

Υ and ψ decays as probes of solutions to the $R(D^{(*)})$ puzzle

Daniel Aloni

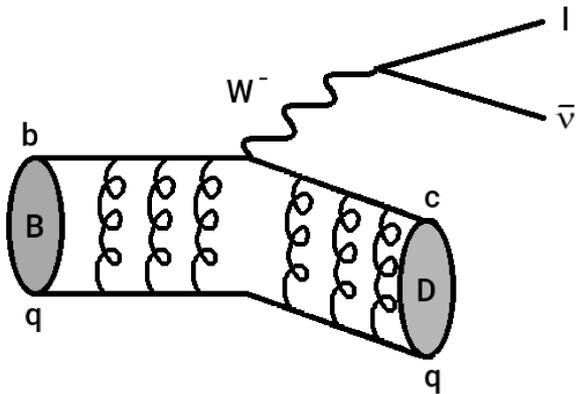
Mini-workshop on $D^{(*)}\tau$ and related topics, Nagoya University

In collaboration with

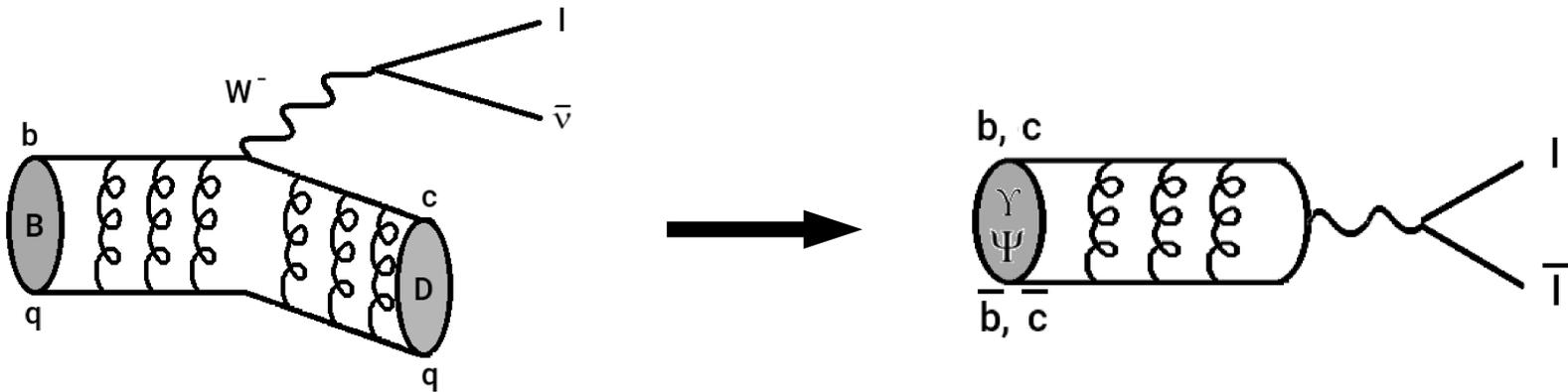
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Υ and ψ decays as probes of solutions to the $R(D^{(*)})$ puzzle



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Outline

- Introduction – The $R(D^{(*)})$ puzzle
- The EFT and emergence of neutral currents
- Vector meson decays
- Implications of EFT on LFU violation in Υ and ψ decays
- Future prospects
- Summary

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The effective field theory

EFT – complete basis

- Demand $G_{SM} = SU(3)_C \times SU(2)_L \times U(1)_Y$ invariance
- Assume no RH neutrinos, *i.e.* $B \rightarrow D\tau\bar{\nu}_L$
- A complete set for $b \rightarrow c\tau\bar{\nu}$ transitions contains only four operators
 - › $(\bar{e}L)(\bar{u}Q)$
 - › $(\bar{e}\sigma^{\mu\nu}L)(\bar{u}\sigma_{\mu\nu}Q)$
 - › $(\bar{L}\gamma^\mu\tau_aL)(\bar{Q}\gamma^\mu\tau_aQ)$
 - › $(\bar{Q}d)(\bar{e}L)$

EFT – unavoidable NC

- All four operators contain also neutral currents (NC)

→ For instance

$$(\bar{e}L)(\bar{u}Q) = \overbrace{(\bar{e}_R\nu_L)(\bar{u}_Rd_L)}^{CC} - \overbrace{(\bar{e}_Re_L)(\bar{u}_Ru_L)}^{NC}$$

