

# Lepton-Flavored Scalar Dark Matter with Minimal Flavor Violation

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## Abstract

We explore scalar dark matter that is part of a lepton flavor triplet satisfying symmetry requirements under the hypothesis of minimal flavor violation. The dark-matter candidate couples to standard-model particles via Higgs-portal renormalizable interactions as well as to leptons through dimension-six operators, all of which have minimal flavor violation built-in. With the simplest parameter choices, we investigate the constraints and implications from a series of experimental data to test the validity of our model. Future high-energy  $e^+e^-$  machines, such as the International Linear Collider, are well suited to probe various aspects of our model more stringently.

## Introduction

### 0.1 Motivation

- (1) Dark matter (DM) exists in the Universe.  $\Rightarrow$  Beyond SM
- (2) Neutrino Oscillation  $\Rightarrow$  Neutrino masses  $\Rightarrow$  Beyond SM
- (3) Flavor-changing neutral currents (FCNC) of leptons  $\Rightarrow$  Probing New Physics
- (4) Recent Experimental Data: Flavor-Violating Higgs Decay

## 1 Framework of MFV and Type-I Seesaw Mechanism

### 1.1 MFV hypothesis [1]:

All sources of flavor and CP violation reside in renormalizable Yukawa couplings defined at tree level

### 1.2 Type-I Seesaw Mechanism

$$\begin{aligned} \mathcal{L}_m &= -(Y_\nu)_{kl} \bar{L}_{k,L} \nu_{l,R} \hat{H} - (Y_e)_{kl} \bar{L}_{k,L} E_{l,R} H - \frac{1}{2} (M_\nu)_{kl} \bar{\nu}_{k,R} \nu_{l,R} + \text{H.c.}, \\ &\supset \frac{-1}{2} (\bar{\nu}_L \ \bar{\nu}_R)^c \begin{pmatrix} 0 & \frac{v}{\sqrt{2}} Y_\nu \\ \frac{v}{\sqrt{2}} Y_\nu^T & M_\nu \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R^c \end{pmatrix} + \text{H.c.} \\ &\Rightarrow m_\nu = -\frac{v^2}{2} Y_\nu M_\nu^{-1} Y_\nu^T = U_{\text{PMNS}} \hat{m}_\nu U_{\text{PMNS}}^T, \quad |m_\nu \times M_\nu| \sim |v^2 Y_\nu^2| \quad (\text{"Seesaw"}) \end{aligned}$$

### 1.3 Flavor Groups and Spurions [2]

$U(3)_L \times U(3)_\nu \times U(3)_E = G_\ell \times U(1)_L \times U(1)_\nu \times U(1)_E$ , with  $G_\ell = \text{SU}(3)_L \times \text{SU}(3)_\nu \times \text{SU}(3)_E$

$$L_L \rightarrow V_L L_L, \quad \nu_R \rightarrow V_\nu \nu_R, \quad E_R \rightarrow V_E E_R, \quad V_{L,\nu,E} \in \text{SU}(3)_{L,\nu,E},$$

Treat the Yukawa couplings as spurion fields

$$Y_\nu \rightarrow V_L Y_\nu V_\nu^\dagger, \quad Y_e \rightarrow V_L Y_e V_E^\dagger.$$

Simple Choice:  $M_\nu = M\mathbf{1}$ ,  $\text{SU}(3)_\nu \rightarrow O(3)_\nu$

$\Rightarrow G_\ell = \text{SU}(3)_L \times \text{SU}(3)_E \times O(3)_\nu$

Building Blocks  $A = Y_\nu Y_\nu^\dagger \sim (8, 1)$ ,  $B = Y_e Y_e^\dagger \sim (8, 1)$ ,  $Y_e \sim (3, \bar{3})$ ,  $Y_\nu \sim (3, 1)$

