

# **Spectroscopy of Heavy Quark Hadrons from QCD**

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# **Introduction: From QCD to Hadron Spectrum**

# From QCD to Hadron Spectrum

# QCD = quarks + gluons with color  $SU(3)_c$  gauge symmetry

$$\mathcal{L} = \bar{q}(i\not{D} - m_q)q - \frac{1}{2}\text{Tr}[G_{\mu\nu}G^{\mu\nu}]$$

**expected low energy modes**

**massless gluons**

**light quarks ( $m_q < 10$  MeV)**



# From QCD to Hadron Spectrum

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expected low energy modes

massless gluons

light quarks ( $m_q < 10$  MeV)

- # In reality,

massless gluons  $\Rightarrow$  glueballs ( $m_{GB} \sim 1.4$  GeV or larger)

light quarks

$\Rightarrow$  mesons (500~800 MeV) except for pion, Kaon

baryons (900 MeV ~)

# From QCD to Hadron Spectrum

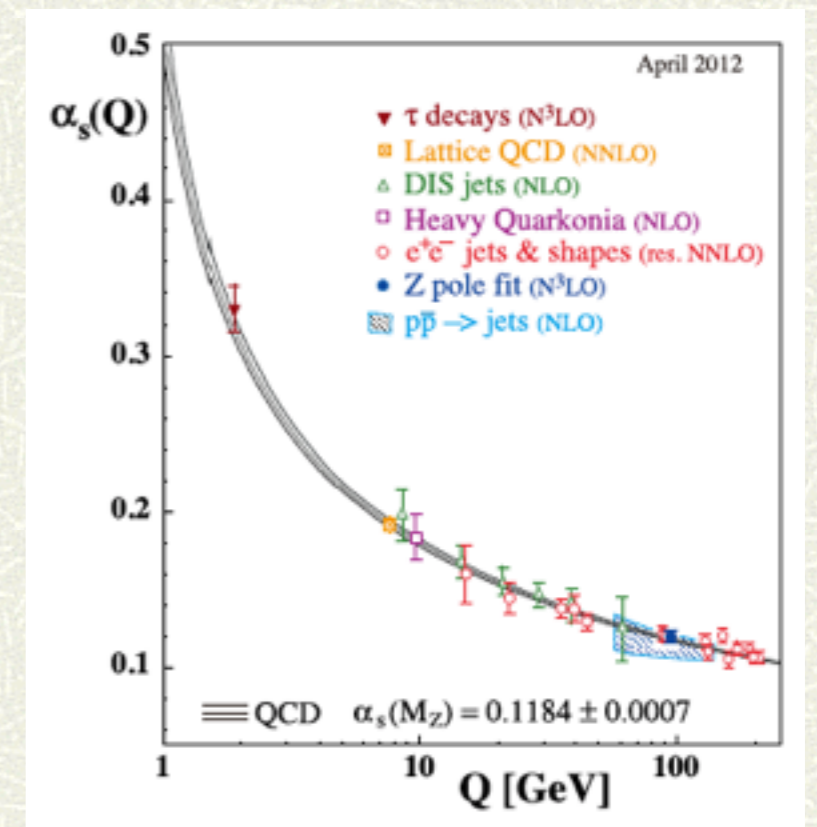
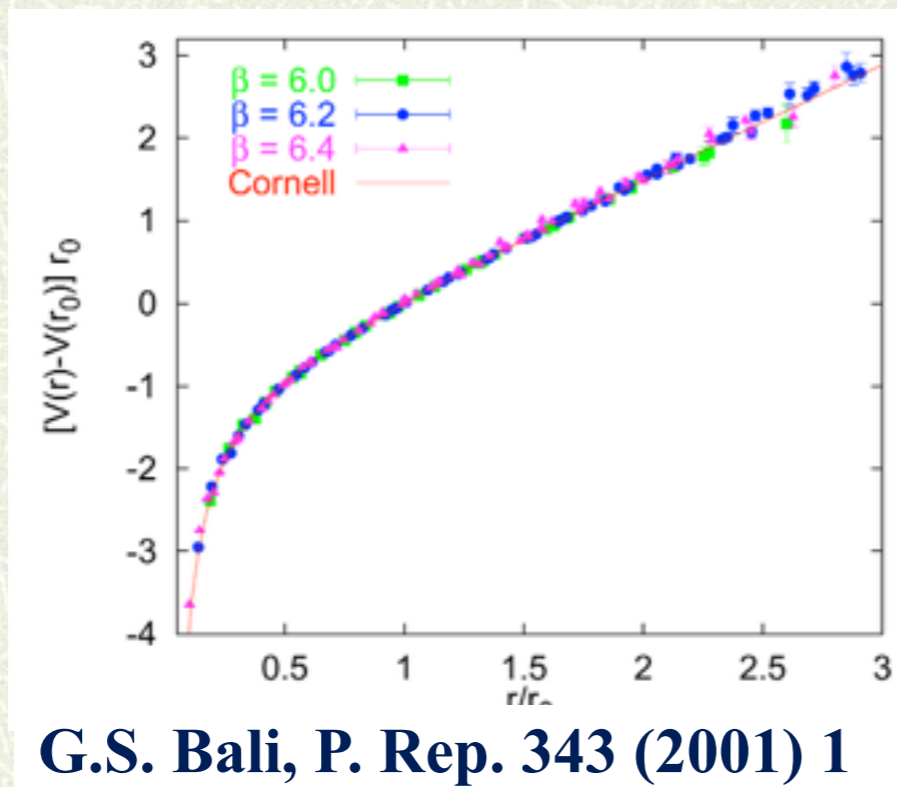
# QCD @ low energy is strongly correlated.

