

Inclusive radiative electroweak penguin decays: $b \rightarrow s\gamma$

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25/05/15

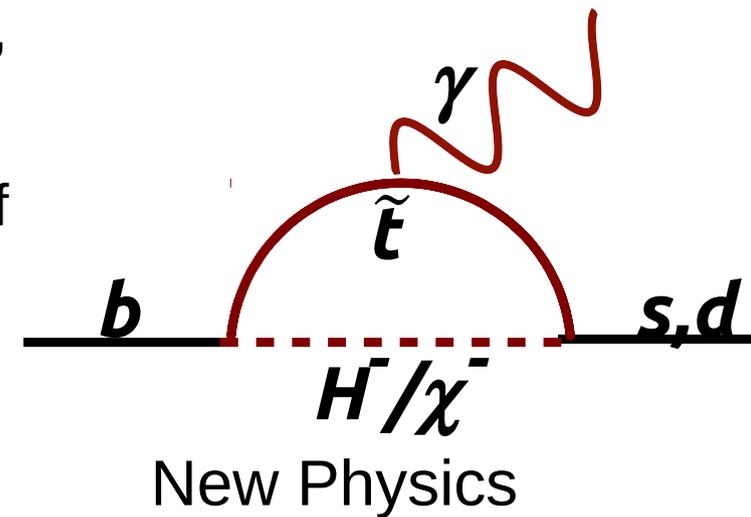
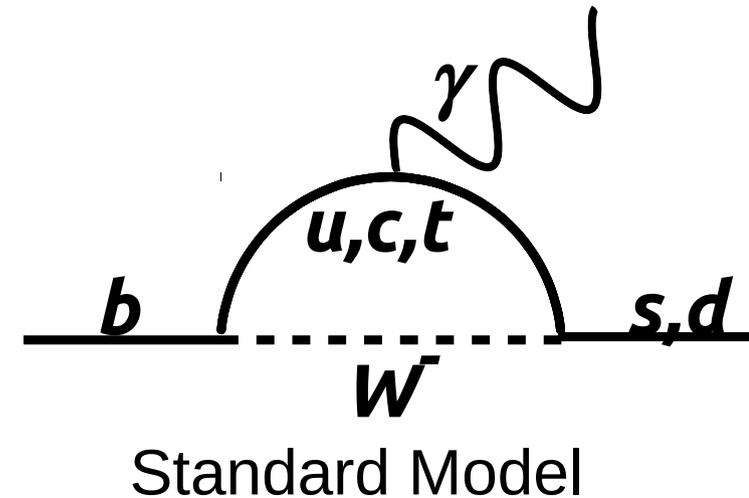




- Electroweak penguins
 - SM predictions & New Physics
- Experimentally
 - Observables: branching fraction and CP asymmetries
 - $\mathbf{B}(B \rightarrow X_s \gamma)$, $\mathbf{B}(B \rightarrow X_{s+d} \gamma)$, $\mathbf{ACP}(B \rightarrow X_s \gamma)$, $\mathbf{ACP}(B \rightarrow X_{s+d} \gamma)$, $\Delta \mathbf{ACP}$
- Belle II
- Limits on 2HDM-II

Introduction

- Electroweak penguins: $b \rightarrow s/d \gamma$ are FCNC, forbidden at tree level in SM
- In NP models, new heavy particles could enter the loop (in 2HDM-II it is the H^-)
 - Modify observables (**BF**, **ACP**, ...)
- Most precise predictions are for inclusive $b \rightarrow s \gamma$
 - Motivates inclusive or semi-inclusive analyses
- Challenges: large BG, missing exclusive modes, fragmentation modeling, etc.
- Suppression for $b \rightarrow d \gamma$ with respect to $b \rightarrow s \gamma$ of order: $|V_{td}/V_{ts}|^2 \approx 1/20$



The inclusive rate

- HQET Hamiltonian:
$$H_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \sum_i C_i(\mu_b) O_i(\mu_b)$$

– $m_W, m_t \gg \mu_b$

- C_i & O_i are the Wilson coefficients and operators.
 C_7 and C_8 are the relevant contributions

$$O_7 = \frac{em_b}{16\pi^2} \bar{s}_L \sigma_{\mu\nu} F^{\mu\nu} b_R$$

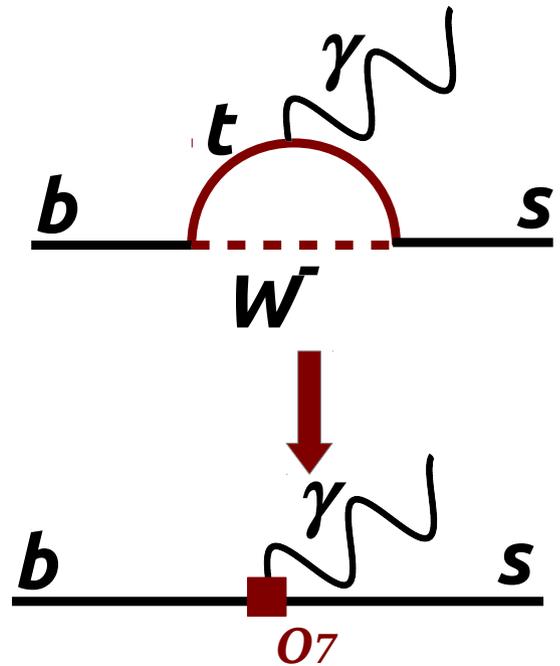
$$O_8 = \frac{gm_b}{16\pi^2} \bar{s}_L \sigma_{\mu\nu} T^a b_R G_a^{\mu\nu}$$

- Photon energy or X_s mass spectra, described by two parameters: m_b, μ_π^2

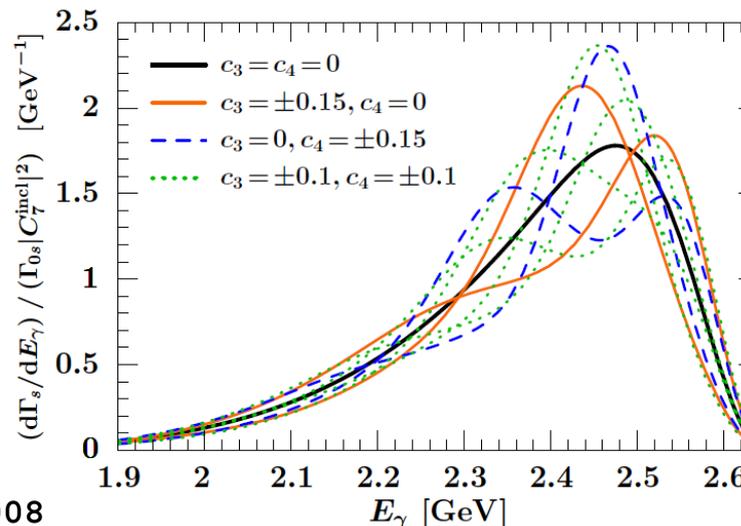
- Strong dependence on input parameters and model

– Use cut-off $E_\gamma > 1.6$ GeV

– Large uncertainty for low E_γ



With NP: $C_i \rightarrow C_i + C_i'$



Phys. Rev. D78:114014, 2008

BF($B \rightarrow X_{s/d} \gamma$) calculation



- Recent update: complete NNLO calculation ($E_\gamma > 1.6$ GeV) [arxiv:1503.01789 \[hep-ph\]](#)
- Central value increased by **6.4%** with respect to 2006 value

$$\mathcal{B}(B \rightarrow X_s \gamma) = (3.36 \pm 0.23) \times 10^{-4}$$
$$\mathcal{B}(B \rightarrow X_d \gamma) = (1.73^{+0.12}_{-0.22}) \times 10^{-5}$$

- Total uncertainty is **~7%** for $\mathcal{B}(B \rightarrow X_s \gamma)$
- Room for improvement: interpolation for $m_c=0$ in new NNLO terms.
- Limit on 2HDM-II charged Higgs mass, based on 2014 HFAG average

$$\mathcal{B}(B \rightarrow X_s \gamma)^{\text{exp}} = (3.43 \pm 0.21 \pm 0.07) \times 10^{-4}$$
$$M(H^-) > 480 \text{ GeV at } 95\% \text{ CL}$$

Direct CP asymmetry



- Direct **CP** Asymmetry: non-vanishing for exclusive cases

$$A_{CP} = \frac{\Gamma(\bar{B} \rightarrow \bar{f}) - \Gamma(B \rightarrow f)}{\Gamma(\bar{B} \rightarrow \bar{f}) + \Gamma(B \rightarrow f)}$$

$$f = X_{s,d}\gamma$$

Channel	$A_{CP}(\text{SM})$
$B \rightarrow X_s \gamma$	$[-0.6\% , +2.8\%]$
$B \rightarrow X_d \gamma$	$[-62\% , +14\%]$
$B \rightarrow X_{s+d} \gamma$	0

PRL 106, 141801 (2011)

- Cancellation for X_{s+d} due to **CKM** unitarity, theory error becomes negligibly small

$$A_{CP} = \frac{\Delta\Gamma_q}{2\Gamma(B \rightarrow f_q)} \longrightarrow \Delta\Gamma_q \propto \Im(V_{ub} V_{cb}^* V_{cq} V_{uq}^*)$$

$$\Delta\Gamma_s = -\Delta\Gamma_d \quad \text{Nucl. Phys. B704 (2005) 56-74}$$

- Difference of **ACP** between charged and neutral modes gives information on Wilson coefficients **C7** and **C8**:

$$\Delta A_{CP} \equiv A_{CP}(B^+ \rightarrow X_s^+ \gamma) - A_{CP}(B^0 \rightarrow X_s^0 \gamma)$$