- We looked for observables sensitive to those NC

- Neutral currents unavoidably modify $b\bar{b}, c\bar{c} \rightarrow \tau\bar{\tau}$

EFT – NC observables

- *D. A. Faroughy, A. Greljo, J. F. Kamenik* * – High P_T distribution of $\tau\bar{\tau}$ signature at the LHC (tomorrow)

- We looked on lepton non universality of Υ and ψ decays

$$R_{\tau/\ell}^V \equiv \frac{\Gamma(V \rightarrow \tau^+ \tau^-)}{\Gamma(V \rightarrow \ell^+ \ell^-)}, \quad (V = \Upsilon, \psi(2s); \ell = e, \mu)$$

- Wilson coefficients are evaluated at the same scale

* *D. A. Fraoughy, A. Greljo, J. F. Kamenik, Phys. Lett. B764 (2017) 126-134*

Vector meson decay

Vector meson decay - SM

- Within the SM

$$R_{\tau/\ell}^V \simeq (1 + 2x_\tau^2)(1 - 4x_\tau^2)^{1/2}$$

where $x_\tau = m_\tau/m_V$.

- Dominantly QED – 1 photon exchange
- For $\ell = e, \mu$ we take $x_\ell = 0$

Vector meson decay – SM corrections

- Within the SM

$$R_{\tau/\ell}^V \simeq (1 + 2x_\tau^2)(1 - 4x_\tau^2)^{1/2}$$

where $x_\tau = m_\tau/m_V$.

- Leading corrections:

- Corrections due to m_μ are $\delta R_{\tau/\ell}^V \lesssim \mathcal{O}(10^{-7})$
- Corrections due to Z exchange are $\delta R_{\tau/\ell}^V \lesssim \mathcal{O}(10^{-5})$
- QED at 1-loop $\delta R_{\tau/\ell}^V \simeq 6 \cdot 10^{-3} x_\tau^2 \sim \mathcal{O}(10^{-4})$ (inclusive)

$R_{\tau/\ell}^V$ - Prediction vs. measurement

$V(nS)$	SM prediction	Exp. value $\pm \sigma_{\text{stat}} \pm \sigma_{\text{syst}}$
$\Upsilon(1S)$	$0.9924 \pm \mathcal{O}(10^{-5})$	$1.005 \pm 0.013 \pm 0.022$
$\Upsilon(2S)$	$0.9940 \pm \mathcal{O}(10^{-5})$	$1.04 \pm 0.04 \pm 0.05$
$\Upsilon(3S)$	$0.9948 \pm \mathcal{O}(10^{-5})$	$1.05 \pm 0.08 \pm 0.05$
$\psi(2S)$	$0.390 \pm \mathcal{O}(10^{-4})$	0.39 ± 0.05

Vector meson decay – dim(6) operators

- Nine independent dim.(6) operators contribute to leptonic meson decays

$$\begin{aligned} \mathcal{L}_{lq} = & C_{VRR}^{q\ell} (\bar{e}_R \gamma^\mu e_R) (\bar{q}_R \gamma_\mu q_R) + C_{VRL}^{q\ell} (\bar{e}_R \gamma^\mu e_R) (\bar{q}_L \gamma_\mu q_L) \\ & + C_{VLR}^{q\ell} (\bar{e}_L \gamma^\mu e_L) (\bar{q}_R \gamma_\mu q_R) + C_{VLL}^{q\ell} (\bar{e}_L \gamma^\mu e_L) (\bar{q}_L \gamma_\mu q_L) \\ & + C_T^{q\ell} (\bar{e}_L \sigma^{\mu\nu} e_R) (\bar{q} \sigma_{\mu\nu} q) + \text{h.c.} \quad (+\text{scalar operators}) \end{aligned}$$

- A straightforward calculation relates the 9 Wilson coefficient $C_A^{q\ell}$ to 4 form factors appearing in the ratio

$$\begin{aligned} R_{\tau/\ell}^V \simeq & \frac{\sqrt{1-4x_\tau^2}}{(4\pi\alpha Q_q)^2} \left[|\tilde{A}_V^{q\tau}|^2 (1+2x_\tau^2) + |\tilde{B}_V^{q\tau}|^2 (1-4x_\tau^2) + \frac{|\tilde{C}_V^{q\tau}|^2}{2} (1-4x_\tau^2)^2 \right. \\ & \left. + \frac{|\tilde{D}_V^{q\tau}|^2}{2} (1-4x_\tau^2) + 2\text{Re} \left[\tilde{A}_V^{q\tau} \tilde{C}_V^{*q\tau} \right] x_\tau (1-4x_\tau^2) \right] \end{aligned}$$