Explicit form of the spurions (Yukawa couplings)

$$Y_e = \frac{\sqrt{2}}{v} \text{diag}(m_e, m_\mu, m_\tau), \quad Y_\nu^{(M)} = \frac{i\sqrt{2}}{v} U_{\text{PMNS}} \hat{m}_\nu^{1/2} O M_\nu^{1/2}, \quad Y_\nu^{(D)} = \frac{\sqrt{2}}{v} U_{\text{PMNS}} \hat{m}_\nu,$$

Double matrix expansion series [3]

$\Delta = \sum \xi_{jkl\dots} A^j B^k A^l \dots$  with  $\xi_{jkl\dots} \lesssim \mathcal{O}(1)$ , &  $\text{Im}(xi_{jkl\dots}) = 0$  (MFV assumption)

$$\begin{aligned} \Delta &= \xi_1 \mathbf{1} + \xi_2 A + \xi_3 B + \xi_4 A^2 + \xi_5 B^2 + \xi_6 AB + \xi_7 BA + \xi_8 ABA + \xi_9 BA^2 + \xi_{10} BAB \\ &\quad + \xi_{11} AB^2 + \xi_{12} ABA^2 + \xi_{13} A^2 B^2 + \xi_{14} B^2 A^2 + \xi_{15} B^2 AB + \xi_{16} AB^2 A^2 + \xi_{17} A^2 B^2 B, \end{aligned}$$

We choose the largest eigenvalue of  $A = Y_\nu Y_\nu^\dagger$  to be unity. Hence terms with B can be neglected.

## 2 Lepton-flavored dark matter

Include additional flavor triplet (SM gauge singlet), imposed  $Z_2$  symmetry for stability

$$\tilde{s} = \begin{pmatrix} \tilde{s}_1 \\ \tilde{s}_2 \\ \tilde{s}_3 \end{pmatrix} \sim (3, 1) \text{ where } G_\ell = \text{SU}(3)_L \times \text{SU}(3)_E,$$

### 2.1 Renormalizable Interaction Terms

$$\begin{aligned} \mathcal{L}^{\text{ren}} &= (\mathcal{D}^\mu H)^\dagger \mathcal{D}_\mu H + \partial^\mu \tilde{s}^\dagger \partial_\mu \tilde{s} - \left[ \mu_H^2 H^\dagger H + \tilde{s}^\dagger \mu_s^2 \tilde{s} + \lambda_H (H^\dagger H)^2 + 2H^\dagger H \tilde{s}^\dagger \Delta_{HS} \tilde{s} + (\tilde{s}^\dagger \Delta_{SS} \tilde{s})^2 \right] \\ &\supset \tilde{s}^\dagger (\mu_{s0}^2 \mathbf{1} + \mu_{s1}^2 A + \mu_{s2}^2 A^2) \tilde{s} + 2H^\dagger H \tilde{s}^\dagger (\lambda_{s0} \mathbf{1} + \lambda_{s1} A + \lambda_{s2} A^2) \tilde{s} + [\tilde{s}^\dagger (\lambda'_{s0} \mathbf{1} + \lambda'_{s1} A + \lambda'_{s2} A^2) \tilde{s}]^2, \end{aligned}$$

$$m_{S_k}^2 = \mu_k^2 + \lambda_k v^2, \quad \mu_k^2 = \mu_{s0}^2 + \mu_{s1}^2 \hat{A}_k + \mu_{s2}^2 \hat{A}_k^2, \quad \lambda_k^{(j)} = \lambda_{s0}^{(j)} + \lambda_{s1}^{(j)} \hat{A}_k + \lambda_{s2}^{(j)} \hat{A}_k^2.$$

With the parameter choices:

