

Tau Physics at Belle II

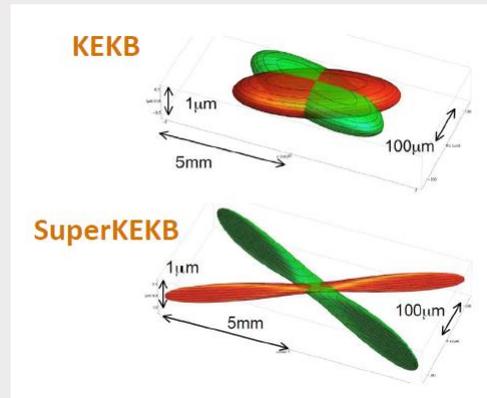
K.Hayasaka (Niigata U.)
for Belle II collaboration

Contents

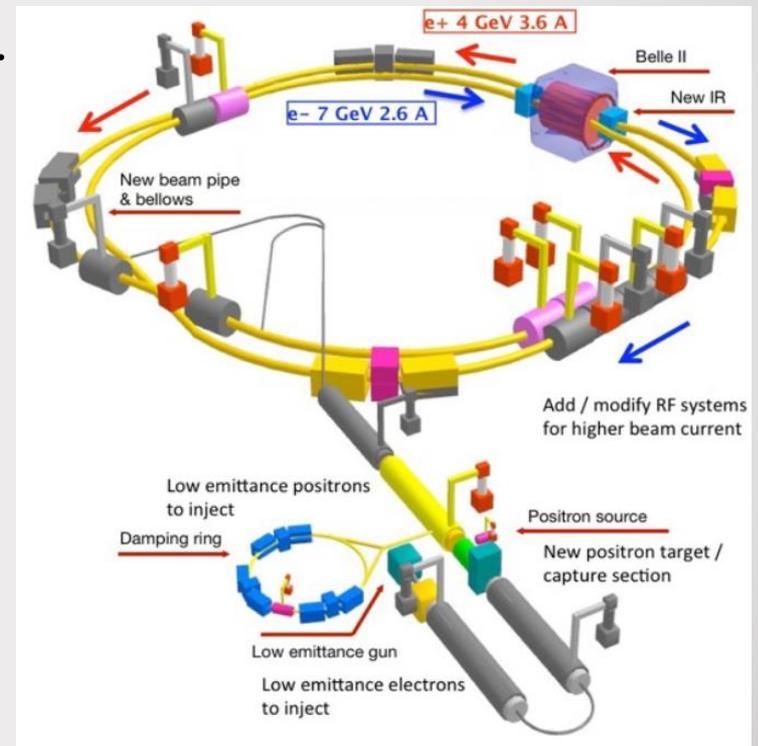
- SuperKEKB/Belle II
- τ lepton
- τ mass measurement with early Belle II data
- τ LFV search
- τ CPV search
- Summary

From KEKB to SuperKEKB

- To obtain 50x larger data sample than that at Belle, designed instant luminosity is 40x higher.
 - Beam current: 2x
 - Beam size: 1/20x

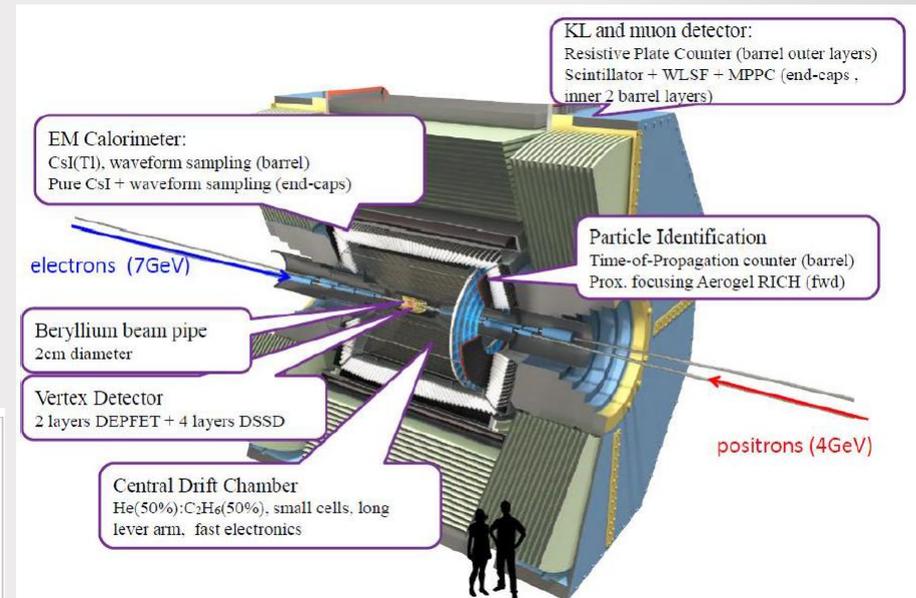
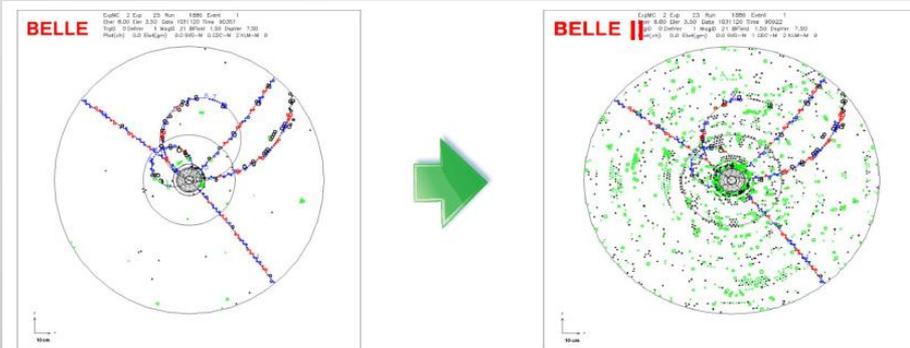


Beam asymmetry : 8GeV/3.5GeV → 7GeV/4GeV



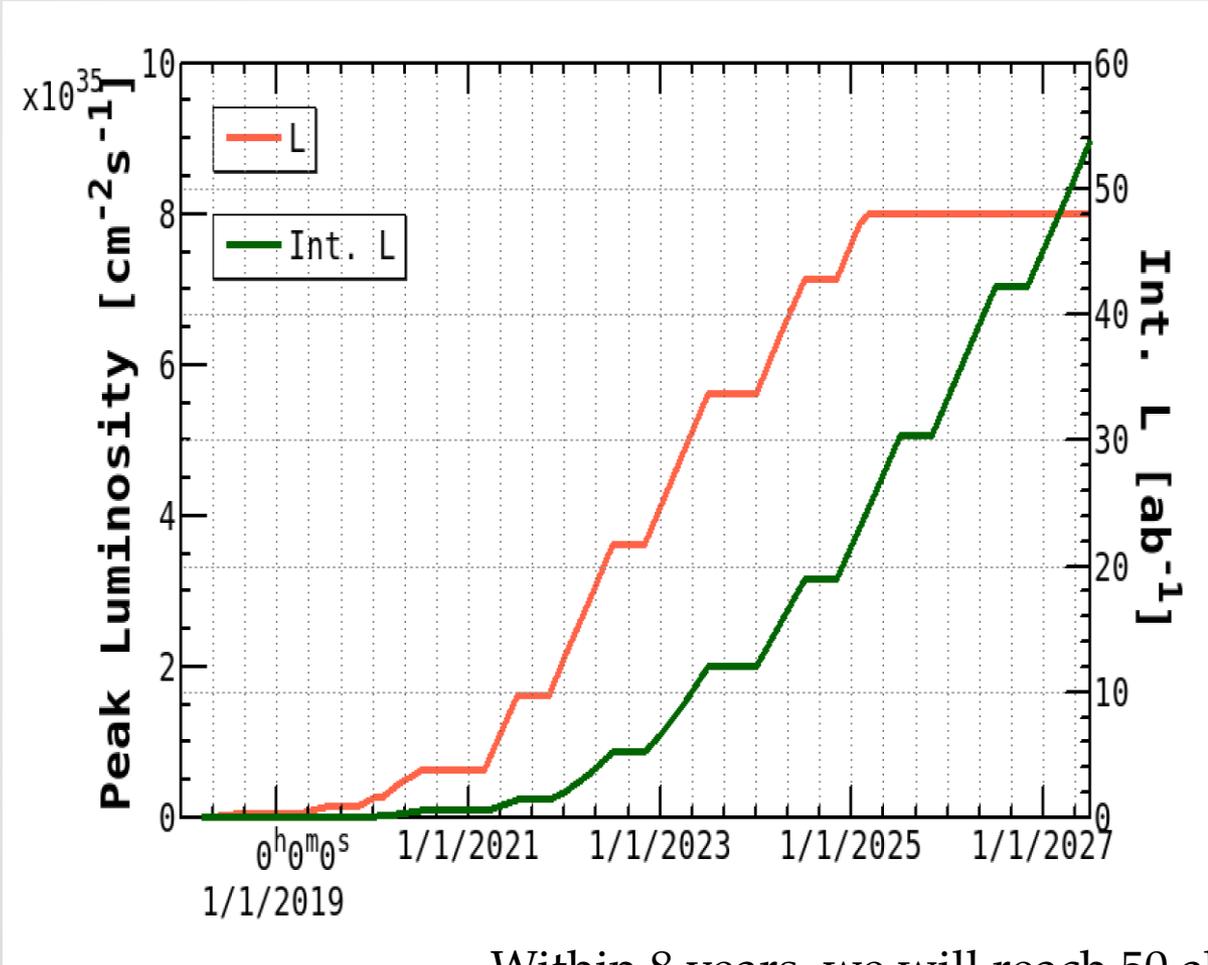
Belle II detector upgrade

- To catch up the high rate event production
 - High rate read out
 - Short dead time
 - Reduce occupancy
 - High resolution against reduced asymmetry
- PID performance



Just an image for track finding in high background environment

Integrated luminosity prospect



1 div
= 4 months

Within 8 years, we will reach 50 ab^{-1} .

