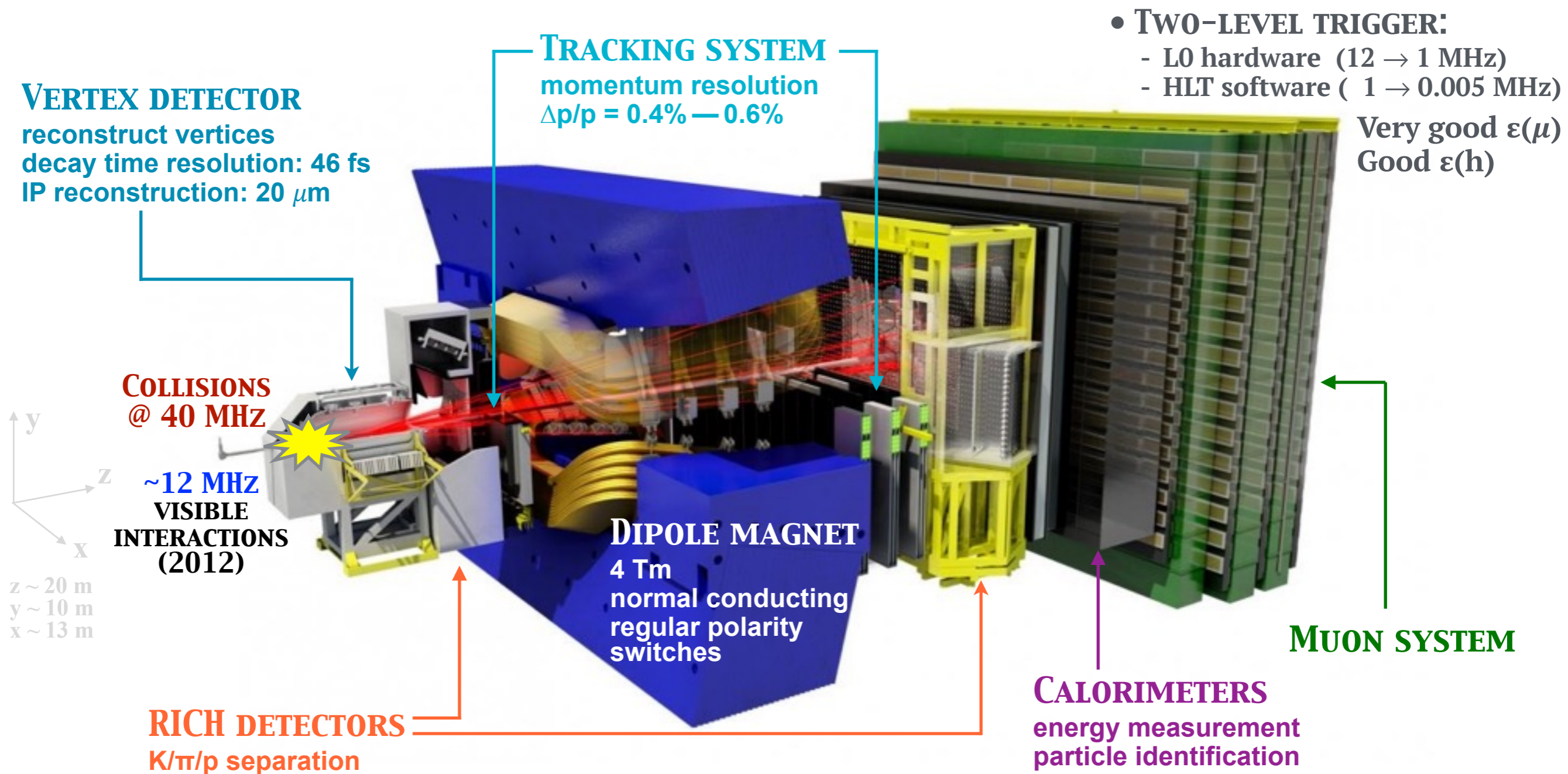
- ▶ $B_d \rightarrow J/\psi \pi^+ \pi^-$



The LHCb experiment

Detector overview

- Forward General-Purpose Detector at the LHC
- ~30 % of heavy quark production cross-section with just 4% of solid angle

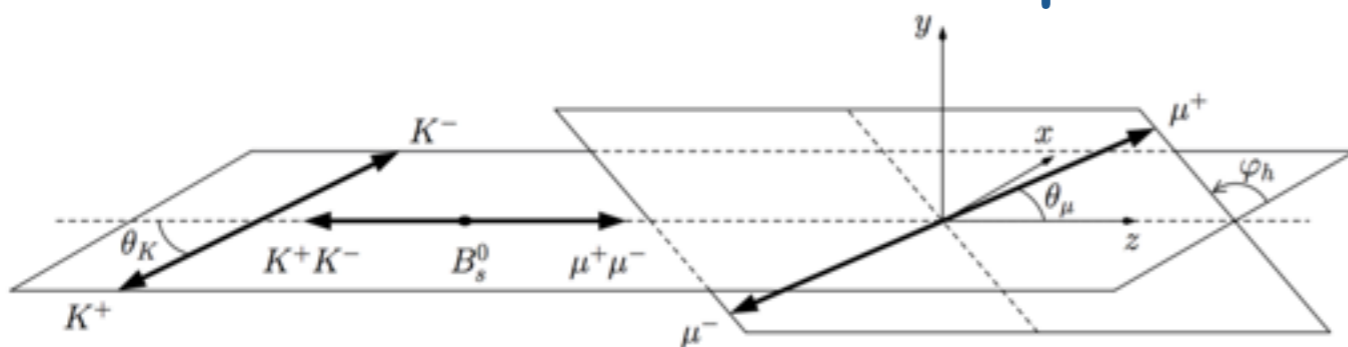


Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

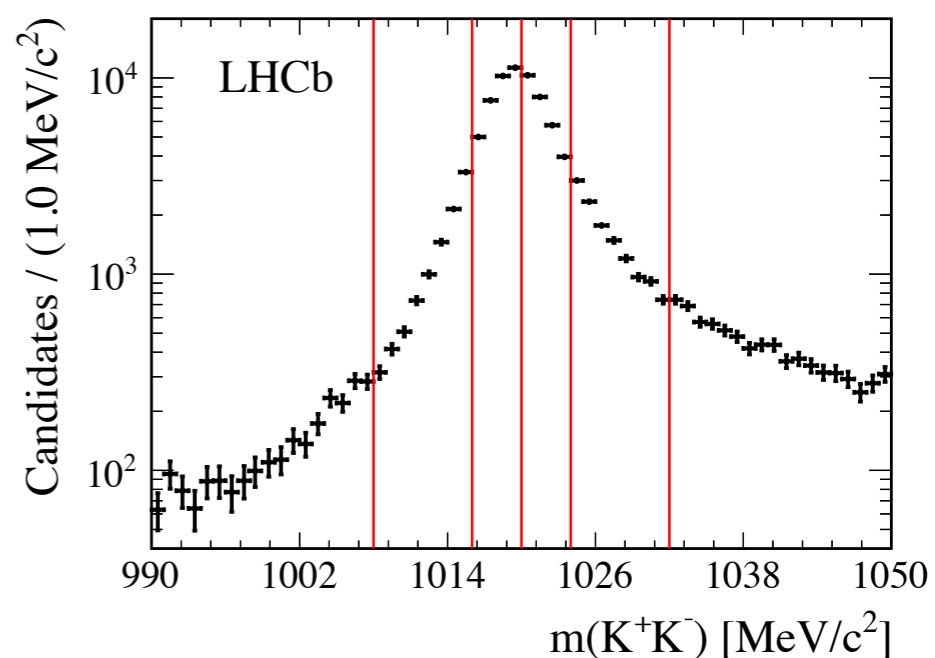
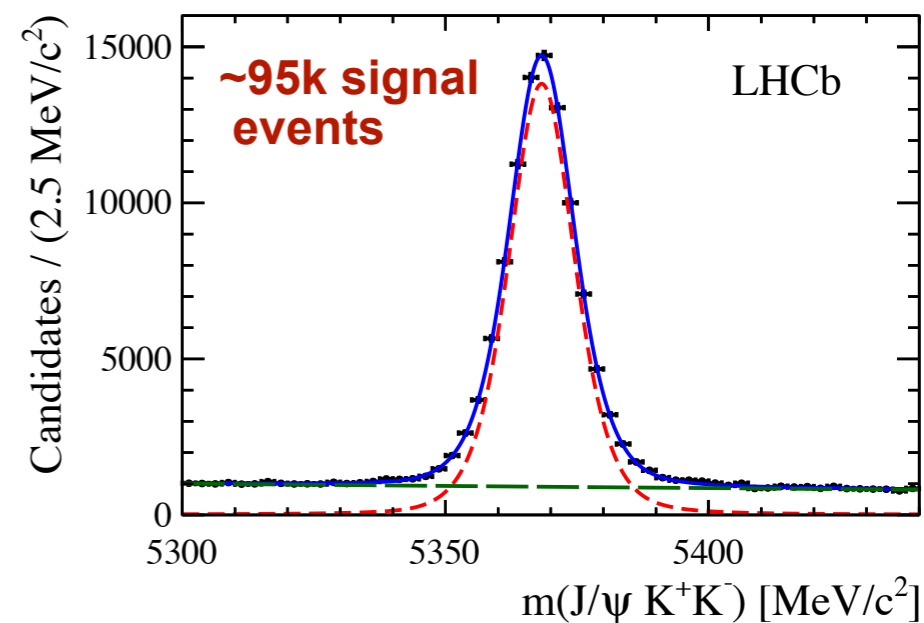
[Phys. Rev. Lett. 114 041801 (2015)]

◆ Analysis overview:

- Measures ϕ_s , Γ_s , $\Delta\Gamma_s$ and $|\lambda|$
 - ▶ Time-dependent tagged angular analysis (using s Weights)
 - 3 P-wave + 1 S-wave components



- tagging power $\sim 3.7\%$
- ▶ Fit simultaneously:
 - 6 bins of m_{KK}
- ▶ Two fit models:
 - polarisation independent (baseline)
 - polarisation dependent (necessary, if CPV does not affect all polarisation states equally)

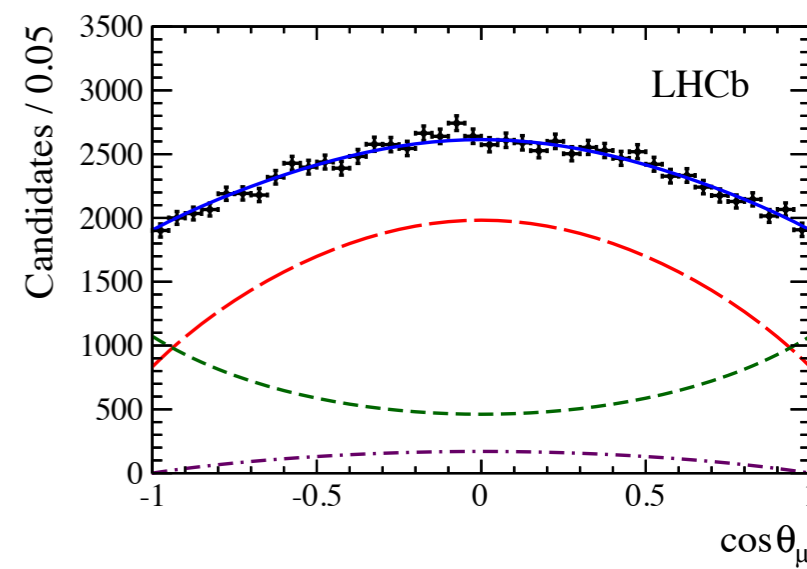
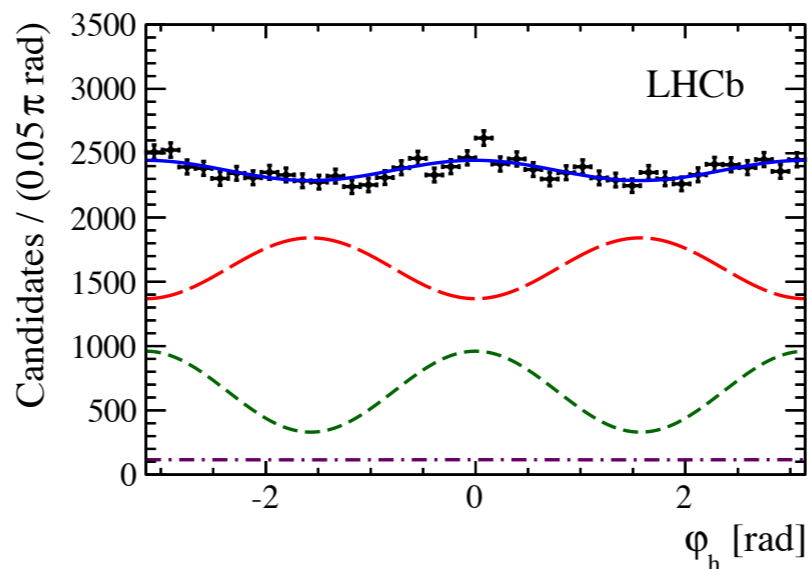
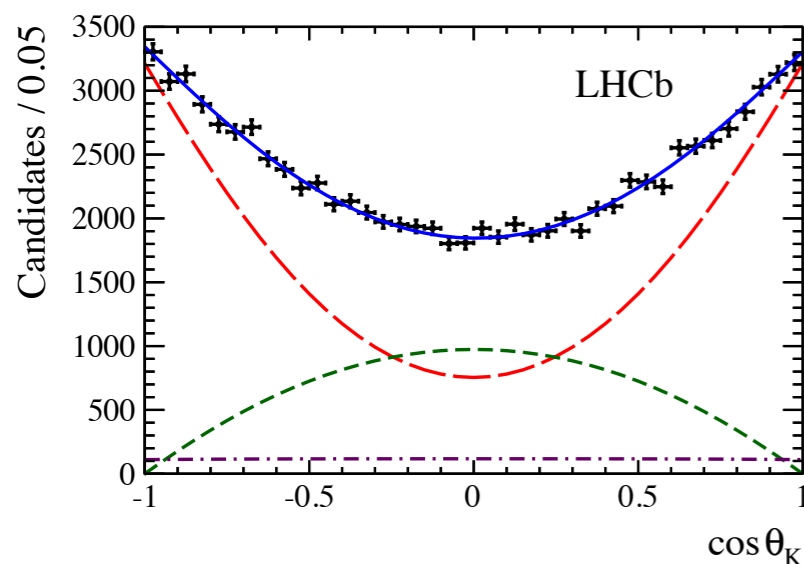
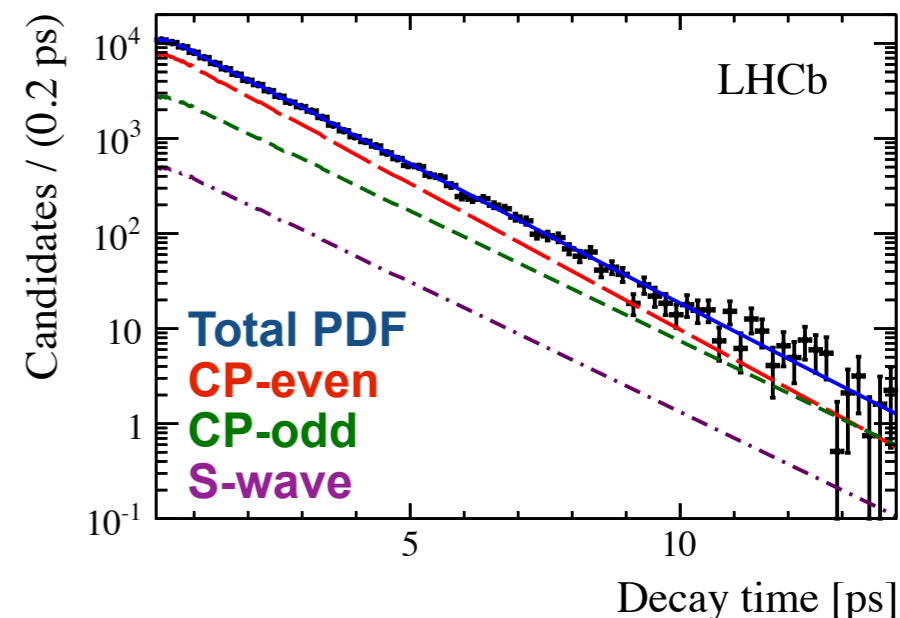


Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

[Phys. Rev. Lett. 114 041801 (2015)]

◆ Results: (polarisation independent)