## 1. coupling constant runs

$$\Lambda_{\text{QCD}}^{(4)} \sim 300 \text{ MeV}$$

## 2. color confinement

mass gap : color singlet = hadrons





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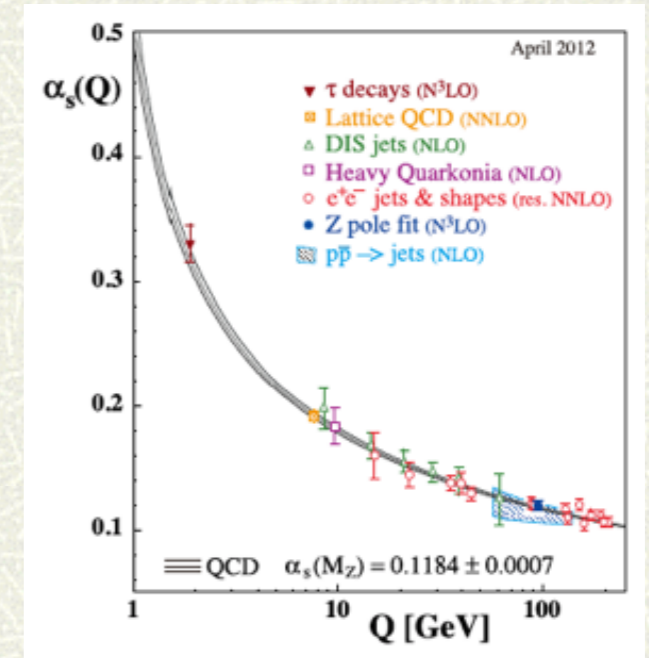
mass gap : color singlet = hadrons

## 3. non-trivial vacuum

requires non-perturbative solution

quark condensate breaks chiral symmetry

gluon condensate breaks scale invariance



# From QCD to Hadron Spectrum

## # Scale anomaly ← gluon condensate

$$\partial_\mu j_D^\mu = \sum_q m_q \bar{q}q + \frac{\beta(\alpha_s)}{\alpha_s} \text{Tr}[G_{\mu\nu} G^{\mu\nu}]$$
$$\langle (\alpha_s/\pi) G^{\mu\nu} G_{\mu\nu} \rangle \sim (350\text{MeV})^4 \sim \Lambda^4$$

## # Chiral symmetry breaking ← quark condensates

$$SU(N_f)_R \times SU(N_f)_L \rightarrow SU(N_f)_V$$

$$\langle \bar{q}q \rangle = \langle \bar{q}_L q_R + \bar{q}_R q_L \rangle \neq 0$$

$$\langle \bar{u}u \rangle \simeq \langle \bar{d}d \rangle \sim -(250\text{MeV})^3 \sim \mathcal{O}(\Lambda^3)$$

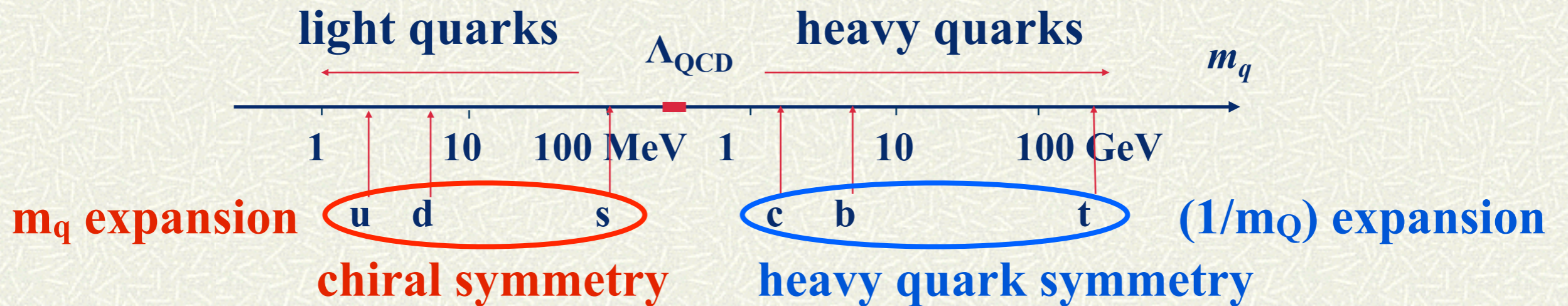
## # Low energy dof: “constituent quark” with mass

$$M_q \sim m_q - G_\chi \langle \bar{q}q \rangle \sim 300\text{MeV} \sim \mathcal{O}(\Lambda)$$

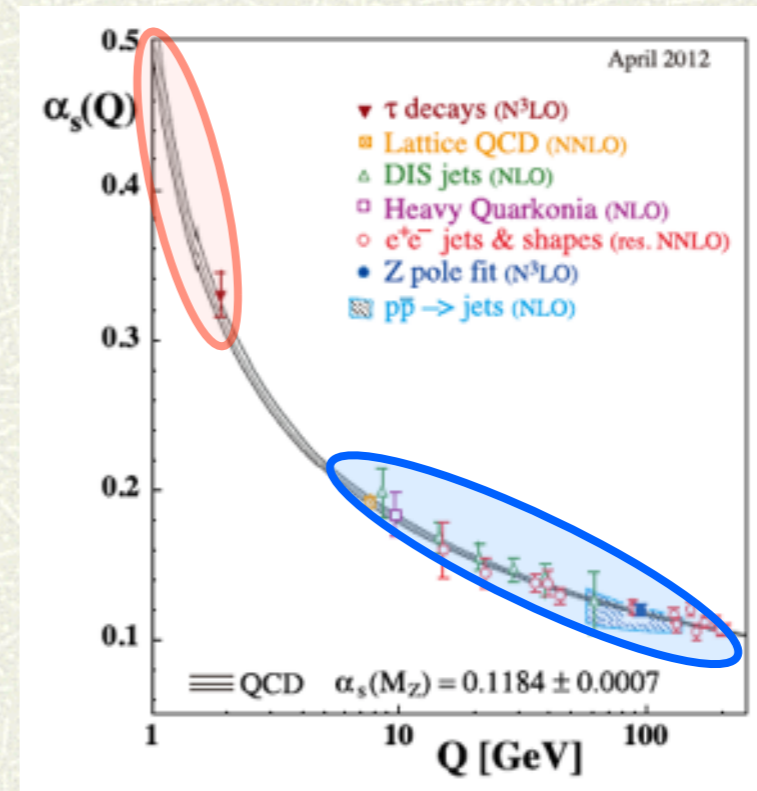


# From QCD to Hadron Spectrum

- # QCD Lagrangian is flavor independent, but the coupling constant runs.

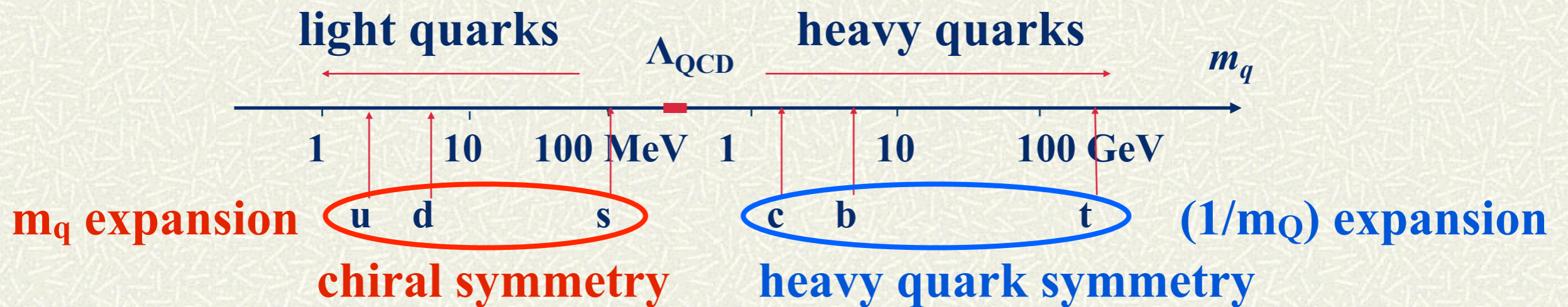


- # Light quarks are nonperturbative/ relativistic.
- # Heavy quarks are perturbative/ non-relativistic.



