

Way to crosscheck  $\mu$ -e conversion in  
the case of no signals of  $\mu \rightarrow e\gamma$  and  $\mu \rightarrow 3e$

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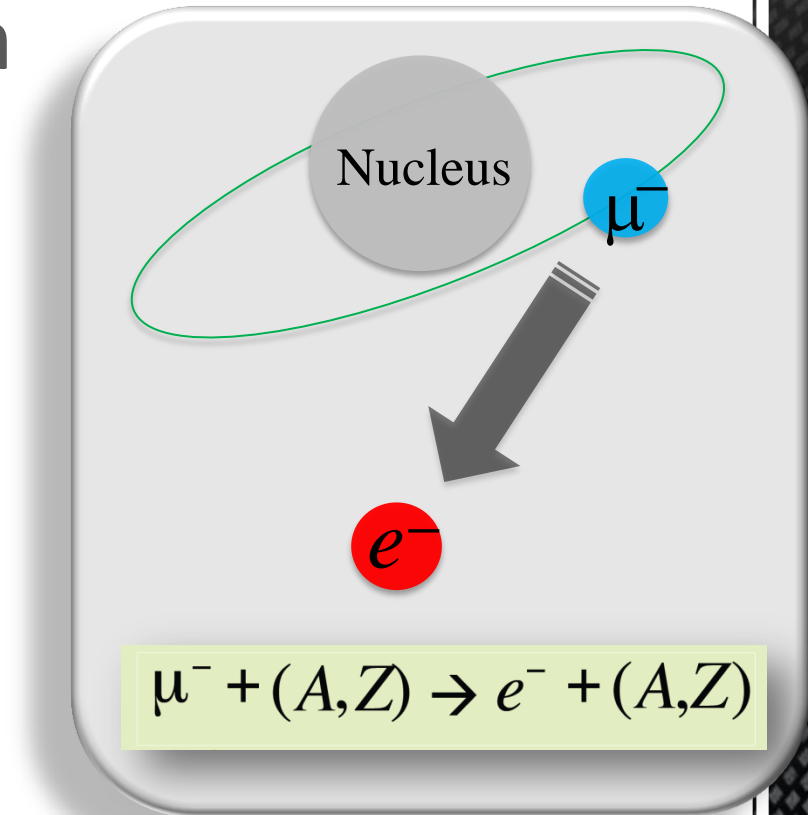
Collaborator Joe Sato  
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**Key ingredient:**

Interplay between measurement of exotic dijet@LHC and  
observations of  $\mu$ -e conv.@near future experiments

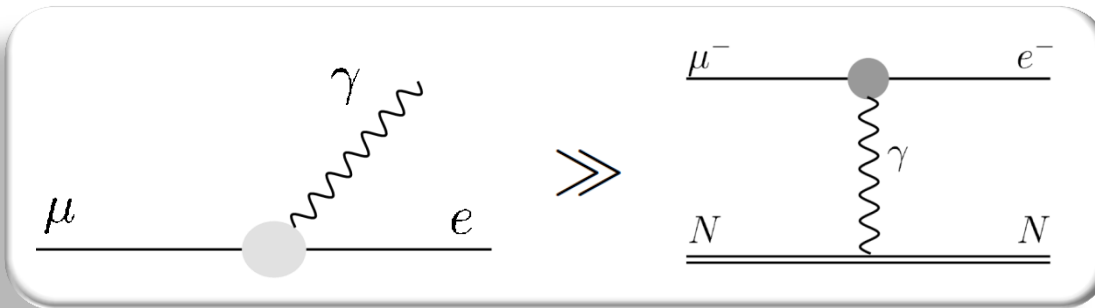
# Waiting for $\mu$ -e conversion

- ☑ COMET, DeeMe, and Mu2e launch soon!
  
- ☑ Discovery of the  $\mu$ -e conv.  
= clear evidence of new physics
  
  
  
  
  
  
  
  
  
  
- ☑ With observations of  $\mu \rightarrow e\gamma$  and/or  $\mu \rightarrow 3e$ 
  - ▣ Identification of type of LFV interaction
  - ▣ Determination of relevant parameters



# Waiting for $\mu$ -e conversion

- ☑ If  $\mu \rightarrow e\gamma$  **will never be** observed after the discovery of  $\mu$ -e conv.
  - ▣ Dipole LFV interaction and relevant models are ruled out



SUSY models, etc.

- ☑  $\mu \rightarrow 3e$  **will never be also** observed
  - ▣ How to confirm the discovery of  $\mu$ -e conversion???
  - ▣ No LFV interaction and no new physics???