Introduction to τ lepton

- Third lepton = τ lepton

FERMIONS		
Leptons spin = 1/2		
Flavor	Mass GeV/c ²	Electric charge
ν_e electron neutrino	$<1 \times 10^{-8}$	0
e electron	0.000511	-1
ν_μ muon neutrino	<0.0002	0
μ muon	0.106	-1
ν_τ tau neutrino	<0.02	0
τ tau	1.7771	-1

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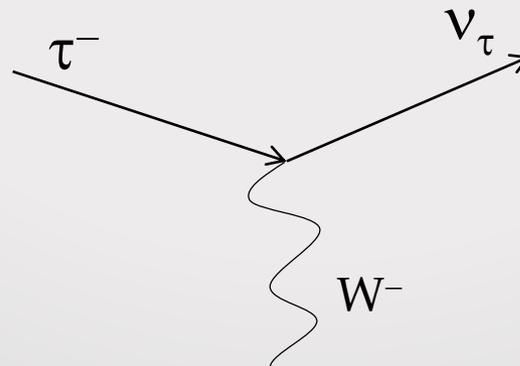
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- \rightarrow Various decay modes are allowed
- In SM, it decays via weak interaction = neutrino(s) appears in the final state.

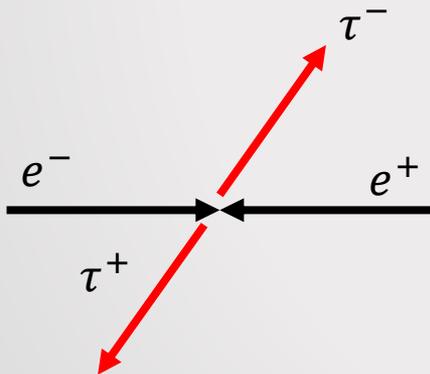


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τ production at SuperKEKB

- At $Y(4S)$, $\sigma(\tau^+\tau^-) = 0.9$ nb while $\sigma(b\bar{b}) = 1.1$ nb.
→ B factory is also τ factory: With 50 ab^{-1} , $\sim 5 \times 10^{10}$ τ -pairs are expected.

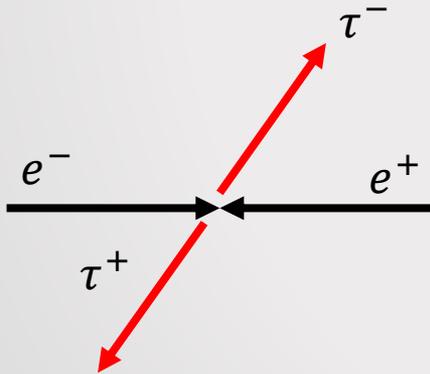
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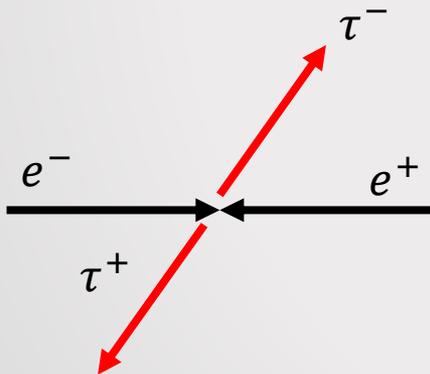
$$M_{Y(4S)} \gg 2 \times M_\tau$$

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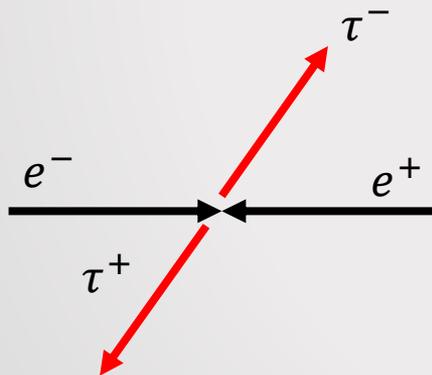
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Low multiplicity event
2-prong: 73%
4-prong: 26%
>6-prong: 1%

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τ analysis in τ -pair events is expected to be clean because of low multiplicity and topologically distinct backgrounds.

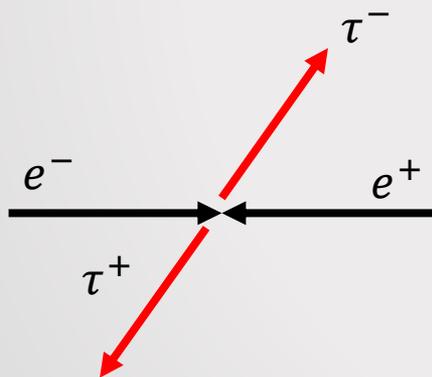
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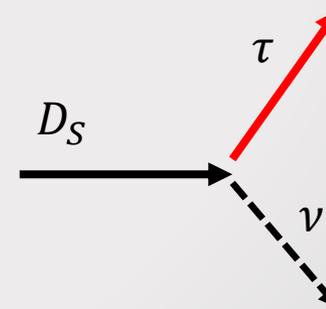


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At LHCb, τ appears as a decay-product in D_S decays, mainly. ($\text{BF}(D_S \rightarrow \tau\nu) = 5.5\%$)

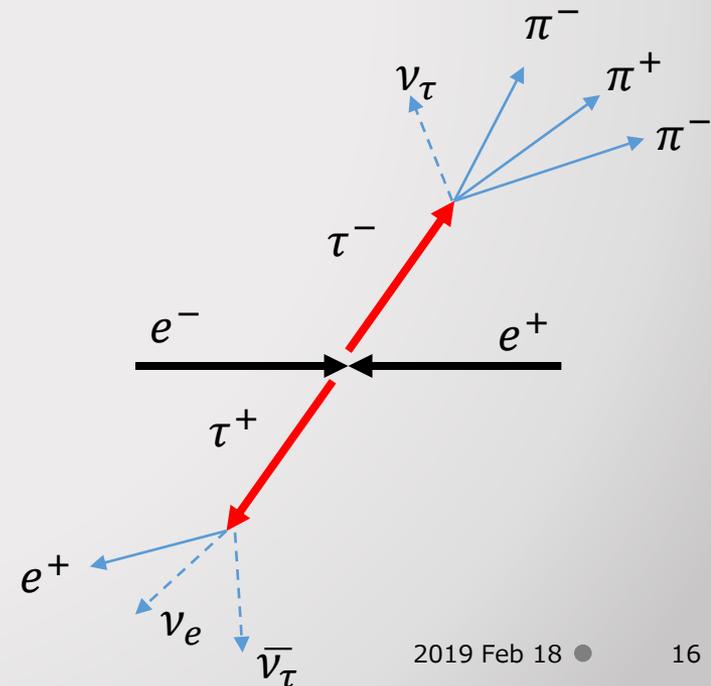


$3 \text{ fb}^{-1} : \sim 10^{11}$ τ 's

τ analysis with the early Belle II data ...

$\tau \rightarrow 3\pi\nu$ in Belle II early data

- $(\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau)(\tau^+ \rightarrow \text{one track} + \bar{\nu}_\tau)$ (and its charge conjugate): one of typical τ -pair events.

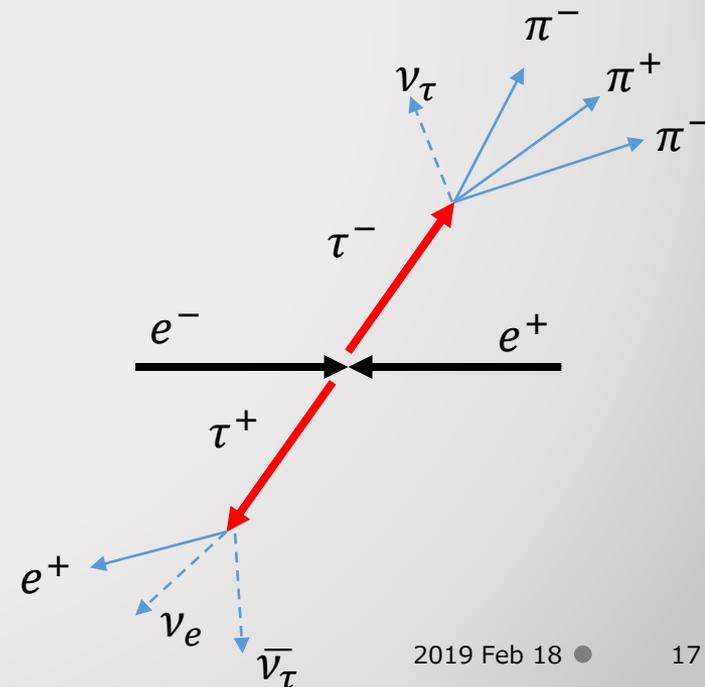


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$q\bar{q}$ BG: event shape is spherical.