$O = \mathbf{1}$ ,  $M_\nu = M\mathbf{1}$ , Inverted Hierarchy neutrino spectrum with  $m_3 = 0$

$$m_{S_3}^2 = \mu_{s0}^2 + \lambda_{s0} v^2 = \mu_{s1}^2 + \lambda_{s1} v^2 = \mu_{s2}^2 + \lambda_{s2} v^2$$

$$m_{S_1}^2 = m_{S_3}^2 \left( 1 + \frac{2Mm_1}{v^2} + \frac{4M^2 m_1^2}{v^4} \right)$$

$$m_{S_2}^2 = m_{S_3}^2 \left( 1 + \frac{2Mm_2}{v^2} + \frac{4M^2 m_2^2}{v^4} \right)$$

### 2.2 Dimension-Six Effective Operators

$$\mathcal{L}' = \frac{C_{bdkl}^L}{\Lambda^2} O_{bdkl}^L + \frac{C_{bdkl}^R}{\Lambda^2} O_{bdkl}^R + \left( \frac{C_{bdkl}^{LR}}{\Lambda^2} O_{bdkl}^{LR} + \text{H.c.} \right),$$

$$\begin{aligned} C_{bdkl}^L &= (\Delta_{LL})_{bd} (\Delta_{SS})_{kl} + (\Delta_{LS})_{bl} (\Delta_{SL})_{kd} + (\Delta_{LS})_{kd} (\Delta_{SL})_{bl} & O_{bdkl}^L &= i \bar{L}_{b,L} \gamma^\rho L_{d,L} \tilde{s}_k^* \partial_\rho \tilde{s}_l \\ C_{bdkl}^R &= \delta_{bd} (\Delta'_{SS})_{kl} & O_{bdkl}^R &= i \bar{E}_{b,R} \gamma^\rho E_{d,R} \tilde{s}_k^* \partial_\rho \tilde{s}_l \\ C_{bdkl}^{LR} &= (\Delta_{LY} Y_e)_{bd} (\Delta'_{SS})_{kl} + (\Delta'_{LS})_{bl} (\Delta_{SY} Y_e)_{kd} & O_{bdkl}^{LR} &= \bar{L}_{b,L} E_{d,R} \tilde{s}_k^* \tilde{s}_l H \end{aligned}$$

This is in analogy to the case of quark-flavored scalar DM [4].

For simplicity, we adopt the following choices

$$C_{bdkl}^L = 2\kappa_L \delta_{bl} \delta_{dk}, \quad C_{bdkl}^R = \kappa_R \delta_{bd} \delta_{kl}, \quad C_{bdkl}^{LR} = \frac{\sqrt{2} \kappa_{LR} m_{\ell_d}}{v} \delta_{bl} \delta_{dk},$$

## 3 Phenomenology Aspects

### 3.1 Renormalizable Higgs-portal interactions

Constraints from DM annihilation, DM-nucleon scattering and Higgs invisible decay data