# Aim of this work

- ☑ Our target situation

$\mu$ -e conversion is discovered, while other muon LFV processes will never be found

- ☑ Aim of this work

- ▣ Understand how to confirm the discovery of  $\mu$ -e conversion
- ▣ Check the feasibility to identify underlying physics and to determine LFV parameters

# Expected structure of LFV interaction

☑ Expected LFV interaction in our target situation

~~☑  $\mu \rightarrow e\gamma$~~

☑ Massive mediator

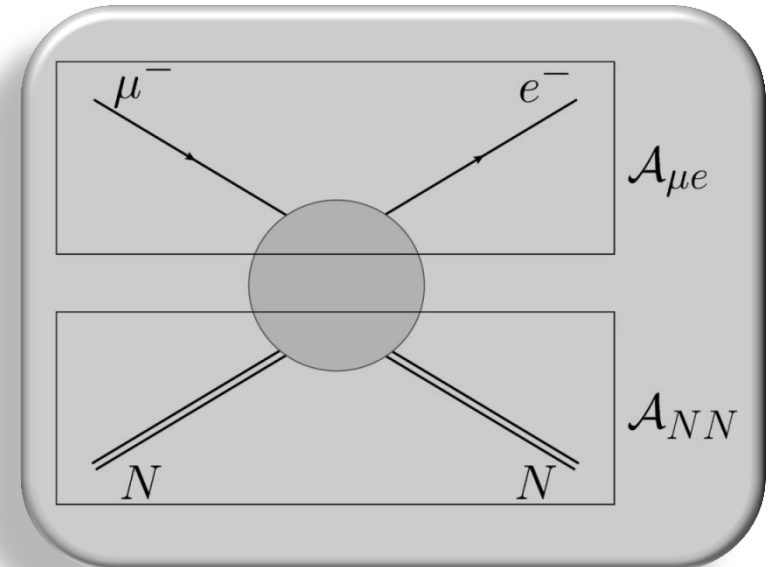
~~☑  $\mu \rightarrow 3e$~~

☑ Small coupling with  $e^-e^+$

☑  $\mu$ - $e$  conversion

☑ Couple to quarks and/or gluons

☑ Flavor violating coupling with  $\mu$  and  $e$



# Benchmark: R-parity violating SUSY

- ☑ One of the benchmark model: R-parity violating (RPV) SUSY
- ☑ In general SUSY models contain RPV terms

$$\mathcal{W}_{\text{RPV}} = \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c + \lambda''_{ijk} U_i^c D_j^c D_k^c$$

Omit to avoid proton decay

- ☑ Setting 1

Flavor diagonal components are larger than off-diagonal

➔  $\lambda'_{ijj} \gg \lambda'_{ijk} \quad (j \neq k)$

Naturally realized unless additional sources of flavor violation are introduced

# Benchmark: R-parity violating SUSY

## ☑ Setting 2

Different generation of left- and right-handed leptons

➔  $\lambda_{ijk}$  ( $i \neq k$  and  $j \neq k$ )

## ☑ Setting 3

SUSY particle contribution: only 3rd generation

Naturally realized by RG evolution with universal masses@GUT scale

## ☑ Lagrangian

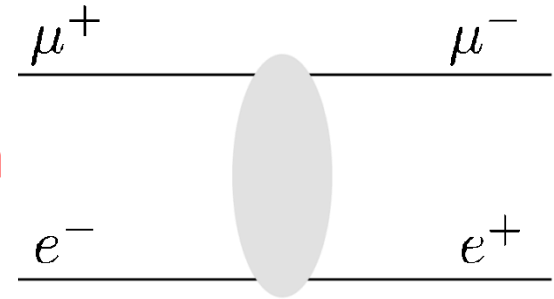
$$\mathcal{L}_{\text{RPV}} = \mathcal{L}_\lambda + \mathcal{L}_{\lambda'}$$

$$\mathcal{L}_\lambda = 2 \left[ \lambda_{312} \tilde{\nu}_{\tau L} \bar{\mu} P_L e + \lambda_{321} \tilde{\nu}_{\tau L} \bar{e} P_L \mu + \lambda_{132} \tilde{\tau}_L \bar{\mu} P_L \nu_e + \lambda_{231} \tilde{\tau}_L \bar{e} P_L \nu_\mu \right] + \text{h.c.}$$

$$\mathcal{L}_{\lambda'} = \left[ \lambda'_{311} (\tilde{\nu}_{\tau L} \bar{d} P_L d - \tilde{\tau}_L \bar{d} P_L u) + \lambda'_{322} (\tilde{\nu}_{\tau L} \bar{s} P_L s - \tilde{\tau}_L \bar{s} P_L c) \right] + \text{h.c.}$$

# Exotic processes in benchmark RPV

muonium conversion

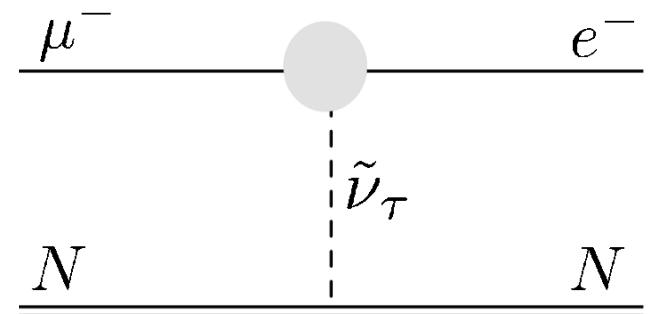


$$\mathcal{L}_{\text{RPV}} = \mathcal{L}_\lambda + \mathcal{L}_{\lambda'}$$

$$\mathcal{L}_\lambda = 2 \left[ \lambda_{312} \tilde{\nu}_{\tau L} \bar{\mu} P_L e + \lambda_{321} \tilde{\nu}_{\tau L} \bar{e} P_L \mu + \lambda_{132} \tilde{\tau}_L \bar{\mu} P_L \nu_e + \lambda_{231} \tilde{\tau}_L \bar{e} P_L \nu_\mu \right] + \text{h.c.}$$