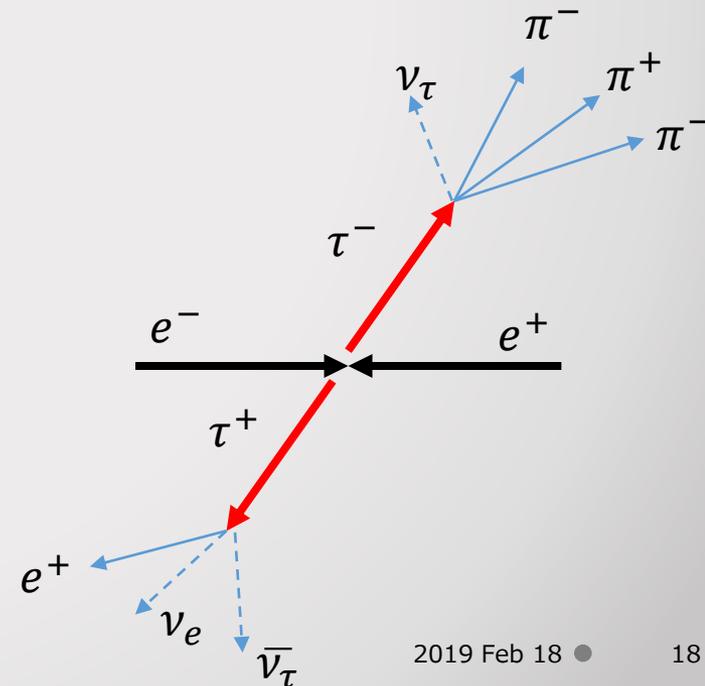
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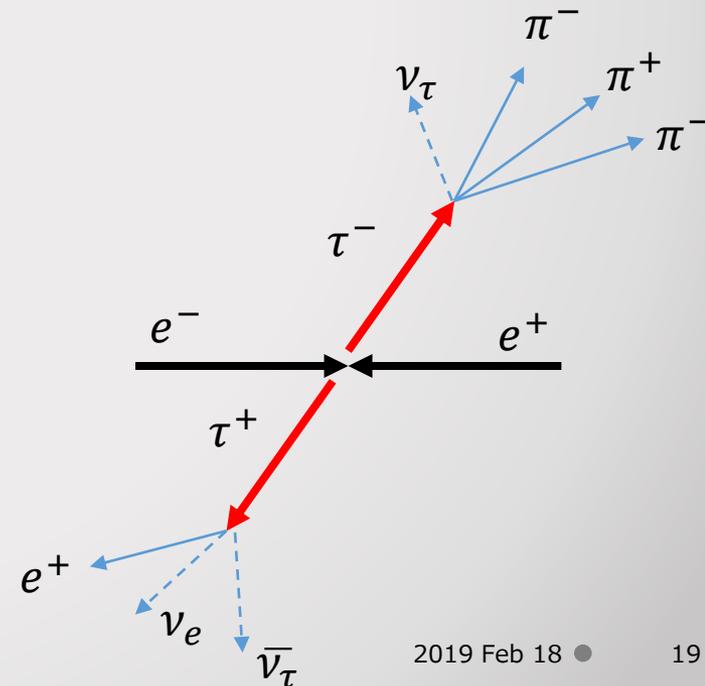
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As a demonstration,
we analyze these events
in Belle II early data
and measured tau mass.



Event selection

- 1-3 prong topology
 - Definition of thrust vector:

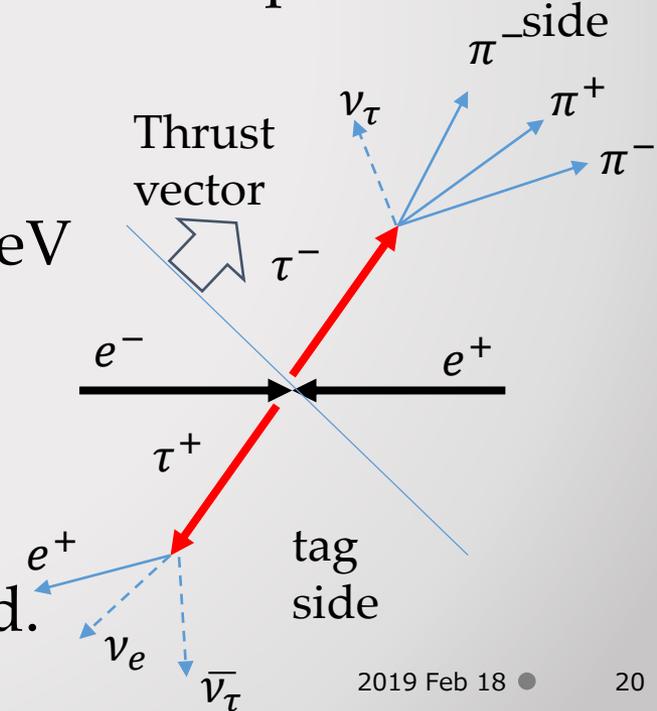
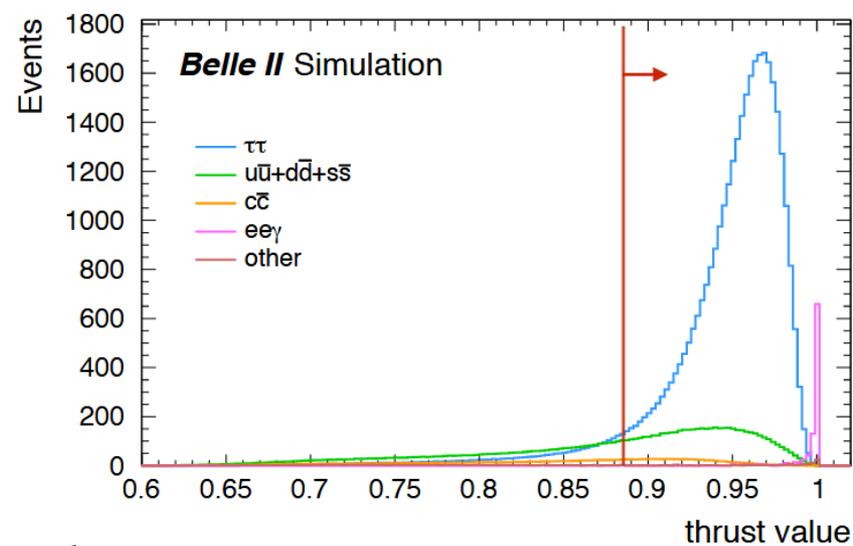
$$V_{th} = \sum_i^{all\ particle} \frac{|\vec{n}_{th} \cdot \vec{p}_i|}{|\vec{p}_i|}$$

Thrust vector (\vec{n}_{th}) maximizes thrust value (V_{th}).

- To reject electron, for signal side, $E/P_{lab} < 0.8$ is required.
- $V_{th} > 0.87$
- Visible Energy in CMS < 9.7 GeV
- Energy for signal side in CMS < 5.29 GeV
- Energy for tag side in CMS < 5.22 GeV

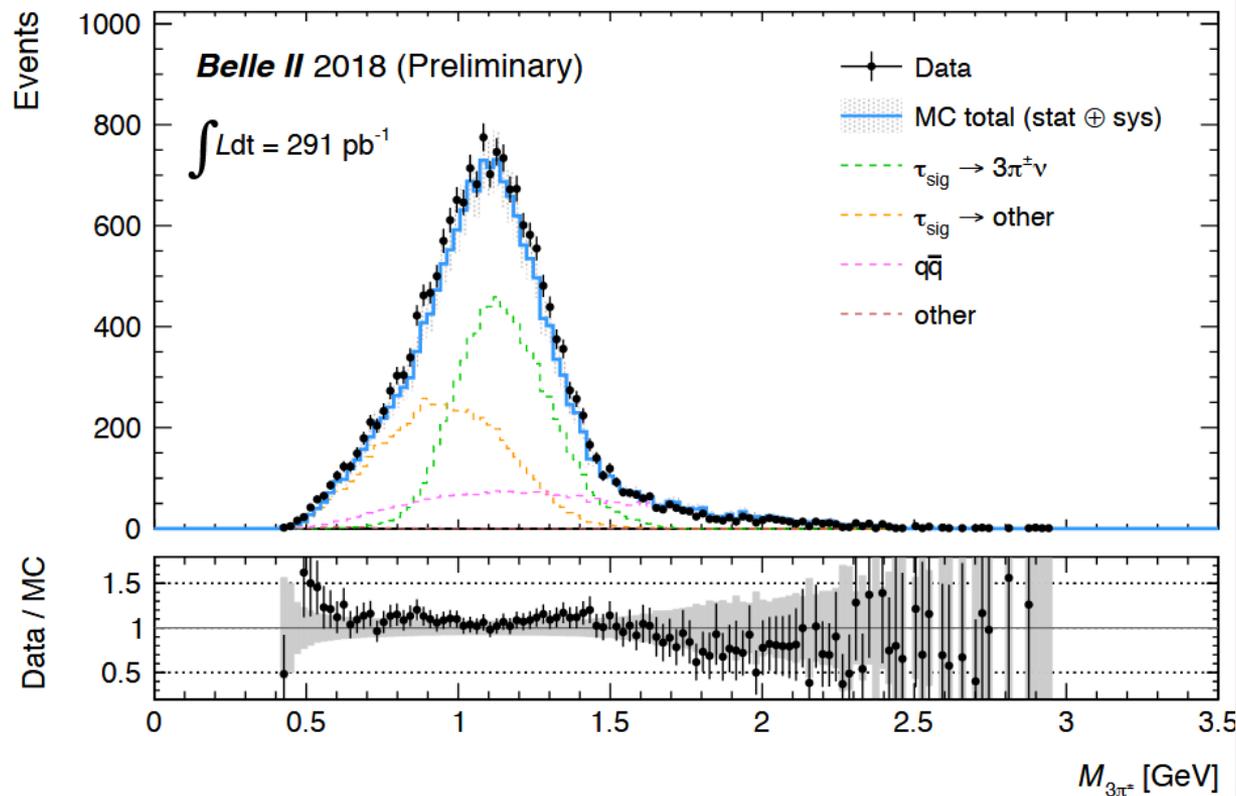
For signal side, at most 1 γ is allowed to accept ISR or FSR photon.

For tag side, any number of γ are allowed.