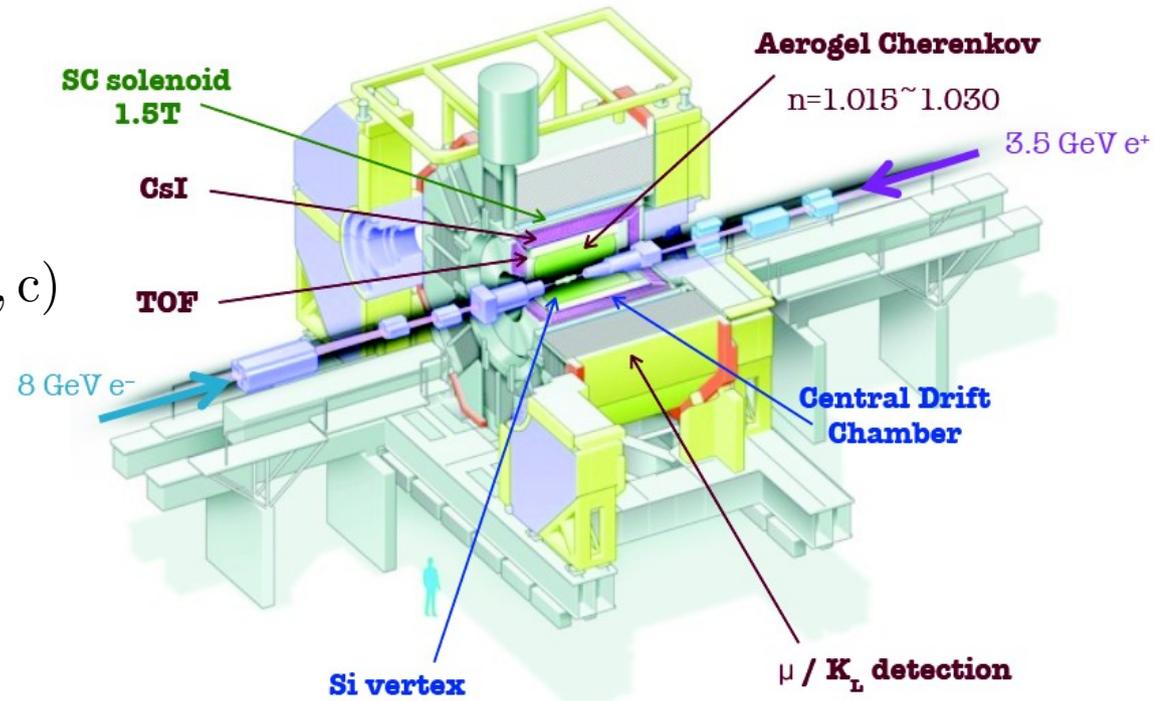
$$\Delta A_{CP} \approx 4\pi^2 \alpha_s \frac{\bar{\Lambda}_{78}}{m_b} \text{Im} \frac{C_8^{\text{eff}}}{C_7^{\text{eff}}}$$



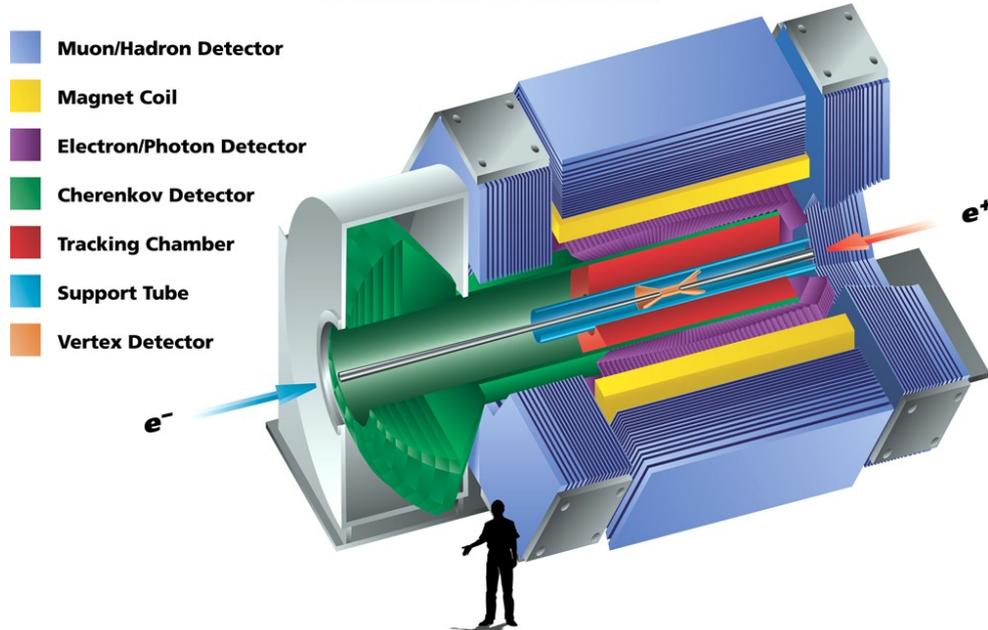
Experimental part

The B-factories

- Asymmetric e^+e^- colliders @ **10.58 GeV** center of mass energy
- On resonance:
 $\sqrt{s} = 10.58\text{GeV}$ $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$
- Continuum:
 \sqrt{s} below $\Upsilon(4S)$ $e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$)
 - Continuum is ~ 3 times more abundant than ***BB***



BABAR Detector



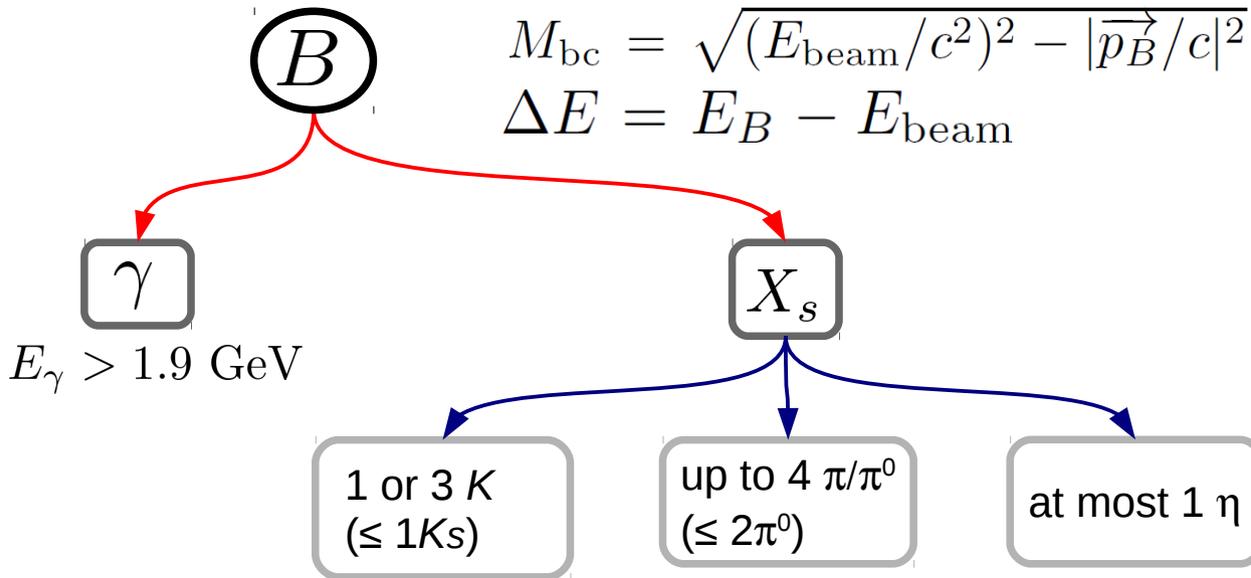
- Belle + BABAR: $711\text{fb}^{-1} + 433\text{fb}^{-1}$ on $Y(4S)$:
 Over 1 billion ***BB*** pairs!
- Continuum: $90\text{fb}^{-1} + 44\text{fb}^{-1}$

Semi-inclusive method: reconstruction

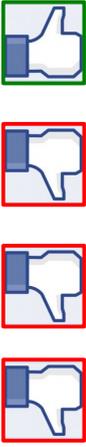


- Reconstruct as many final states as possible

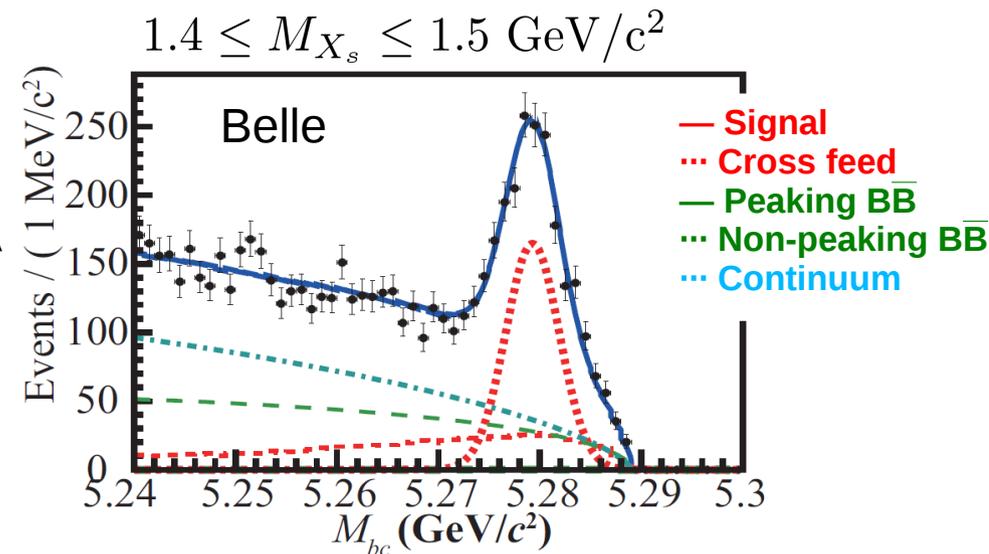
Belle: Phys. Rev. D 91, 052004 (2015)
 BABAR: Phys. Rev. D 86, 052012 (2012)



- 38 exclusive X_s states
- Large combinatoric BG and cross-feed
- X_s selection efficiencies hard to determine
- 70% of total BF