Parameter	Value
Γ_s [ps^{-1}]	$0.6603 \pm 0.0027 \pm 0.0015$
$\Delta\Gamma_s$ [ps^{-1}]	$0.0805 \pm 0.0091 \pm 0.0032$
ϕ_s [rad]	$-0.058 \pm 0.049 \pm 0.006$
$ \lambda $	$0.964 \pm 0.019 \pm 0.007$



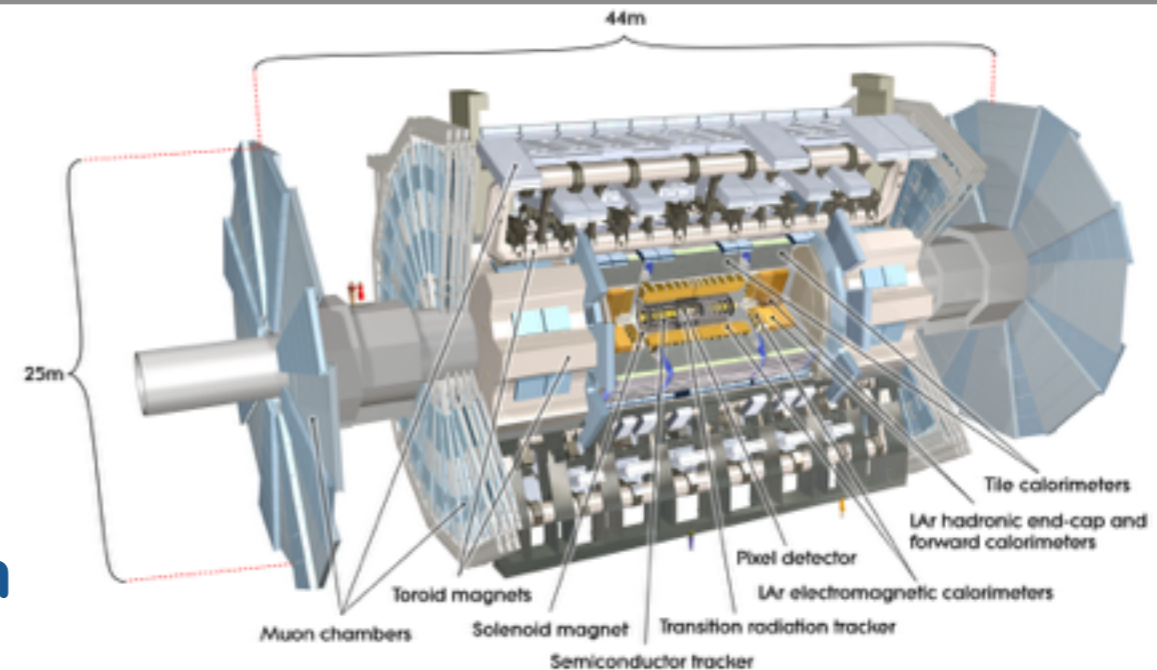
- World most precise single measurement
- Consistent with SM prediction

Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (4.9 fb^{-1})

[Phys. Rev. D. 90, 052007 (2014)]

Analysis overview:

- Performed on 2011 data
- Measures ϕ_s , Γ_s and $\Delta\Gamma_s$
 - ▶ Time-dependent tagged angular analysis (classic fit)
 - including background contribution
 - S-wave compatible with 0
 - tagging power $\sim 1.5\%$
 - $|\lambda|$ fixed to unity



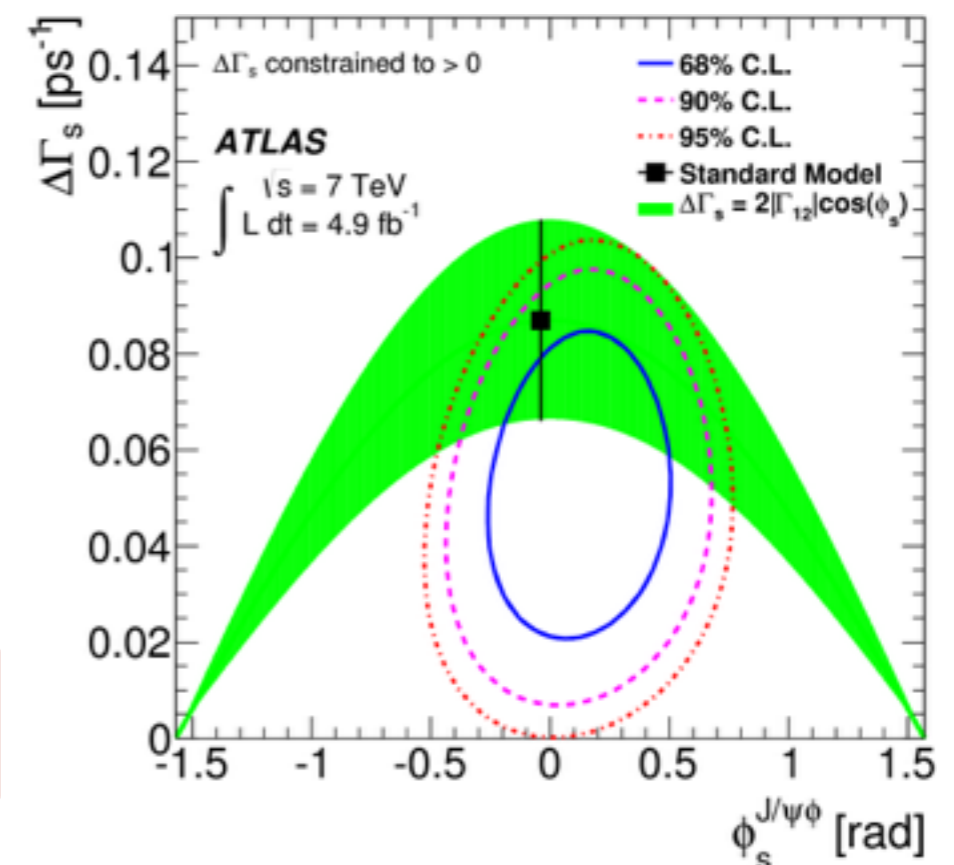
Results:

$$\phi_s = 0.12 \pm 0.25 \text{ (stat.)} \pm 0.05 \text{ (syst.) rad}$$

$$\Delta\Gamma_s = 0.053 \pm 0.021 \text{ (stat.)} \pm 0.010 \text{ (syst.) ps}^{-1}$$

$$\Gamma_s = 0.677 \pm 0.007 \text{ (stat.)} \pm 0.004 \text{ (syst.) ps}^{-1}$$

- Consistent with SM & world average
- Expect an update with 2012 data soon...



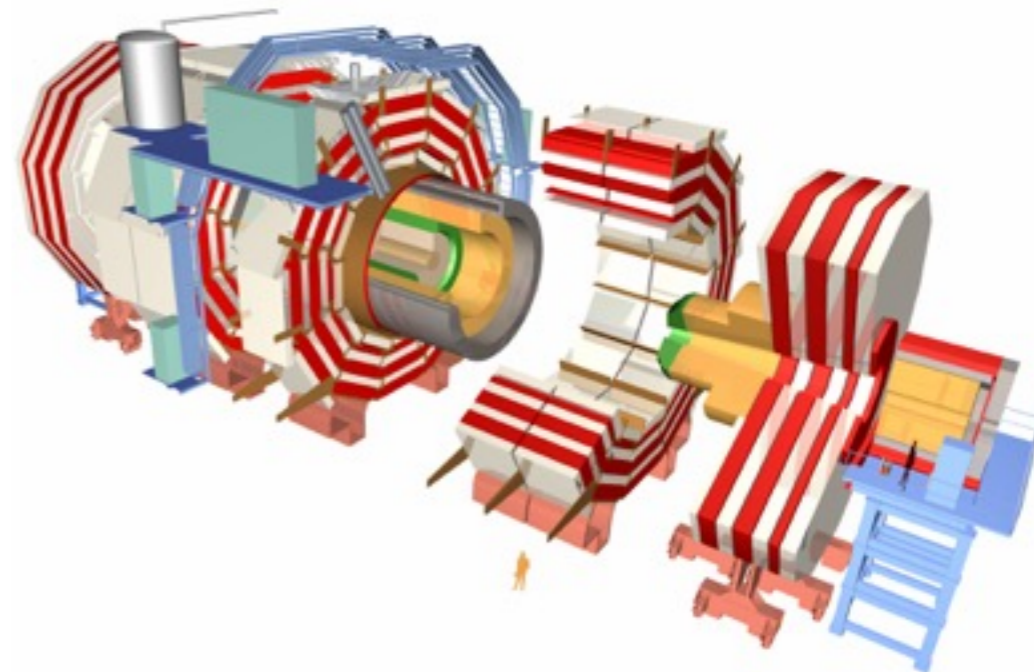


Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (20 fb^{-1})

[CMS-PAS-BPH-13-012]

◆ Analysis overview:

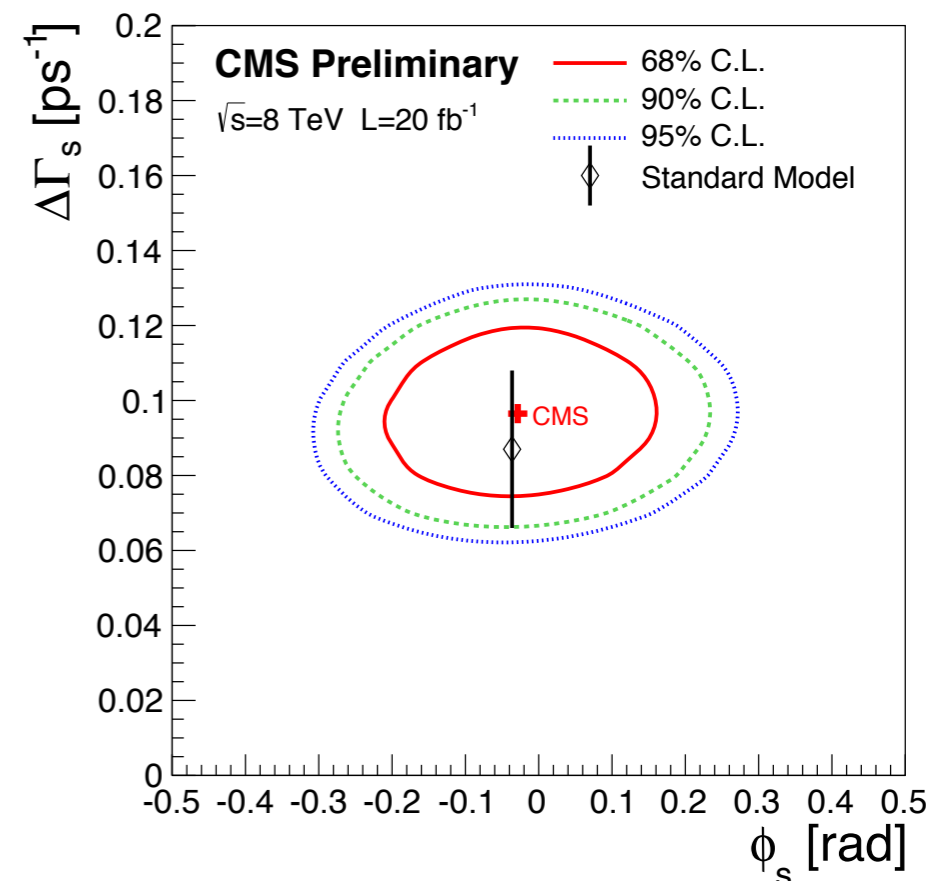
- Performed on 2012 data
- Measures ϕ_s and $\Delta\Gamma_s$
 - ▶ Time-dependent tagged angular analysis (classic fit)
 - including background contribution
 - S-wave compatible with 0
 - tagging power $\sim 1.0\%$
 - $|\lambda|$ fixed to unity (let free for syst.)



◆ Preliminary results:

$$\begin{aligned}\phi_s &= -0.03 \pm 0.11 \text{ (stat.)} \pm 0.03 \text{ (syst.) rad,} \\ \Delta\Gamma_s &= 0.096 \pm 0.014 \text{ (stat.)} \pm 0.007 \text{ (syst.) ps}^{-1}\end{aligned}$$

- Consistent with SM & world average

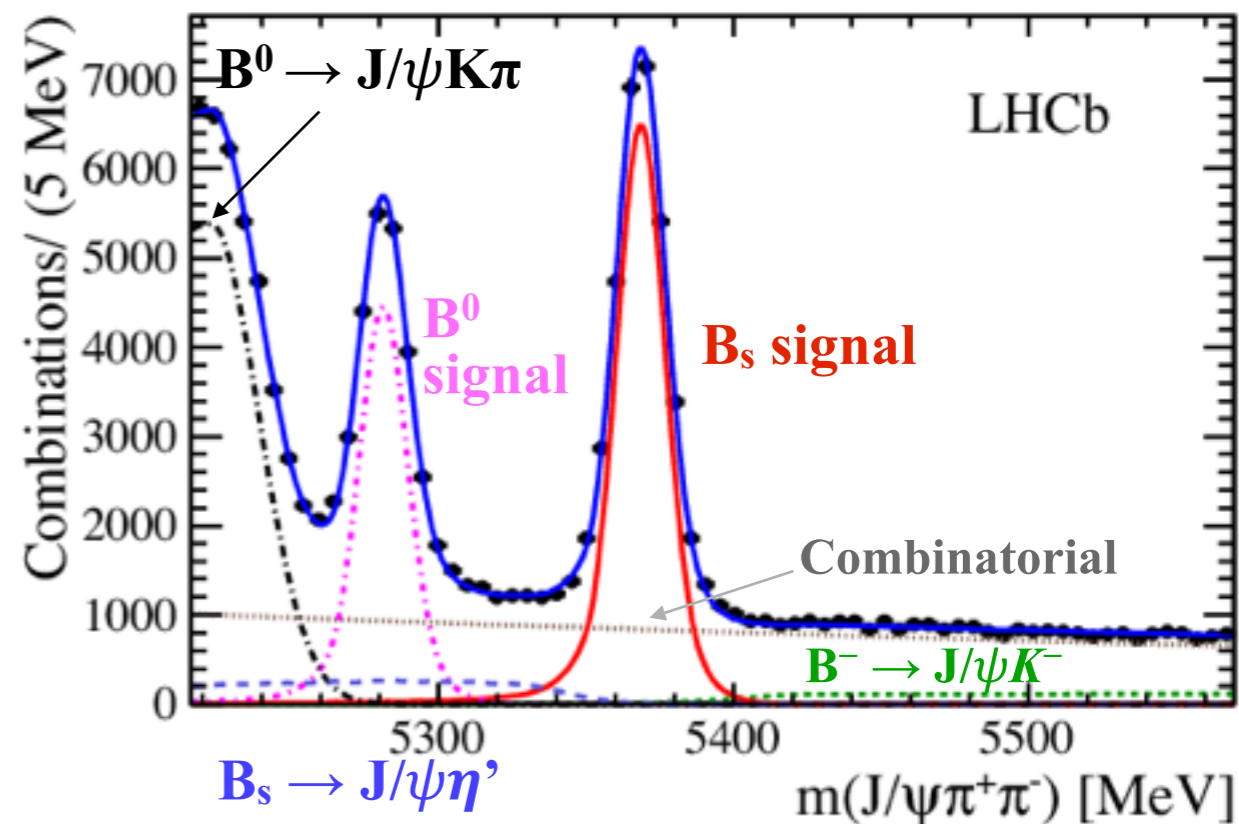


Measurement of ϕ_s in $B_s \rightarrow J/\psi \pi^+ \pi^-$ (3 fb^{-1})

[Phys. Lett. B 736 (2014) 186]

◆ Analysis overview:

- Measures ϕ_s , and $|\lambda|$
 - ▶ Time-dependent flavor-tagged amplitude analysis
 - $\sim 27\text{k}$ signal events
 - classic fit (signal + background)
 - study $\pi\pi$ invariant-mass up to $m_{\pi\pi} \sim 2.3 \text{ GeV}$
 - tagging power $\sim 3.9\%$
 - amplitude fit performed only on events within $\pm 20 \text{ MeV}$ from the B_s mass peak
 - includes 5 resonant + 1 non-resonant amplitudes



Measurement of ϕ_s in $B_s \rightarrow J/\psi \pi^+ \pi^-$ (3 fb^{-1})

[Phys. Lett. B 736 (2014) 186]