3π mass distribution in $\tau \rightarrow 3\pi\nu$

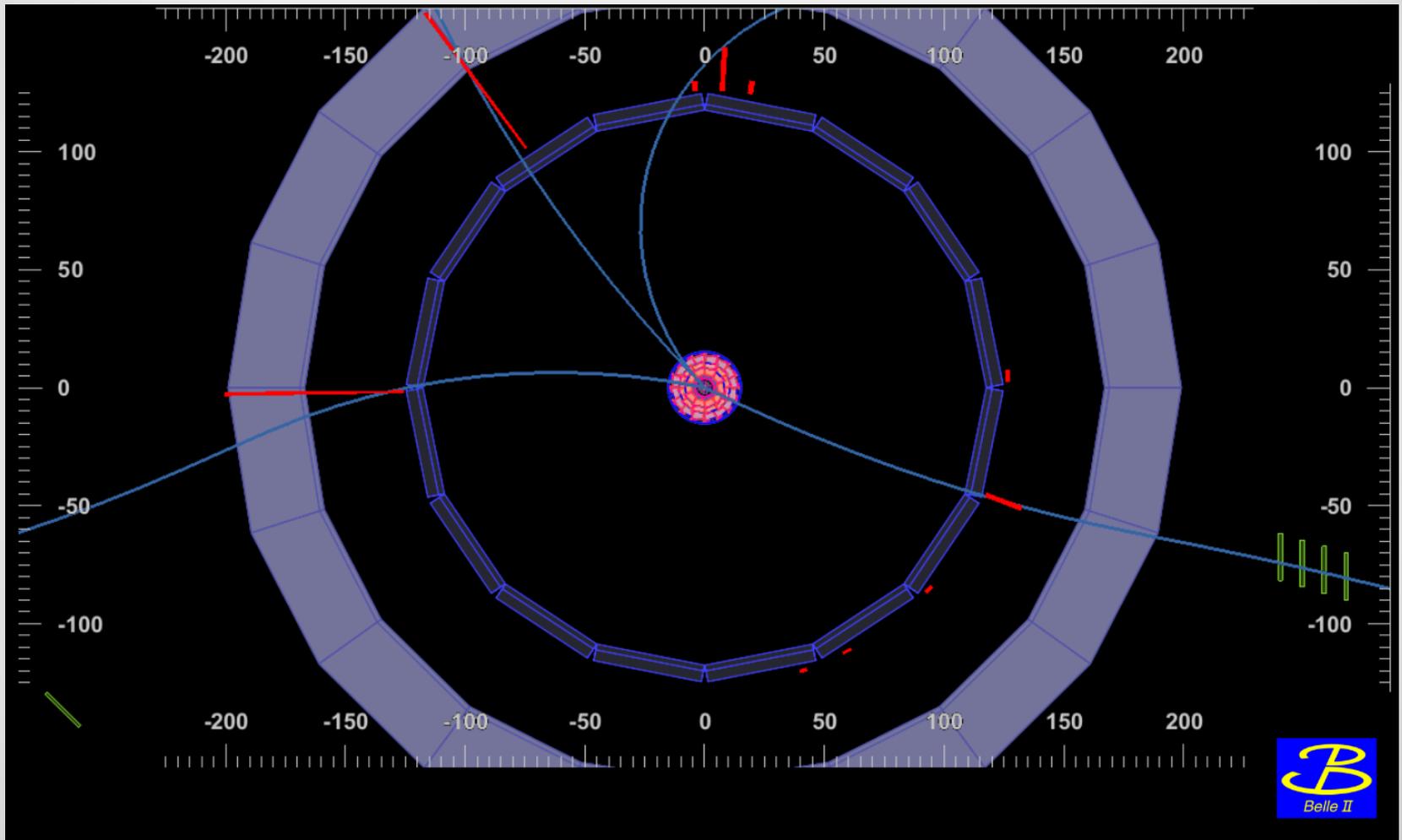
- After the selection, we can obtain:



$M_{3\pi}$ distribution @ 291 pb^{-1}

Good agreement between data and MC is found. Simulation works well. Data is well-understood.

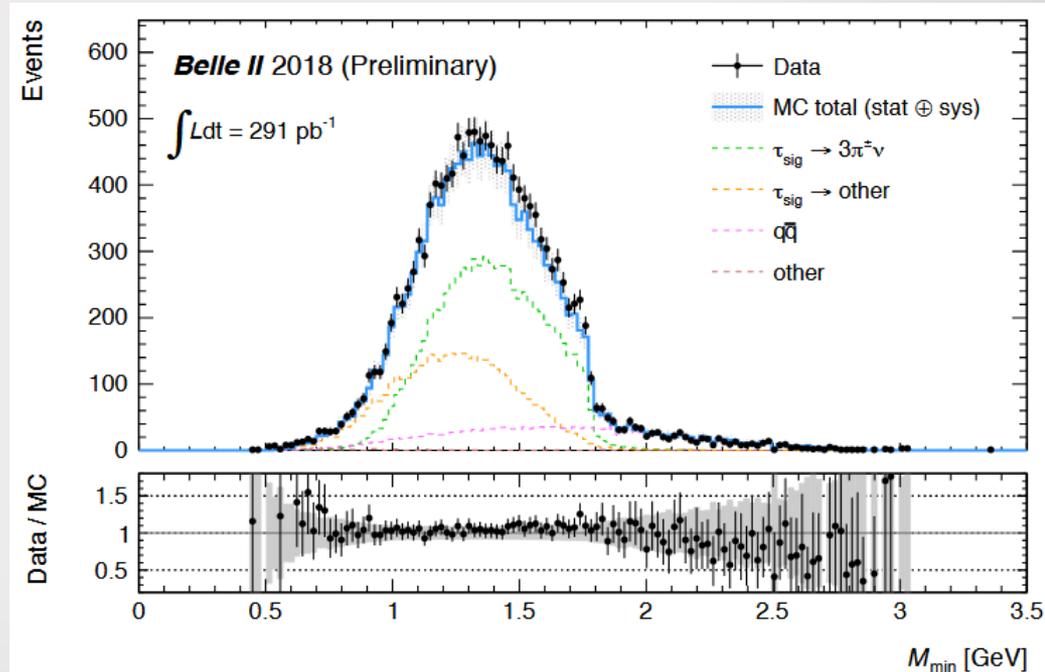
Event display of typical event candidate



τ mass measurement (1)

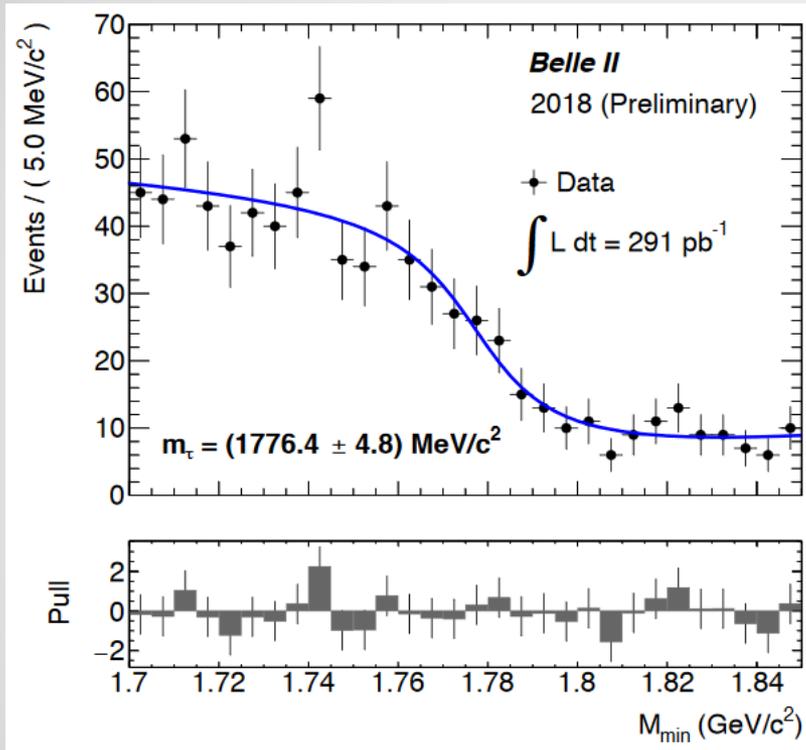
- Since it is difficult to reconstruct τ fully in SM decay, it cannot be seen as a peak at the τ mass, i.e., apparent existence of τ .
- On the other hand, in the special distribution, called pseudo mass, the distribution has some drop, that indicates τ mass.

$$\text{Pseudo mass} = \sqrt{M_{3\pi}^2 + 2(E_{beam} - E_{3\pi})(E_{3\pi} - P_{3\pi})}$$



τ mass measurement (2)

- Zoom of the previous plot

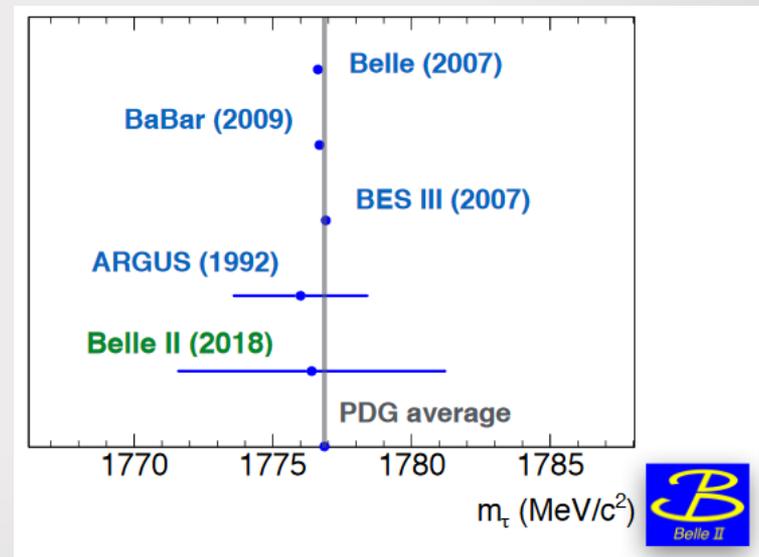


Fit by empirical PDF:

$$(p_3 + p_4 M) \tan^{-1} \left[\frac{(M - p_1)}{p_2} \right] + p_5 M + 1$$

p_1, p_2, \dots, p_5 are fit parameters and p_1 shows the evaluated τ mass.