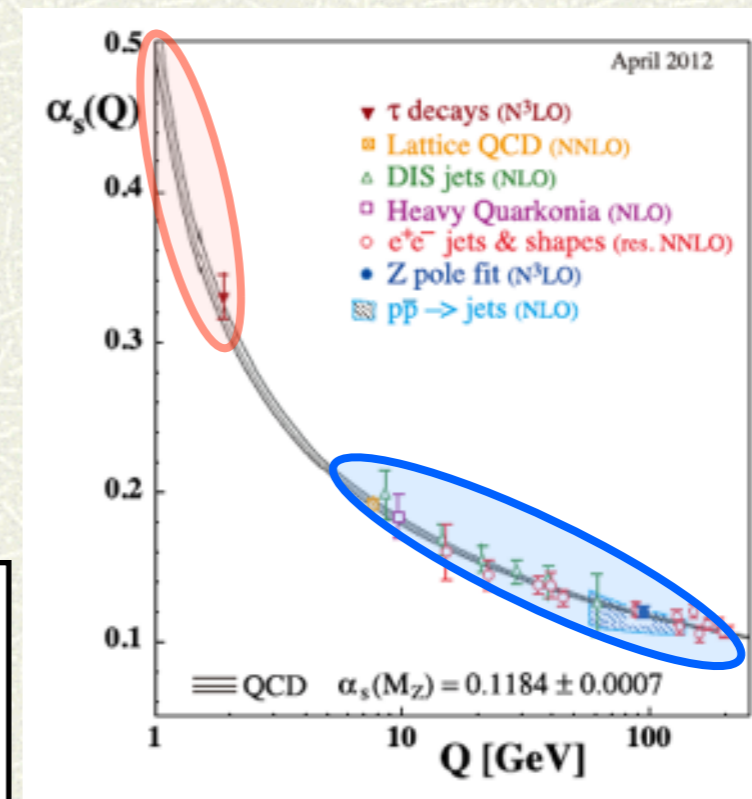
# From QCD to Hadron Spectrum

- # QCD Lagrangian is flavor independent, but the coupling constant runs.



- # Light quarks are nonperturbative/ relativistic.
- # Heavy quarks are perturbative/ non-relativistic.

Light and Heavy quarks look different in QCD





# Quarkonium

# Quarkonium

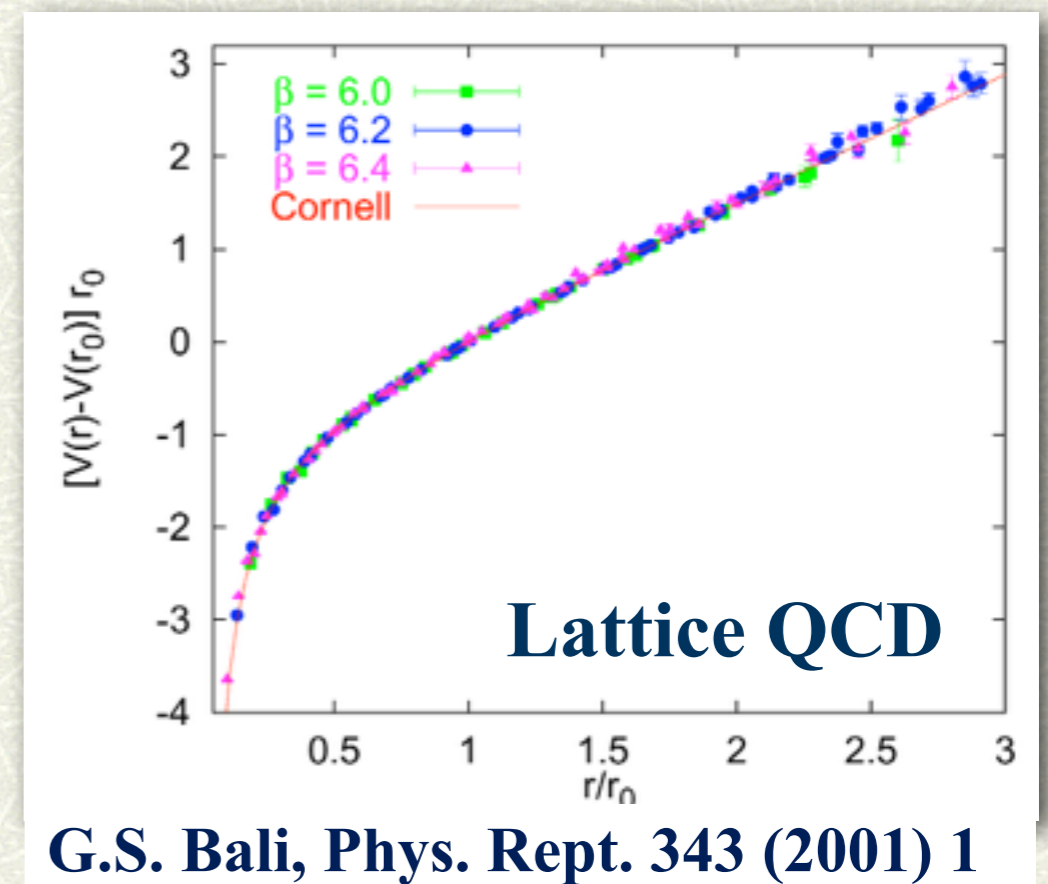
- # After 50 years since it was born, the quark model gives very good guidelines to classify and interpret the hadron spectrum.
- # The charmonium spectrum is a textbook example.  
*“hydrogen atom” in QCD*