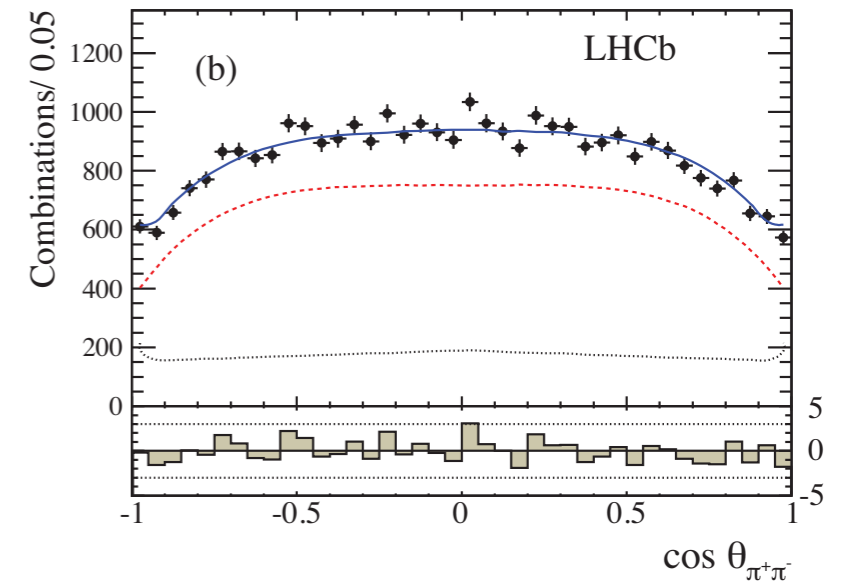
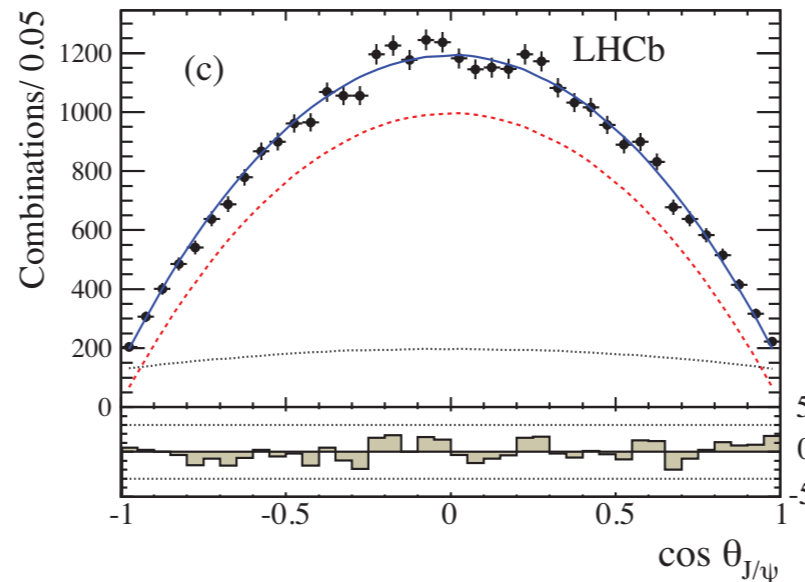
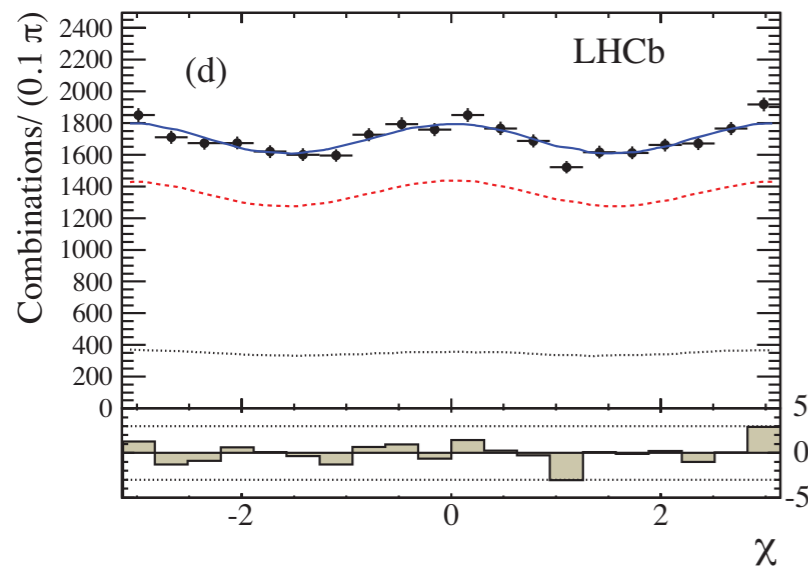
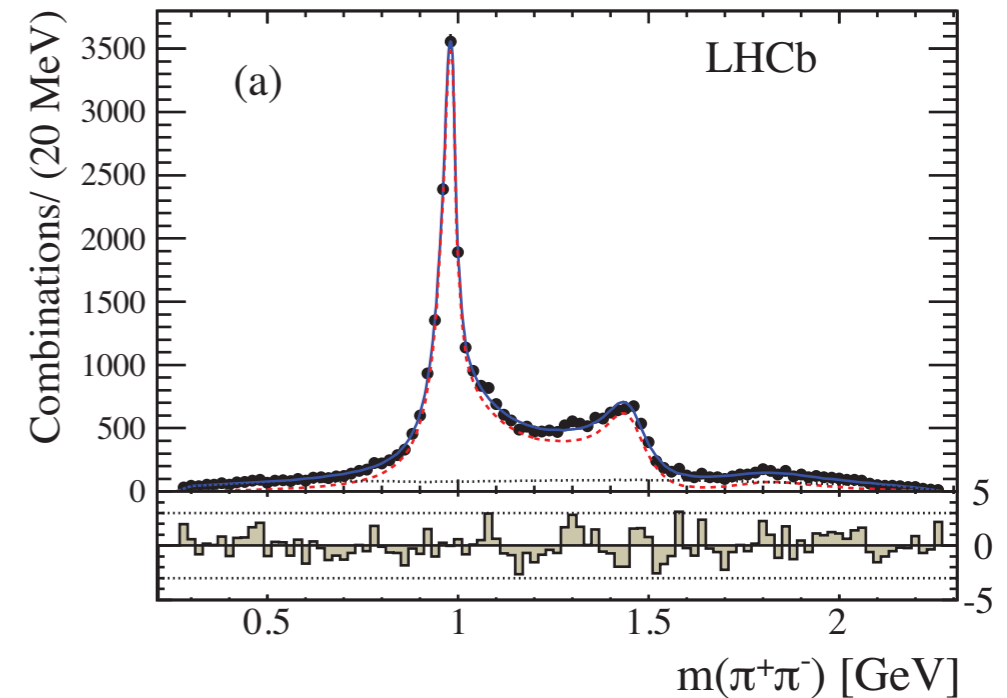
◆ Results:

$$\phi_s = 0.070 \pm 0.068 \pm 0.008 \text{ rad}$$

$$|\lambda| = 0.89 \pm 0.05 \pm 0.01$$

$$\phi_s = 0.075 \pm 0.067 \pm 0.008 \text{ rad}$$

for λ fixed to one (no direct CPV)



- World second most precise single measurement
- Consistent with SM prediction & world average

Measurement of ϕ_s in $B_s \rightarrow D_s^+ D_s^-$ (3 fb^{-1})

[Phys. Rev. Lett. 113 (2014) 211801]

◆ Analysis overview:

• Measures ϕ_s and $|\lambda|$

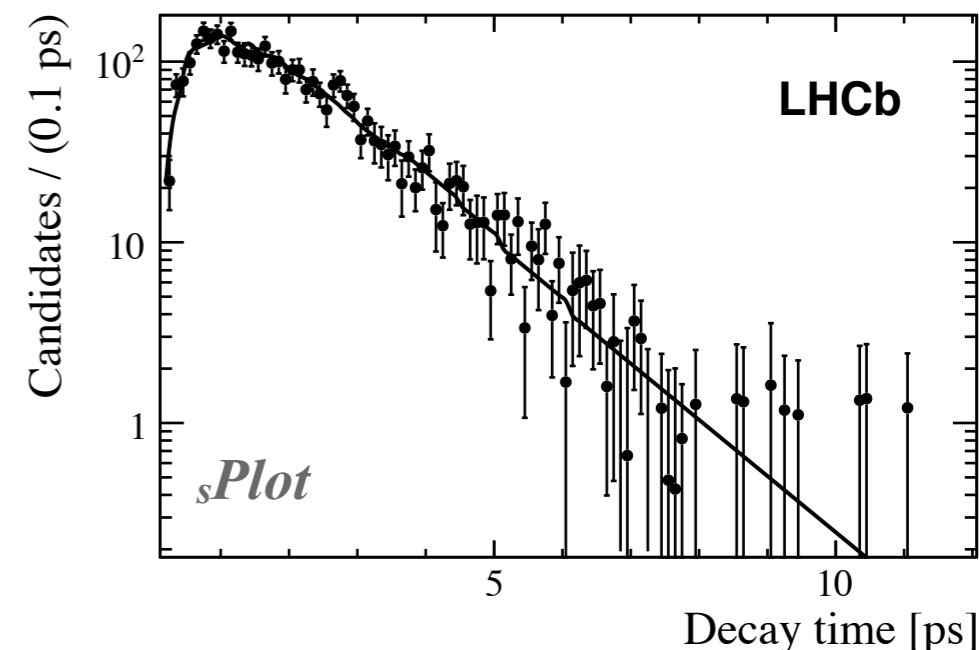
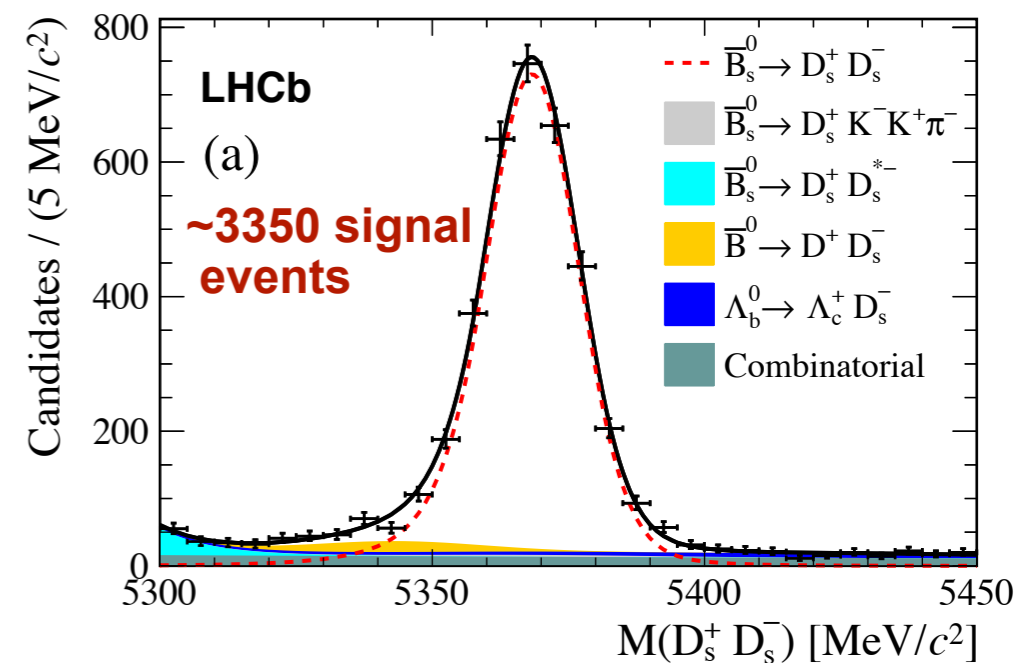
- ▶ Time-dependent flavor-tagged analysis (classic fit)
 - purely CP-even mode (no angular fit needed)
 - D_s reconstructed as $KK\pi$, $K\pi\pi$ or $\pi\pi\pi$
 - Using $B^0 \rightarrow D^- D_s^+$ as control channel
 - tagging power $\sim 5.3\%$

◆ Results:

$$\phi_s = 0.02 \pm 0.17 \text{ (stat)} \pm 0.02 \text{ (syst)} \text{ rad}$$

$$|\lambda| = 0.91^{+0.18}_{-0.15} \text{ (stat)} \pm 0.02 \text{ (syst)}$$

- Consistent with SM & world average



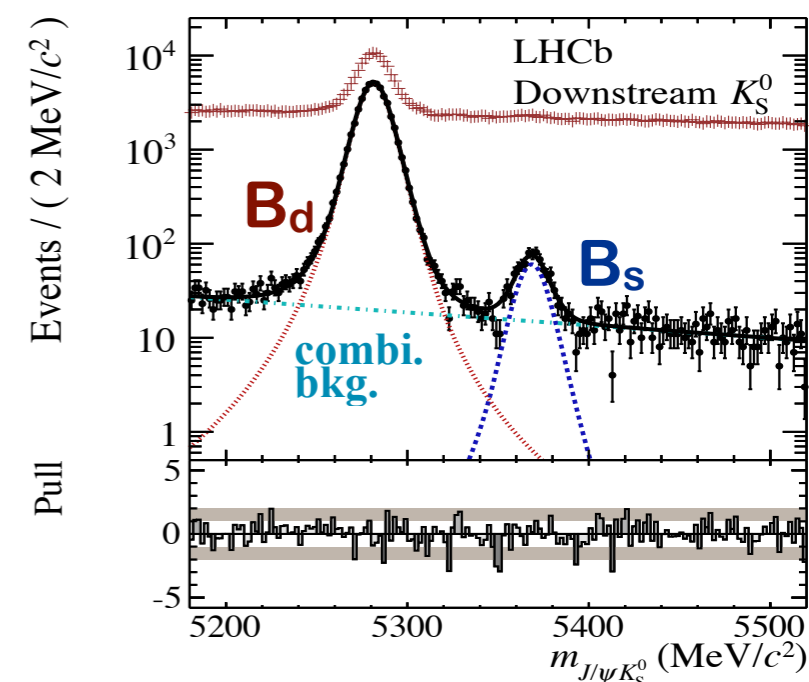
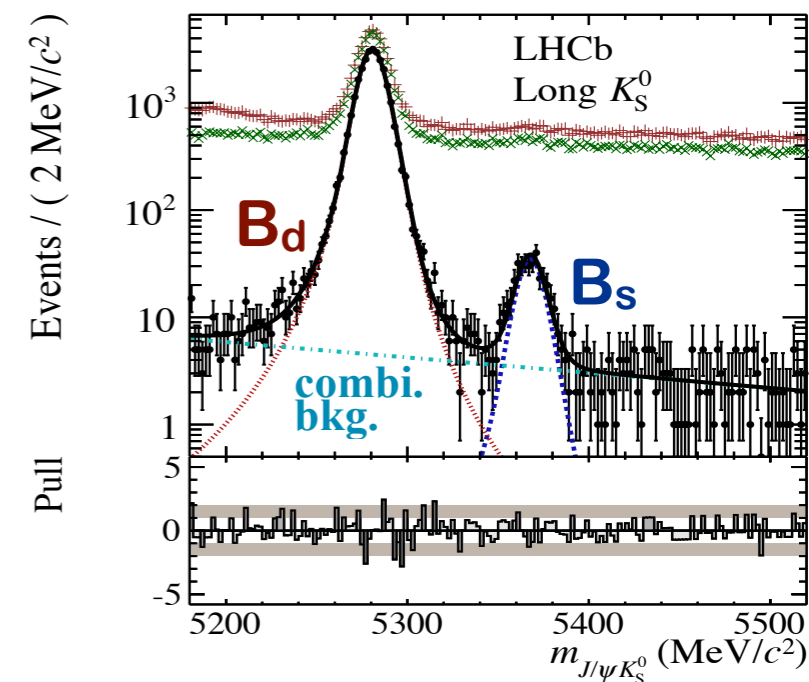
Measurement of TDCP asymmetries in $B_s \rightarrow J/\psi K_S^0$ (3 fb^{-1})

Article submitted to JHEP [[arXiv:1503.07055](https://arxiv.org/abs/1503.07055)]

♦ Analysis overview:

- First **time-dependent CPV** measurements in this channel
- Flavor-tagged time-dependent analysis:
 - ▶ simultaneous fit to a mixed sample of many B_d and few B_s events (**100/1**)
 - ▶ use of multivariate selection trained on B_d proxy
 - ▶ split sample in two categories:
 - **Downstream K_S** (no velo hits)
 - **Long K_S** (velo hits \rightarrow better resolution)
 - ▶ tagging power:
 - $B_s \sim 3.8\%$ / $B_d \sim 2.6\%$
 - ▶ also fits for $\sin 2\beta$ (as cross-check)
 - see previous talk