$$\mathcal{L}_{\lambda'} = \left[ \lambda'_{311} (\tilde{\nu}_{\tau L} \bar{d} P_L d - \tilde{\tau}_L \bar{d} P_L u) + \lambda'_{322} (\tilde{\nu}_{\tau L} \bar{s} P_L s - \tilde{\tau}_L \bar{s} P_L c) \right] + \text{h.c.}$$

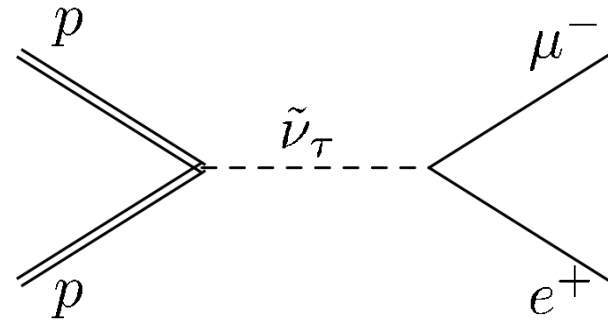
$\mu$ - $e$  conversion





# Exotic processes in benchmark RPV

$pp \rightarrow \mu^- e^+$

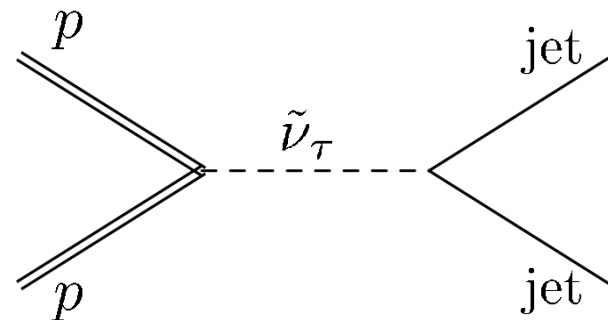


$$\mathcal{L}_{\text{RPV}} = \mathcal{L}_\lambda + \mathcal{L}_{\lambda'},$$

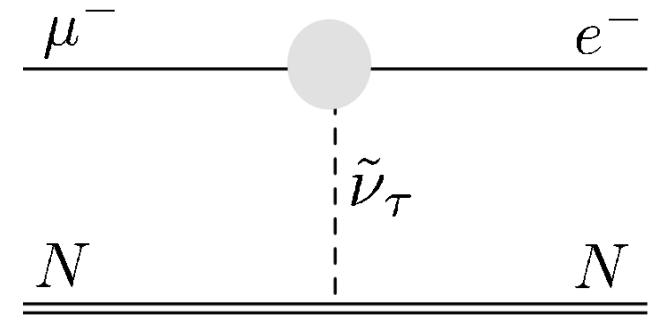
$$\mathcal{L}_\lambda = 2 \left[ \lambda_{312} \tilde{\nu}_{\tau L} \bar{\mu} P_L e + \lambda_{321} \tilde{\nu}_{\tau L} \bar{e} P_L \mu + \lambda_{132} \tilde{\tau}_L \bar{\mu} P_L \nu_e + \lambda_{231} \tilde{\tau}_L \bar{e} P_L \nu_\mu \right] + \text{h.c.}$$

$$\mathcal{L}_{\lambda'} = \left[ \lambda'_{311} (\tilde{\nu}_{\tau L} \bar{d} P_L d - \tilde{\tau}_L \bar{d} P_L u) + \lambda'_{322} (\tilde{\nu}_{\tau L} \bar{s} P_L s - \tilde{\tau}_L \bar{s} P_L c) \right] + \text{h.c.}$$

$pp \rightarrow \text{dijet}$



# $\mu$ -e conversion



- Amplitude: overlap of wave functions of  $\mu$ ,  $e$ , and nucleus

$$\mathcal{M} = \frac{G_F}{\sqrt{2}} \sum_{q=d,s} \int d^3 \mathbf{x} \left( g_{LS(q)} \bar{\psi}^{(e)} P_R \psi_{1S}^{(\mu)} + g_{RS(q)} \bar{\psi}^{(e)} P_L \psi_{1S}^{(\mu)} \right) \langle N | \bar{q} q | N \rangle$$