- # The Hamiltonian with a Linear + Coulomb potential

$$V(r) = -\frac{e}{r} + \sigma r$$

E. Eichten, et al., PRL 34 (1975) 369

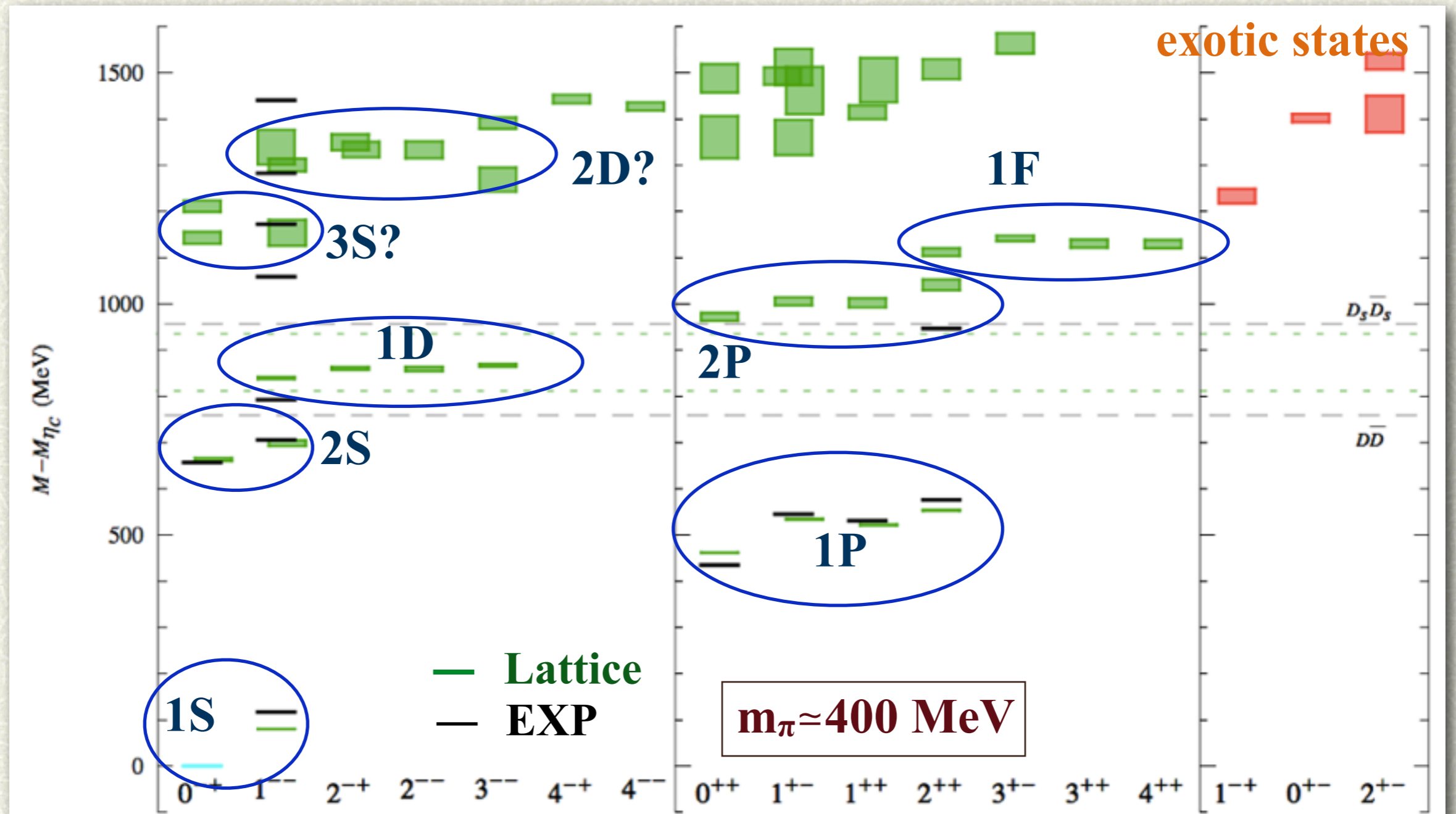
gives a good fit to the 1S, 1P, 2S, . . . charmonium (and bottomonium) states.