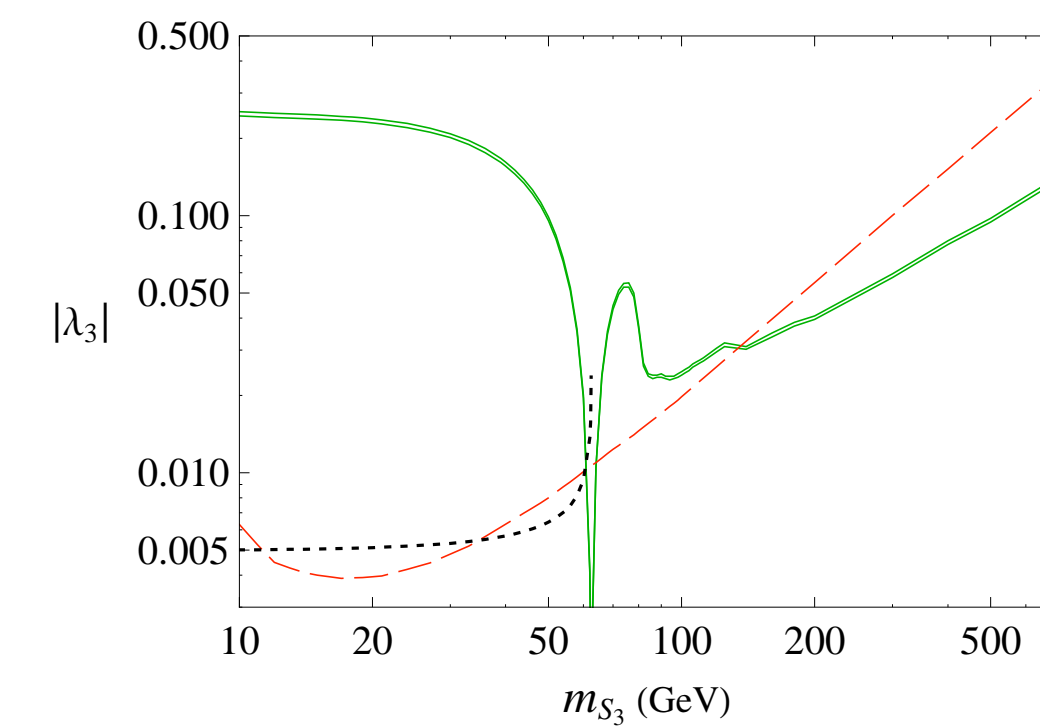


Figure 1: Values of  $|\lambda_3|$  consistent with the relic density data (green solid curve), compared to upper limits on  $|\lambda_3|$  from Higgs measurements (black dotted curve) and from null results of DM direct searches (red dashed curve). The numbers we used here are  $\mathcal{B}(h \rightarrow S^* S) < 0.19$ ,  $\Omega h^2 = 0.1198 \pm 0.0026$ . Direct search data is from LUX.

### 3.2 Non-Renormalizable Effective couplings

- (1) The DM annihilates to leptons  $S_3 S_3^* \rightarrow \ell_b^- \ell_d^+, \nu_b \nu_d$
- (2) Constraints from LEP II data on the monophoton production process  $e^+e^- \rightarrow \gamma \cancel{E}$  with missing energy  $\cancel{E}$  in the final state.

$$\sigma_{e\bar{e} \rightarrow \gamma S \bar{S} \rightarrow \gamma \cancel{E}} = \sum_{k,l=1}^3 \sigma_{e\bar{e} \rightarrow \gamma S_k \bar{S}_l} \mathcal{B}_{k3} \mathcal{B}_{l3}$$

with the branching ratios

$$\mathcal{B}_{13} = \mathcal{B}(S_1 \rightarrow \nu \nu' S_3), \quad \mathcal{B}_{23} = \mathcal{B}(S_2 \rightarrow \nu \nu' S_3) + \mathcal{B}(S_2 \rightarrow \nu \nu' S_1) \mathcal{B}_{13}, \quad \mathcal{B}_{33} = 1,$$

- (3) The International Linear Collider(ILC) can test this process more stringently in the future.