Connecting charge currents to neutral currents

The need for assumptions

- There are four independent CC operators
- There are nine independent NC operators
- CC + Gauge invariance \longrightarrow NC
 - Not enough measurements to fix the values of the Wilson coefficients of the four CC operators *
 - No information on the other five NC operators

* *D. Bardhan, P. Byakti, D. Ghosh, **JHEP 1701**, 125 (2017)*

EFT from simplified models

- Recall that
 - Within the SM $b \rightarrow c\tau\bar{\nu}$ is a tree-level process
 - Central value is $\sim 30\%$ enhanced compared to prediction
- Huge enhancement of tree-level suggests new bosons which also modify $b \rightarrow c\tau\bar{\nu}$ at tree-level
- There are eight different possible mediators
 $W'_\mu \sim (1, 3)_0, U_\mu \sim (3, 1)_{2/3}, X_\mu \sim (3, 3)_{2/3}, S \sim (3, 1)_{-1/3},$
 $T \sim (3, 3)_{-1/3}, \phi \sim (1, 2)_{1,2}, D \sim (3, 2)_{7/6}, V_\mu \sim (3, 2)_{-5/6}$

EFT – fixing all NC

- Motivated by FCNC and LHC constraints
 - We impose $U(2)_Q$ symmetry of the light left-handed quarks
 - We assume flavor alignment to the down mass basis
- Choosing a simplified model
 - Fixes the 4 CC Wilson coefficients (up to overall normalization)
 - Fixes the 4 corresponding NC, as well as the 5 other NC. For instance a mediator which generates $(\bar{u}L)(\bar{e}Q)$ will also generate $(\bar{u}L)(\bar{L}u)$, $(\bar{e}Q)(\bar{Q}e)$

Numerical results

Numerical results – analysis

- Complete list of simplified models -

$$W'_\mu \sim (1, 3)_0, U_\mu \sim (3, 1)_{2/3}, X_\mu \sim (3, 3)_{2/3}, S \sim (3, 1)_{-1/3},$$

$$T \sim (3, 3)_{-1/3}, \phi \sim (1, 2)_{1,2}, D \sim (3, 2)_{7/6}, V_\mu \sim (3, 2)_{-5/6}$$

- Normalize the Wilson coefficients by Integrating out the heavy mediator
- Find best-fit values of new couplings to minimize the $R(D^{(*)})$ anomaly (χ^2)
- Calculate the *p-value* for each model
- Find the 95% C.L. interval of the new couplings
- Calculate $R_{\tau/\ell}^\Upsilon$ and $R_{\tau/\ell}^\psi$ within the allowed region

Numerical results – example $U_\mu \sim (3, 1)_{2/3}$

- UV

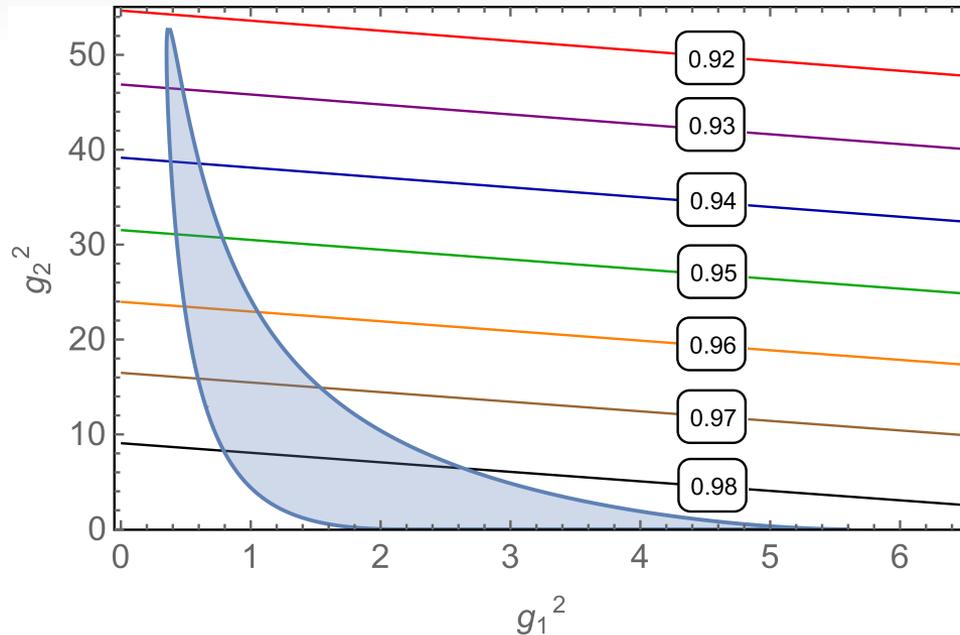
$$\mathcal{L}_U = g_1 \bar{Q}_3 \Psi L_3 + g_2 \bar{d}_3 \Psi e_3 + h.c.$$