The result is: $(1.776.4 \pm 4.8) \text{ GeV}/c^2$
(only statistical error is given.)



τ LFV search

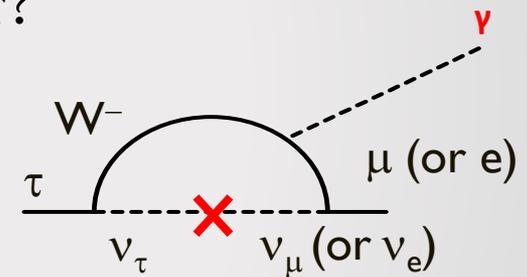
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Charged Lepton Flavor Violation

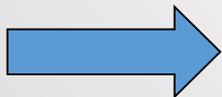
- In the neutrino sector, lepton flavor has not been conserved.
 - LF is not exact symmetry.
 - How about the charged lepton sector?

- SM + ν oscillation

$$Br(\tau \rightarrow \ell \gamma)_{SM} \propto \left(\frac{\delta m_\nu^2}{m_W^2} \right)^2 < 10^{-54}$$



Not reachable in the current experiments

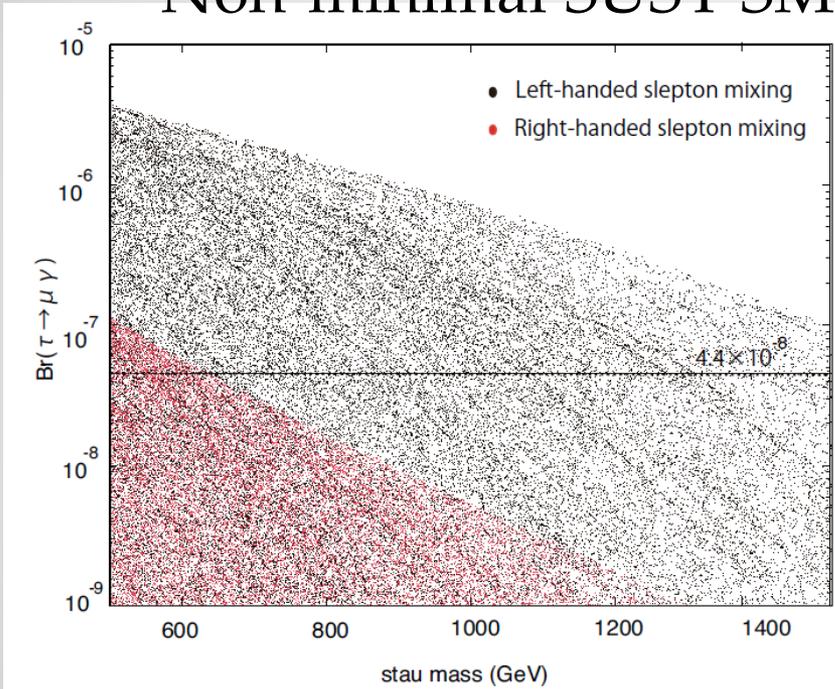


Observation of the LFV decay indicates the existence of New physics.

Theoretical prediction for $\tau \rightarrow \mu \gamma$

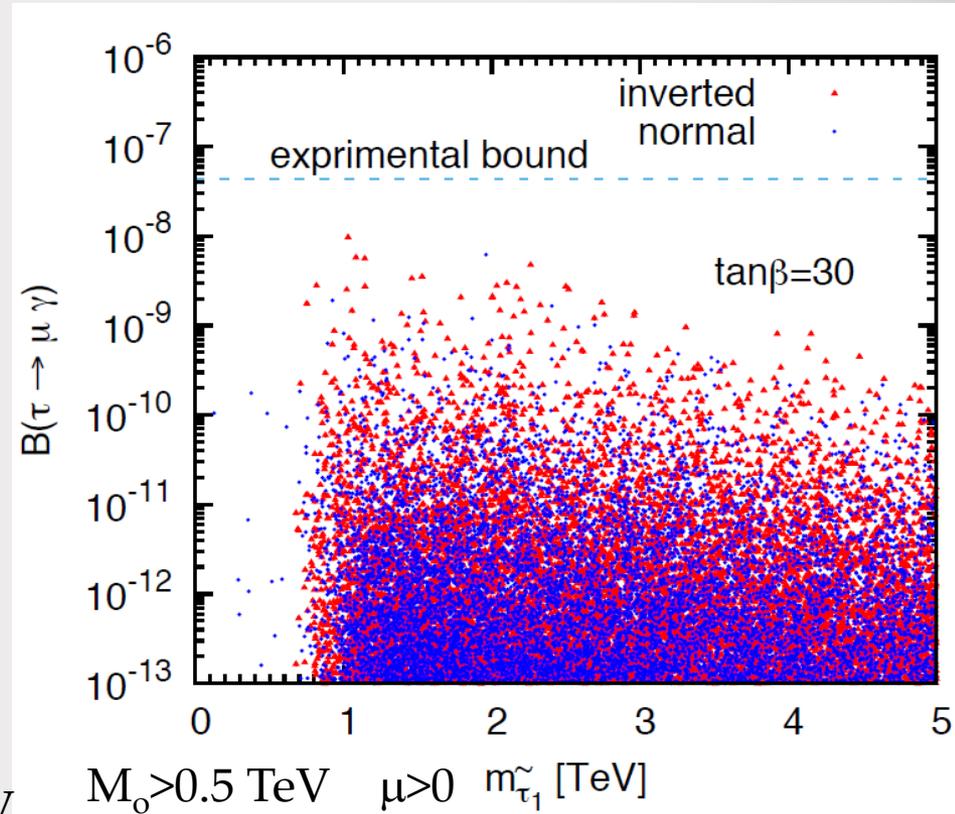
When the recent experimental results are considered,
MSSM cannot make $\tau \rightarrow \mu \gamma$.

Non-minimal SUSY SM



$M_{\text{bino}} = 250 \text{ GeV}$ $\tan\beta = 30$
 $M_{\text{wino}} = 500 \text{ GeV}$ LH slepton mix = 0.5~2 TeV
 $M_{\text{higgsino}} = 1 \text{ TeV}$ RH slepton mix = 5 TeV

CMSSM



$M_0 > 0.5 \text{ TeV}$ $\mu > 0$ $m_{\tilde{\tau}_1} [\text{TeV}]$
 $M_{1/2} < 10 \text{ TeV}$ $|A_0| < 3$

The Belle II Physics Book
 arXiv:1808.10567

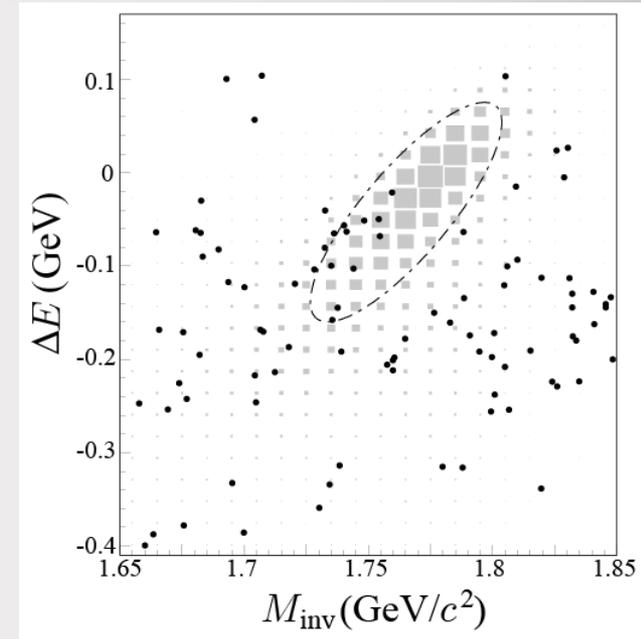
● These models predict $\tau \rightarrow \mu \gamma$ with reachable BF by Belle II!

Belle result for $\tau \rightarrow \mu \gamma$

- Belle result with 550 fb^{-1}
 - Signal detection efficiency: 6.1%
 - 10 events are found in signal ellipse.
 - $\text{BF} < 4.5 \times 10^{-8}$ @90%CL
 - Main BG

$\tau \rightarrow \mu \nu \nu + \text{extra } \gamma$

It is impossible to be distinguished from
the signal by PID.



■ : Signal MC dense
▪ : data

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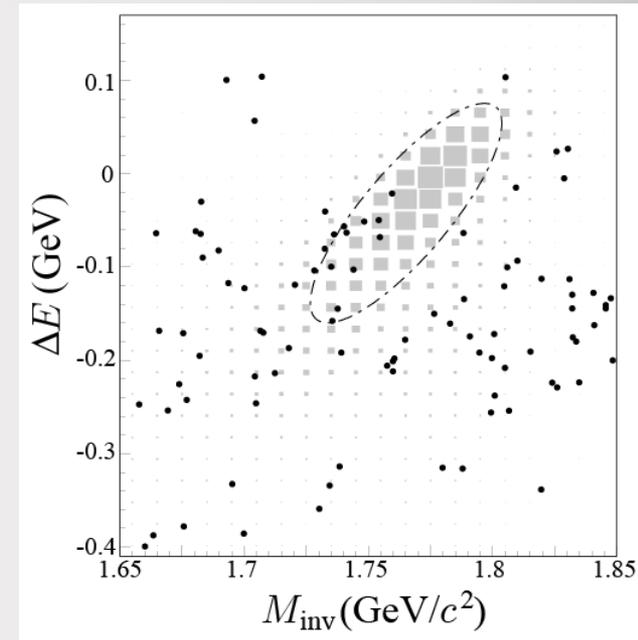
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Source of extra γ

ISR γ : 90%

Beam BG: 10%

(Beam BG means the fake γ induced by the beam particle which did not join the collision.)