Function of  $\lambda_{ijk}$ ,  $\lambda'_{ijk}$ ,  
and tau sneutrino mass

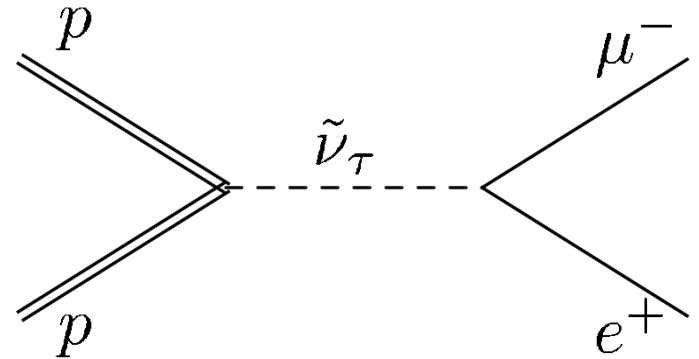
Matrix element determined by  
nucleon density for each N

- Branching ratio

$$\begin{aligned} \text{BR}(\mu^- \text{Al} \rightarrow e^- \text{Al}) &= 2.092 \times 10^{-15} \left( \frac{1 \text{TeV}}{m_{\tilde{\nu}_\tau}} \right)^4 \left( \frac{\lambda'_{311} \lambda}{10^{-8}} \right)^2 \left| 1 + 0.530 \left( \frac{\lambda'_{322}}{\lambda'_{311}} \right) \right|^2 \\ &= 5.881 \times 10^{-16} \left( \frac{1 \text{TeV}}{m_{\tilde{\nu}_\tau}} \right)^4 \left( \frac{\lambda'_{322} \lambda}{10^{-8}} \right)^2 \left| 1 + 1.886 \left( \frac{\lambda'_{311}}{\lambda'_{322}} \right) \right|^2 \end{aligned}$$

# $pp \rightarrow \mu^- e^+$ and $pp \rightarrow \text{dijet}@LHC$

- ☑ Dominant: s-channel resonance
- ☑ Cross sections are approximated by the Breit-Wigner formula



$$\begin{aligned}\sigma(pp \rightarrow f_1 f_2) &= F(\sqrt{s}, m_{\tilde{\nu}_\tau}, q_1, q_2) \times \Gamma_{\tilde{\nu}_\tau} \text{BR}(\tilde{\nu}_\tau \rightarrow q_1 q_2) \text{BR}(\tilde{\nu}_\tau \rightarrow f_1 f_2) \\ &= F(\sqrt{s}, m_{\tilde{\nu}_\tau}, q_1, q_2) m_{\tilde{\nu}_\tau} \times \gamma_{\tilde{\nu}_\tau} \text{BR}(\tilde{\nu}_\tau \rightarrow q_1 q_2) \text{BR}(\tilde{\nu}_\tau \rightarrow f_1 f_2)\end{aligned}$$

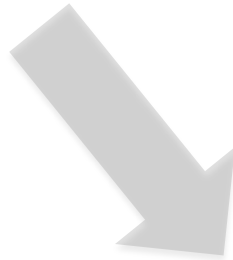
Determined by initial quarks  
and mediator mass

Depends only on couplings

$$\gamma_{\tilde{\nu}_\tau} = \Gamma_{\tilde{\nu}_\tau} / m_{\tilde{\nu}_\tau}$$

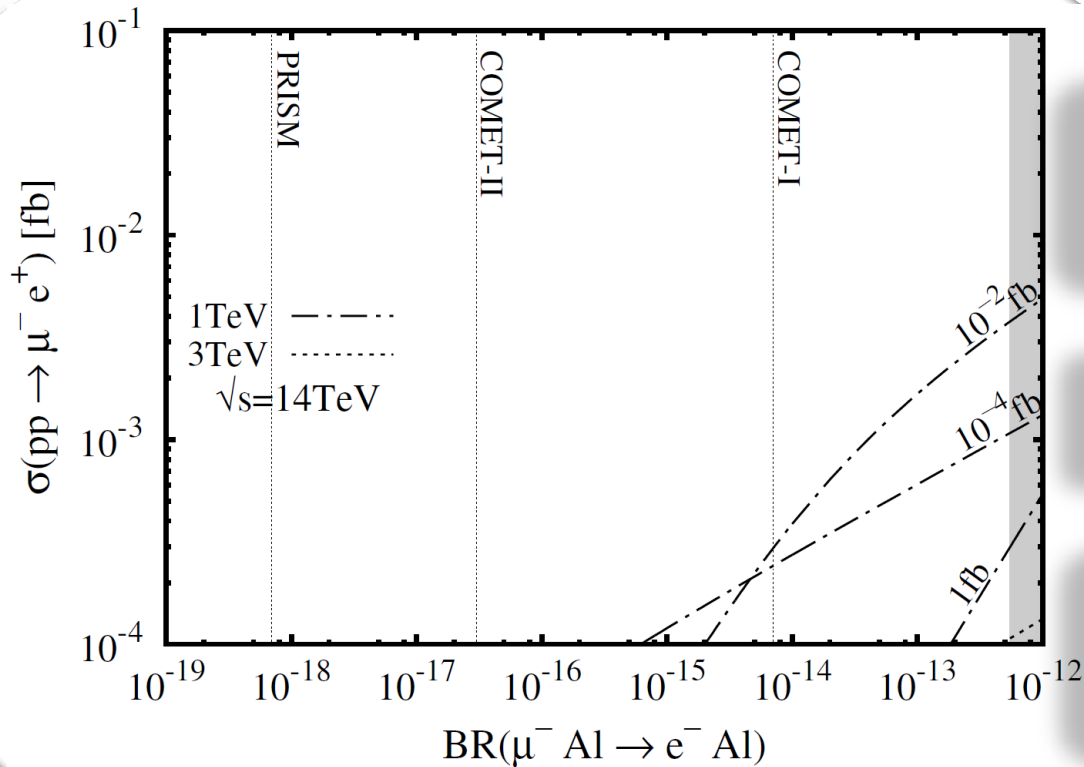
# Correlation of $\mu$ -e conv. and LHC signals