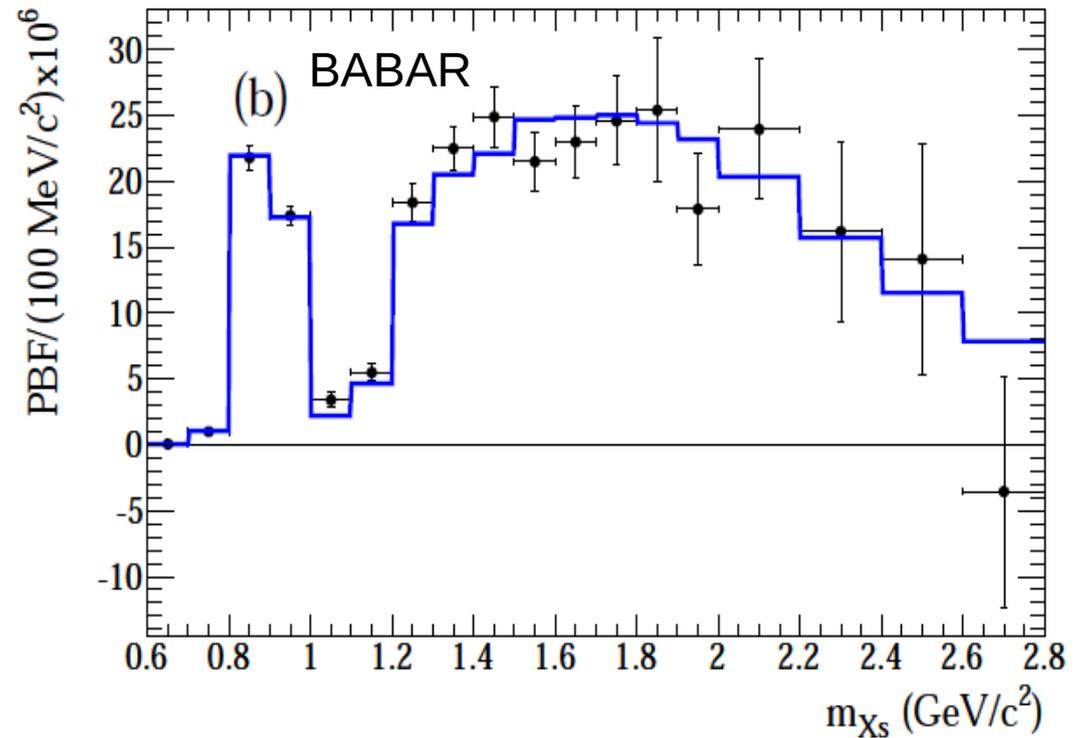
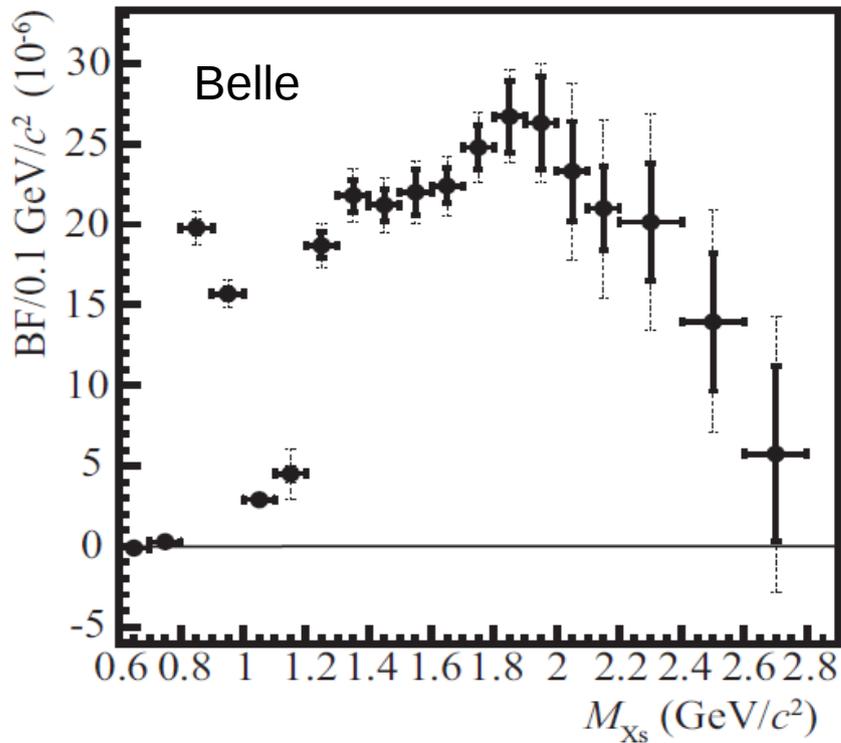
- Use of **MVAs** to reduce background
- Selection efficiencies and fraction of missing modes estimated using JETSET and PYTHIA



Semi-inclusive method: reconstruction



- **BF** extracted in hadronic mass $M(X_s)$ bins: $0.6 \leq M_{X_s} \leq 2.8 \text{ GeV}/c^2$
- Partial **BF**:



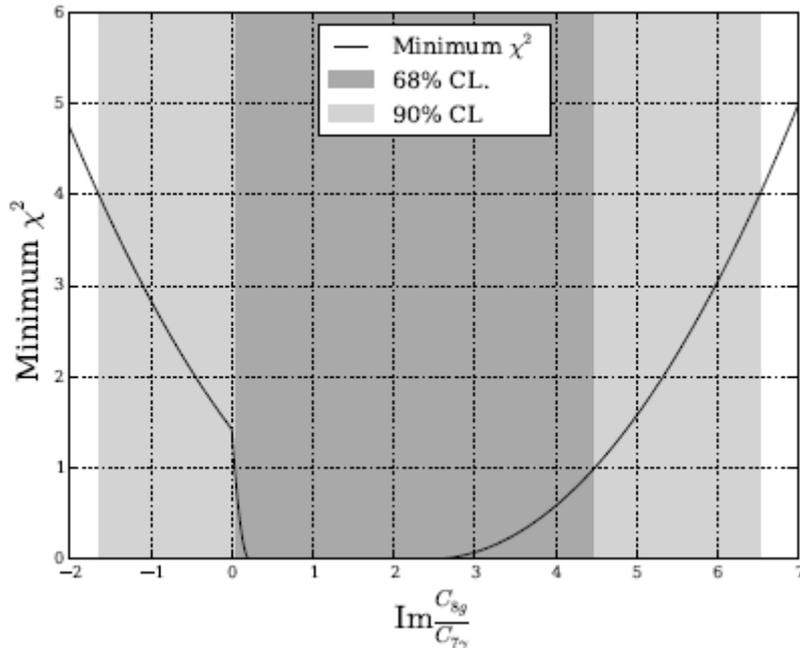
- Integrated **BF** $> 1.9 \text{ GeV}$

Belle:	$\mathcal{B}(B \rightarrow X_s \gamma) = (3.51 \pm 0.17 \pm 0.33) \times 10^{-4}$
BABAR:	$\mathcal{B}(B \rightarrow X_s \gamma) = (3.29 \pm 0.19 \pm 0.48) \times 10^{-4}$

- Systematics: missing modes (1%-30%), background fitting ($\sim 4\%$), detector response ($\sim 3\%$)

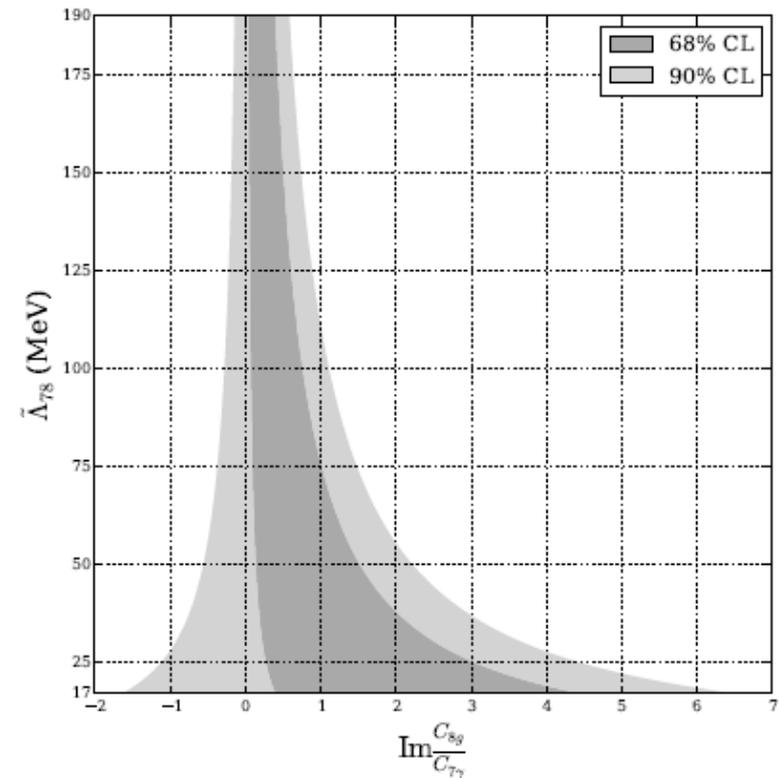
Semi-inclusive method: A_{CP} and ΔA_{CP}

- BABAR uses 16 self-tagging modes
- Consistent with SM $B \rightarrow X_s \gamma$: $-0.6\% < A_{CP}^{SM} < 2.8\%$ $A_{CP}^{meas} = (1.7 \pm 1.9 \pm 1.0)\%$
- $\Delta A_{CP} \equiv A_{CP}(B^+ \rightarrow X_s^+ \gamma) - A_{CP}(B^0 \rightarrow X_s^0 \gamma)$
 $\Delta A_{CP} \approx 0.12 \frac{\bar{\Lambda}_{78}}{100 \text{ MeV}} \text{Im}(C_8/C_7)$, where $17 \text{ MeV} < \bar{\Lambda}_{78} < 190 \text{ MeV}$
- From $\Delta A_{CP} = (5.0 \pm 3.9 \pm 1.5)\%$ confidence intervals for C_8/C_7 can be derived



$$0.07 \leq \text{Im} \frac{C_{8g}}{C_{7\gamma}} \leq 4.48, \quad 68\% \text{ CL},$$