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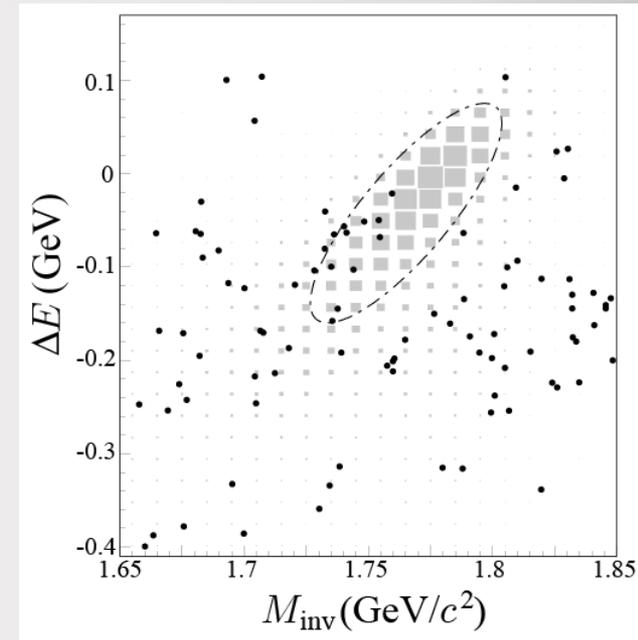
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On Belle II, beam BG will be large due to the instant luminosity increase.

→Need to develop the way to reduce fake γ in the analysis.

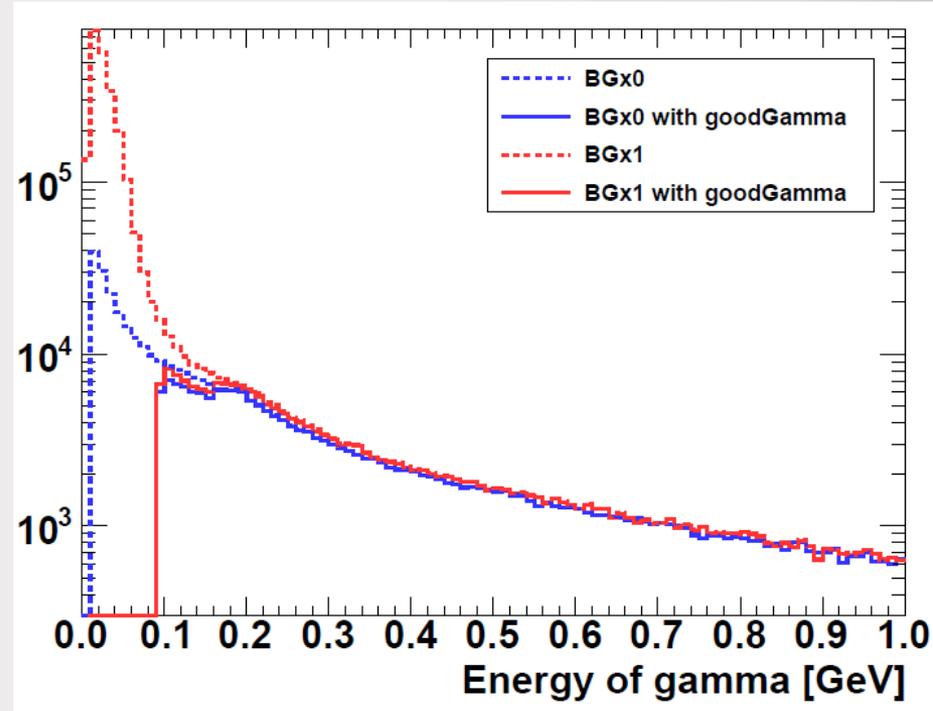
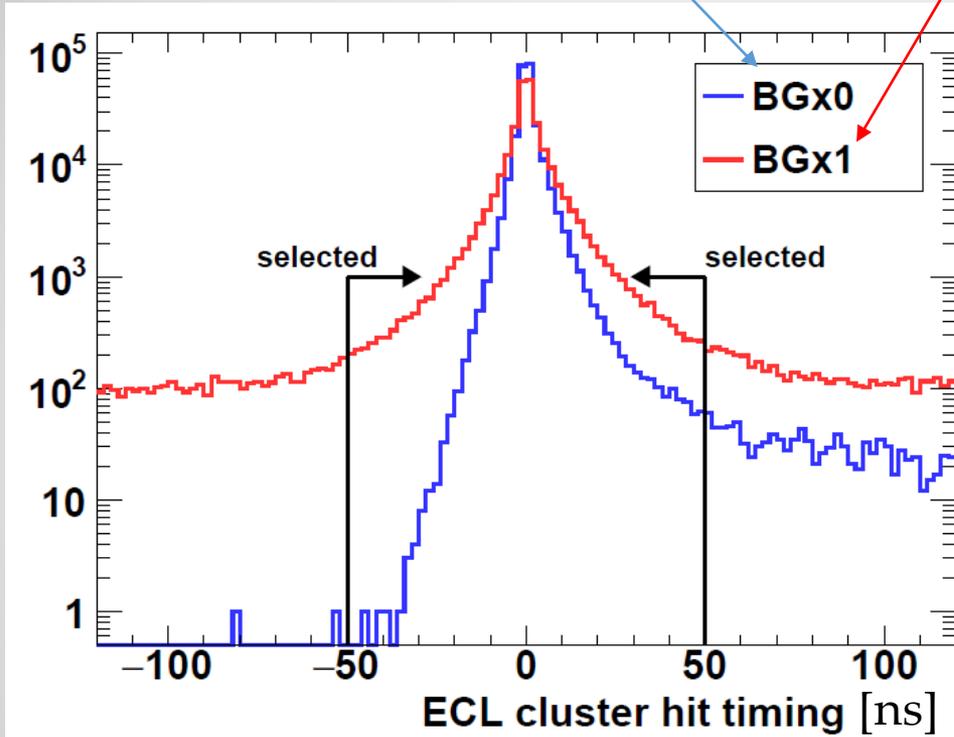


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Beam BG reduction

MC not included beam BG

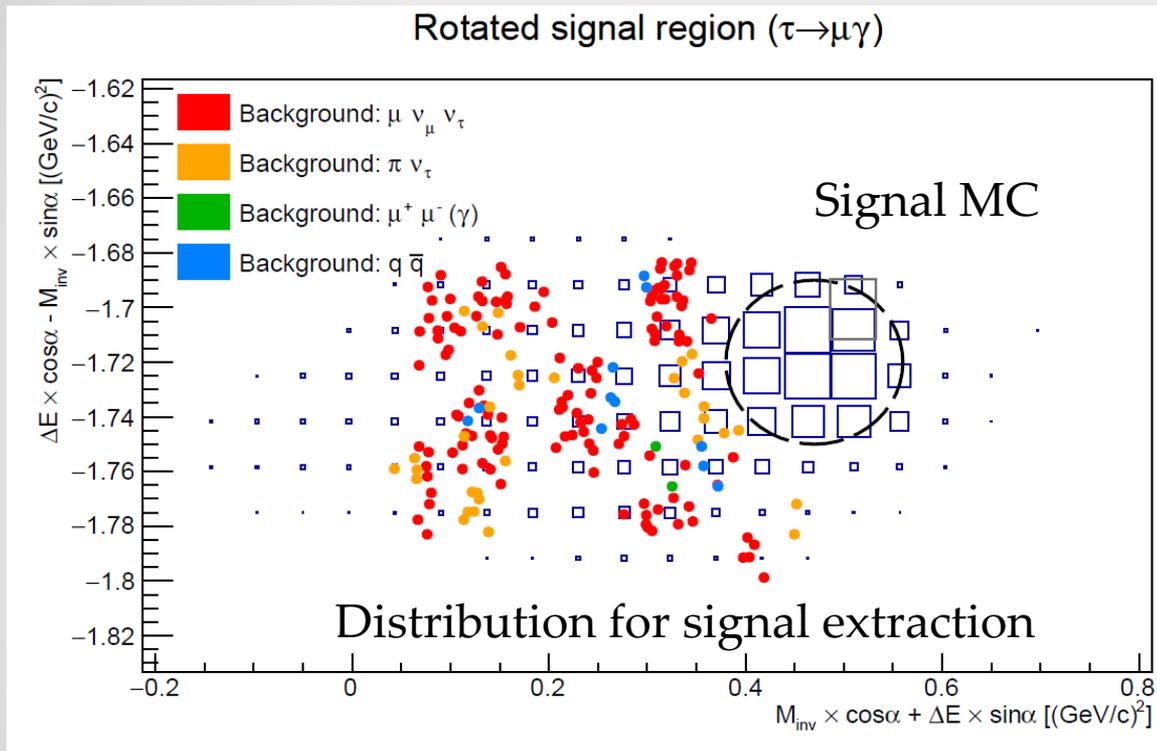
MC included beam BG



MC study tells us timing information and rejection of the low energy γ candidate reduce beam BG mostly while the signal detection efficiency is lost around 16% relatively in $\tau \rightarrow \mu \gamma$ analysis.

ISR γ reduction

- MC BG study for $\tau \rightarrow \mu \gamma$ using 1 ab^{-1}



By introducing event shape variable called a Fox-Wolfram moment into the selection criteria, it turns out that a high-purity signal region can be defined.

→ Need to confirm this with larger MC sample.

τ CPV search

...