- ☑ How to confirm  $\mu$ -e conversion event
- ☑ How to discriminate the benchmark scenario and other models



- ☑ Check the correlations of
  - ▣  $\text{BR}(\mu^- + N \rightarrow e^- + N)$
  - ▣  $\sigma(pp \rightarrow \mu\bar{e})$
  - ▣  $\sigma(pp \rightarrow jj)$

# Correlation of $\mu$ -e conv. and LHC signals



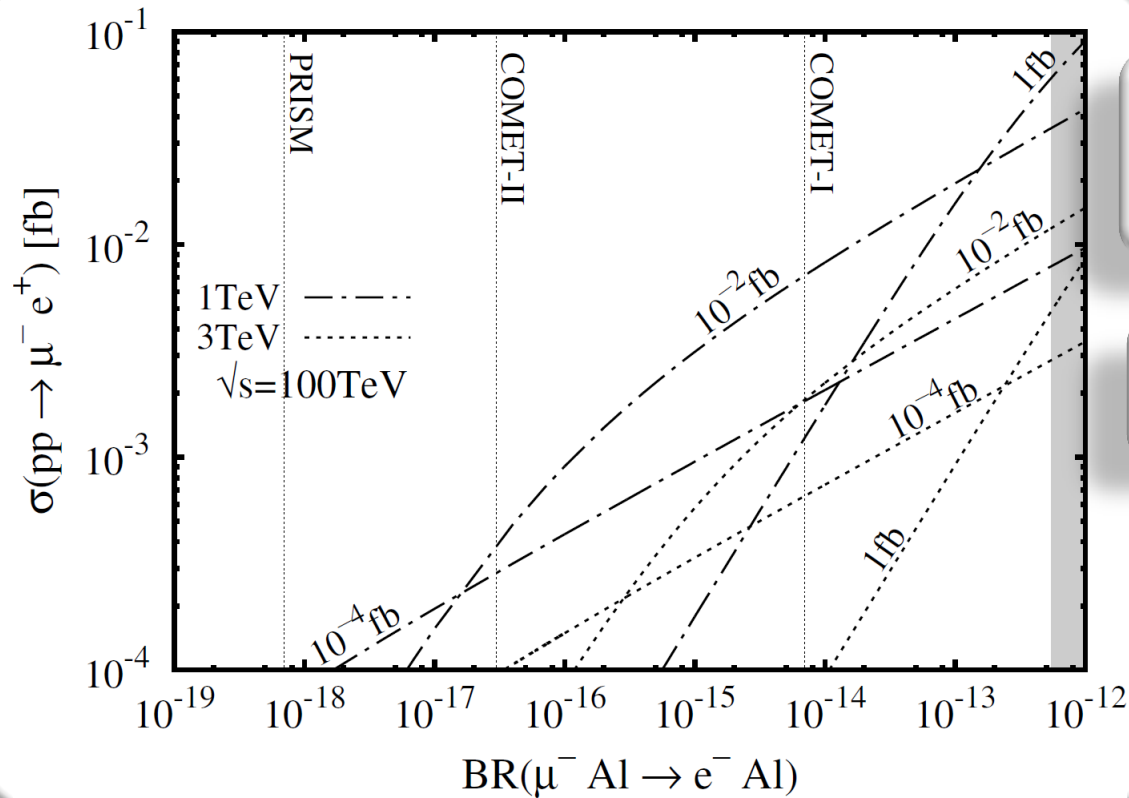
$\sigma(pp \rightarrow \mu^- e^+)$  as a function of  $\text{BR}(\mu^- \text{Al} \rightarrow e^- \text{Al})$

each line :  $\sigma(pp \rightarrow jj)$

Vertical line: experimental reach of  $\mu$ -e conversion search

- ☑ Unique behavior: larger  $\sigma(pp \rightarrow jj)$  suggests smaller  $\sigma(pp \rightarrow \mu^- e^+)$
- ☑ Check the correlations and the behavior to discriminate models

# Correlation of $\mu$ -e conv. and LHC signals



$\sigma(pp \rightarrow \mu^- e^+)$  as a function of  $\text{BR}(\mu^- \text{Al} \rightarrow e^- \text{Al})$