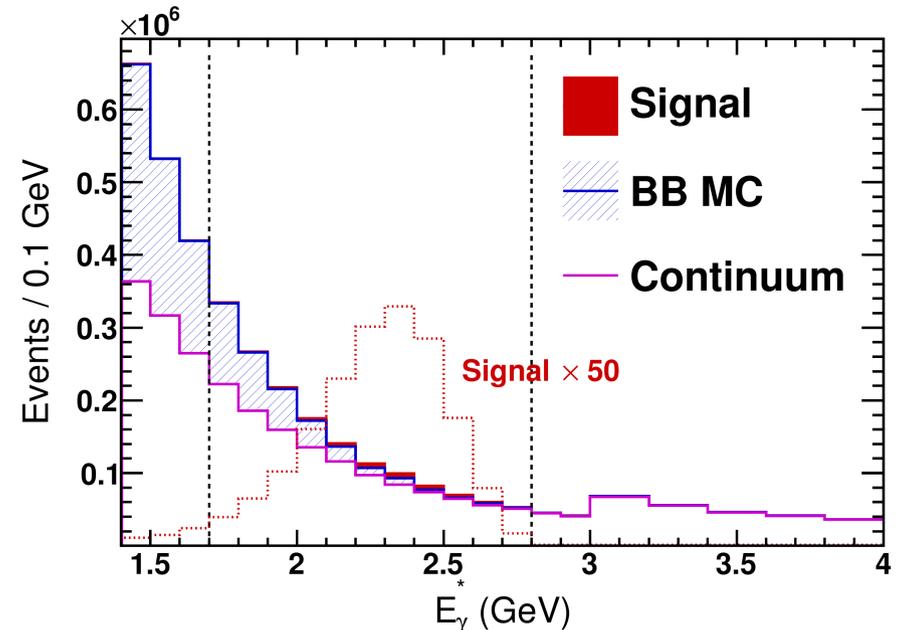
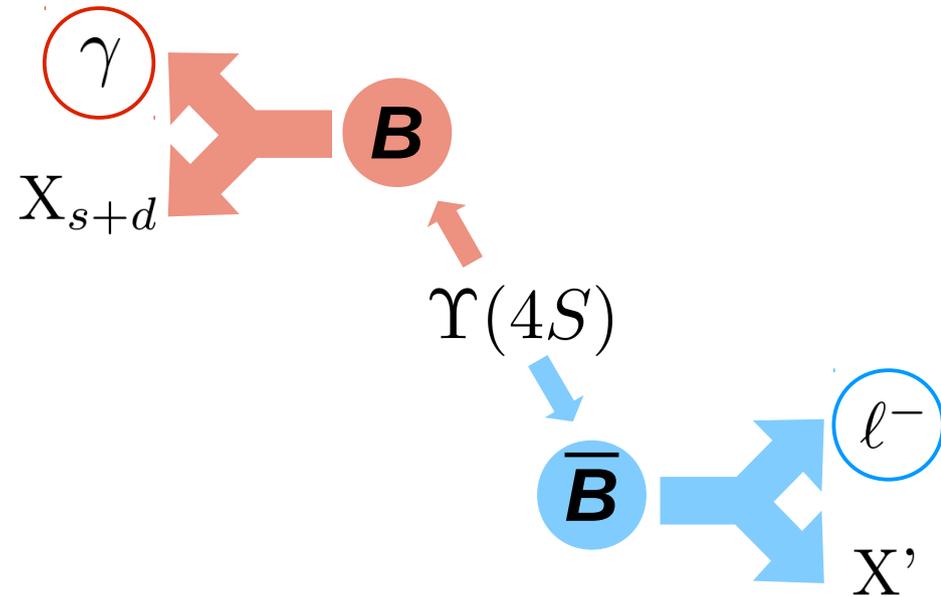
$$-1.64 \leq \text{Im} \frac{C_{8g}}{C_{7\gamma}} \leq 6.52, \quad 90\% \text{ CL}.$$



BABAR: Phys. Rev. D 90, 092001 (2014)

Inclusive method: reconstruction

- Inclusive analysis:
 - High energy **photon** $E_\gamma > 1.7$ GeV
 - High momentum **lepton**
 - Continuum suppression and flavor tagging (for **ACP**)
- Veto light meson decays $\pi^0(\eta) \rightarrow \gamma\gamma$
- Statistics are limiting factor (continuum data subtraction)
- Does not distinguish $b \rightarrow s\gamma$ from $b \rightarrow d\gamma$
- Large background: need for **MVAs**



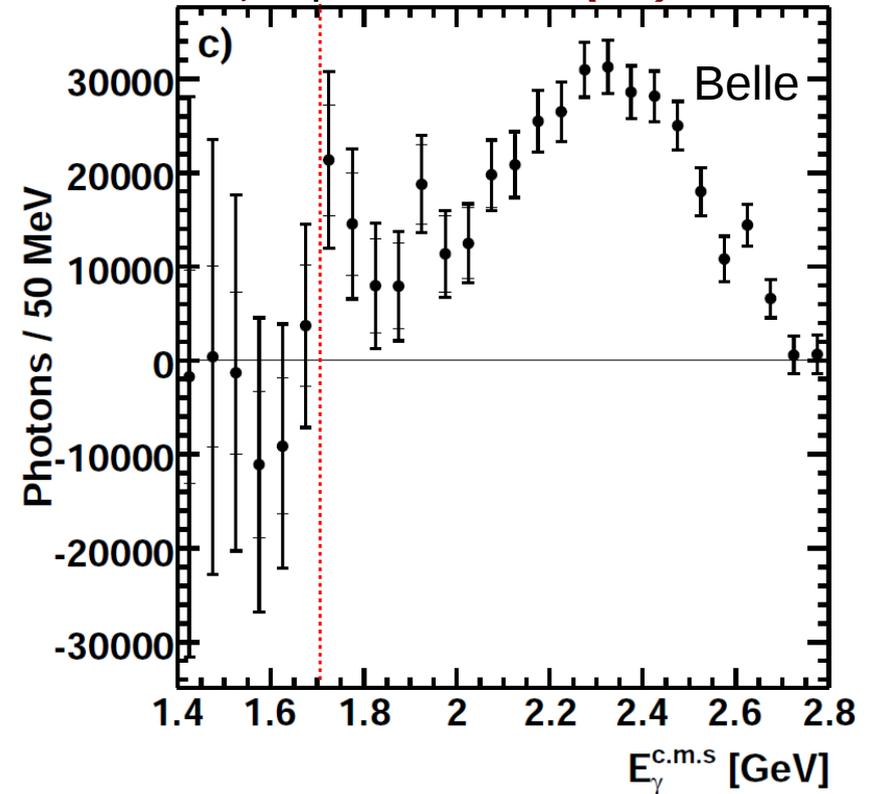
Inclusive method: BF



Belle: Phys. Rev. Lett. 103:241801 (2009)

BABAR: Phys. Rev. D. 86, 112008 (2012)

Unfolded E_{γ}^* spectrum in $Y(4S)$ frame



Belle 657M $B\bar{B}$ BABAR 383M $B\bar{B}$

$B(B \rightarrow X_s \gamma) \quad E_{\gamma} > 1.7 \text{ GeV}$

Belle $(3.45 \pm 0.15 \pm 0.40) \times 10^{-4}$

$B(B \rightarrow X_s \gamma) \quad E_{\gamma} > 1.9 \text{ GeV}$

Belle $(3.21 \pm 0.11 \pm 0.16) \times 10^{-4}$

BABAR $(3.00 \pm 0.14 \pm 0.19 \pm 0.06) \times 10^{-4}$

- Important issues
 - **MVA** for continuum suppression
 - Normalization of π/η background
 - Unfolding
- BABAR, main systematics from:
 - BB background modeling (7.8%)
 - Selection efficiency uncertainty (3.1%)
- Belle measured **BF** with and without lepton tag (and $E_{\gamma} > 1.7 \text{ GeV}$).
 - 7.5% uncertainty from continuum
 - 7.5% uncertainty from BB

Inclusive method: $ACP(B \rightarrow X_{s+d}\gamma)$

- Number of events tagged by a positive or negative lepton:

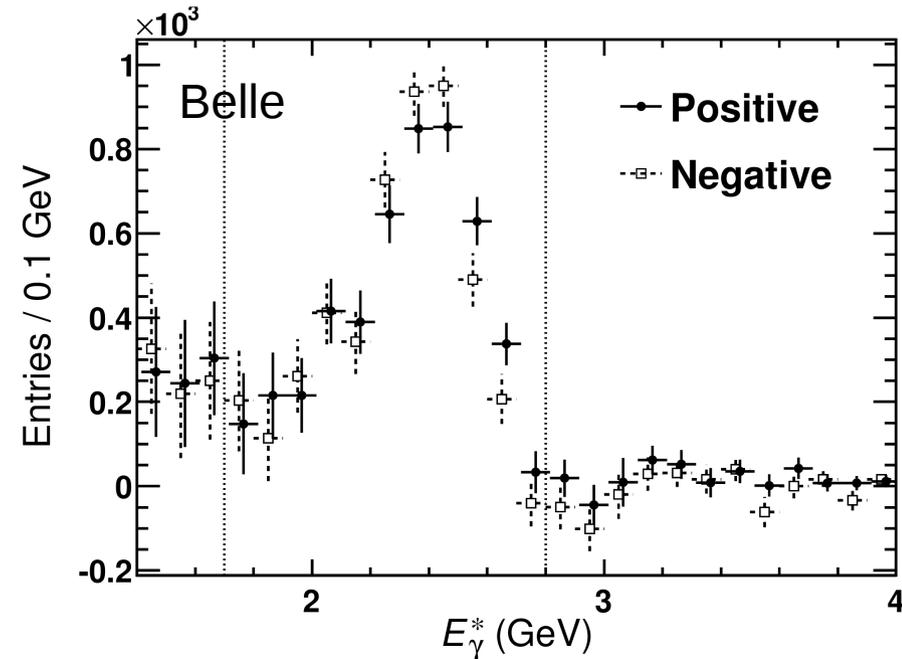
$$A_{CP}^{\text{meas}} = \frac{N(\ell^+) - N(\ell^-)}{N(\ell^+) + N(\ell^-)}$$

- Correct for various effects:

$$A_{CP}^{\text{true}} = \frac{1}{1 - 2\omega} (A_{CP}^{\text{meas}} - A_{\text{bkg}} - A_{\text{det}})$$

- Wrong tag factor $\omega \approx 14\%$:** oscillation, secondaries, fakes
- Detector asymmetry $A_{\text{det}} \approx (0.0 \pm 0.3)\%$:** tag and probe, mapping of the whole detector, use $B \rightarrow X J/\psi(\ell^+ \ell^-)$
- Background asymmetry $\approx (0.0 \pm 0.7)\%$:** in data $E_\gamma < 1.7$ GeV

- Independent of choice of E^*_{γ} threshold.