τ CPV Search

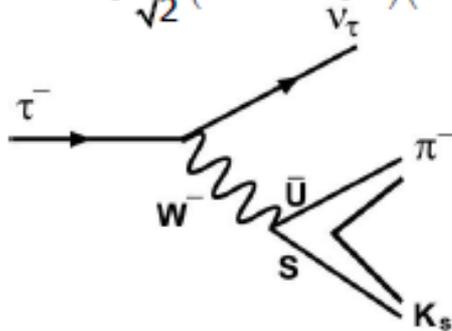
- CPV in lepton sector has not been seen yet.
 - Some model predicts that CPV appears in the decay angle difference between τ^+ and τ^- .
 - This will be induced by charged Higgs-like particle. So, CPV is expected to appear $|\Delta s|=1$ process rather than $|\Delta s|=0$.
 - $\tau \rightarrow K\pi\nu, \tau \rightarrow K\pi\pi\nu$

CPV search in $\tau \rightarrow \pi K_S^0 \nu$

-Effective Hamiltonian

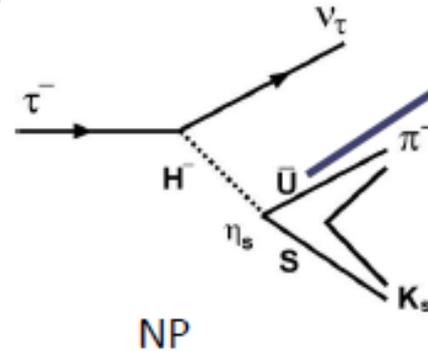
SM

$$H_{SM} = \sin \theta_c \frac{G}{\sqrt{2}} (\bar{\nu} \gamma^\mu (1 - \gamma_5) \tau) (\bar{s} \gamma_\mu (1 - \gamma_5) u)$$



Scalar Boson

$$H_{NP} = \sin \theta_c \frac{G}{\sqrt{2}} (\bar{\nu} (1 + \gamma_5) \tau) (\bar{s} (\eta_s + \eta_p \gamma_5) u)$$



Complex coupling constant

$$J_\mu^{K\pi} = \langle K(p_1) \pi(p_2) | \bar{s} \gamma_\mu u | 0 \rangle$$

$$= (p_1 - p_2)^\nu T_{\nu\mu} F(Q^2) + Q_\mu F_s(Q^2)$$

$$T_{\mu\nu} = g_{\mu\nu} - \frac{Q_\mu Q_\nu}{Q^2}$$

Form factor : F (Vector)
 F_s (Scalar)

$$F_s(Q^2) \rightarrow F_s(Q^2) = F_s(Q^2) + \frac{\eta_s}{m_\tau} F_H(Q^2)$$

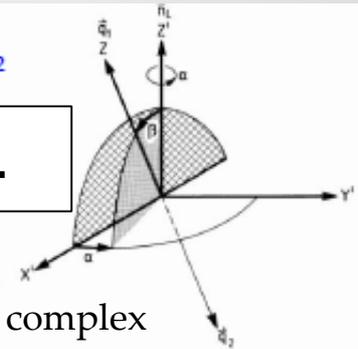
$$F_H(Q^2) \equiv \langle K(p_1) \pi(p_2) | \bar{s} u | 0 \rangle$$

Differential decay width and CPV

$$\frac{d\Gamma(\tau^-)}{dQ^2 d\cos\theta d\cos\beta} = [A(Q^2) - B(Q^2)(3\cos^2\Psi - 1)(3\cos^2\beta - 1)] \cdot |F|^2 + m_\tau^2 |F_s|^2$$

$$- C(Q^2) \cos\beta \cos\psi \cdot \text{Re}(FF_s^*(\eta_s))$$

CPV appears here.



η should be complex

$Q^2 = M_{K\pi}^2$, $A(Q^2), B(Q^2), C(Q^2)$: known function.

β : direction of K_s in $K_s\pi$ rest frame

Ψ : direction of τ in the $K_s\pi$ rest frame.

(θ : direction of $K_s\pi$ system in the τ rest frame. Correlated with Ψ)

$$A_i^{\text{cp}} = \frac{\iiint_{Q_{1,i}^2}^{Q_{2,i}^2} \cos\beta \cos\psi \left(\frac{d\Gamma_{\tau^-}}{d\omega} - \frac{d\Gamma_{\tau^+}}{d\omega} \right) d\omega}{\frac{1}{2} \iiint_{Q_{1,i}^2}^{Q_{2,i}^2} \left(\frac{d\Gamma_{\tau^-}}{d\omega} + \frac{d\Gamma_{\tau^+}}{d\omega} \right) d\omega}$$

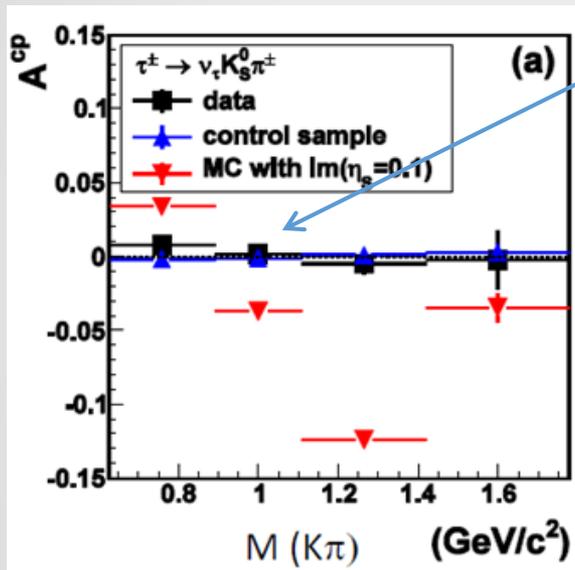
$$\simeq \langle \cos\beta \cos\psi \rangle_{\tau^-}^i - \langle \cos\beta \cos\psi \rangle_{\tau^+}^i$$

experimental observable

with $d\omega = dQ^2 d\cos\theta d\cos\beta$.

Belle result and prospect for Belle II

data : 700 fb⁻¹



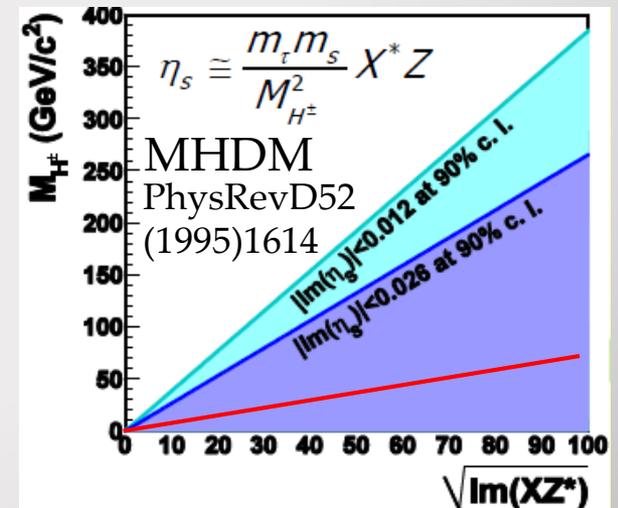
$$A_{cp} = (1.8 \pm 2.1(stat) \pm 1.4(sys)) \times 10^{-3}$$

$|\text{Im}(\eta_s)| < (0.012-0.026)$ at 90 %C.L.

To correct detector and selection-biased asymmetry control sample of $\tau \rightarrow \pi\pi\pi\nu$ is used since the final state is similar to $K_S^0\pi\nu$.

Statistics of control sample dominates the systematics of this analysis.

So, with 50 ab⁻¹, 10 x more sensitive result can be expected.



Black : data

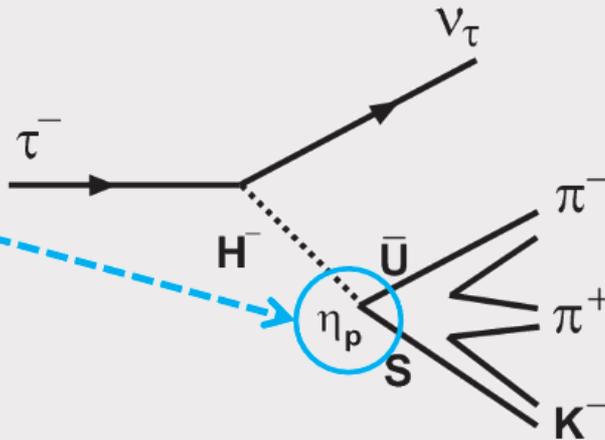
Blue : data in sideband region (CS)

Red : MC having CPV
with the 10x larger CPV
than that of UL evaluated by CLEO

CPV in $\tau \rightarrow K\pi\pi\nu$ (1)

Very similar to $\tau \rightarrow K_S^0 \pi \nu$ analysis, not scalar but pseudo-scalar will induce to CPV.

$$F_4 \longrightarrow \tilde{F}_4 = F_4 + \frac{f_H}{m_\tau} \eta_p$$



$$\begin{aligned} J^\mu &\equiv \langle K^-(p_1)\pi^-(p_2)\pi^+(p_3) | \bar{s}\gamma^\mu(1-\gamma^5)u | 0 \rangle \\ &= [F_1(s_1, s_2, Q^2)(p_1 - p_3)_\nu + F_2(s_1, s_2, Q^2)(p_2 - p_3)_\nu] T^{\mu\nu} \\ &\quad + iF_3(s_1, s_2, Q^2)\epsilon^{\mu\nu\rho\sigma} p_{1\nu}p_{2\rho}p_{3\sigma} + \tilde{F}_4(s_1, s_2, Q^2)Q^\mu \end{aligned}$$