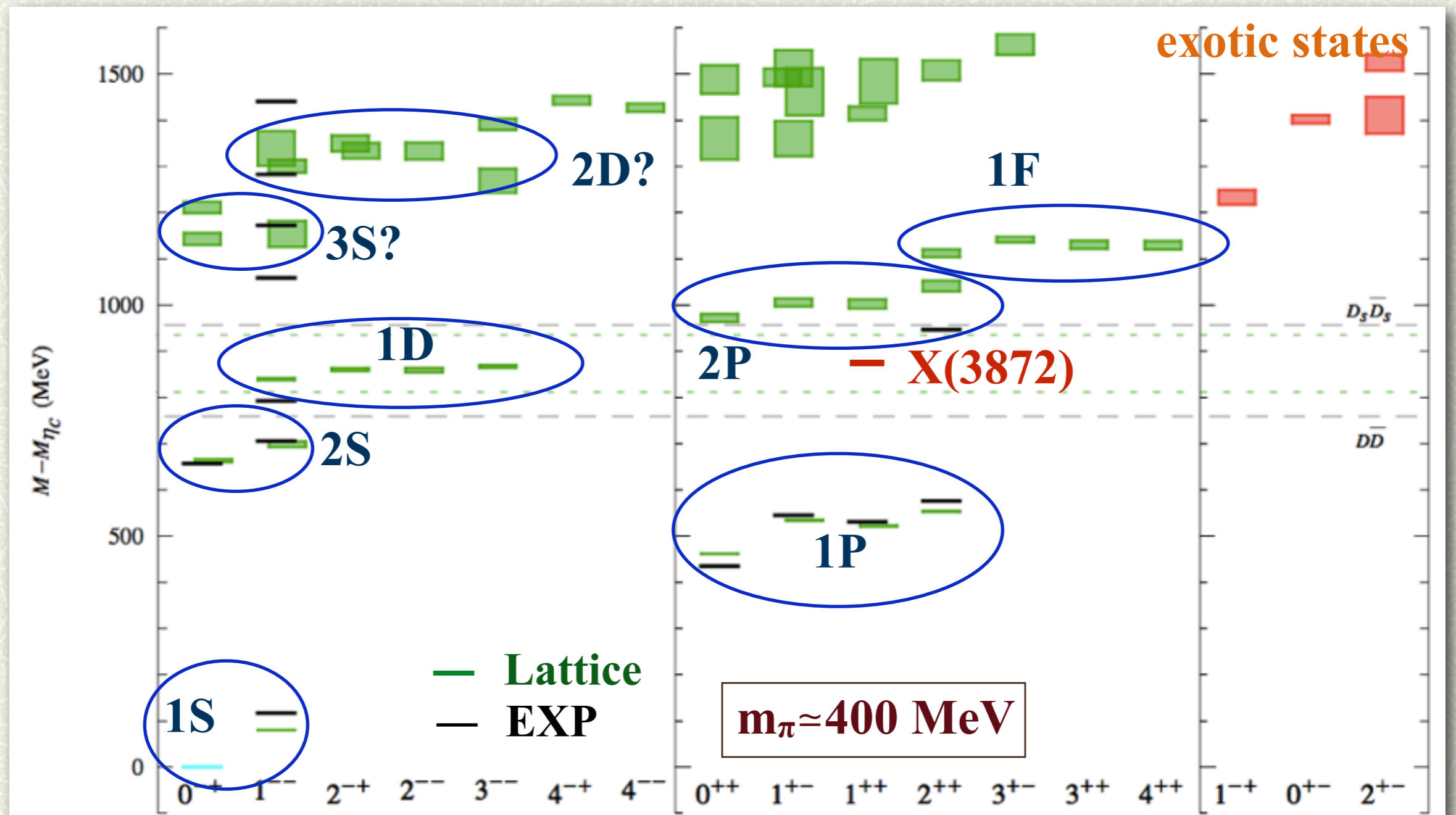
# Charmonium spectra on Lattice

Liuming Liu, et al. (Hadron Spectrum Collaboration)  
 JHEP 07, 126 (2012)



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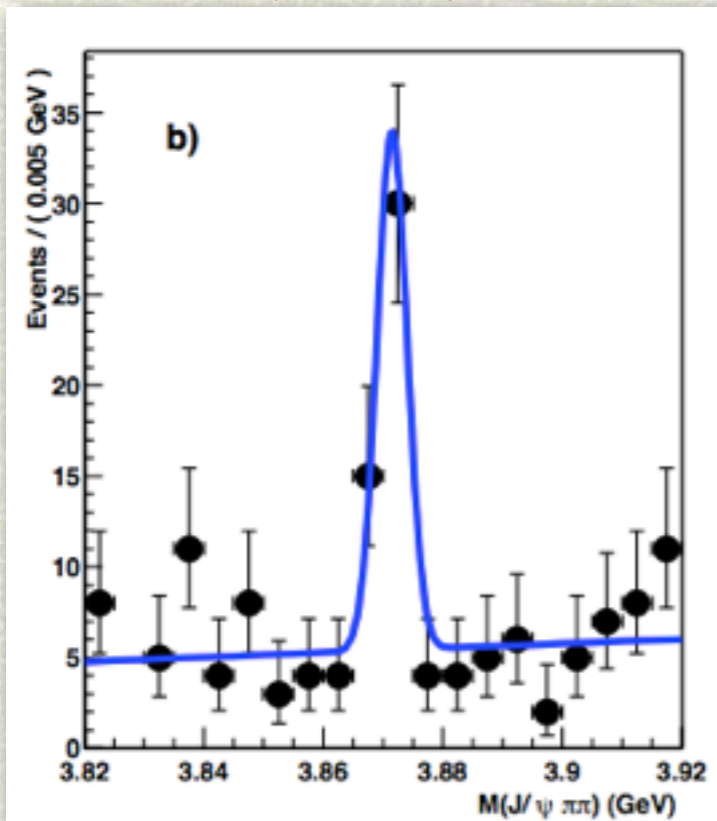
# New Charmonium-like States

- # X(3872) found in 2003 by Belle (KEK)
- # Z(3900), Z(4430) etc. : Charged hidden charm states

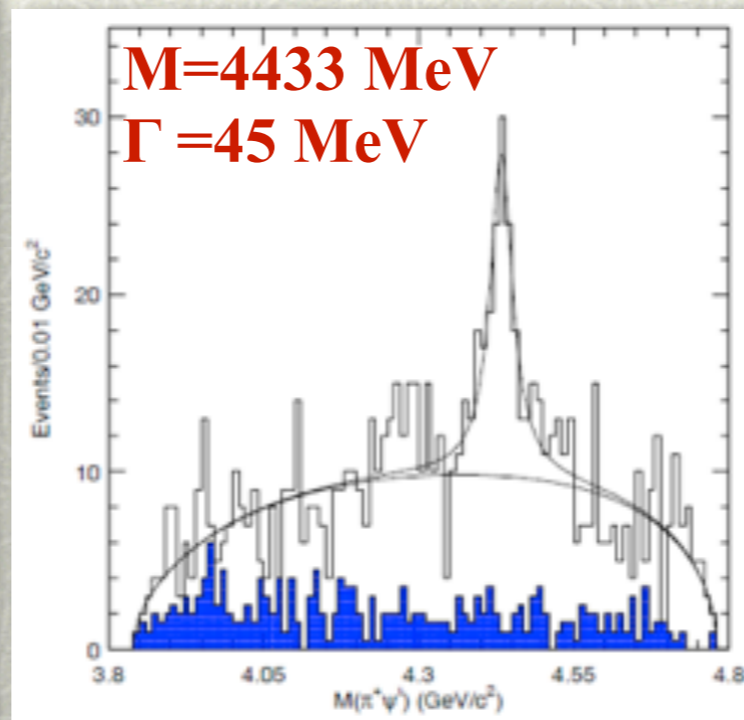
X(3872)

Z<sub>c</sub><sup>+</sup>(4430)

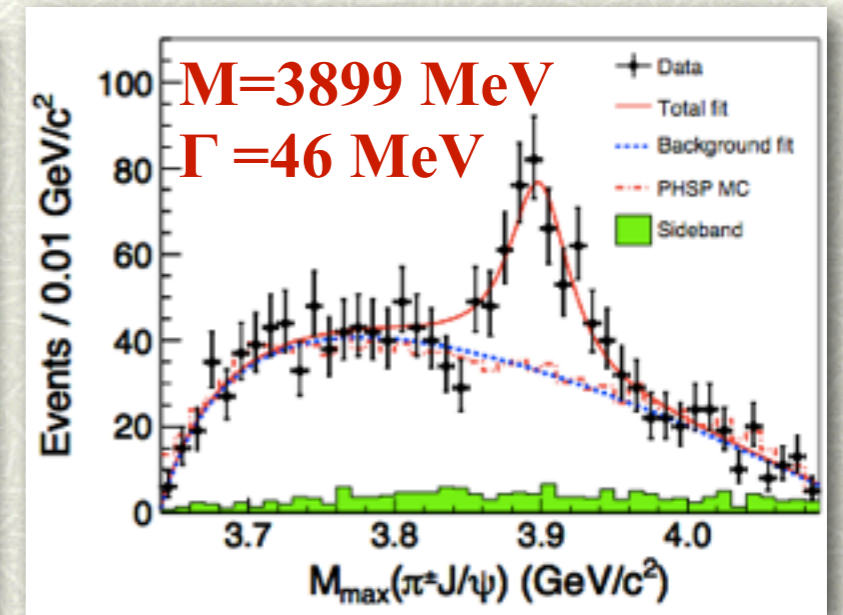
Z<sub>c</sub><sup>+</sup>(3900)