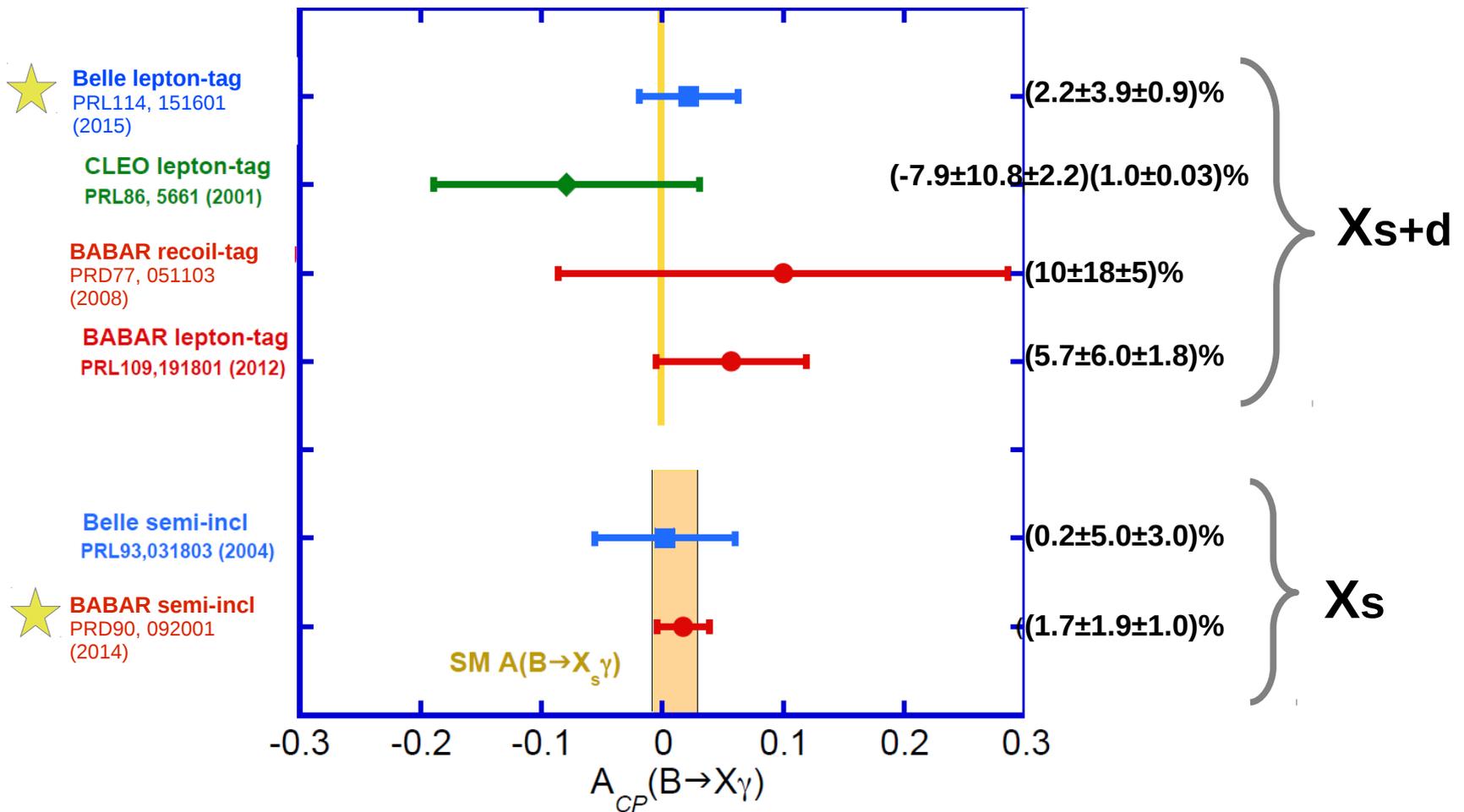
	$E^*_{\gamma} > 2.1 \text{ GeV}$
	$A_{CP}(X_{s+d}\gamma)$
Belle	$(2.2 \pm 3.9 \pm 0.9)\%$
BABAR	$(5.7 \pm 6.0 \pm 1.8)\%$

Belle: Phys. Rev. Lett. 114, 151601 (2015)

BABAR: Phys. Rev. D. 86, 112008 (2012)

Direct A_{CP} in $B \rightarrow X_{s+d}\gamma$ and $B \rightarrow X_s\gamma$

- Precision greatly affected by statistics \rightarrow can be improved in Belle II
 - Most systematics cancel
- No deviation from Standard Model

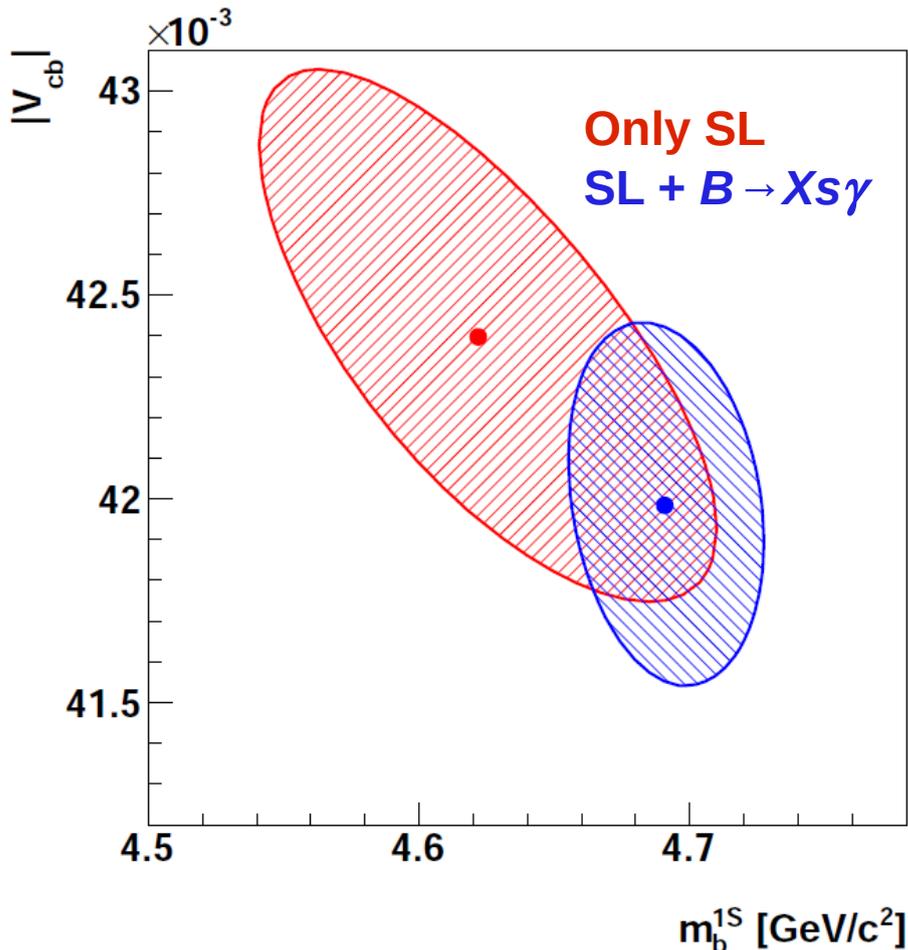


Using the $B \rightarrow X_s \gamma$ spectrum

- Example: 1st and 2nd moments can be used to constrain m_b in the **1S** scheme. Input from BABAR, Belle and CLEO

$$E_1 : \langle E_\gamma \rangle$$

$$E_2 : \langle (E_\gamma - \langle E_\gamma \rangle)^2 \rangle$$
- More precise determination of $|V_{cb}|$, respect to only semileptonic inputs



	m_b^{1S} (GeV/c ²)
SL	4.62 ± 0.09
SL+B $\rightarrow X_s \gamma$	4.69 ± 0.04

	$ V_{cb} \times 10^3$
SL	42.40 ± 0.65
SL+B $\rightarrow X_s \gamma$	41.98 ± 0.45

Phys. Rev. D78:032016, 2008

HFAG14:arXiv:1412.7515

Exclusive decays : $B_s \rightarrow \phi(K^-K^+)\gamma$

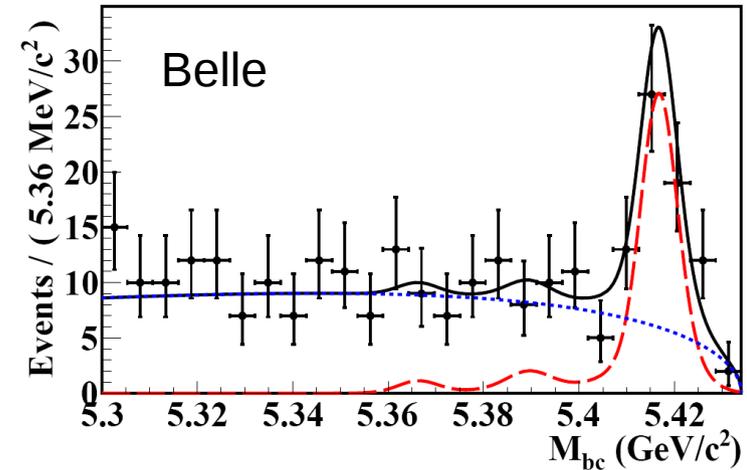
- Rare decay: $\mathcal{B}(B_s \rightarrow \phi\gamma)^{SM} = (3.9 \pm 1.1 \pm 0.5-) \times 10^{-5}$

Phys. Rev. D75:054004, 2007

- Belle's 121fb⁻¹ on **Y(5S)**

- NN for continuum suppression and fitting (**CNB**)

- 4-D extended maximum likelihood fit: M_{bc} , ΔE , $\cos\theta_{hel}$, **CNB**. (Show 2 projections)

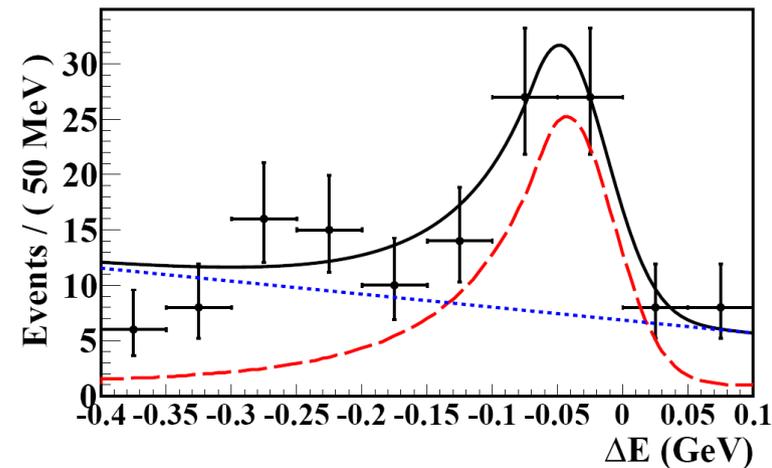


- Find 91_{-13}^{+14} candidates, $\varepsilon = (36.1 \pm 0.1)\%$

$$\mathcal{B}(B_s \rightarrow \phi\gamma) = (3.6 \pm 0.5(\text{st.}) \pm 0.3(\text{sys.}) \pm 0.6(f_s)) \cdot 10^{-5}$$

Belle: PRD 91, 011101(R) (2015)

fraction of **Bs** and **bb** cross section at **Y(5S)** (17%, 4.7%), NN requirement (4.8%)