Yield	Long K_S^0	Downstream K_S^0
$B^0 \rightarrow J/\psi K_S^0$	$27\,801 \pm 168$	$51\,351 \pm 231$
$B_s^0 \rightarrow J/\psi K_S^0$	307 ± 20	601 ± 30
Combinatorial background	658 ± 37	$2\,852 \pm 74$



Measurement of TDCP asymmetries in $B_s \rightarrow J/\psi K_S^0$ (3 fb^{-1})

Article submitted to JHEP [[arXiv:1503.07055](https://arxiv.org/abs/1503.07055)]

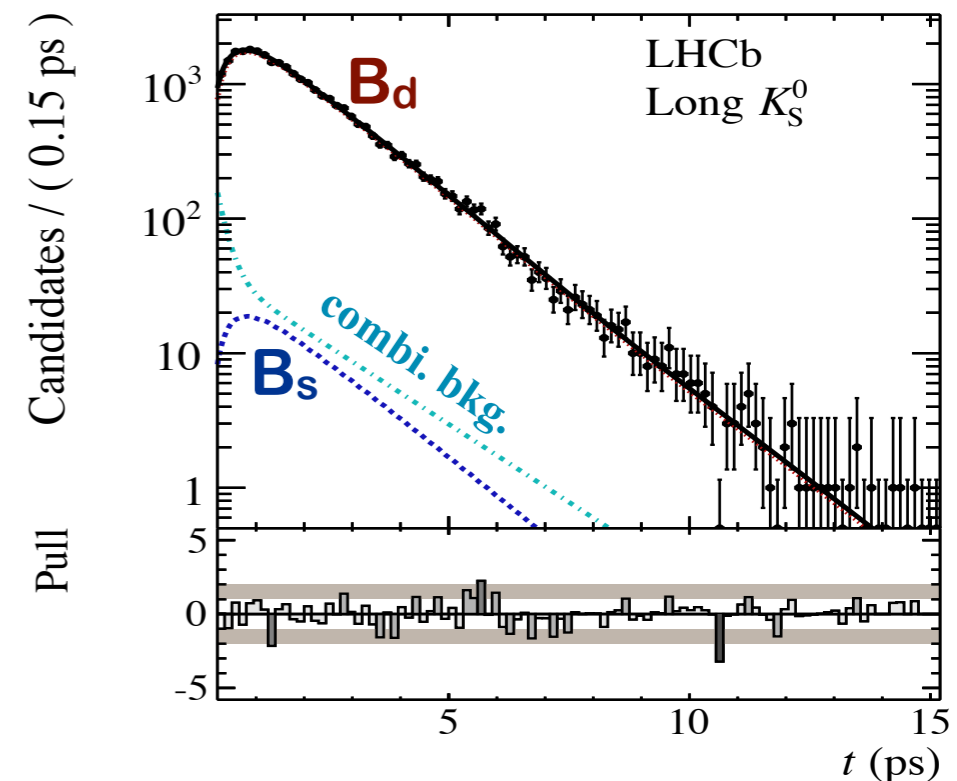
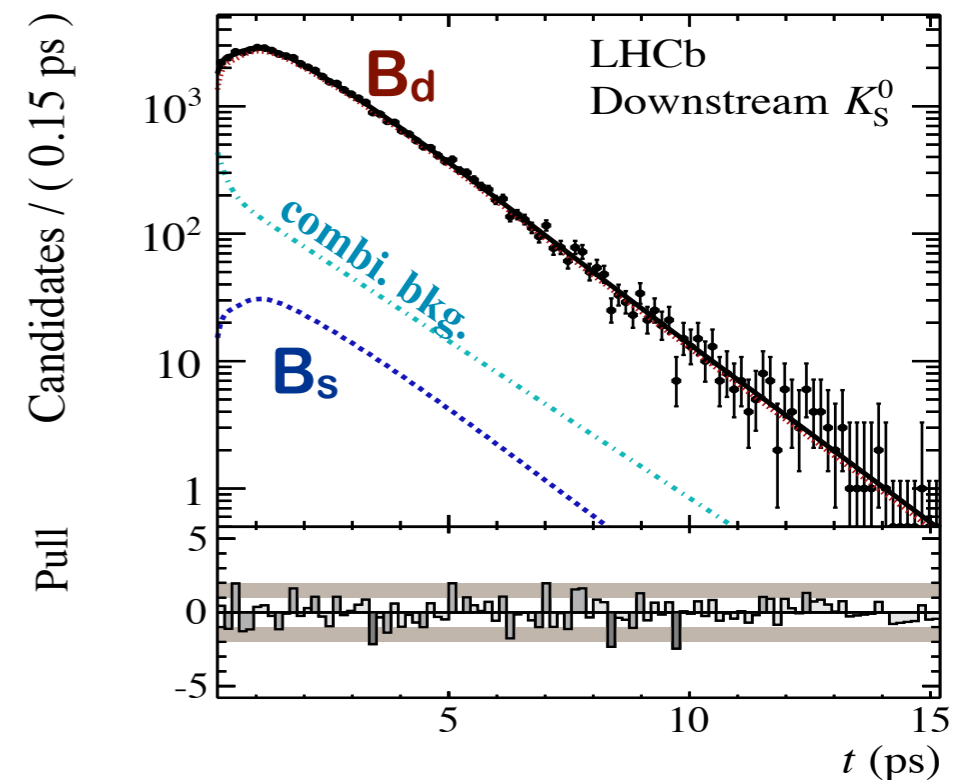
◆ Preliminary results:

$$\begin{aligned} \mathcal{A}_{\Delta\Gamma}(B_s^0 \rightarrow J/\psi K_S^0) &= 0.49 \pm_{0.65}^{0.77} \text{ (stat)} \pm 0.06 \text{ (syst)} \\ C_{\text{dir}}(B_s^0 \rightarrow J/\psi K_S^0) &= -0.28 \pm 0.41 \text{ (stat)} \pm 0.08 \text{ (syst)} \\ S_{\text{mix}}(B_s^0 \rightarrow J/\psi K_S^0) &= -0.08 \pm 0.40 \text{ (stat)} \pm 0.08 \text{ (syst)} \end{aligned}$$

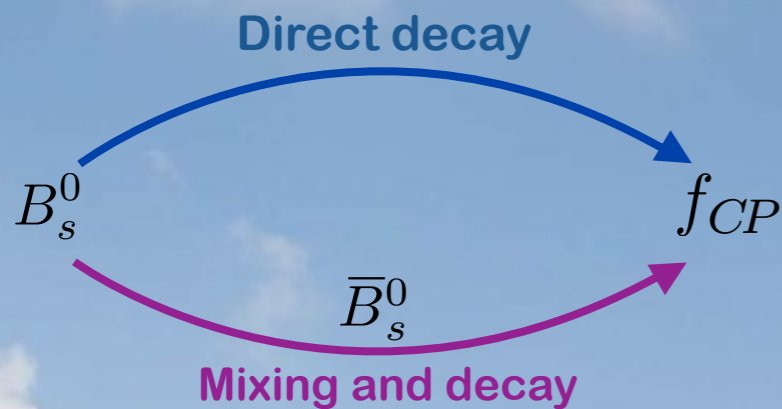
Recent prediction: [[arXiv:1412.6834](https://arxiv.org/abs/1412.6834)]

$$\begin{aligned} \mathcal{A}_{\Delta\Gamma}(B_s^0 \rightarrow J/\psi K_S^0) &= 0.957 \pm 0.061 \\ C_{\text{dir}}(B_s^0 \rightarrow J/\psi K_S^0) &= 0.003 \pm 0.021 \\ S_{\text{mix}}(B_s^0 \rightarrow J/\psi K_S^0) &= 0.29 \pm 0.20 \end{aligned}$$

- Successful proof of concept waiting for more statistics
- Can be used to estimate the penguin effects in $\sin 2\beta$ as well as in ϕ_s



OUTLINE



1 Physics motivation

2 Measurement ingredients

3 Measurement of ϕ_s :

- ▶ $B_s \rightarrow J/\psi K^+ K^-$
- ▶ $B_s \rightarrow J/\psi \pi^+ \pi^-$
- ▶ $B_s \rightarrow D_s^+ D_s^-$
- ▶ $B_s \rightarrow J/\psi K_S^0$



4 Constraining penguins in ϕ_s :

- ▶ $B_d \rightarrow J/\psi \pi^+ \pi^-$



Analysis overview:

- Measures $2\beta^{\text{eff}}$ and α_{CP}

$$\alpha_{CP} = \frac{1 - |\lambda_f|}{1 + |\lambda_f|}$$

- Similar to $B_s \rightarrow J/\psi \pi^+ \pi^-$
 - Time-dependent flavor-tagged angular analysis (classic fit)
 - ~ 18k signal events

Results:

$$2\beta^{\text{eff}}(B^0 \rightarrow J/\psi \rho^0) = (41.7 \pm 9.6(\text{stat})_{-6.3}^{+2.8}(\text{syst}))^\circ$$

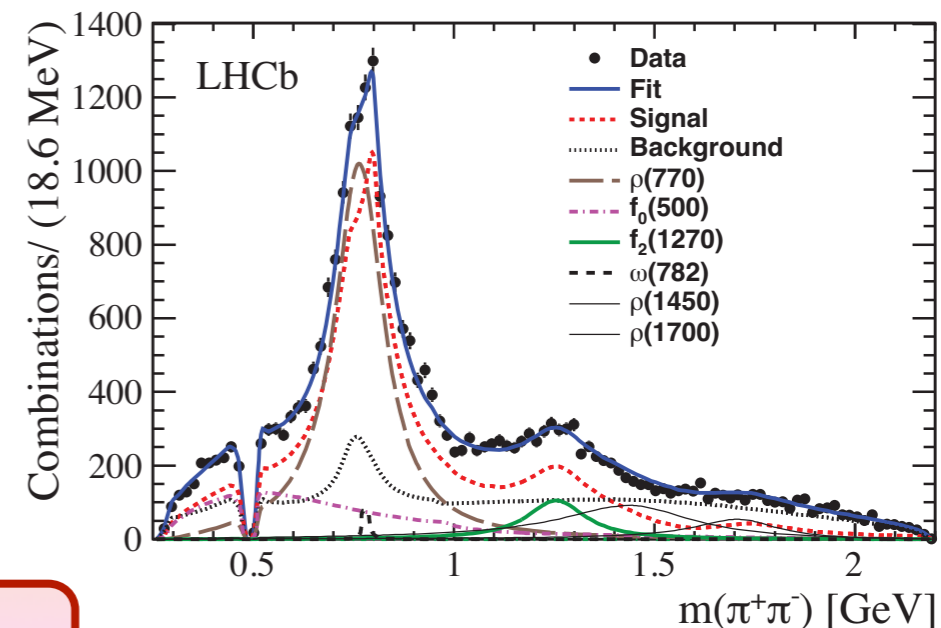
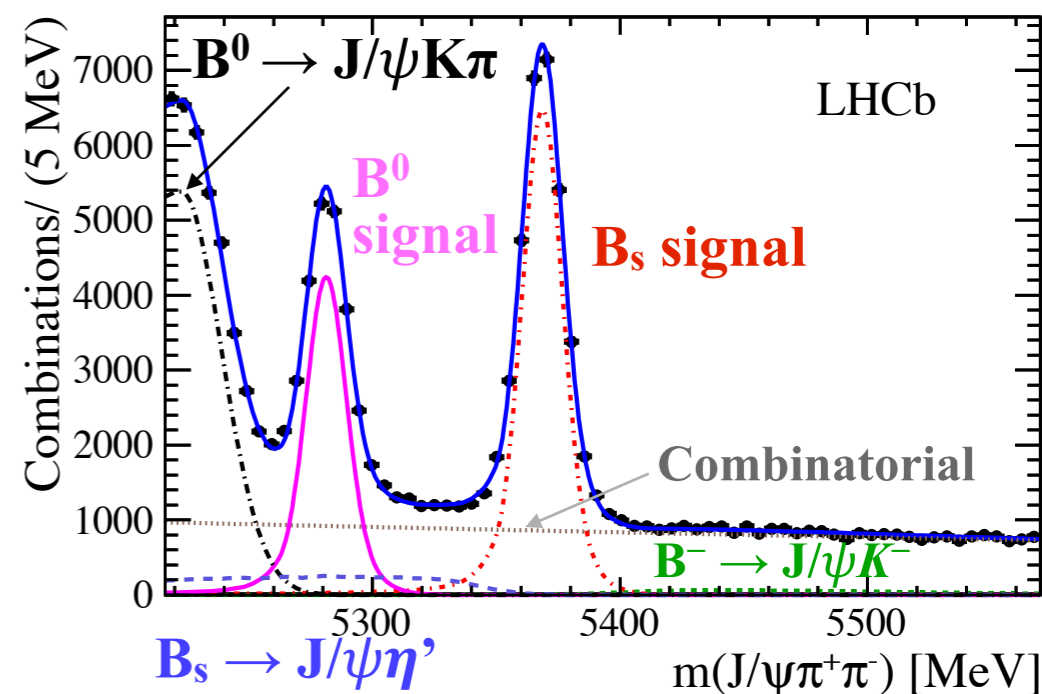
$$\alpha_{CP}(B^0 \rightarrow J/\psi \rho^0) = -(32 \pm 28(\text{stat})_{-9}^{+7}(\text{syst})) \times 10^{-3}$$

Used in penguin contribution estimation (next slide)

$$\mathcal{S}_{J/\psi \rho^0} = -0.66_{-0.12}^{+0.13}(\text{stat})_{-0.03}^{+0.09}(\text{syst})$$

$$\mathcal{C}_{J/\psi \rho^0} = -0.063 \pm 0.056(\text{stat})_{-0.014}^{+0.019}(\text{syst})$$

Most precise CP asymmetry measurement in this mode



◆ Limits on penguin effects:

$$A(B^0 \rightarrow J/\psi \rho^0) = \tilde{A} \left[1 - a e^{i\theta} e^{i\gamma} \right]$$

$$A(B_s^0 \rightarrow J/\psi \phi) = \tilde{A}' \left[1 - \epsilon a' e^{i\theta'} e^{i\gamma} \right]$$

$$\epsilon \equiv \lambda_c^2 / (1 - \lambda_c^2) = 0.0534$$

$$|\lambda_f| = \left| \frac{1 - a e^{i\theta} e^{-i\gamma}}{1 - a e^{i\theta} e^{i\gamma}} \right| \quad \alpha_{CP} = \frac{1 - |\lambda_f|}{1 + |\lambda_f|}$$

$$\Delta 2\beta = (2\beta^{\text{eff}} - 2\beta) = -\arg \left(\frac{1 - a e^{i\theta} e^{-i\gamma}}{1 - a e^{i\theta} e^{i\gamma}} \right)$$

$$\Delta \phi_s = -\arg \left(\frac{(\lambda'_f e^{2i\gamma} - 1) + \epsilon(\lambda'_f - 1)}{(\lambda'_f e^{2i\gamma} - 1) + \epsilon(\lambda'_f - 1)e^{2i\gamma}} \right) \quad \lambda'_f \equiv |\lambda_f| e^{-i\Delta 2\beta}$$