- EFT

$$\begin{aligned} \mathcal{L}_U^{EFT} = & -\frac{|g_1|^2}{2M_U^2} \overbrace{(\bar{L}\gamma^\mu L)(\bar{Q}\gamma_\mu Q)}^{N.C.} - \frac{2|g_1|^2}{M_U^2} \overbrace{(\bar{L}\gamma^\mu \tau_a L)(\bar{Q}\gamma_\mu \tau_a Q)}^{N.C.+C.C.} \\ & - \frac{|g_2|^2}{M_U^2} \overbrace{(\bar{e}\gamma^\mu e)(\bar{d}\gamma_\mu d)}^{N.C.} + \left[\frac{g_1 g_2^*}{M_U^2} \overbrace{(\bar{Q}d)(\bar{e}L)}^{N.C.+C.C.} + h.c. \right] \end{aligned}$$

Numerical results – example $U_\mu \sim (3, 1)_{2/3}$

- Results: $(g_1^{2 \text{ bfp}}, g_2^{2 \text{ bfp}}) = (3.3, 0.4) \left(\frac{M_U}{\text{TeV}}\right)^2$, $p = 100\%$



$$R_{\tau/\ell}^{\Upsilon(1S)} = 0.922 - 0.990$$

$$R_{\tau/\ell}^{\Upsilon(2S)} = 0.915 - 0.991$$

$$R_{\tau/\ell}^{\Upsilon(3S)} = 0.911 - 0.992$$

- $R_{\tau/\ell}^{\psi(2S)}$ is not modified

Numerical results

UV field content	$R_{\tau/\ell}^{\Upsilon(1S)}$	$R_{\tau/\ell}^{\psi(2S)}$	Predicted modification to $R_{\tau/\ell}^{\Upsilon(1S)}$
$W'_\mu \sim (1, 3)_0$	0.989-0.991	0.390	Decrease by 0.2% – 0.4%
$U_\mu \sim (3, 1)_{+2/3}$	0.922-0.990	SM	Decrease by 0.3% – 7.1%
$S \sim (3, 1)_{-1/3}$	SM	0.389-0.390	–
$V_\mu \sim (3, 2)_{-5/6}$	0.975-0.985	SM	Decrease by 0.7% – 1.7%
SM	0.992	0.390	
Current measurement	1.005 ± 0.025	0.39 ± 0.05	
Achievable uncertainty (with current data)	± 0.01	± 0.02	
Projected uncertainty ($\mathcal{L}^{\Upsilon(3S)} = 1/\text{ab}$ in Belle II)	± 0.004	–	