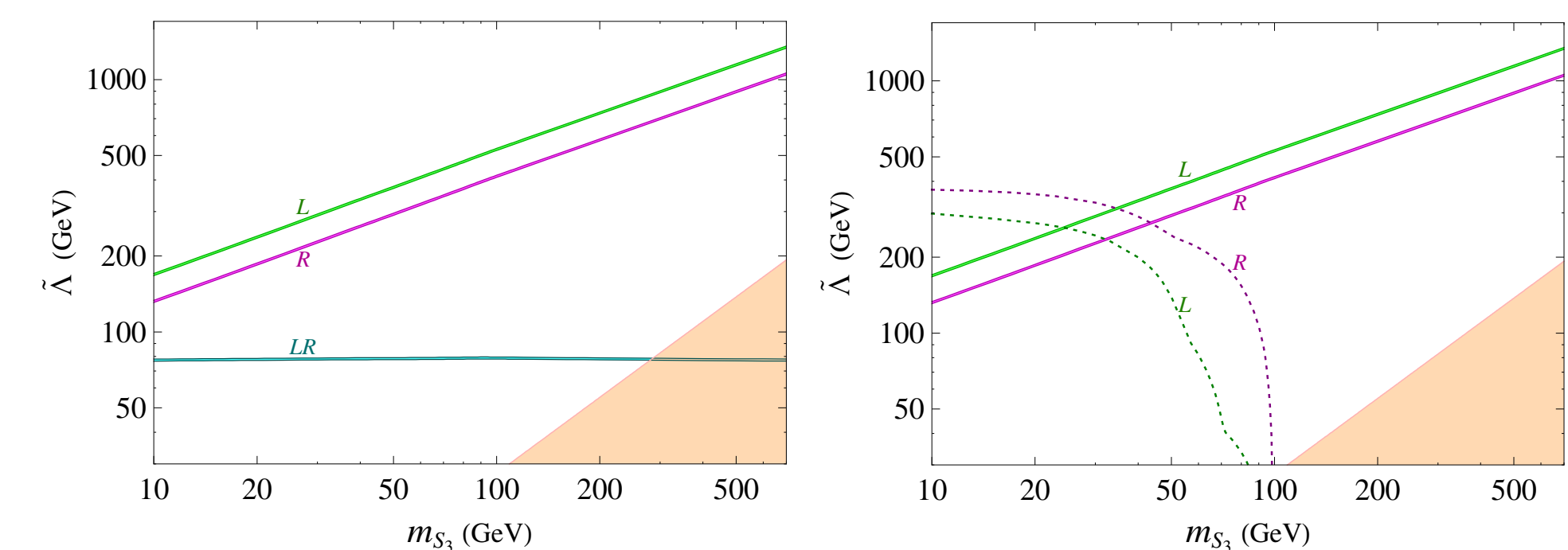


Figure 2: Values of  $\tilde{\lambda} = \Lambda/|\kappa_c|^{1/2}$  for  $\epsilon = L, R, LR$  fulfilling the relic density constraint. The orange region depicts where the EFT approach breaks down. The dotted curves represent restraints from  $e^+e^- \rightarrow \gamma \cancel{E}$  at LEP II.