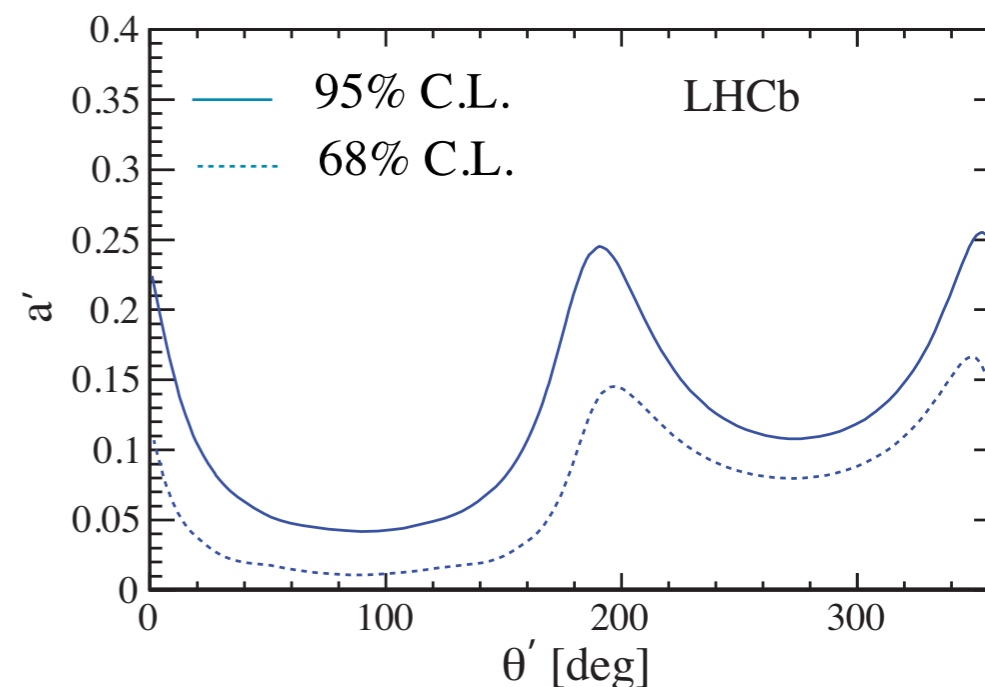
- Assuming perfect SU(3) flavor symmetry: $a = a' \quad \theta = \theta'$

$$\begin{aligned} \Delta 2\beta &= (2\beta^{J/\psi \rho} - 2\beta^{J/\psi K_S^0}) \\ &= (-0.9 \pm 9.7(\text{stat})_{-6.3}^{+2.8}(\text{syst}))^\circ \end{aligned}$$

$$\Delta \phi_s \sim -\epsilon \Delta 2\beta$$

$$\Delta \phi_s \in [-1.05^\circ, 1.18^\circ] \text{ at } 95\% \text{ C.L.}$$

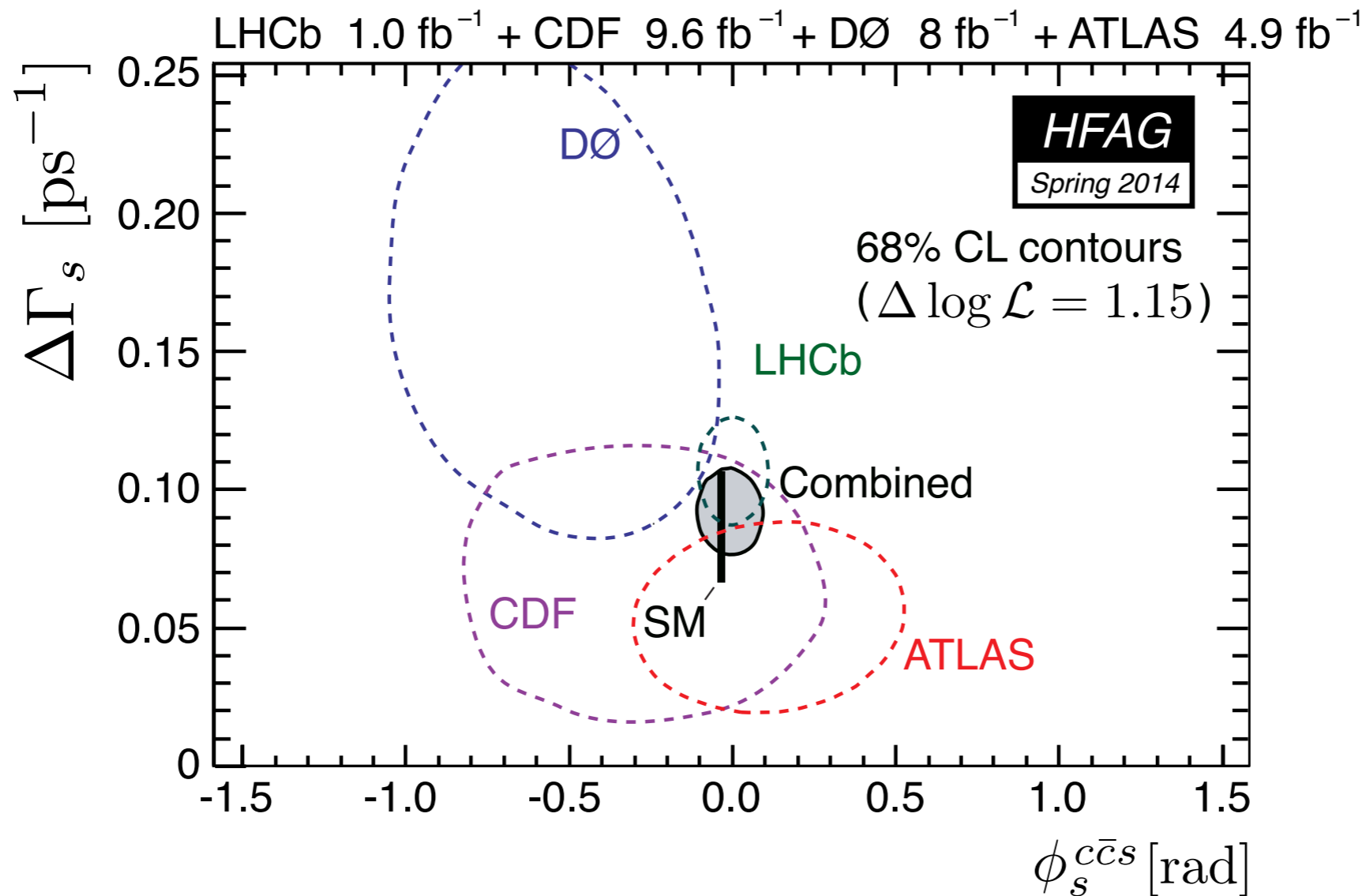
First experimental constraint on penguin contribution on ϕ_s



IN SUMMARY

◆ Toward a precise measurement of ϕ_s :

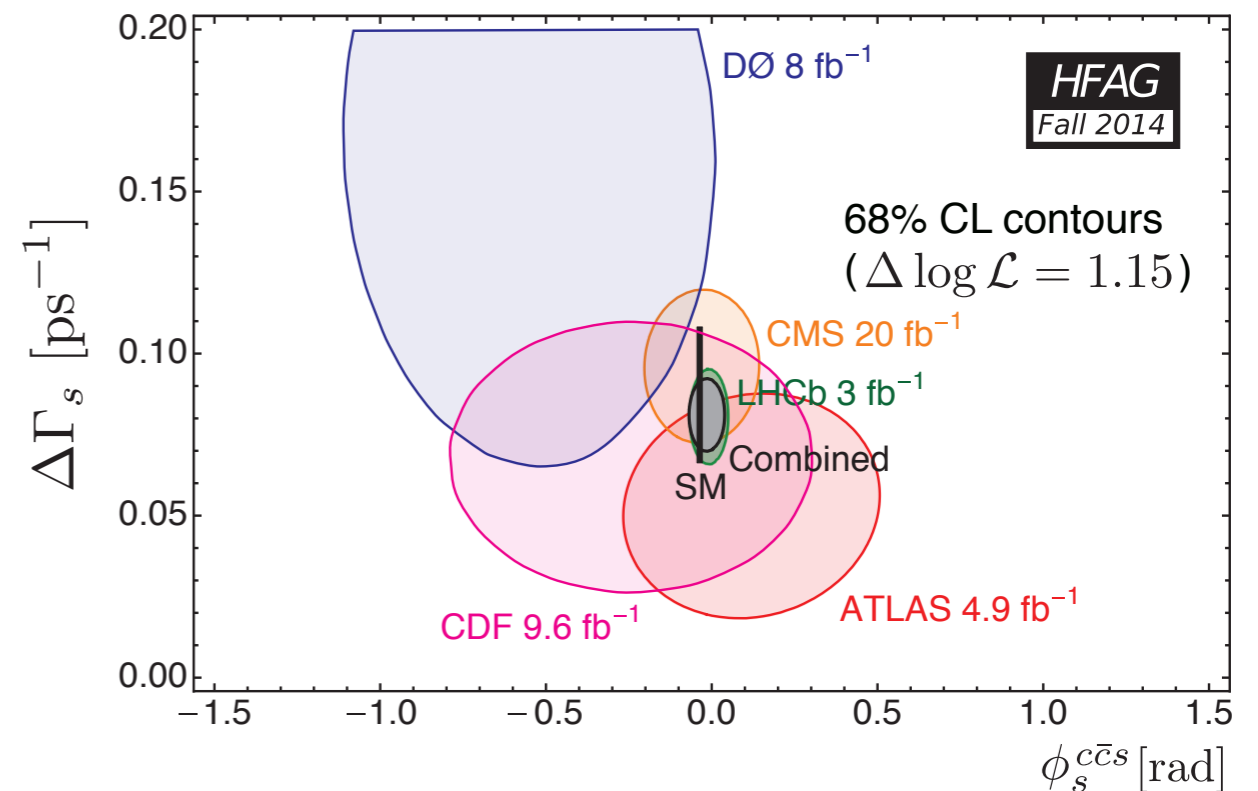
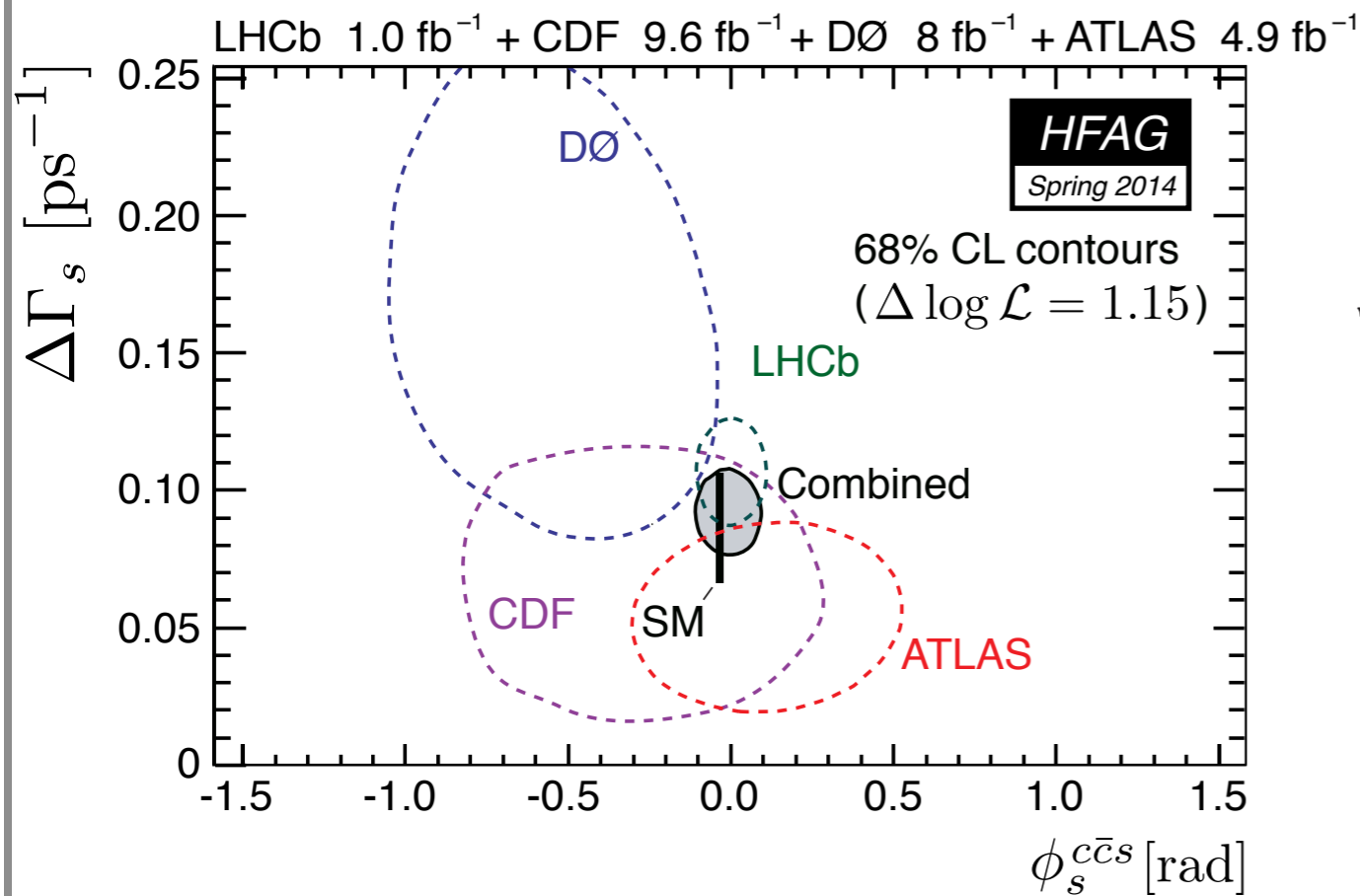
State of the art
at FPCP 2014



IN SUMMARY

◆ Toward a precise measurement of ϕ_s :

State of the art
at FPCP 2015



IN SUMMARY

◆ Toward a precise measurement of ϕ_s :

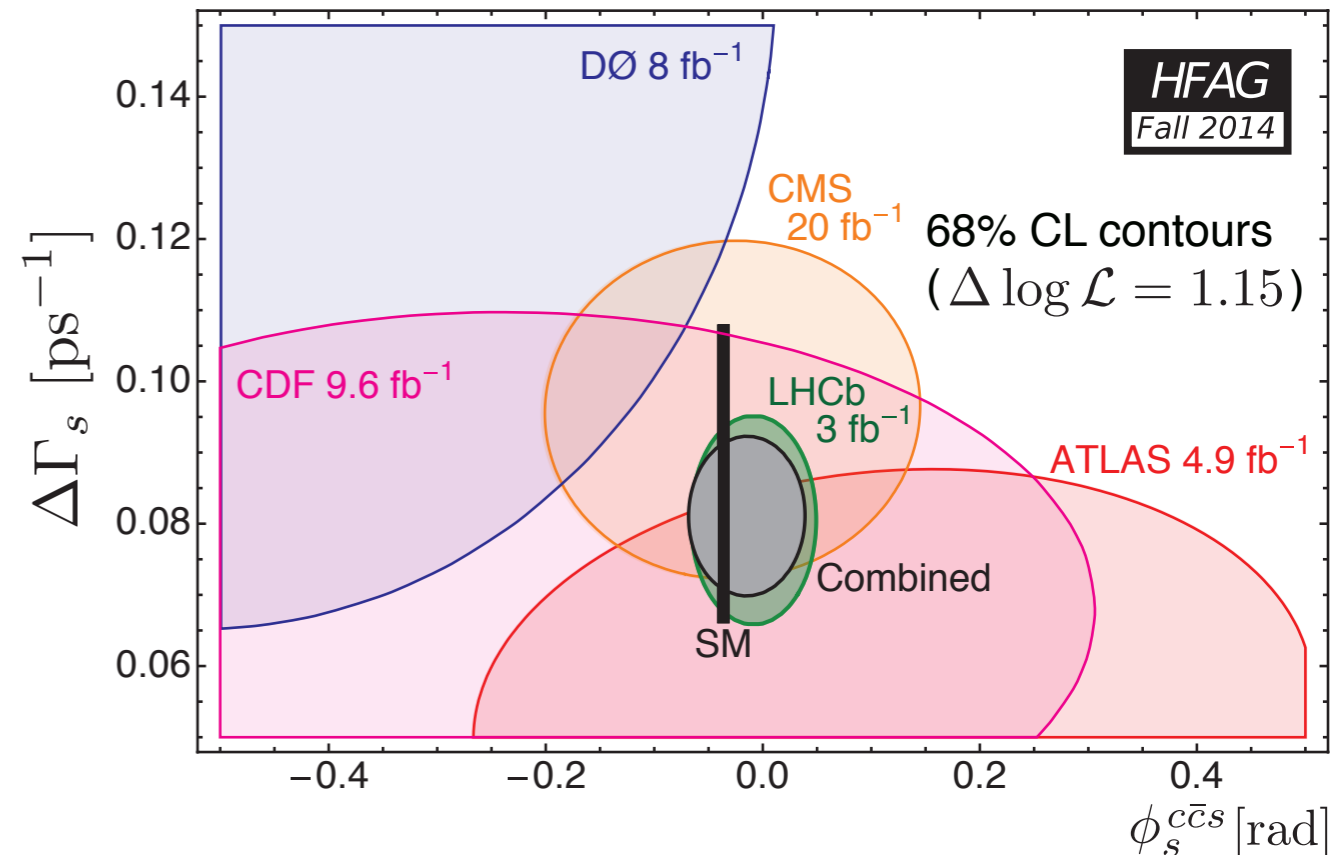
State of the art
at FPCP 2015

$$\begin{aligned}\phi_s^{c\bar{c}s} &= -2\beta_s + \Delta\phi_s^{\text{Peng.}} + \delta^{\text{NP}} \\ &= -0.015 \pm 0.035 \text{ [HFAG]}\end{aligned}$$

$$-2\beta_s = -0.0365^{+0.0013}_{-0.0012} \text{ [CKMFitter]}$$

$$\Delta\phi_s^{\text{Peng.}} = 0.001 \pm 0.010$$

$$\delta^{\text{NP}} = ??$$



- Entered era of precise CPV measurement in the B_s system
- First step in controlling penguin contributions
- Precision will further increase with LHC RunII & Upgrades adding statistics and new measurements!