- $R_{\tau\ell}^{\Upsilon(1S)}$ is starting to probe relevant models

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Future prospects

Future prospects - $\psi(2S)$

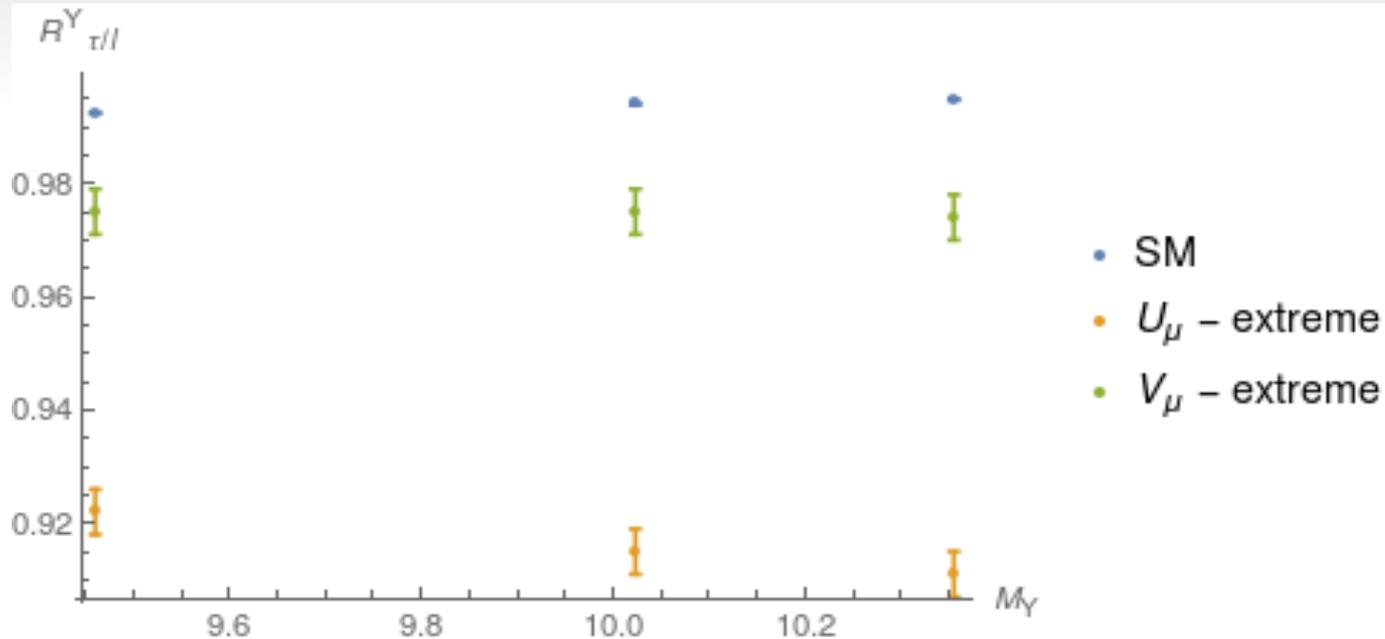
- Current error is $\sigma \sim 13\%$
- Bess II already has 10 times larger data sample than what was analyzed, giving $\sigma \sim 4\%$
- We predict that $R_{\tau/\ell}^{\psi}$ is modified by at most few per-mil
- Removing the imposed $U(2)_Q$ symmetry might lead to a much larger modification (work in progress)
- An order of magnitude improvement is needed to be achieved in Bess III

Future prospects - $\Upsilon(nS)$

- Current error is $\sim \sigma_{1S}^{BaBar} \sim 2\%$, $\sigma_{2S}^{CLEO} \sim 5\%$, $\sigma_{3S}^{CLEO} \sim 8\%$
- Babar and Belle have 16-20 times larger data samples than what was analyzed, giving $\sigma \sim 1\%$
- Running at $\Upsilon(3S)$ with $\mathcal{L} \sim 1/ab$ Belle II might reach $\sigma_{1S} \simeq 0.4\%$
- LFU in Υ decays provide additional motivation to study $\Upsilon(3S)$ at early physics program of Belle II (w/o full vertex detector)

Future prospects - $\Upsilon(nS)$

- We suggest a SM test:



$$R_{\tau/l}(m_{\Upsilon(nS)}) = \left[1 + 2x_{\tau,1S}^2 \left(\frac{m_{\Upsilon(1S)}}{m_{\Upsilon(nS)}} \right)^2 \right] \left[1 - 4x_{\tau,1S}^2 \left(\frac{m_{\Upsilon(1S)}}{m_{\Upsilon(nS)}} \right)^2 \right]^{1/2}$$

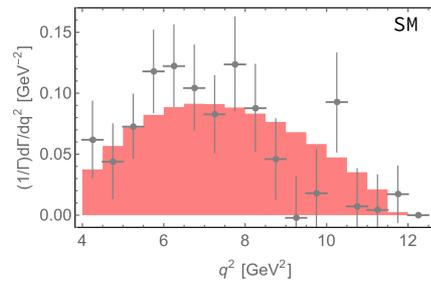
Summary

- $R(D^{(*)})$ is enhanced compared to the SM at 3.9σ
- Explaining this enhancement suggests new bosons which mediate the $b \rightarrow c\tau\nu$ transition at tree-level
- Such bosons can generate observable LFU violation in vector meson decay
- Current measurements of ψ decays do not have the required accuracy
- Current (not analyzed) data of $\Upsilon(1S)$ can already disfavor some of the parameter space
- Belle II can contribute significantly if operates below the $\Upsilon(4S)$ resonance