### 3.3 Constraints from Lepton Flavor Violating Rare Decay $\ell_a^- \rightarrow \ell_b^- \ell_c^- \ell_d^+$

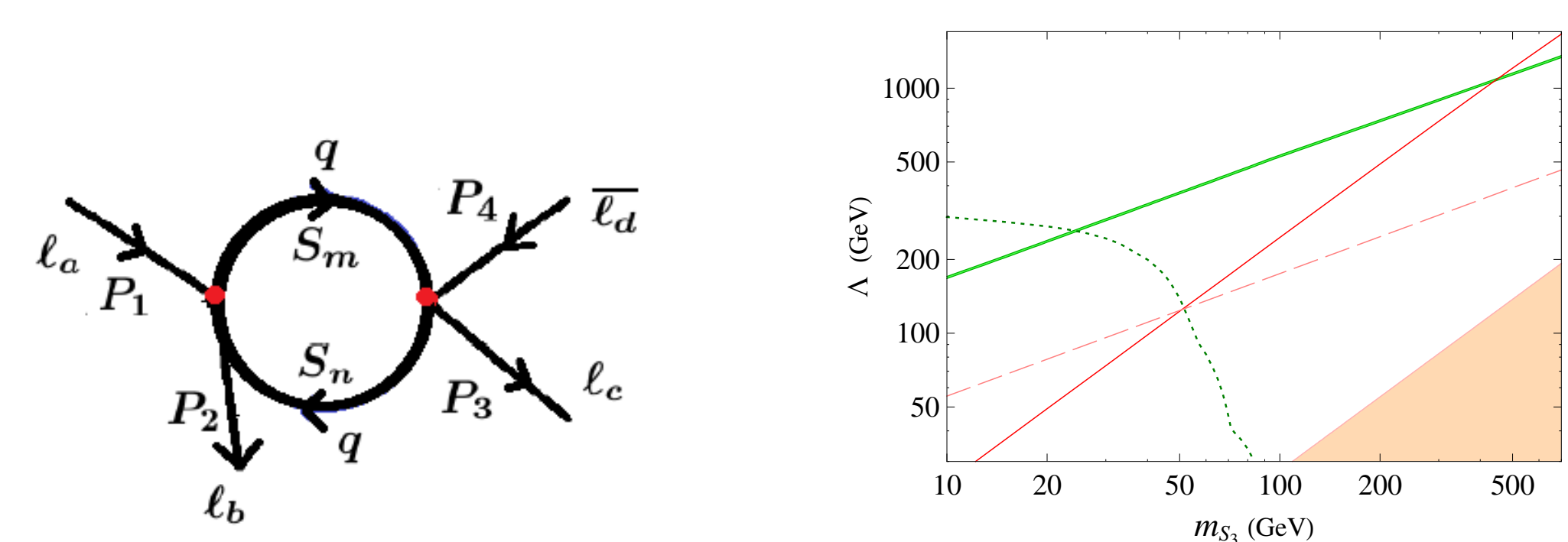


Figure 3: Constraints from lepton flavor violating rare decay:  $\mu^- \rightarrow e^- e^- e^+$  (red solid curve) and  $\tau^- \rightarrow \mu^- \mu^- e^+$  (pink dashed curve)

### 3.4 Flavor-violating Higgs Decay $h \rightarrow \mu\tau$

$$\Gamma_{h \rightarrow \ell_b \ell_d} = \frac{m_h |y_{bd}^{\text{SM}} + y_{bd}^{\text{new}}|^2}{16\pi v^2} (m_{\ell_b}^2 + m_{\ell_d}^2)$$

The CMS Collaboration has recently detected a slight excess of  $h \rightarrow \mu^\pm \tau^\mp$  events with a significance of  $2.5\sigma$ . As a statistical fluctuation it translates into a limit of

$\mathcal{B}(h \rightarrow \mu\tau) < 1.57\%$  at 95% CL

ATLAS and CMS recent data also suggest  $0.7 < \frac{\Gamma_{h \rightarrow \mu\tau}}{\Gamma_{h \rightarrow \tau\tau}^{\text{SM}}} < 1.8$ ,  $\frac{\Gamma_{h \rightarrow \mu\bar{\mu}}}{\Gamma_{h \rightarrow \mu\mu}^{\text{SM}}} < 6.7$ ,

Our model can accommodate this  $h \rightarrow \mu\tau$  hint. Select sample point from blue curve in Figure 2

$$(m_{S_3}, \Lambda) = (200, 78) \text{ GeV} \xrightarrow{(h \rightarrow \mu\tau)} -2.9 < \lambda_1 < -2.4 \xrightarrow{\text{Prediction}} \begin{cases} 1.6 < \Gamma_{h \rightarrow \tau\tau} / \Gamma_{h \rightarrow \tau\tau}^{\text{SM}} < 1.8 \\ 1.8 < \Gamma_{h \rightarrow \mu\bar{\mu}} / \Gamma_{h \rightarrow \mu\mu}^{\text{SM}} < 2.0 \end{cases}$$

## 4 Summary

- (1) We apply the MFV principle to a lepton-flavored scalar DM model supplemented with the type-I seesaw mechanism.
- (2) In addition to Higgs-portal renormalizable interaction terms, we can construct three possible effective couplings which conform the SM gauge symmetry and the flavor symmetry from the effective field theory point of view.
- (3) The MFV framework allows us to make interesting phenomenological connections between the evidence and searches for DM, Higgs collider measurements, and available data on lepton-flavor-violating processes. The future experiments at the LHC and ILC can probe various aspects of our model in greater detail.

## References

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