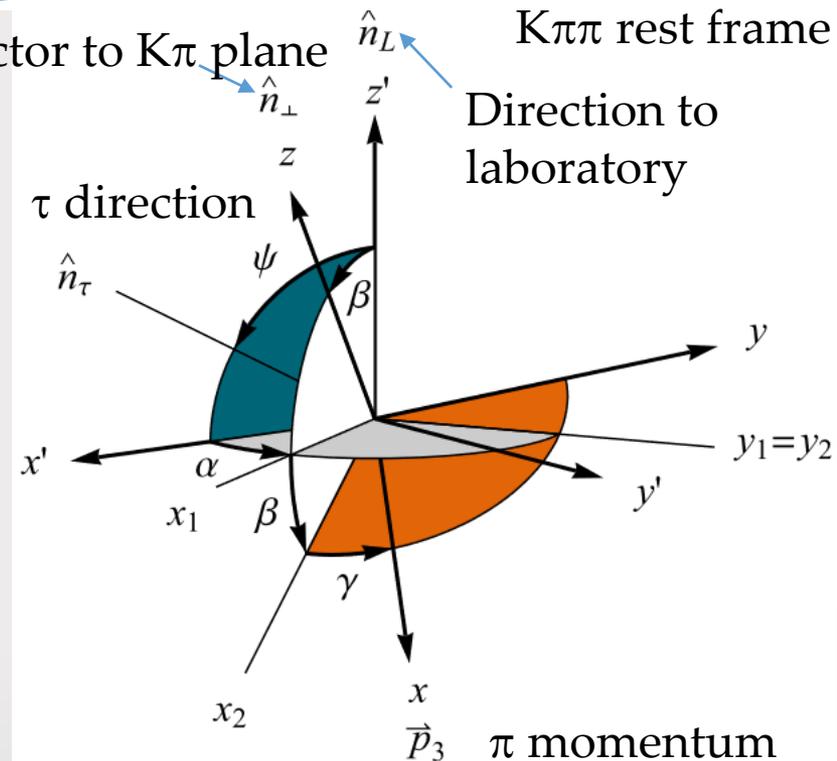
Belle, BaBar have not searched for it.

CPV in $\tau \rightarrow K\pi\pi\nu$ (2)

Differential decay width is written down:

$$\begin{aligned} \frac{d\Gamma}{dQ^2 ds_1 ds_2 d\gamma d\cos\beta d\cos\theta} = & \frac{G_F^2 \sin^2\theta_c (m_\tau^2 - Q^2)^2}{512(2\pi)^6 m_\tau^3 Q^2} \left\{ \left[\frac{2}{3}K_1 + K_2 + \frac{1}{3}\bar{K}_1(3\cos^2\beta - 1)/2 \right] (|B_1|^2 + |B_2|^2) \right. \\ & + \left[\frac{2}{3}K_1 + K_2 - \frac{2}{3}\bar{K}_1(3\cos^2\beta - 1)/2 \right] |B_3|^2 + K_2|B_4|^2 - \frac{1}{2}\bar{K}_1\sin^2\beta\cos 2\gamma (|B_1|^2 - |B_2|^2) \\ & + \bar{K}_1\sin^2\beta\sin 2\gamma \operatorname{Re}(B_1B_2^*) + 2\bar{K}_3 \sin\beta\sin\gamma \operatorname{Re}(B_1B_3^*) + 2\bar{K}_2 \sin\beta\cos\gamma \operatorname{Re}(B_1B_4^*) \\ & + 2\bar{K}_3 \sin\beta\cos\gamma \operatorname{Re}(B_2B_3^*) - 2\bar{K}_2 \sin\beta\sin\gamma \operatorname{Re}(B_2B_4^*) + 2\bar{K}_3 \cos\beta \operatorname{Im}(B_1B_2^*) \\ & \left. + \bar{K}_1\sin 2\beta\cos\gamma \operatorname{Im}(B_1B_3^*) - \bar{K}_1\sin 2\beta\sin\gamma \operatorname{Im}(B_2B_3^*) + 2\bar{K}_2 \cos\beta \operatorname{Im}(B_3B_4^*) \right\}, \quad (25) \end{aligned}$$

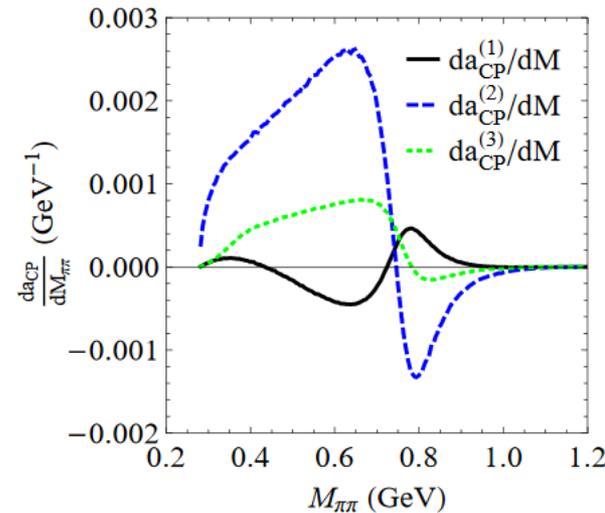
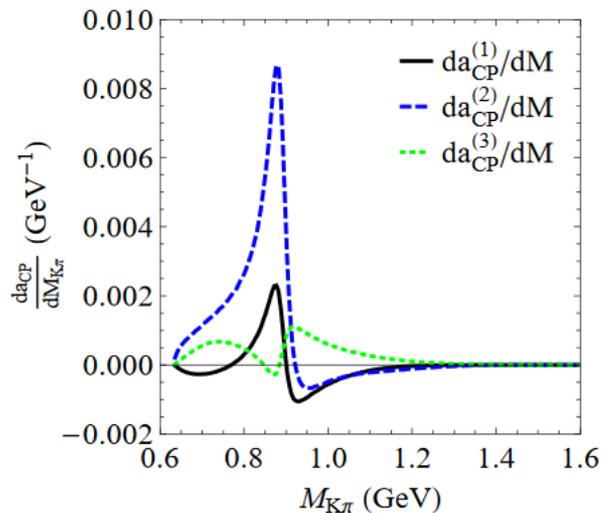
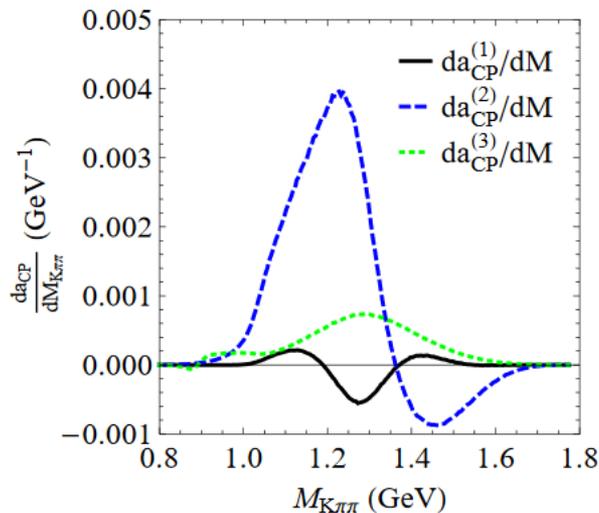
Via these terms, CPV appears. Similarly to the analysis of $\tau \rightarrow \pi K_S^0 \nu$, the differences of the decay angle between τ^+ and τ^- are evaluated, i.e., $\sin\beta\sin\gamma$, $\sin\beta\cos\gamma$ and $\cos\beta$.



CPV in $\tau \rightarrow K\pi\pi\nu$ (3)

- In $\tau \rightarrow K_S\pi\nu$, A_{CP} is evaluated bin by bin of $M(K_S\pi)$.
 \rightarrow 3 body-decay, evaluated of $M(K\pi\pi)$, $M(K\pi)$, $M(\pi\pi)$
 Since dA_{CP}/dM takes both negative and positive values,
 da_{CP}/dM is more sensitive to CP asymmetry.

$A_{CP}^{(i)} = a_{CP}^{(i)} f_H \text{Im}(\eta_P)$, $a_{CP}^{(i)}$ distributions independent from form factor and coupling



$i: 1=\sin\beta\sin\gamma, 2=\sin\beta\cos\gamma, 3=\cos\beta$

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Difficulty of $\tau \rightarrow K\pi\pi\nu$ analysis

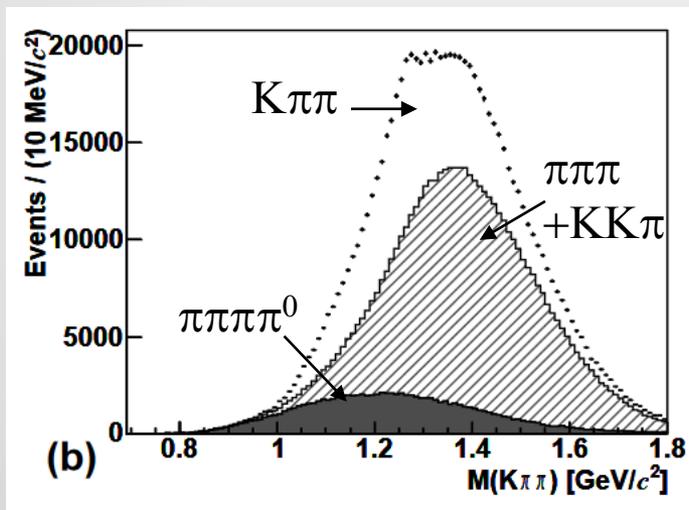
- In $\tau \rightarrow K\pi\pi\nu$ analysis, large BGs appear.

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In Belle analysis, $\pi\pi\pi$ BG is 2x-3x more than signals.

In Belle II, since PID devices are improved, less BGs are expected.

(But, almost same amount of BGs is estimated.)

Summary

- Belle II is a great place to study tau physics.
- Recently, with early data, tau mass is evaluated.
- Near future,
 - Tau LFV will be searched for with 10-50x more sensitivity.
 - Tau CPV will be searched for with 10x more sensitivity.