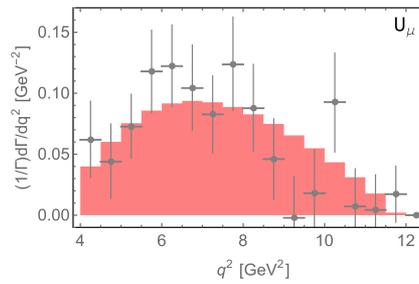
Thank you!

Backup

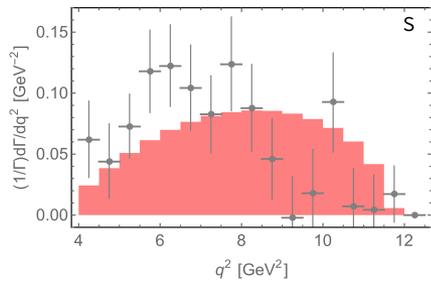
q^2 distributions



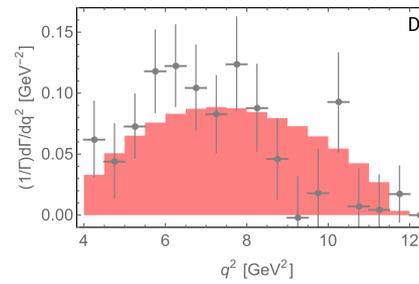
(a) SM



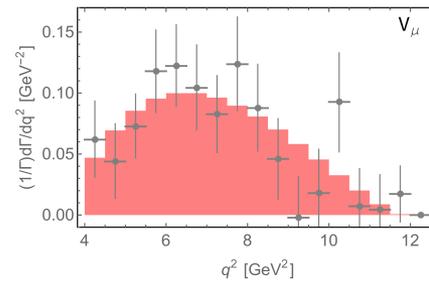
(b) U_μ



(c) S



(d) D



(e) V_μ

Corrections – Z exchange

$$\delta R_V^Z = \left(\frac{\epsilon}{\epsilon - 1} \right)^2 \left(\frac{g_V^q}{8Q_q c_W^2 s_W^2} \right)^2 \left(\frac{64x_\ell^2}{1 + 2x_\ell^2} \right)$$

Where $\epsilon = m_V^2/m_Z^2$ and $g_V^q = T_3^q - 2Q_q s_W^2$

Corrections – QED 1-loop

$$R_{\tau/\ell}^V = (1 - 4x_\tau^2)^{1/2} (1 + 2x_\tau^2) \cdot \left[1 + \frac{4\alpha x_\tau^2}{\pi} (2 - \log[4]) \right]$$

Vector meson decay – Dim(6) operators

Relation between Wilson coefficient and Form-factors:

$$A_V^{q\ell} = -4\pi\alpha Q_q + \frac{m_V^2}{4} \left[\left(C_{VLL}^{q\ell} + C_{VRR}^{q\ell} + C_{VLR}^{q\ell} + C_{VRL}^{q\ell} \right) + 16x_\ell \frac{f_V^T}{f_V} \text{Re} \left[C_T^{q\ell} \right] \right],$$

$$B_V^{q\ell} = \frac{m_V^2}{4} \left(C_{VRR}^{q\ell} + C_{VRL}^{q\ell} - C_{VLR}^{q\ell} - C_{VLL}^{q\ell} \right),$$

$$C_V^{q\ell} = 2m_V^2 \frac{f_V^T}{f_V} \text{Re} \left[C_T^{q\ell} \right],$$

$$D_V^{q\ell} = 2m_V^2 \frac{f_V^T}{f_V} \text{Im} \left[C_T^{q\ell} \right].$$

where

$$\langle 0 | \bar{q} \gamma^\mu | V(p) \rangle = f_V m_V \epsilon^\mu(p), \quad \langle 0 | \bar{q} \sigma^{\mu\nu} | V(p) \rangle = f_V^T [\epsilon^\mu(p) p^\nu - \epsilon^\nu(p) p^\mu]$$