SPARE SLIDES

★ Mixing-induced CP violation in penguin dominated transitions: $\phi_s^{s\bar{s}s}$

▸ $B_s \rightarrow \phi\phi$ [[Phys. Rev. D90, 052011 \(2014\)](#)]

★ Complementary material on $\phi_s^{c\bar{c}s}$ measurements

▸ $B_{d(s)} \rightarrow \pi^+\pi^-(K^+K^-)$ [[Phys. Lett. B 741 \(2015\) 1](#)]

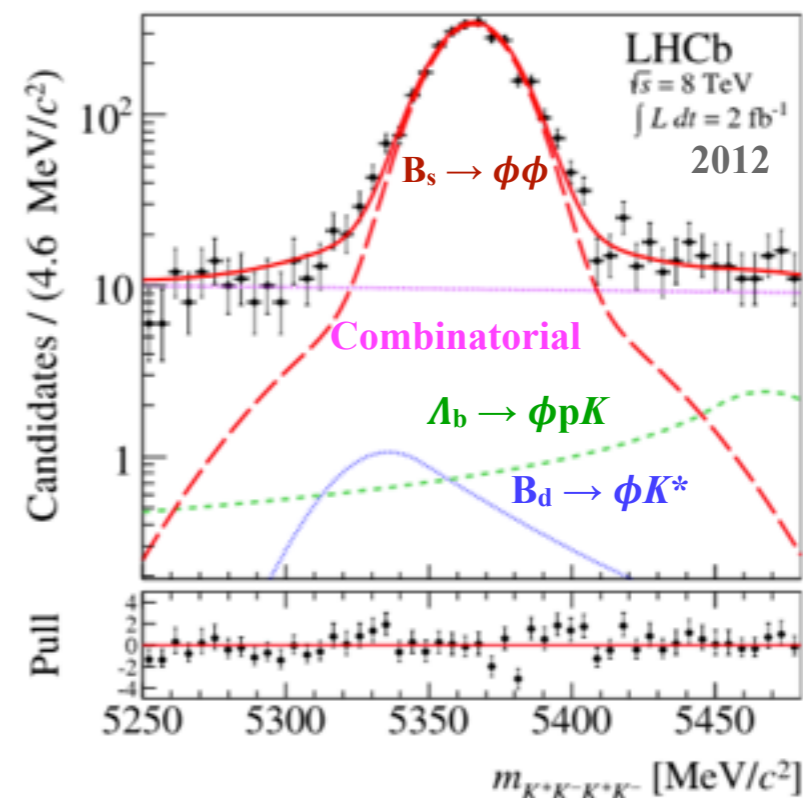
Analysis not presented here.

Making use of CKM angle γ as input in the determination of $-2\beta_s$

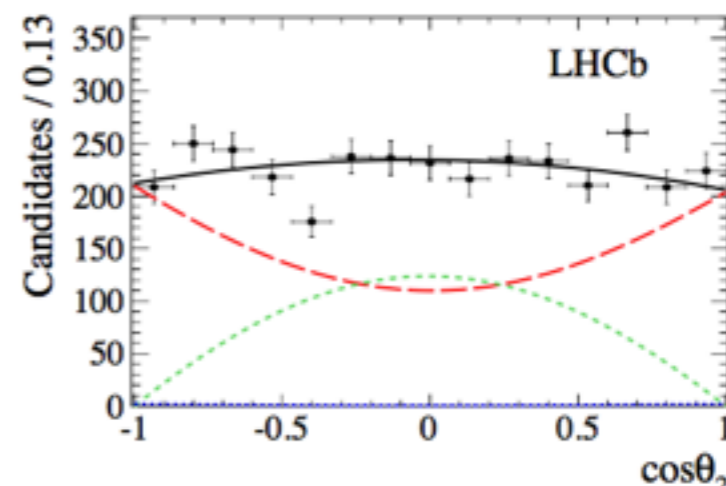
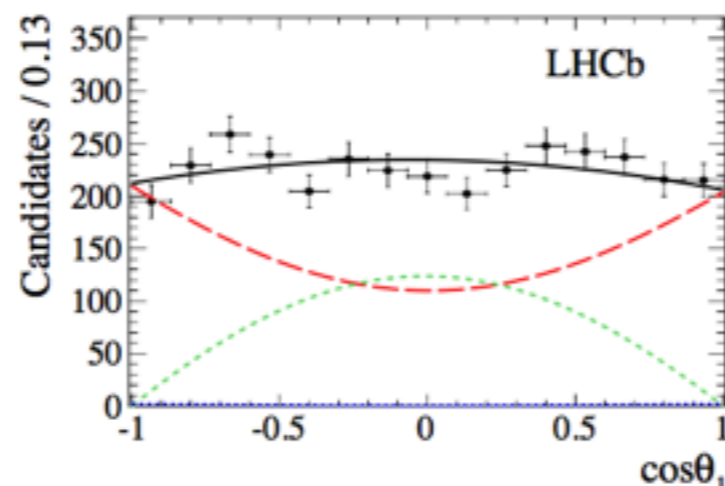
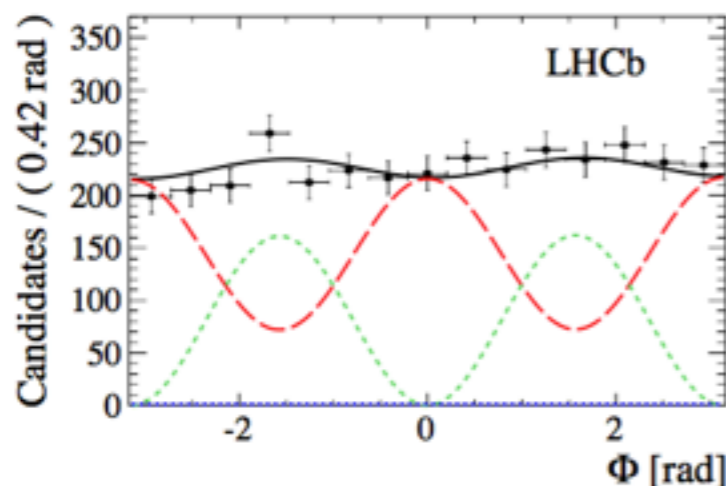


Analysis overview:

- ϕ_s in $b \rightarrow s\bar{s}$ transitions:
 - ▶ Dominated by gluonic penguin loops
 - ▶ Good sensitivity to NP
 - ▶ SM prediction $\phi_s(b \rightarrow s\bar{s}) \sim 0$
- Time-dependent flavor-tagged angular analysis (using s Weights):
 - ▶ ~ 4000 signal events



- ## Results:
- $$\phi_s = -0.17 \pm 0.15 \text{ (stat)} \pm 0.03 \text{ (syst)} \text{ rad,}$$
- $$|\lambda| = 1.04 \pm 0.07 \text{ (stat)} \pm 0.03 \text{ (syst).}$$



Measurement of ϕ_s

Motivations for the Upgrades



[CERN-LHCC-2012-007] LHCb Upgrade TDR

Statistical uncertainties

Type	Observable	Current precision	LHCb 2018	Upgrade (50 fb ⁻¹)	Theory uncertainty
B_s^0 mixing	$2\beta_s (B_s^0 \rightarrow J/\psi \phi)$	0.10 [9]	0.025	0.008	~ 0.003
$\phi_s^{c\bar{c}s}$	$2\beta_s (B_s^0 \rightarrow J/\psi f_0(980))$	0.17 [10]	0.045	0.014	~ 0.01
	$A_{fs}(B_s^0)$	6.4×10^{-3} [18]	0.6×10^{-3}	0.2×10^{-3}	0.03×10^{-3}
Gluonic	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow \phi\phi)$	–	0.17	0.03	0.02
penguin	$2\beta_s^{\text{eff}}(B_s^0 \rightarrow K^{*0} \bar{K}^{*0})$	–	0.13	0.02	< 0.02
	$2\beta_s^{\text{eff}}(B^0 \rightarrow \phi K_S^0)$	0.17 [18]	0.30	0.05	0.02

[ATL-PHYS-PUB-2013-010]



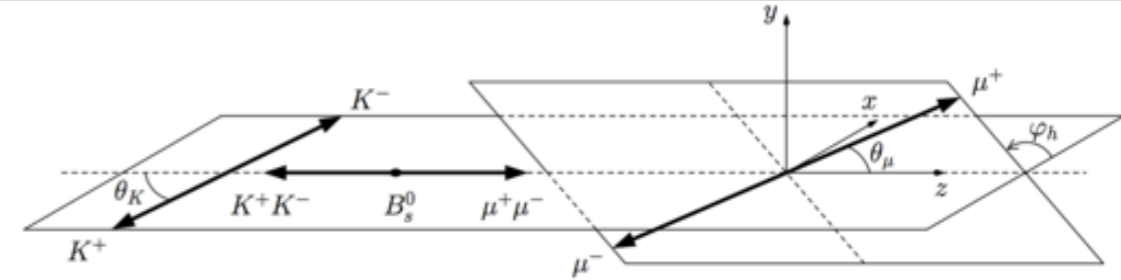
	2011	2012	2015-17		2019-21	2023-30+
Detector	current	current	IBL		IBL	ITK
Average interactions per BX $\langle \mu \rangle$	6-12	21	60		60	200
Luminosity, fb ⁻¹	4.9	20	100		250	3 000
Di- μ trigger p_T thresholds, GeV	4 - 4(6)	4 - 6	6 - 6	11 - 11	11 - 11	11 - 11
Signal events per fb ⁻¹	4 400	4 320	3 280	460	460	330
Signal events	22 000	86 400	327 900	45 500	114 000	810 000
Total events in analysis	130 000	550 000	1 874 000	284 000	758 000	6 461 000
MC $\sigma(\phi_s)$ (stat.), rad	0.25	0.12	0.054	0.10	0.064	0.022

- Will be on the verge of reaching theoretical uncertainties!

Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

[Phys. Rev. Lett. 114 041801 (2015)]

$$\frac{d^4\Gamma(t)}{dm_{KK}^2 d\cos\theta_K d\cos\theta_l d\phi} = \sum_{k=1}^{10} N_k h_k(t) f_k(\theta_K, \theta_l, \phi),$$



$$h_k(t) = \frac{3}{4\pi} e^{-\Gamma t} \left\{ a_k \cosh \frac{\Delta\Gamma t}{2} + b_k \sinh \frac{\Delta\Gamma t}{2} + c_k \cos(\Delta m t) + d_k \sin(\Delta m t) \right\}.$$