- Consistent with SM and LHCb:

$$\mathcal{B}(B_s \rightarrow \phi\gamma) = (3.5 \pm 0.4) \cdot 10^{-5}$$

LHCb: Nucl. Phys. B867, 1 (2013)

Best measurement of $\sigma(e^+e^- \rightarrow B_s^{(*)}\bar{B}_s^{(*)})$
with half the uncertainty

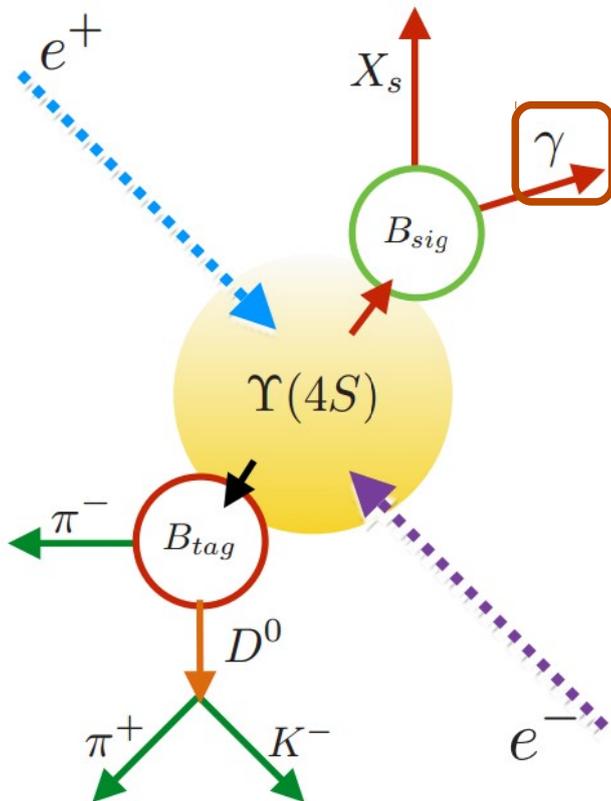
Belle arXiv:1504.02004

Prospects for Belle II

- Statistical uncertainties and several systematics will be improved:

	ΔA_{CP}	$A_{CP}(X_s\gamma)$	$A_{CP}(X_{s+d}\gamma)$
Now	5%	2%	4%
Belle II 50 ab^{-1}	$\sim 0.7\%$	$\sim 0.5\%$	$\sim 0.6\%$

- Total uncertainty in **BF** could be halved
- Different approach: hadronic tag



- Not yet feasible \rightarrow low efficiency
- No continuum, lower model dependence
- Measures for B^+ and B^0 independently
- BABAR: 210 fb^{-1} and $\sim 27\%$ uncertainty
Phys. Rev. D **77**, 051103, (2008)

$$\mathcal{B}(B \rightarrow X_s\gamma) = (3.91 \pm 0.91 \pm 0.64) \times 10^{-4}$$

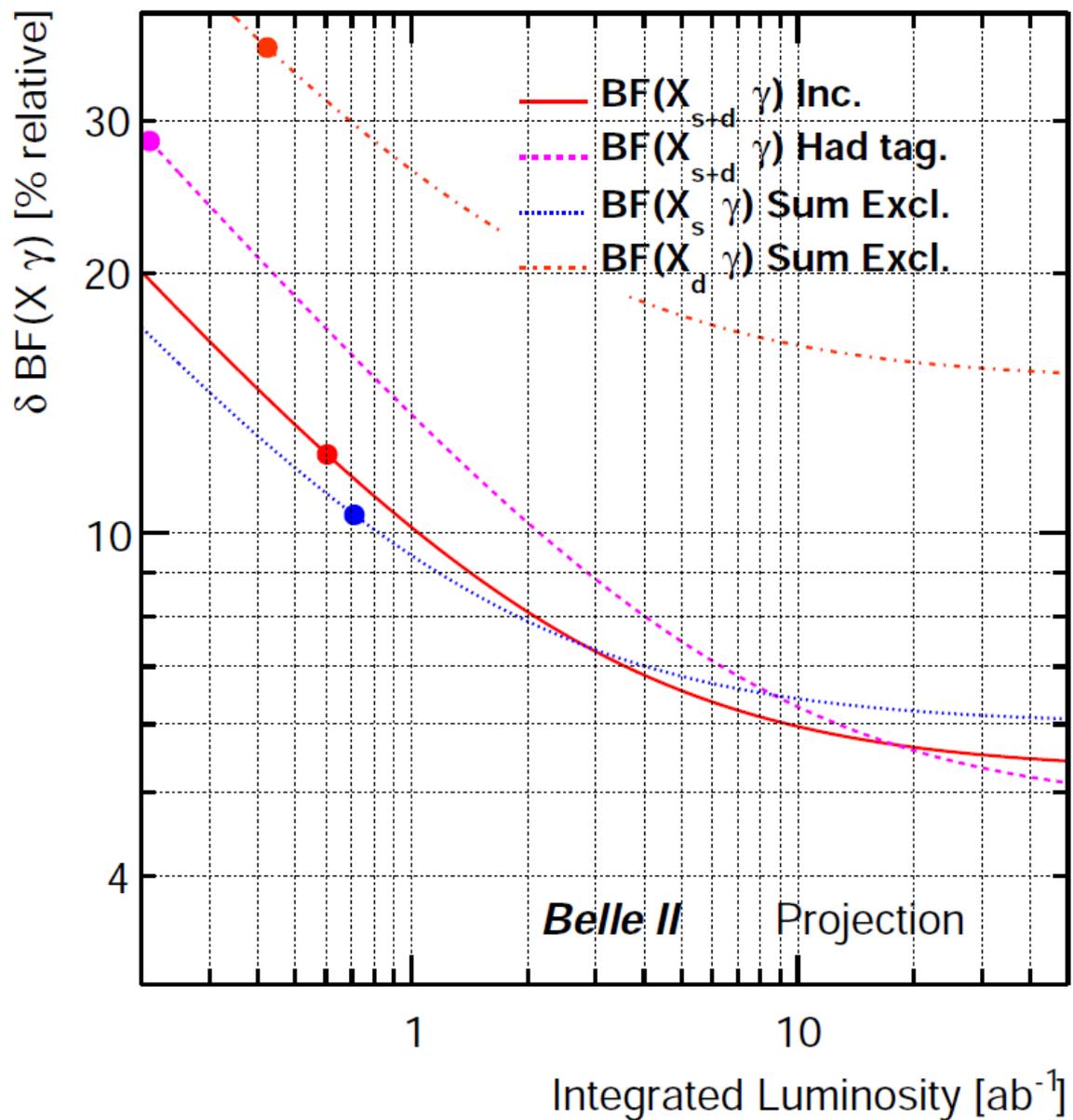
$$E_\gamma > 1.6 \text{ GeV}$$

- Systematics: background modeling (12%), fit parameters (7.5%), detector response (11%)
- 5% uncertainty for Belle-II 50 ab^{-1}