PRL 91 (2003) 262001



PRL 100 (2008) 142001



PRL 110 (2013) 252001

**These states require at least 4 quarks,  
*i.e., tetra-quarks or hadron molecules.***

# New Charmonium-like States

# **X(3872)** @ Belle,  $J^{PC}=1^{++}$ , confirmed @ LHCb, *PRL 110 (2013)*

# **X(3872)** is NOT a  $cc^{\text{bar}}$  state, because . .

■ Its mass, just at the  $DD^*$  threshold, is significantly lower than  $\chi_{c1}(2P)$  prediction. (cf.  $\chi_{c2}(2P)=3930\text{MeV}$ )

■ Decay  $\rightarrow \gamma\psi(2S)$  is suppressed.

■ The isospin violation observed in the decays

$$X(3872) \rightarrow J/\psi + \rho \quad (I=1)$$

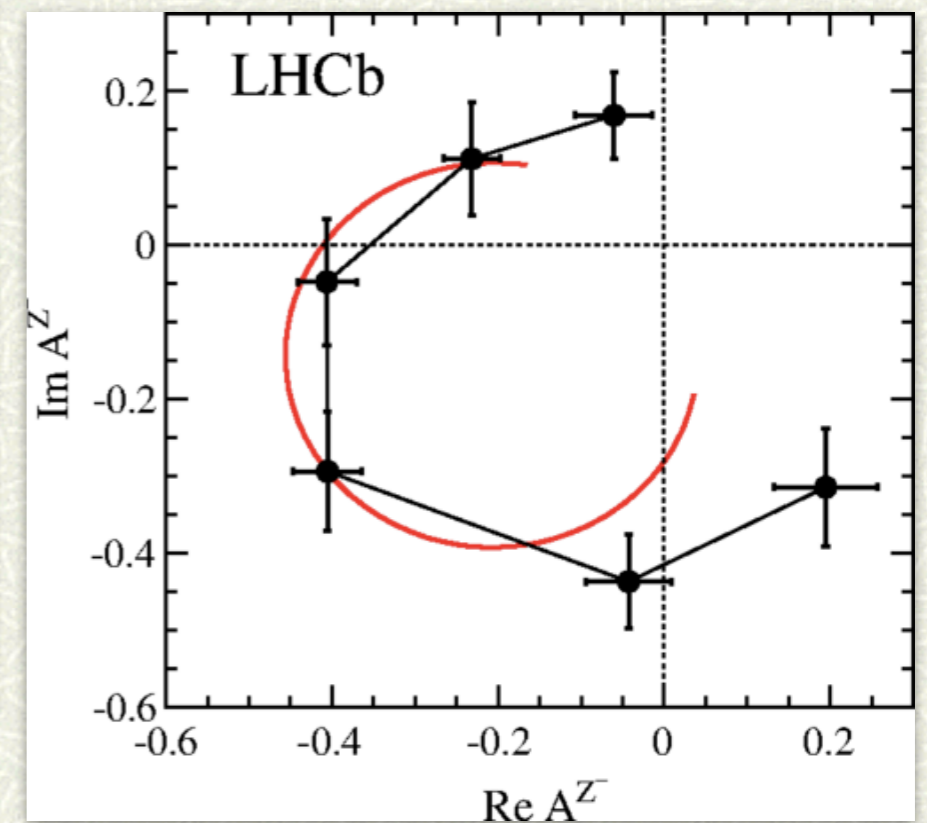
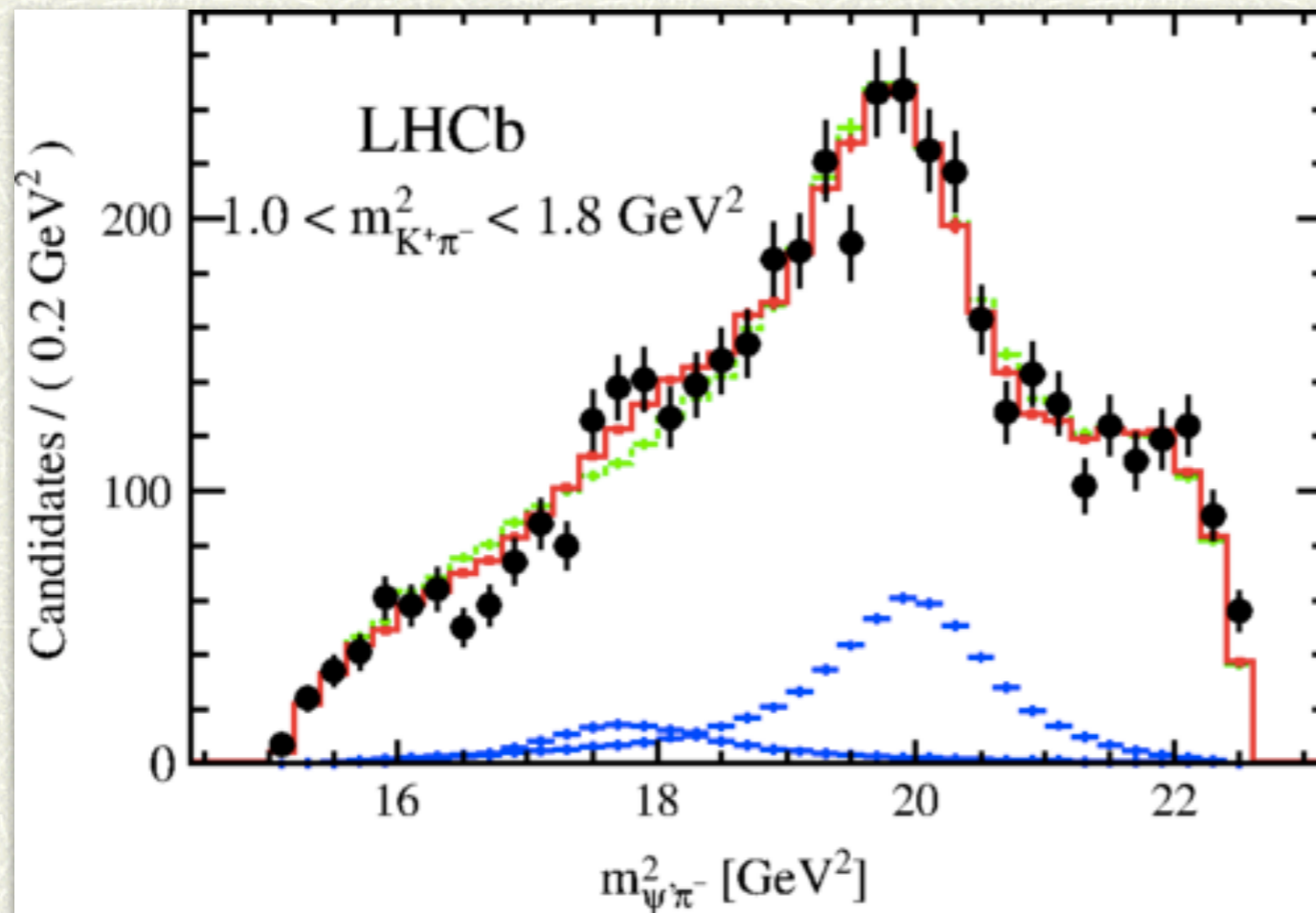
$$\rightarrow J/\psi + \omega \quad (I=0)$$