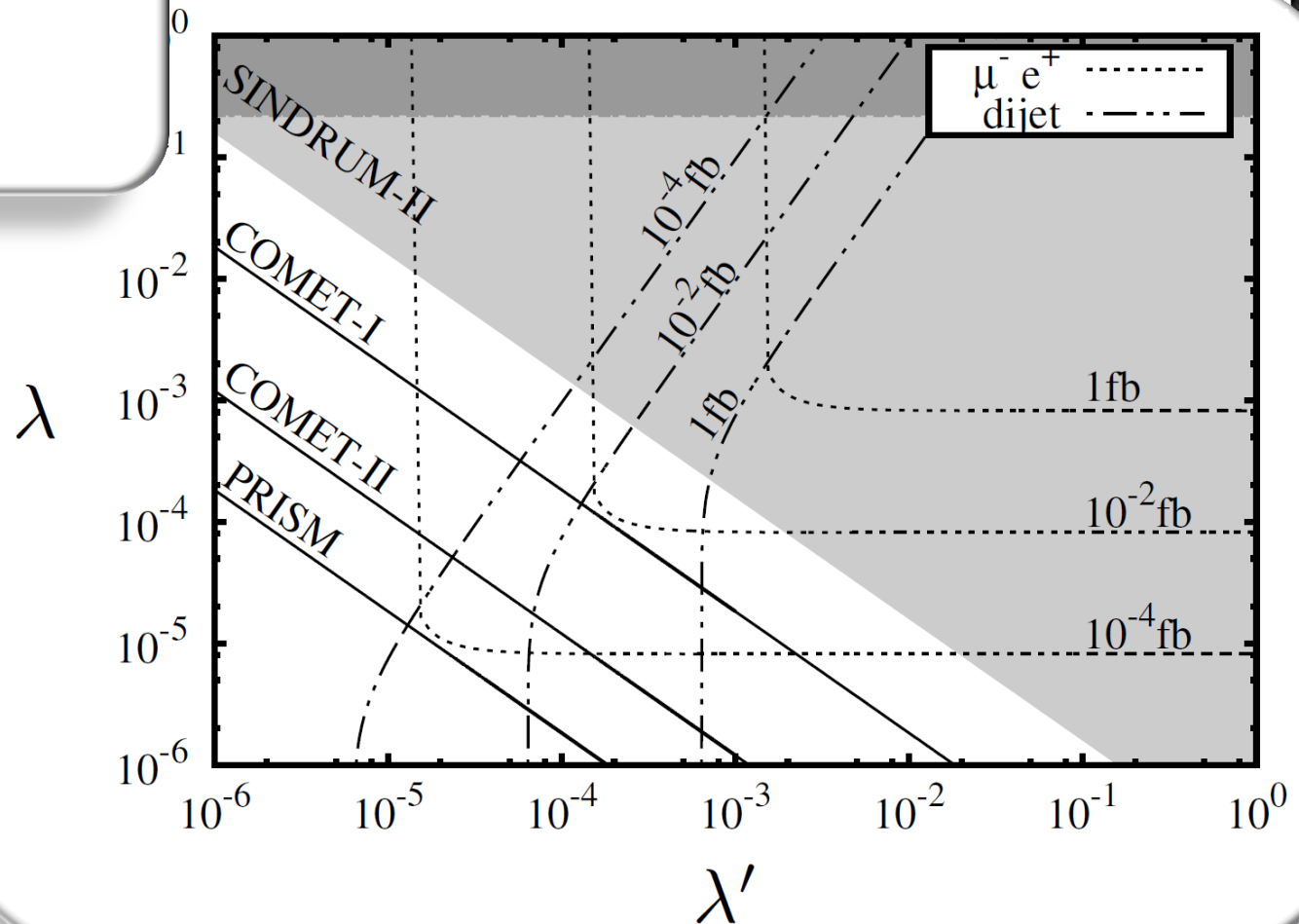
each line :  $\sigma(pp \rightarrow jj)$

- ☑ Accessible up to  $\sim 3\text{TeV}$  slepton
- ☑ Exhibit the correlation to check LFV in our target situation

# Determination of model parameters

Contour plot of

- $\text{BR}(\mu^- + N \rightarrow e^- + N)$
- $\sigma(pp \rightarrow \mu\bar{e})$
- $\sigma(pp \rightarrow jj)$



# Determination of model parameters

- sneutrino mass  $m_{\tilde{\nu}_\tau} = 1\text{TeV}$
- collision energy  $\sqrt{s} = 100\text{TeV}$

- Shaded region: excluded by SINDRUM-II
- Solid line: experimental reach of  $\mu$ -e conversion search

- ☑  $\mu$ -e conversion searches will cover parameter space wherein LHC can survey
- ☑  $\mu$ -e conv. searches and LHC precisely determine RPV parameters!