Prospects for Belle II



- Projection of uncertainty in BF for Belle II

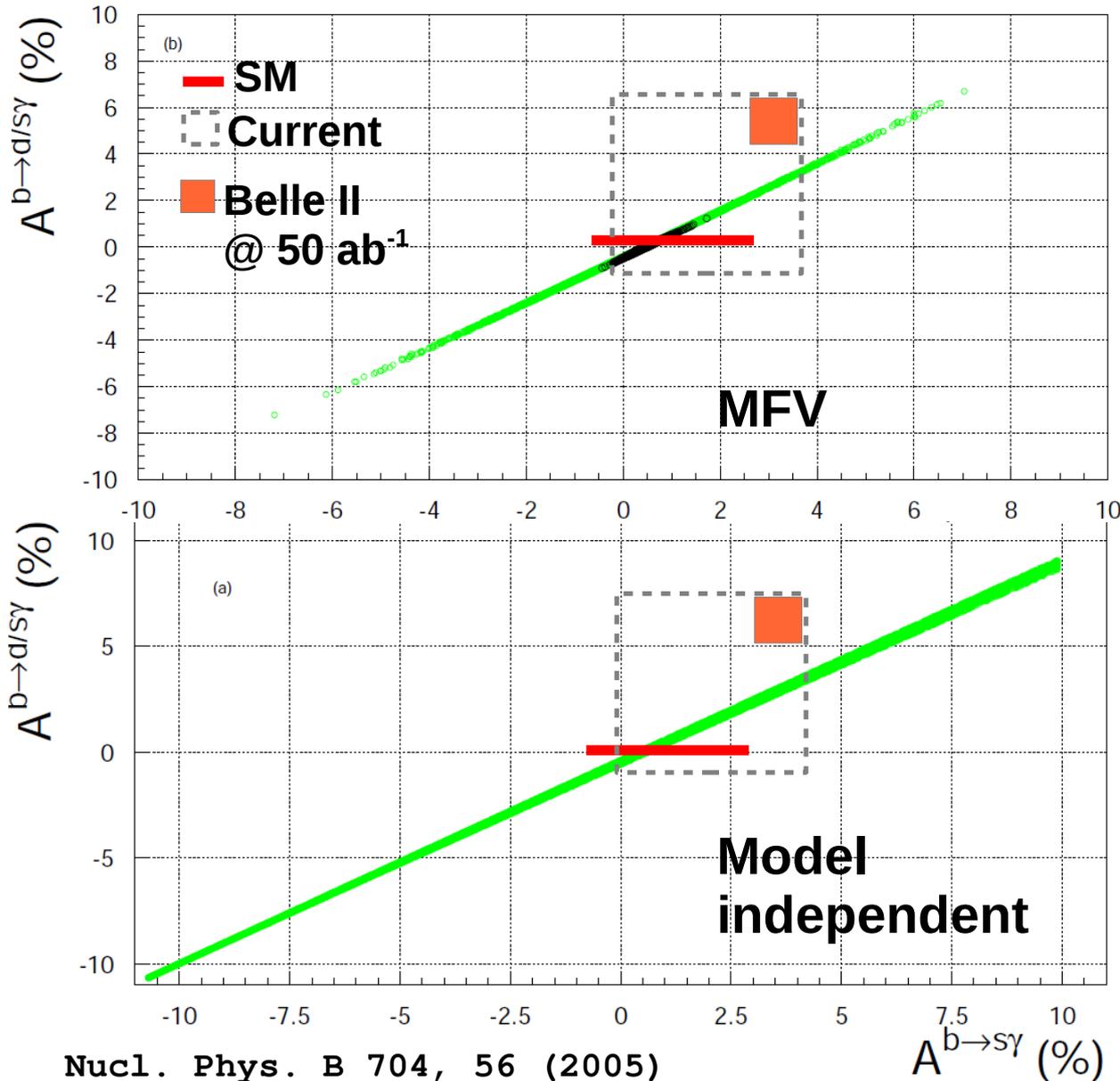




New Physics

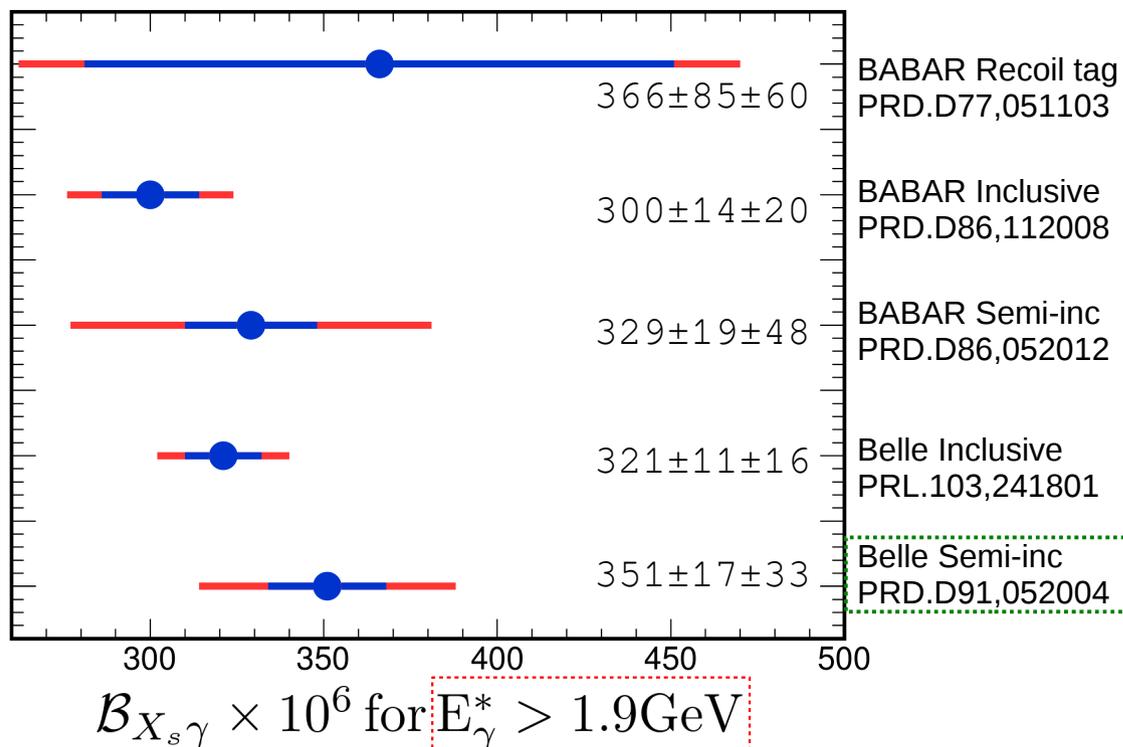
Beyond SM - MFV

- Strict proportionality between tagged and untagged **ACP**.
- In MFV $\sim 2\%$, more generic approaches allow for **ACP** as large as 10%



- If **ACP** $\neq 0$, current experimental precision does not suffice to distinguish between these scenarios

Beyond SM - 2HDM-II



$$\mathcal{B}_{X_s \gamma}^{\text{SM}} = (336 \pm 23) \times 10^{-6}$$

$$\mathcal{B}_{X_s \gamma}^{\text{exp}} = (341 \pm 16(\text{exp}) \pm 4(\text{extrap})) \times 10^{-6}$$

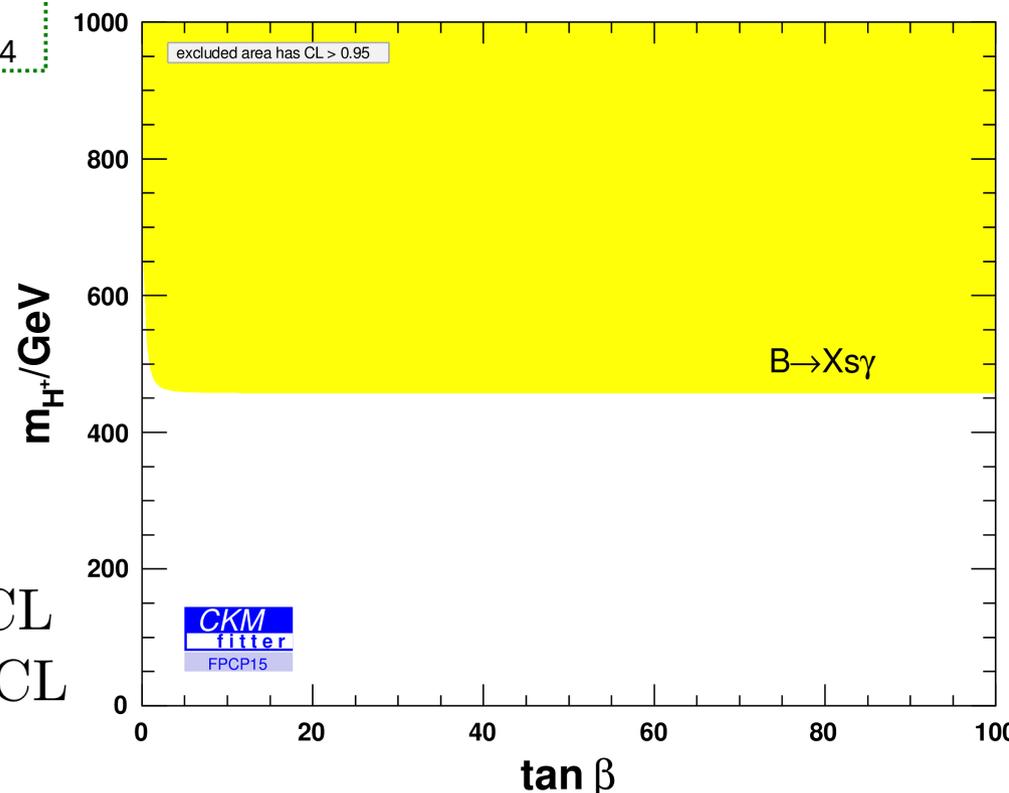
- For charged Higgs in 2HDM of type II:

2014 avg: $M(H^-) > 480 \text{ GeV}$ at 95% CL

1.9 GeV avg: $M(H^-) > 540 \text{ GeV}$ at 95% CL

- $BF(B \rightarrow X_s \gamma)$ for 1.9 GeV photon energy threshold (and excluding CLEO)
- Extrapolate to 1.6 GeV using kinetic scheme

Phys.Rev.D73:073008 (2006)



Beyond SM - 2HDM-II

Leptonic : $\frac{K \rightarrow \ell\nu}{\pi \rightarrow \ell\nu}$ & $\frac{\tau \rightarrow K\nu}{\tau \rightarrow \pi\nu}$, $\frac{K \rightarrow \pi\mu\nu}{K \rightarrow \pi e\nu}$, $\mathcal{B}(Ds \rightarrow \mu\nu)$, $\mathcal{B}(D \rightarrow \mu\nu)$, $\mathcal{B}(B \rightarrow \tau\nu)$

Box and loop : $\frac{\mathcal{B}(B \rightarrow X_s\gamma)}{\mathcal{B}(B \rightarrow X_c\ell\nu)}$, $R_b = \frac{Z \rightarrow b\bar{b}}{Z \rightarrow \text{hadrons}}$, $B_{s,d}\bar{B}_{s,d}$ oscillation frequencies

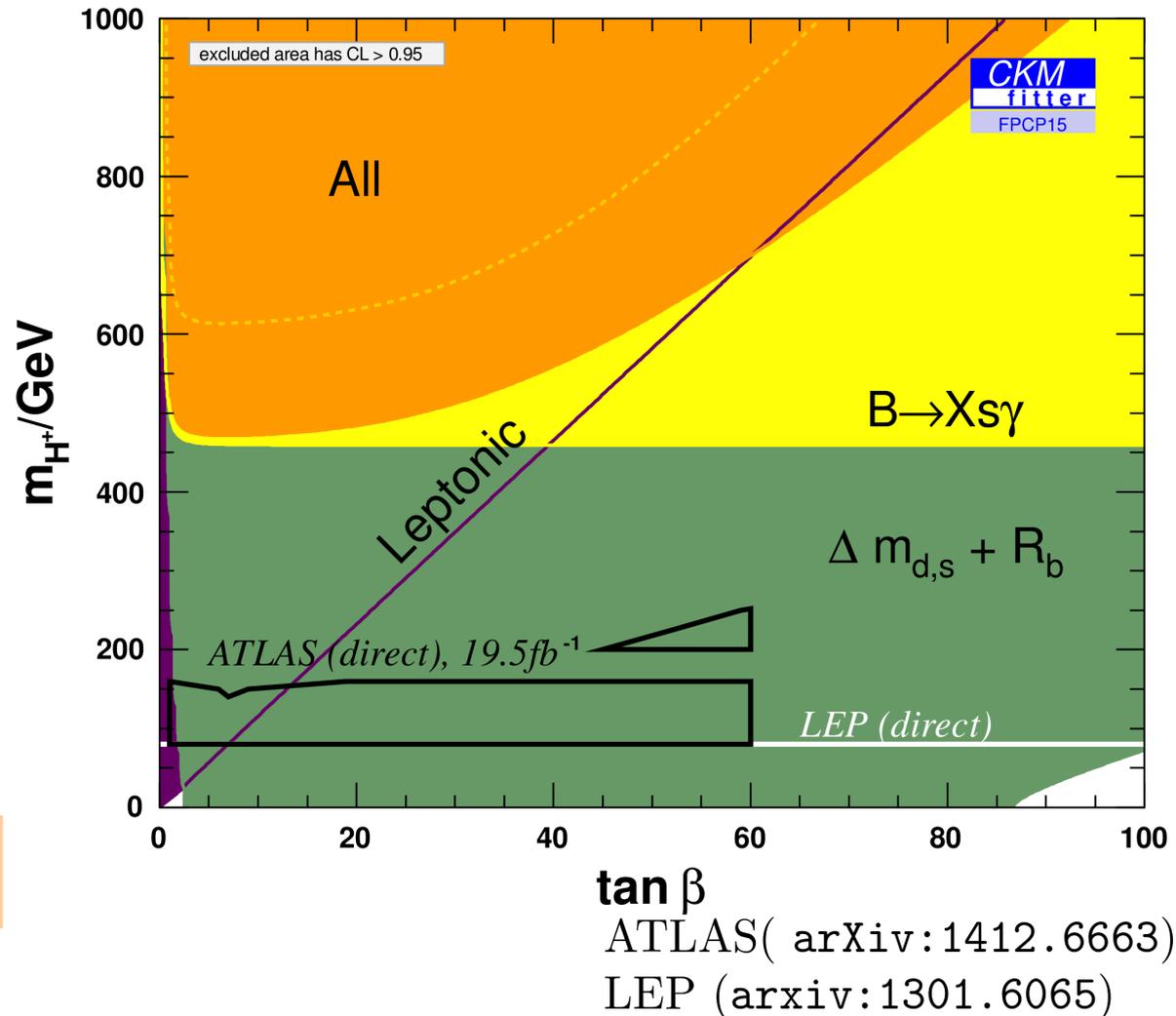
- Determination of CKM parameters (A, λ, ρ, η) with limited set of inputs