indicates a strong coupling to  $D^0D^{0*}(3872)$ .



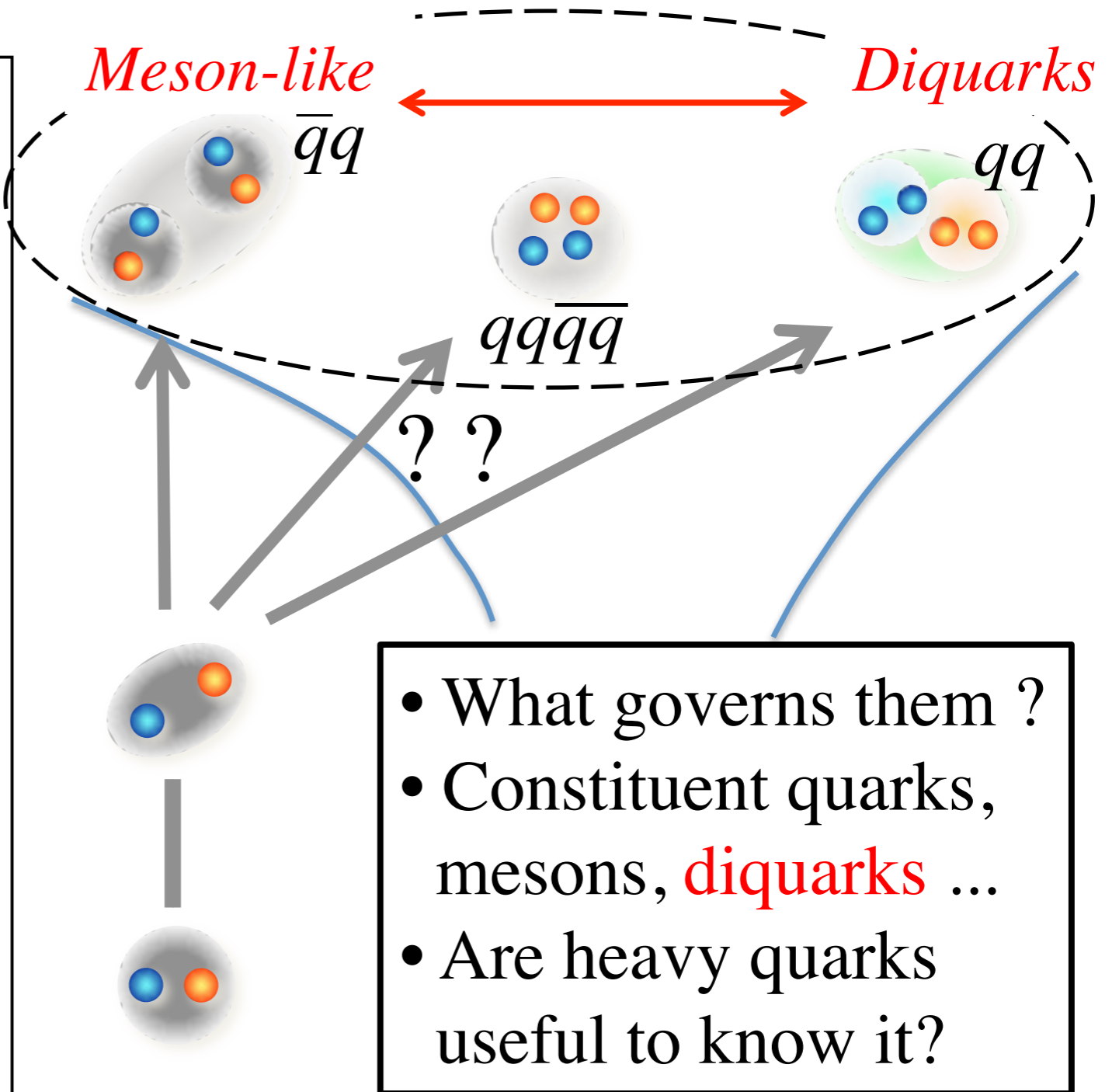
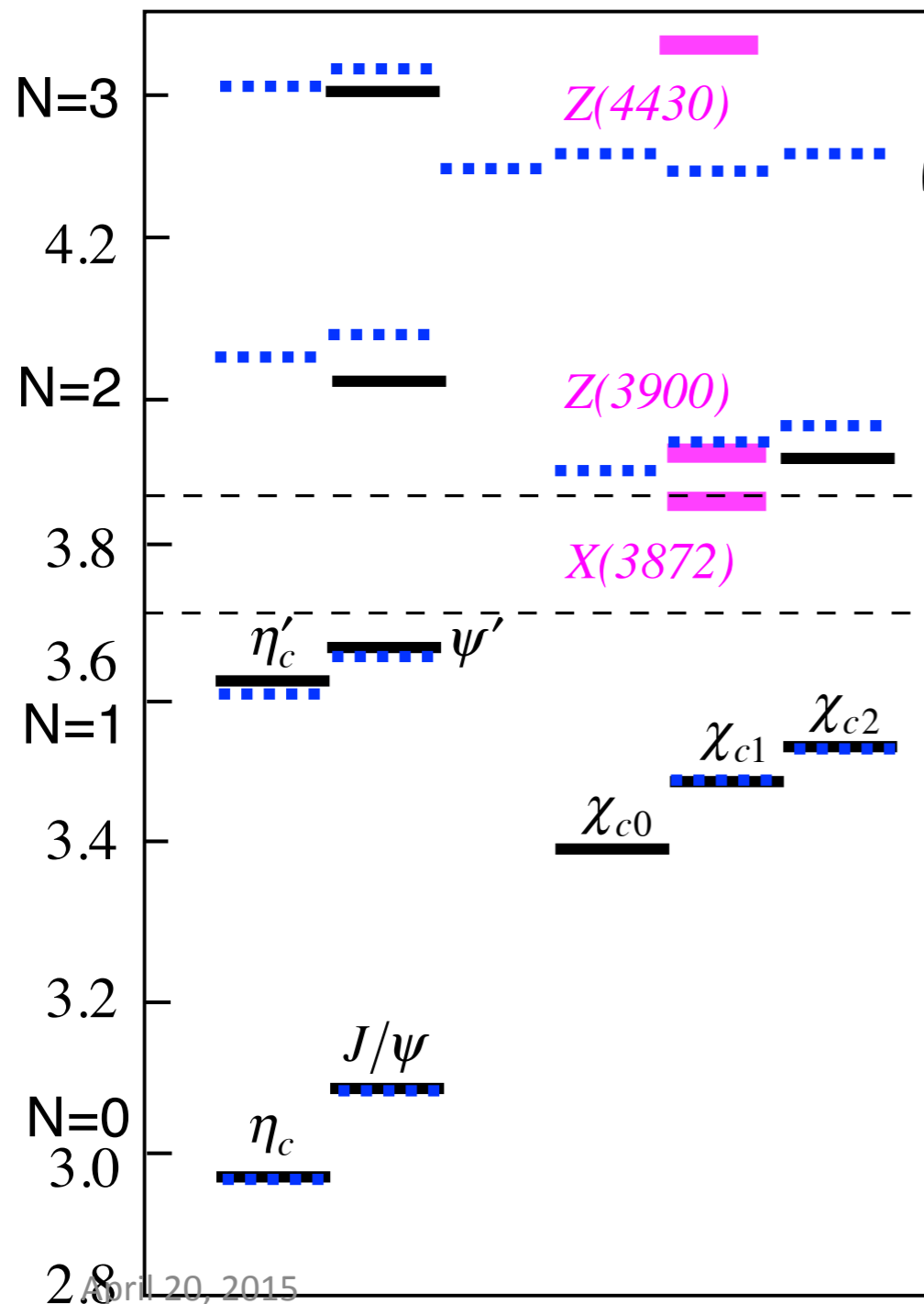
# New Charmonium-like States