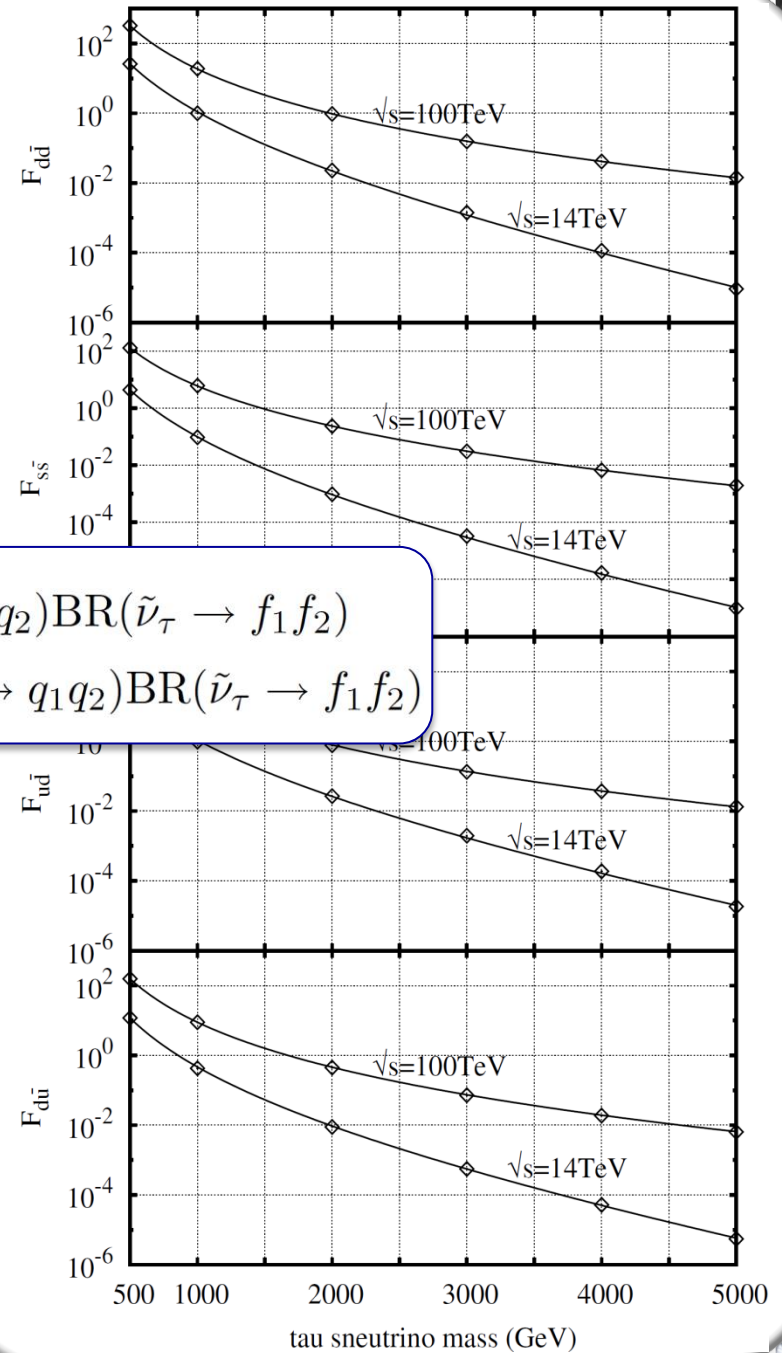
# Summary

- ☑ We studied the situation that  $\mu$ - $e$  conversion is discovered while other muon LFV processes will never be observed
- ☑ Important issues in such a situation are
  - ▣ How to confirm the discovery of  $\mu$ - $e$  conversion
  - ▣ How to determine LFV parameters and its underlying physics
- ☑ We expected LFV interaction in such a situation, and studied R-parity violating SUSY as a benchmark
- ☑ Key ingredients are  $pp \rightarrow \mu^- e^+$  and  $pp \rightarrow$  dijet
- ☑ We can discriminate models and determine parameters from the correlation of  $BR(\mu^- N \rightarrow e^- N)$ ,  $\sigma(pp \rightarrow jj)$ , and  $\sigma(pp \rightarrow \mu^- e^+)$