- However BABAR's measurement on $B \rightarrow D^{(*)}\tau\nu$ rule out 2HDM-II with 99.8% CL

- But also rules out the SM

- **LHCb and Belle show new results on $R(D^{(*)})$ in the next session!**





- **Flavor can provide valuable information for SM and NP**
 - **BF($B \rightarrow X_s \gamma$)** is calculated and measured with 7% precision
 - Improvements in SM calculations and experiment put $m(H^-) > 540$ GeV
- **Belle II prospects are very exciting**
 - Direct **A_{CP}** measurements greatly limited by statistics: room for improvement
 - Full hadronic tag approach will be feasible
 - Several systematics do scale with statistics
- **Understanding of f_s and bb cross section currently limits $Y(5S)$ studies**
 - New and more precise **B_s** measurements are being produced.



BACKUP

Reconstructed $B \rightarrow X_s \gamma$ modes

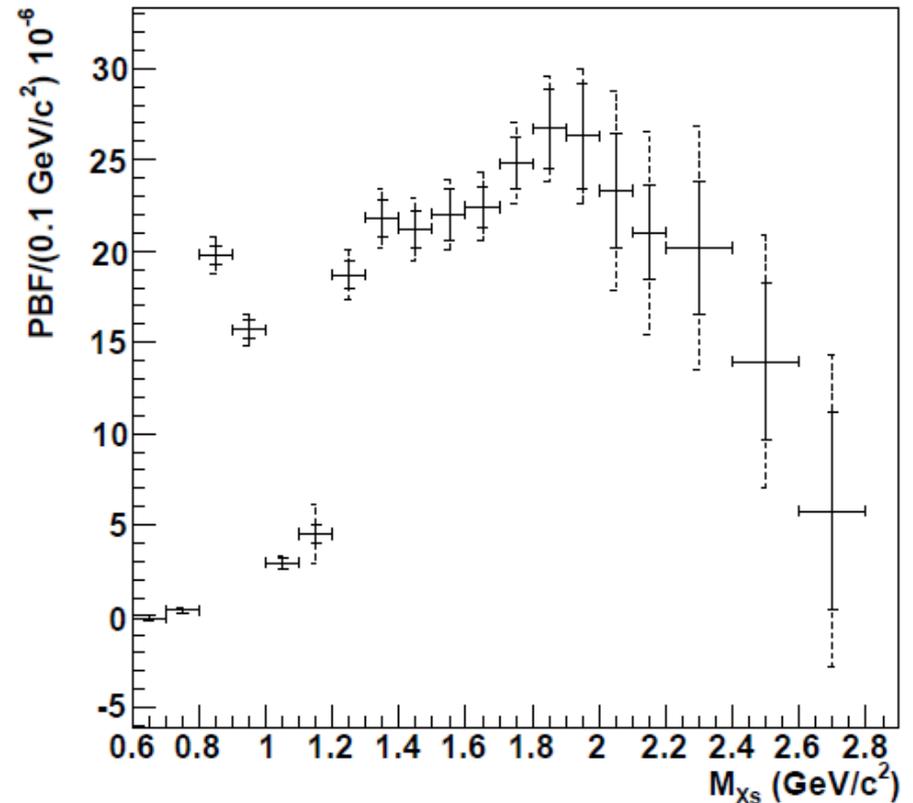
Mode ID	Final state	Mode ID	Final state	Mode ID	Final state
1	$K^+ \pi^-$	16	$K_s \pi^+ \pi^+ \pi^- \pi^0$	31	$K^+ \eta \pi^- \pi^0$
2	$K_s \pi^+$	17	$K^+ \pi^0 \pi^0$	32	$K_s \eta \pi^+ \pi^0$
3	$K^+ \pi^0$	18	$K_s \pi^0 \pi^0$	33	KKK
4	$K_s \pi^0$	19	$K^+ \pi^- \pi^0 \pi^0$	34	KKK_s
5	$K^+ \pi^+ \pi^-$	20	$K_s \pi^+ \pi^0 \pi^0$	35	$KK_s K_s$
6	$K_s \pi^+ \pi^-$	21	$K^+ \pi^+ \pi^- \pi^0 \pi^0$	36	$K^+ K^+ K^- \pi^-$
7	$K^+ \pi^+ \pi^0$	22	$K_s \pi^+ \pi^- \pi^0 \pi^0$	37	$K^+ K^- K_s \pi^+$
8	$K_s \pi^+ \pi^0$	23	$K^+ \eta$	38	$K^+ K^+ K^- \pi^0$
9	$K^+ \pi^+ \pi^- \pi^-$	24	$K_s \eta$		
10	$K_s \pi^+ \pi^+ \pi^-$	25	$K^+ \eta \pi^-$		
11	$K_s \pi^+ \pi^0$	26	$K_s \eta \pi^+$		
12	$K_s \pi^+ \pi^0$	27	$K^+ \eta \pi^0$		
13	$K^+ \pi^+ \pi^+ \pi^- \pi^-$	28	$K_s \eta \pi^0$		
14	$K_s \pi^+ \pi^+ \pi^- \pi^-$	29	$K^+ \eta \pi^+ \pi^-$		
15	$K_s \pi^+ \pi^+ \pi^- \pi^0$	30	$K_s \eta \pi^+ \pi^-$		

Partial $B \rightarrow X_s \gamma$ BF



Table 9.12: The partial branching ratio on M_{X_s}

M_{X_s} bin(GeV/c^2)	$\mathcal{BR}(10^{-6})$
0.6-0.7	$-0.1 \pm 0.1 \pm 0.0$
0.7-0.8	$0.3 \pm 0.1 \pm 0.1$
0.8-0.9	$19.8 \pm 0.5 \pm 0.9$
0.9-1.0	$15.7 \pm 0.5 \pm 0.7$
1.0-1.1	$2.9 \pm 0.3 \pm 0.2$
1.1-1.2	$4.8 \pm 0.5 \pm 1.5$
1.2-1.3	$18.7 \pm 0.8 \pm 1.1$
1.3-1.4	$21.8 \pm 1.0 \pm 1.3$
1.4-1.5	$21.2 \pm 1.0 \pm 1.4$
1.5-1.6	$22.0 \pm 1.4 \pm 1.3$
1.6-1.7	$22.4 \pm 1.1 \pm 1.5$
1.7-1.8	$24.8 \pm 1.4 \pm 1.7$
1.8-1.9	$26.7 \pm 2.2 \pm 1.9$
1.9-2.0	$26.3 \pm 2.9 \pm 2.3$
2.0-2.1	$23.3 \pm 3.1 \pm 4.5$
2.1-2.2	$21.0 \pm 2.6 \pm 4.9$
2.2-2.4	$40.3 \pm 7.2 \pm 11$
2.4-2.6	$27.9 \pm 8.6 \pm 11$
2.6-2.8	$11.5 \pm 11 \pm 13$

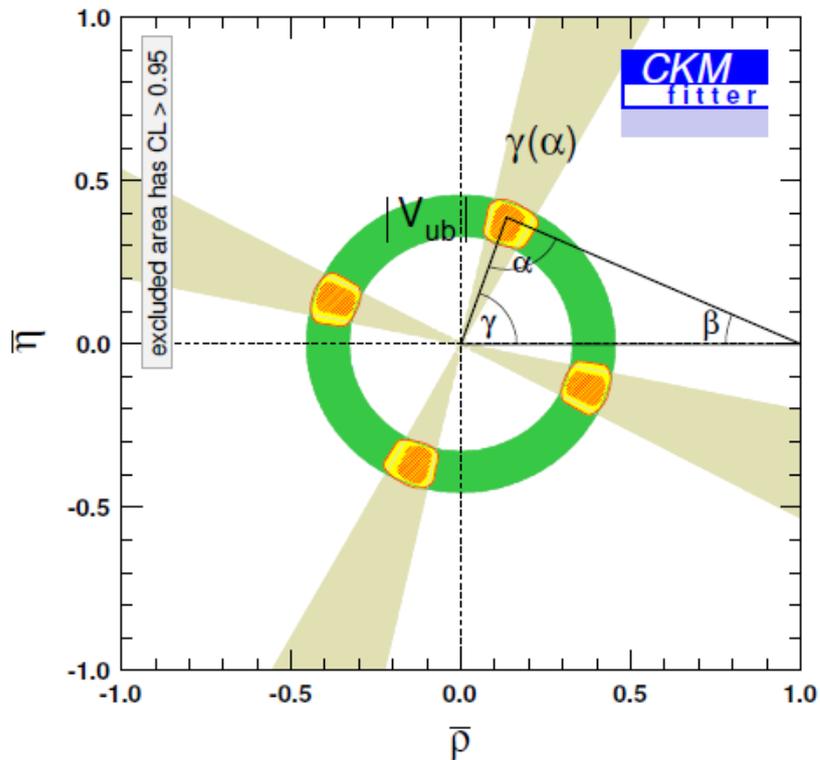


- (a) Partial branching ratio. The first solid error is the statistical one and the second dashed error is a quadratic sum of the statistical and systematic errors.

SM inputs for 2HDM-II limits



Inputs must not be sensitive to NP, so take tree-level processes where the ratio $m_{q1} \cdot m_{q2} / m_{H^+}^2$ is negligibly small:



- λ from $|V_{ud}|$ (super-allowed β decays)
- A from $|V_{cb}|$ (semileptonic $b \rightarrow c$ decays), and λ
- $\rho + i\eta$:
 - from γ from $\alpha + \beta$ (don't use γ from $B \rightarrow DK$)
 - $|V_{ub}|$ (semileptonic $b \rightarrow u$ decays)

Less powerful than global fit