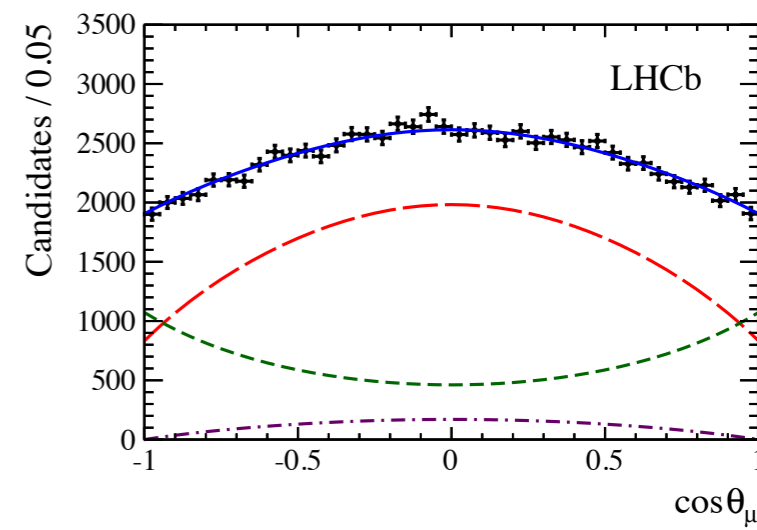
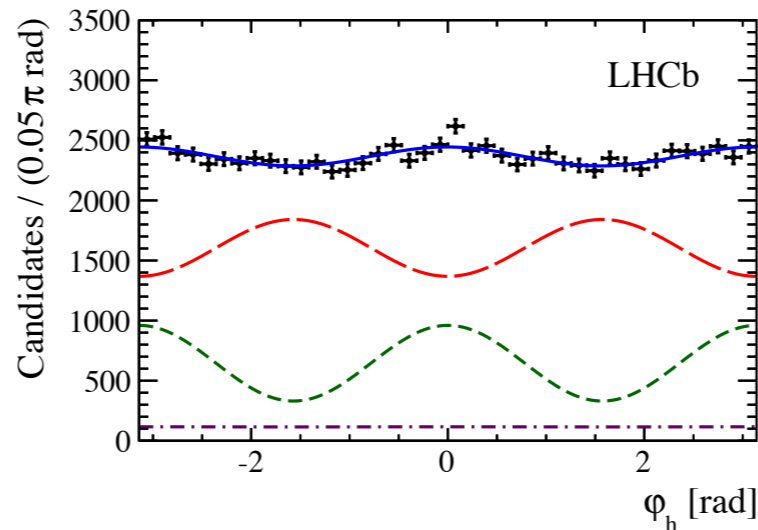
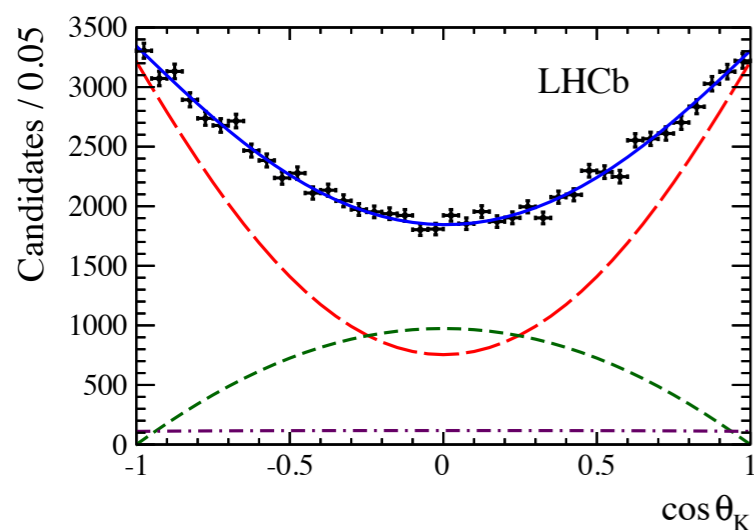
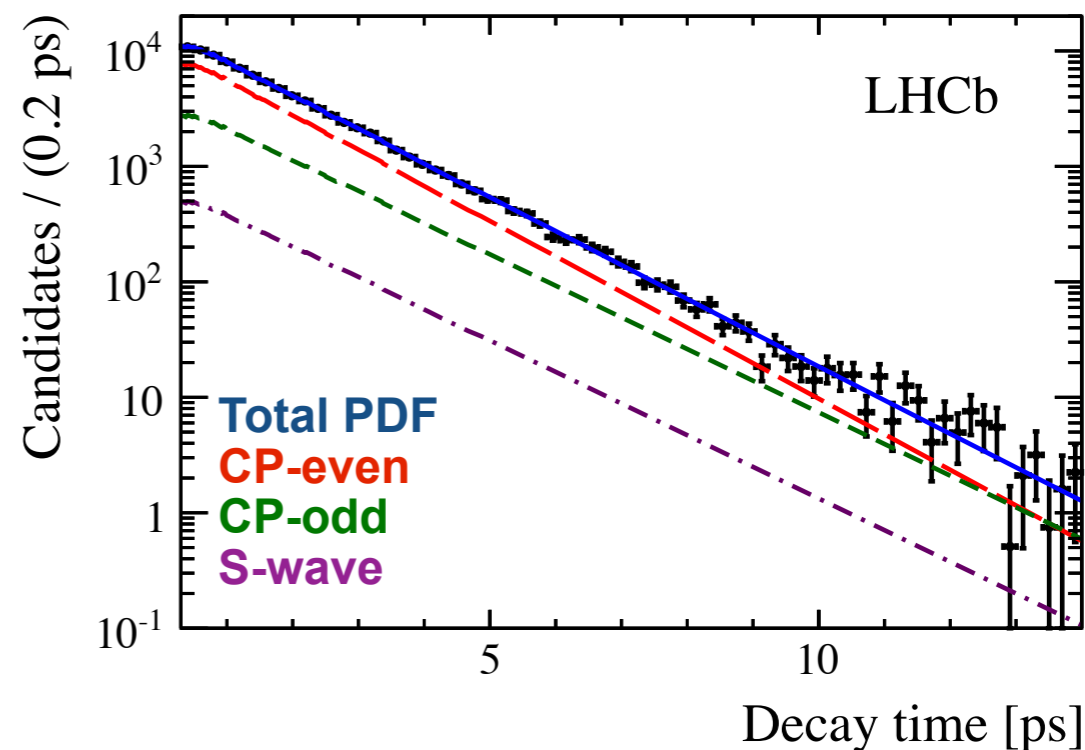
f_k	N_k	a_k	b_k	c_k	d_k
$c_K^2 s_l^2$	$ A_0 ^2$	$\frac{1}{2}(1 + \lambda_0 ^2)$	$- \lambda_0 \cos(\phi_0)$	$\frac{1}{2}(1 - \lambda_0 ^2)$	$ \lambda_0 \sin(\phi_0)$
$\frac{1}{2} s_K^2 (1 - c_\phi^2 s_l^2)$	$ A_{ } ^2$	$\frac{1}{2}(1 + \lambda_{ } ^2)$	$- \lambda_{ } \cos(\phi_{ })$	$\frac{1}{2}(1 - \lambda_{ } ^2)$	$ \lambda_{ } \sin(\phi_{ })$
$\frac{1}{2} s_K^2 (1 - s_\phi^2 s_l^2)$	$ A_{\perp} ^2$	$\frac{1}{2}(1 + \lambda_{\perp} ^2)$	$ \lambda_{\perp} \cos(\phi_{\perp})$	$\frac{1}{2}(1 - \lambda_{\perp} ^2)$	$- \lambda_{\perp} \sin(\phi_{\perp})$
$s_K^2 s_l^2 s_\phi c_\phi$	$ A_{\perp} A_{ } $	$\frac{1}{2} \left[\sin(\delta_{\perp} - \delta_{ }) - \lambda_{\perp} \lambda_{ } \sin(\delta_{\perp} - \delta_{ } - \phi_{\perp} + \phi_{ }) \right]$	$\frac{1}{2} \left[\lambda_{\perp} \sin(\delta_{\perp} - \delta_{ } - \phi_{\perp}) + \lambda_{ } \sin(\delta_{ } - \delta_{\perp} - \phi_{ }) \right]$	$\frac{1}{2} \left[\sin(\delta_{\perp} - \delta_{ }) + \lambda_{\perp} \lambda_{ } \sin(\delta_{\perp} - \delta_{ } - \phi_{\perp} + \phi_{ }) \right]$	$-\frac{1}{2} \left[\lambda_{\perp} \cos(\delta_{\perp} - \delta_{ } - \phi_{\perp}) + \lambda_{ } \cos(\delta_{ } - \delta_{\perp} - \phi_{ }) \right]$
$\sqrt{2} s_K c_K s_l c_l c_\phi$	$ A_0 A_{ } $	$\frac{1}{2} \left[\cos(\delta_0 - \delta_{ }) + \lambda_0 \lambda_{ } \cos(\delta_0 - \delta_{ } - \phi_0 + \phi_{ }) \right]$	$-\frac{1}{2} \left[\lambda_0 \cos(\delta_0 - \delta_{ } - \phi_0) + \lambda_{ } \cos(\delta_{ } - \delta_0 - \phi_{ }) \right]$	$\frac{1}{2} \left[\cos(\delta_0 - \delta_{ }) - \lambda_0 \lambda_{ } \cos(\delta_0 - \delta_{ } - \phi_0 + \phi_{ }) \right]$	$-\frac{1}{2} \left[\lambda_0 \sin(\delta_0 - \delta_{ } - \phi_0) + \lambda_{ } \sin(\delta_{ } - \delta_0 - \phi_{ }) \right]$
$-\sqrt{2} s_K c_K s_l c_l s_\phi$	$ A_0 A_{\perp} $	$-\frac{1}{2} \left[\sin(\delta_0 - \delta_{\perp}) - \lambda_0 \lambda_{\perp} \sin(\delta_0 - \delta_{\perp} - \phi_0 + \phi_{\perp}) \right]$	$\frac{1}{2} \left[\lambda_0 \sin(\delta_0 - \delta_{\perp} - \phi_0) + \lambda_{\perp} \sin(\delta_{\perp} - \delta_0 - \phi_{\perp}) \right]$	$-\frac{1}{2} \left[\sin(\delta_0 - \delta_{\perp}) + \lambda_0 \lambda_{\perp} \sin(\delta_0 - \delta_{\perp} - \phi_0 + \phi_{\perp}) \right]$	$-\frac{1}{2} \left[\lambda_0 \cos(\delta_0 - \delta_{\perp} - \phi_0) + \lambda_{\perp} \cos(\delta_{\perp} - \delta_0 - \phi_{\perp}) \right]$
$\frac{1}{3} s_l^2$	$ A_S ^2$	$\frac{1}{2}(1 + \lambda_S ^2)$	$ \lambda_S \cos(\phi_S)$	$\frac{1}{2}(1 - \lambda_S ^2)$	$- \lambda_S \sin(\phi_S)$
$\frac{2}{\sqrt{6}} s_K s_l c_l c_\phi$	$ A_S A_{ } $	$\frac{1}{2} \left[\cos(\delta_S - \delta_{ }) - \lambda_S \lambda_{ } \cos(\delta_S - \delta_{ } - \phi_S + \phi_{ }) \right]$	$\frac{1}{2} \left[\lambda_S \cos(\delta_S - \delta_{ } - \phi_S) - \lambda_{ } \cos(\delta_{ } - \delta_S - \phi_{ }) \right]$	$\frac{1}{2} \left[\cos(\delta_S - \delta_{ }) + \lambda_S \lambda_{ } \cos(\delta_S - \delta_{ } - \phi_S + \phi_{ }) \right]$	$\frac{1}{2} \left[\lambda_S \sin(\delta_S - \delta_{ } - \phi_S) - \lambda_{ } \sin(\delta_{ } - \delta_S - \phi_{ }) \right]$
$-\frac{2}{\sqrt{6}} s_K s_l c_l s_\phi$	$ A_S A_{\perp} $	$-\frac{1}{2} \left[\sin(\delta_S - \delta_{\perp}) + \lambda_S \lambda_{\perp} \sin(\delta_S - \delta_{\perp} - \phi_S + \phi_{\perp}) \right]$	$-\frac{1}{2} \left[\lambda_S \sin(\delta_S - \delta_{\perp} - \phi_S) - \lambda_{\perp} \sin(\delta_{\perp} - \delta_S - \phi_{\perp}) \right]$	$-\frac{1}{2} \left[\sin(\delta_S - \delta_{\perp}) - \lambda_S \lambda_{\perp} \sin(\delta_S - \delta_{\perp} - \phi_S + \phi_{\perp}) \right]$	$-\frac{1}{2} \left[- \lambda_S \cos(\delta_S - \delta_{\perp} - \phi_S) + \lambda_{\perp} \cos(\delta_{\perp} - \delta_S - \phi_{\perp}) \right]$
$\frac{2}{\sqrt{3}} c_K s_l^2$	$ A_S A_0 $	$\frac{1}{2} \left[\cos(\delta_S - \delta_0) - \lambda_S \lambda_0 \cos(\delta_S - \delta_0 - \phi_S + \phi_0) \right]$	$\frac{1}{2} \left[\lambda_S \cos(\delta_S - \delta_0 - \phi_S) - \lambda_0 \cos(\delta_0 - \delta_S - \phi_0) \right]$	$\frac{1}{2} \left[\cos(\delta_S - \delta_0) + \lambda_S \lambda_0 \cos(\delta_S - \delta_0 - \phi_S + \phi_0) \right]$	$\frac{1}{2} \left[\lambda_S \sin(\delta_S - \delta_0 - \phi_S) - \lambda_0 \sin(\delta_0 - \delta_S - \phi_0) \right]$

Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

[Phys. Rev. Lett. 114 041801 (2015)]

◆ Results: (polarisation independent)

Parameter	Value
Γ_s [ps^{-1}]	$0.6603 \pm 0.0027 \pm 0.0015$
$\Delta\Gamma_s$ [ps^{-1}]	$0.0805 \pm 0.0091 \pm 0.0032$
$ A_\perp ^2$	$0.2504 \pm 0.0049 \pm 0.0036$
$ A_0 ^2$	$0.5241 \pm 0.0034 \pm 0.0067$
δ_\parallel [rad]	$3.26^{+0.10}_{-0.17} {}^{+0.00}_{-0.07}$
δ_\perp [rad]	$3.08^{+0.14}_{-0.15} \pm 0.06$
ϕ_s [rad]	$-0.058 \pm 0.049 \pm 0.006$
$ \lambda $	$0.964 \pm 0.019 \pm 0.007$
Δm_s [ps^{-1}]	$17.711^{+0.055}_{-0.057} \pm 0.011$



Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

[Phys. Rev. Lett. 114 041801 (2015)]

◆ Systematics: (polarisation independent)

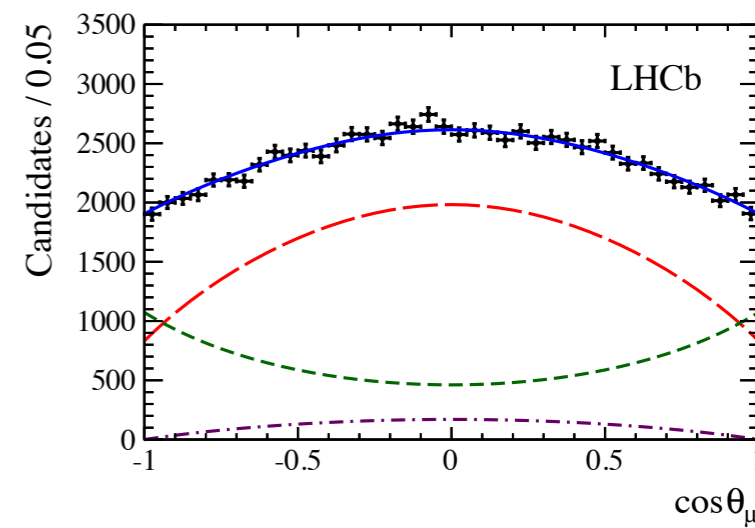
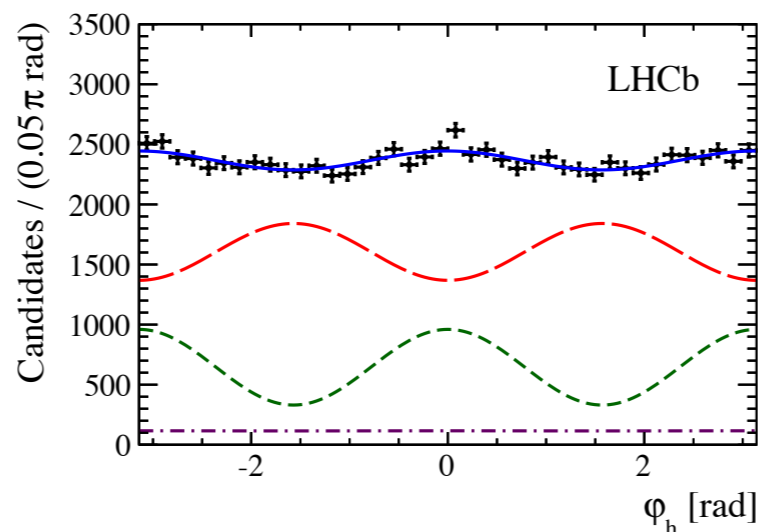
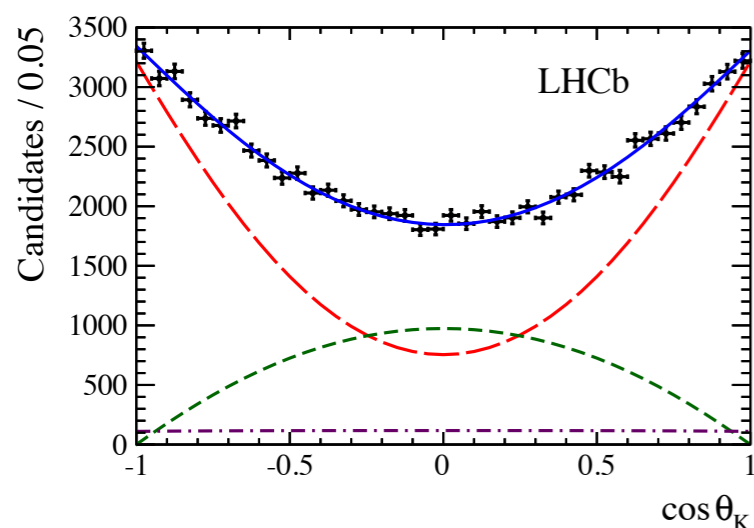
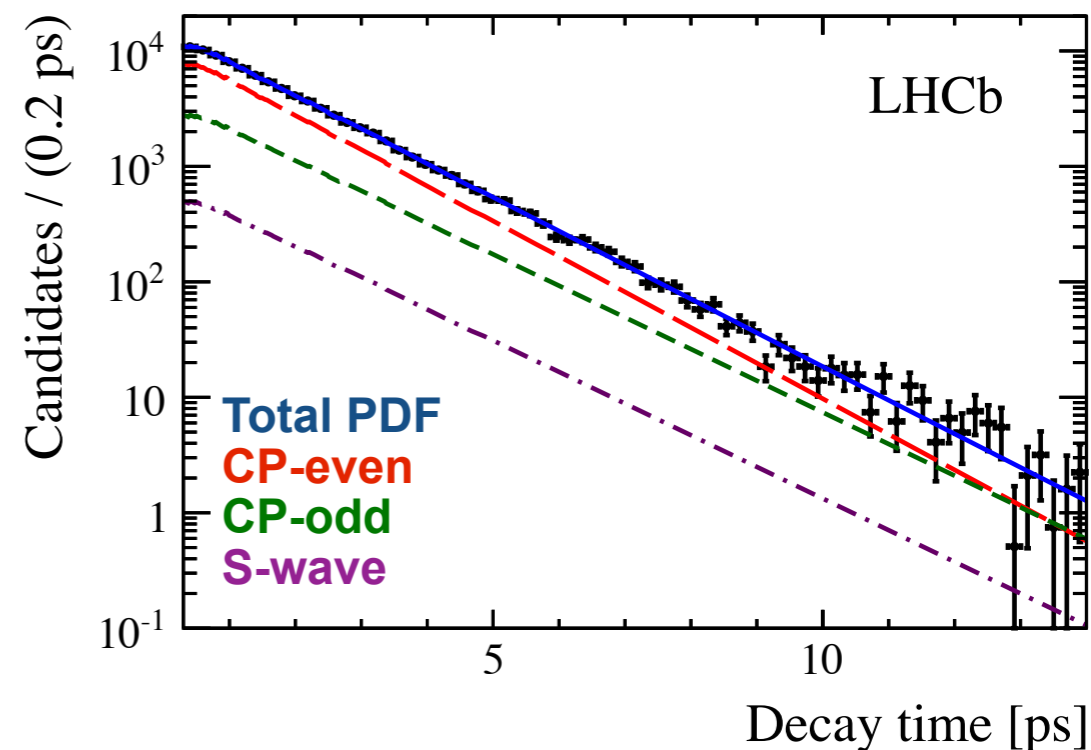
Source	Γ_s [ps ⁻¹]	$\Delta\Gamma_s$ [ps ⁻¹]	$ A_\perp ^2$	$ A_0 ^2$	δ_\parallel [rad]	δ_\perp [rad]	ϕ_s [rad]	$ \lambda $	Δm_s [ps ⁻¹]
Total stat. uncertainty	0.0027	0.0091	0.0049	0.0034	+0.10 -0.17	+0.14 -0.15	0.049	0.019	+0.055 -0.057
Mass factorisation	–	0.0007	0.0031	0.0064	0.05	0.05	0.002	0.001	0.004
Signal weights (stat.)	0.0001	0.0001	–	0.0001	–	–	–	–	–
b -hadron background	0.0001	0.0004	0.0004	0.0002	0.02	0.02	0.002	0.003	0.001
B_c^+ feed-down	0.0005	–	–	–	–	–	–	–	–
Angular resolution bias	–	–	0.0006	0.0001	+0.02 -0.03	0.01	–	–	–
Ang. efficiency (reweighting)	0.0001	–	0.0011	0.0020	0.01	–	0.001	0.005	0.002
Ang. efficiency (stat.)	0.0001	0.0002	0.0011	0.0004	0.02	0.01	0.004	0.002	0.001
Decay-time resolution	–	–	–	–	–	0.01	0.002	0.001	0.005
Trigger efficiency (stat.)	0.0011	0.0009	–	–	–	–	–	–	–
Track reconstruction (simul.)	0.0007	0.0029	0.0005	0.0006	+0.01 -0.02	0.002	0.001	0.001	0.006
Track reconstruction (stat.)	0.0005	0.0002	–	–	–	–	–	–	0.001
Length and momentum scales	0.0002	–	–	–	–	–	–	–	0.005
S-P coupling factors	–	–	–	–	0.01	0.01	–	0.001	0.002
Fit bias	–	–	0.0005	–	–	0.01	–	0.001	–
Quadratic sum of syst.	0.0015	0.0032	0.0036	0.0067	+0.06 -0.07	0.06	0.006	0.007	0.011

Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

[Phys. Rev. Lett. 114 041801 (2015)]

◆ Results: (polarisation dependent)

Parameter	Value
$ \lambda^0 $	$1.012 \pm 0.058 \pm 0.013$
$ \lambda^{\parallel}/\lambda^0 $	$1.02 \pm 0.12 \pm 0.05$
$ \lambda^{\perp}/\lambda^0 $	$0.97 \pm 0.16 \pm 0.01$
$ \lambda^S/\lambda^0 $	$0.86 \pm 0.12 \pm 0.04$
ϕ_s^0 [rad]	$-0.045 \pm 0.053 \pm 0.007$
$\phi_s^{\parallel} - \phi_s^0$ [rad]	$-0.018 \pm 0.043 \pm 0.009$
$\phi_s^{\perp} - \phi_s^0$ [rad]	$-0.014 \pm 0.035 \pm 0.006$
$\phi_s^S - \phi_s^0$ [rad]	$0.015 \pm 0.061 \pm 0.021$



Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

[Phys. Rev. Lett. 114 041801 (2015)]

◆ Systematics: (polarisation dependent)

Source	$ \lambda^0 $	$ \lambda^{\parallel}/\lambda^0 $	$ \lambda^{\perp}/\lambda^0 $	$ \lambda^S/\lambda^0 $	ϕ_s^0 [rad]	$\phi_s^{\parallel} - \phi_s^0$ [rad]	$\phi_s^{\perp} - \phi_s^0$ [rad]	$\phi_s^S - \phi_s^0$ [rad]
Total stat. uncertainty	0.058	0.12	0.16	0.12	0.053	0.043	0.035	0.061
Mass factorisation	0.010	0.04	0.01	0.03	0.003	0.005	0.003	0.016
b -hadron background	0.002	0.01	–	0.01	0.003	0.001	0.001	0.009
Ang. efficiency (reweighting)	–	–	–	0.02	0.001	0.002	0.001	0.007
Ang. efficiency (stat.)	0.004	0.02	0.01	0.01	0.004	0.007	0.005	0.004
Decay-time resolution	0.006	0.01	–	0.01	0.003	0.002	0.001	0.002
S-P coupling factors	–	–	–	–	–	–	–	0.006
Quadratic sum of syst.	0.013	0.05	0.01	0.04	0.007	0.009	0.006	0.021

Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

◆ Results:

[Phys. Rev. D. 90, 052007 (2014)]



$$\begin{aligned}\phi_s &= 0.12 \pm 0.25 \text{ (stat.)} \pm 0.05 \text{ (syst.) rad} \\ \Delta\Gamma_s &= 0.053 \pm 0.021 \text{ (stat.)} \pm 0.010 \text{ (syst.) ps}^{-1} \\ \Gamma_s &= 0.677 \pm 0.007 \text{ (stat.)} \pm 0.004 \text{ (syst.) ps}^{-1} \\ |A_{\parallel}(0)|^2 &= 0.220 \pm 0.008 \text{ (stat.)} \pm 0.009 \text{ (syst.)} \\ |A_0(0)|^2 &= 0.529 \pm 0.006 \text{ (stat.)} \pm 0.012 \text{ (syst.)} \\ \delta_{\perp} &= 3.89 \pm 0.47 \text{ (stat.)} \pm 0.11 \text{ (syst.) rad}\end{aligned}$$

[CMS-PAS-BPH-13-012]



Parameter	Fit result
$ A_0 ^2$	0.511 ± 0.006
$ A_S ^2$	0.015 ± 0.016
$ A_{\perp} ^2$	0.242 ± 0.008
δ_{\parallel} [rad]	3.48 ± 0.09
$\delta_{S\perp}$ [rad]	0.34 ± 0.24
δ_{\perp} [rad]	2.73 ± 0.36
$c\tau$ [μm]	447.3 ± 3.0
$\Delta\Gamma_s$ [ps^{-1}]	0.096 ± 0.014
ϕ_s [rad]	-0.03 ± 0.11

Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

◆ Systematics:

	ϕ_s [rad]	$\Delta\Gamma_s$ [ps ⁻¹]	Γ_s [ps ⁻¹]	$ A_{\parallel}(0) ^2$	$ A_0(0) ^2$	$ A_S(0) ^2$	δ_{\perp} [rad]	δ_{\parallel} [rad]	$\delta_{\perp} - \delta_S$ [rad]
ID alignment	$<10^{-2}$	$<10^{-3}$	$<10^{-3}$	$<10^{-3}$	$<10^{-3}$	-	$<10^{-2}$	$<10^{-2}$	-
Trigger efficiency	$<10^{-2}$	$<10^{-3}$	0.002	$<10^{-3}$	$<10^{-3}$	$<10^{-3}$	$<10^{-2}$	$<10^{-2}$	$<10^{-2}$
B^0 contribution	0.03	0.001	$<10^{-3}$	$<10^{-3}$	0.005	0.001	0.02	$<10^{-2}$	$<10^{-2}$
Tagging	0.03	$<10^{-3}$	$<10^{-3}$	$<10^{-3}$	$<10^{-3}$	$<10^{-3}$	0.04	$<10^{-2}$	$<10^{-2}$
Acceptance	0.02	0.004	0.002	0.002	0.004	-	-	$<10^{-2}$	-
Models:									
Default fit	$<10^{-2}$	0.003	$<10^{-3}$	0.001	0.001	0.006	0.07	0.01	0.01
Signal mass	$<10^{-2}$	0.001	$<10^{-3}$	$<10^{-3}$	0.001	$<10^{-3}$	0.03	0.04	0.01
Background mass	$<10^{-2}$	0.001	0.001	$<10^{-3}$	$<10^{-3}$	0.002	0.06	0.02	0.02
Resolution	0.02	$<10^{-3}$	0.001	0.001	$<10^{-3}$	0.002	0.04	0.02	0.01
Background time	0.01	0.001	$<10^{-3}$	0.001	$<10^{-3}$	0.002	0.01	0.02	0.02
Background angles	0.02	0.008	0.002	0.008	0.009	0.027	0.06	0.07	0.03
Total	0.05	0.010	0.004	0.009	0.012	0.028	0.11	0.09	0.04

Source of uncertainty	$ A_0 ^2$	$ A_S ^2$	$ A_{\perp} ^2$	$\Delta\Gamma_s$ [ps ⁻¹]	δ_{\parallel} [rad]	$\delta_{S\perp}$ [rad]	δ_{\perp} [rad]	ϕ_s [rad]	$c\tau$ [μm]
Statistical uncertainty	0.0058	0.016	0.0077	0.0138	0.092	0.24	0.36	0.109	3.0
Angular efficiency	0.0060	0.008	0.0104	0.0021	0.674	0.14	0.66	0.016	0.8
$ \lambda $ as a free parameter	0.0001	0.005	0.0001	0.0003	0.002	0.01	0.03	0.015	-
Model bias	0.0008	-	-	0.0012	0.025	0.03	-	0.015	0.4
Kaon p_T re-weighting	0.0094	0.020	0.0041	0.0015	0.085	0.11	0.02	0.014	1.1
Proper decay length resolution	0.0009	-	0.0008	0.0021	0.004	-	0.02	0.006	2.9
PDF modelling assumptions	0.0016	0.002	0.0021	0.0021	0.010	0.03	0.04	0.006	0.2
Flavour tagging	-	-	-	-	-	-	0.02	0.005	-
Background mistag modelling	0.0021	-	0.0013	0.0018	0.074	1.10	0.02	0.002	0.7
Proper decay length efficiency	0.0015	-	0.0023	0.0057	-	-	-	0.002	1.0
Total systematics	0.0116	0.022	0.0117	0.0073	0.684	1.12	0.66	0.032	3.5

[Phys. Rev. D. 90, 052007 (2014)]



[CMS-PAS-BPH-13-012]



Measurement of ϕ_s in $B_s \rightarrow J/\psi K^+ K^-$ (3 fb^{-1})

◆ Tagging:

[Phys. Rev. D. 90, 052007 (2014)]



Tagger	Efficiency [%]	Dilution [%]	Tagging Power [%]
Combined μ	3.37 ± 0.04	50.6 ± 0.5	0.86 ± 0.04
Segment Tagged μ	1.08 ± 0.02	36.7 ± 0.7	0.15 ± 0.02
Jet charge	27.7 ± 0.1	12.68 ± 0.06	0.45 ± 0.03
Total	32.1 ± 0.1	21.3 ± 0.08	1.45 ± 0.05

[CMS-PAS-BPH-13-012]



	Muons	Electrons
Mistag fraction ω [%]	$30.7 \pm 0.4 \pm 0.7$	$34.8 \pm 0.3 \pm 1.0$
Tagging efficiency ϵ_{tag} [%]	$4.55 \pm 0.03 \pm 0.08$	$3.26 \pm 0.02 \pm 0.01$
Tagging power P_{tag} [%]	$0.68 \pm 0.03 \pm 0.05$	$0.30 \pm 0.02 \pm 0.04$

Measurement of ϕ_s in $B_s \rightarrow D_s^+ D_s^-$ (3 fb^{-1})

[Phys. Rev. Lett. 113 (2014) 211801]

◆ Systematics:

Systematic uncertainty	ϕ_s ($ \lambda = 1$)	ϕ_s	$ \lambda $
Resolution	$\pm 0.098 \sigma$	$\pm 0.094 \sigma$	$\pm 0.100 \sigma$
Mass	$\pm 0.044 \sigma$	$\pm 0.043 \sigma$	$\pm 0.010 \sigma$
Acceptance (model)	$\pm 0.022 \sigma$	$\pm 0.027 \sigma$	$\pm 0.027 \sigma$
Acceptance (stat.)	$\pm 0.013 \sigma$	$\pm 0.013 \sigma$	$\pm 0.014 \sigma$
Background subtraction	$\pm 0.009 \sigma$	$\pm 0.008 \sigma$	$\pm 0.046 \sigma$
Total	$\pm 0.11 \sigma$	$\pm 0.11 \sigma$	$\pm 0.11 \sigma$

Measurement of TDCP asymmetries in $B_s \rightarrow J/\psi K^0_S$ (3 fb^{-1})

Article submitted to JHEP [[arXiv:1503.07055](https://arxiv.org/abs/1503.07055)]

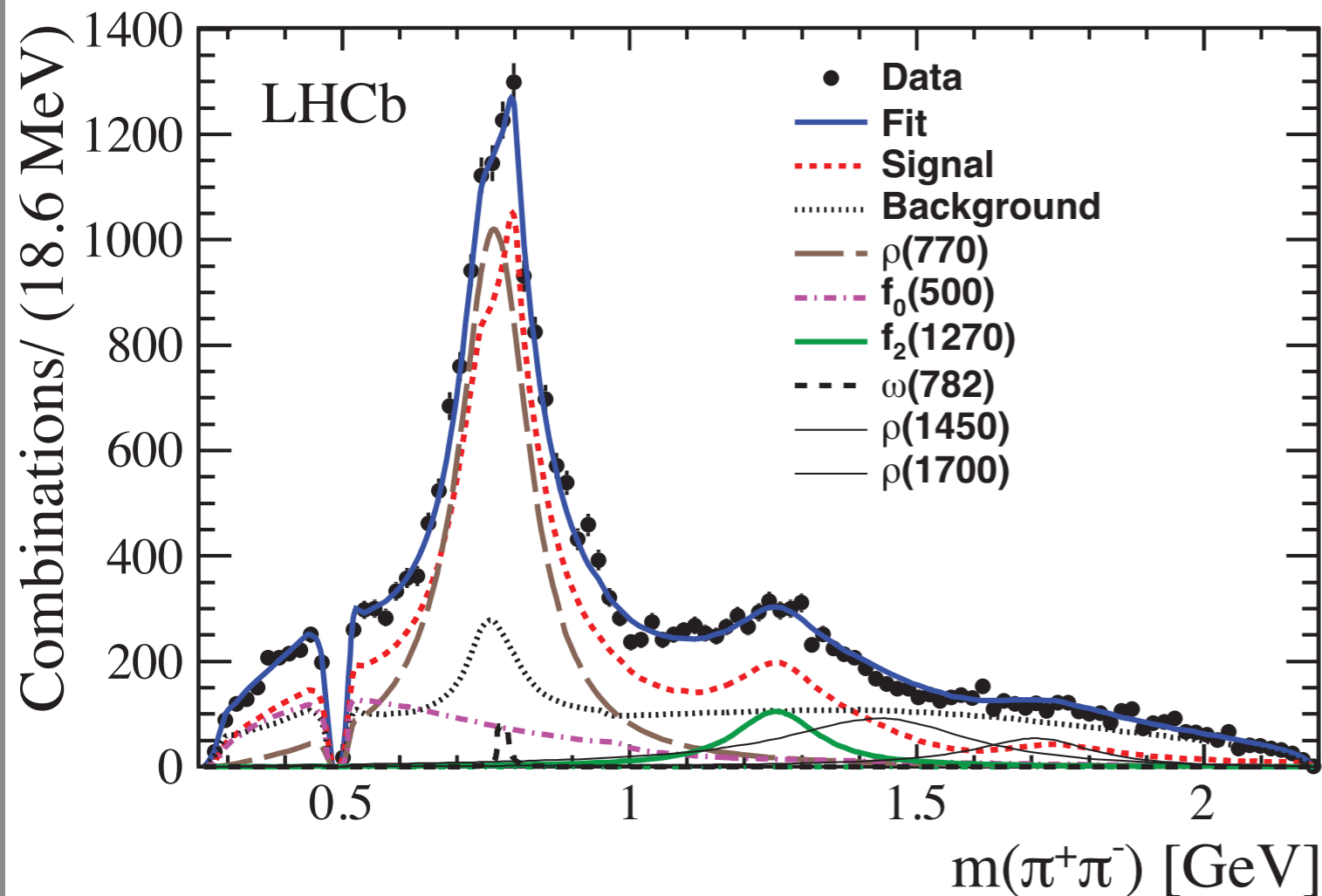
◆ Systematics:

Source	$\mathcal{A}_{\Delta\Gamma}$	C_{dir}	S_{mix}	Long $R \times 10^5$	Downstream $R \times 10^5$
Mass modelling	0.045	0.009	0.009	15.5	17.2
Decay-time resolution	0.038	0.066	0.070	0.6	0.3
Decay-time acceptance	0.022	0.004	0.004	0.6	0.5
Tagging calibration	0.002	0.021	0.023	0.1	0.2
Mass resolution	0.010	0.005	0.006	12.6	8.0
Mass-time correlation	0.003	0.037	0.036	0.2	0.1
Total	0.064	0.079	0.083	20.0	19.0

◆ Systematics:

Sources	ϕ_s (mrad)	λ
Decay time acceptance	± 0.6	± 0.0008
Mass acceptance	± 0.3	± 0.0003
Background time PDF	± 0.2	± 0.0011
Background mass distribution PDF	± 0.6	± 0.0016
Resonance model	± 6.0	± 0.0100
Resonance parameters	± 0.7	± 0.0007
Other fixed parameters	± 0.4	± 0.0009
Production asymmetry	± 5.8	± 0.0017
Total	± 8.4	± 0.010

◆ $\pi\pi$ spectrum resonant composition:



Component	Fit fraction (%)
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$\rho(770)$	65.6 ± 1.9
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$f_0(500)$	20.1 ± 0.7
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$f_2(1270)$	7.8 ± 0.6
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$\omega(782)$	$0.64^{+0.19}_{-0.13}$
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$\rho(1450)$	9.0 ± 1.8
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$\rho(1700)$	3.1 ± 0.7
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