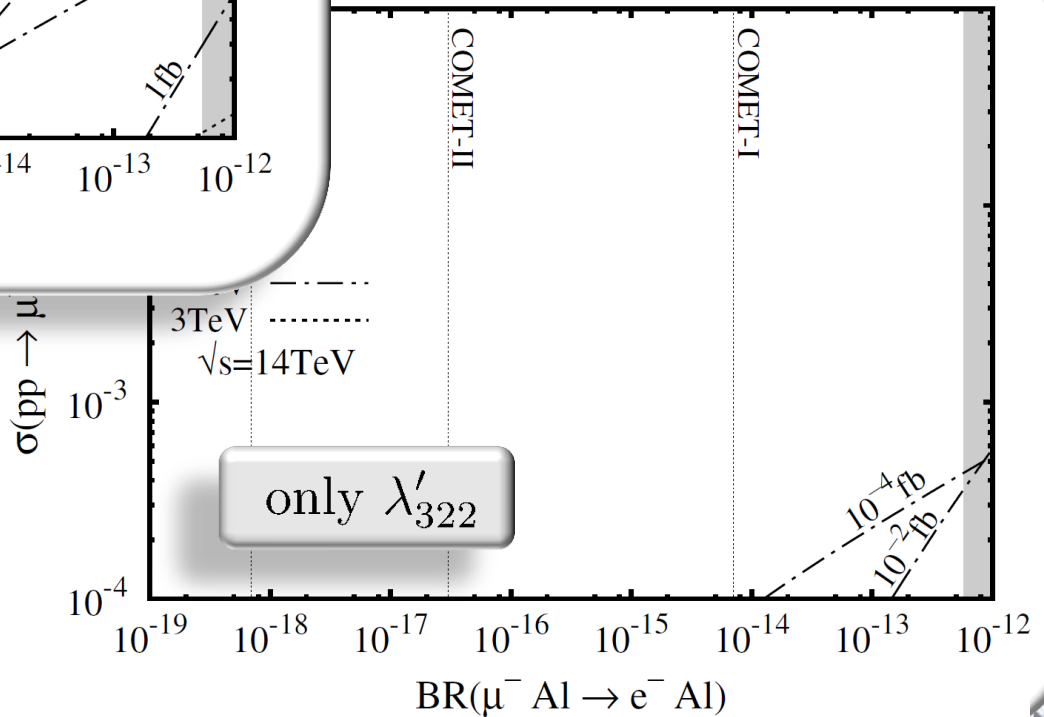
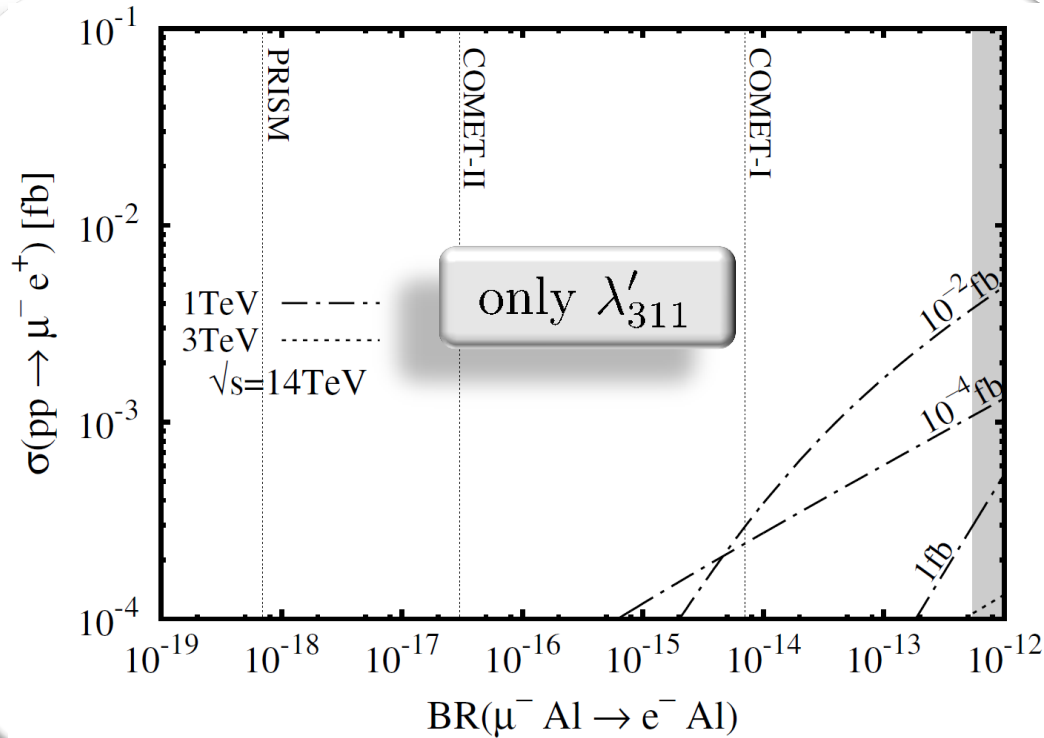
Backup slides

# Cross section

$$\begin{aligned} \sigma(pp \rightarrow f_1 f_2) &= F(\sqrt{s}, m_{\tilde{\nu}_\tau}, q_1, q_2) \times \Gamma_{\tilde{\nu}_\tau} \text{BR}(\tilde{\nu}_\tau \rightarrow q_1 q_2) \text{BR}(\tilde{\nu}_\tau \rightarrow f_1 f_2) \\ &= F(\sqrt{s}, m_{\tilde{\nu}_\tau}, q_1, q_2) m_{\tilde{\nu}_\tau} \times \gamma_{\tilde{\nu}_\tau} \text{BR}(\tilde{\nu}_\tau \rightarrow q_1 q_2) \text{BR}(\tilde{\nu}_\tau \rightarrow f_1 f_2) \end{aligned}$$



# Correlation of $\mu$ -e conv. and LHC signals



HogeHoge