- # **Z(4430) confirmed at LHCb, PRL 112, 222002 (2015)**  
in  $B^0 \rightarrow \psi' \pi^- K^+$  decay spectrum



# Above the threshold

## $q\bar{q}$ creation and rearrangement of multiquarks

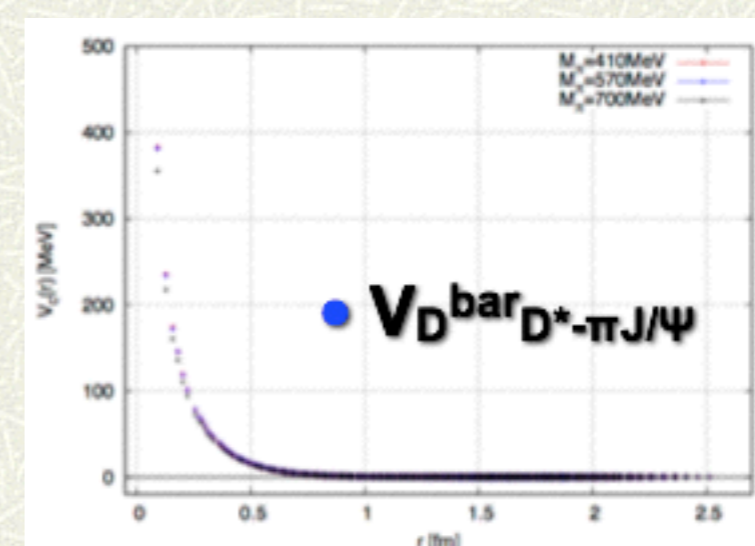
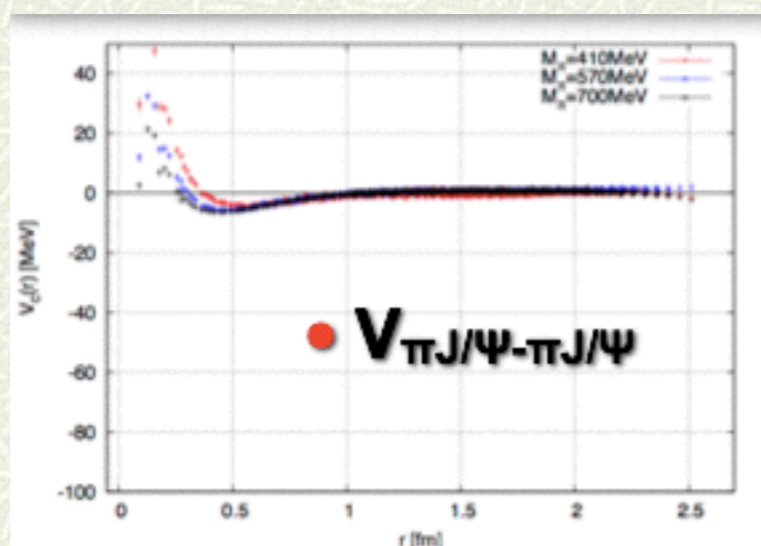
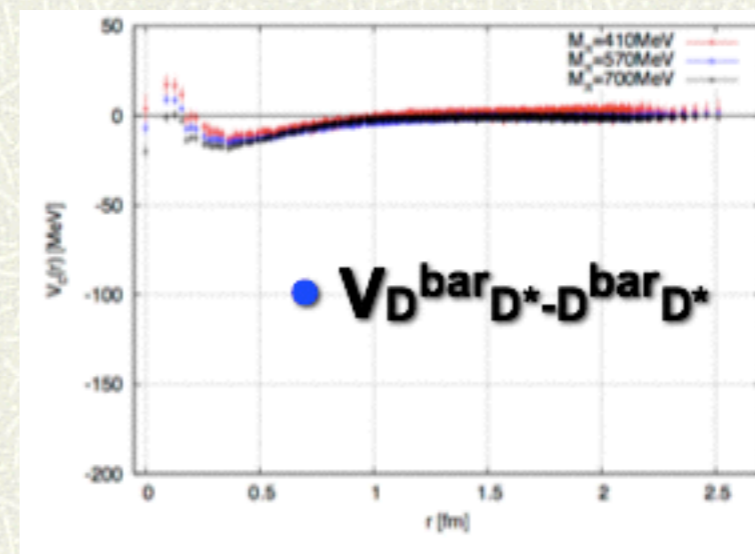
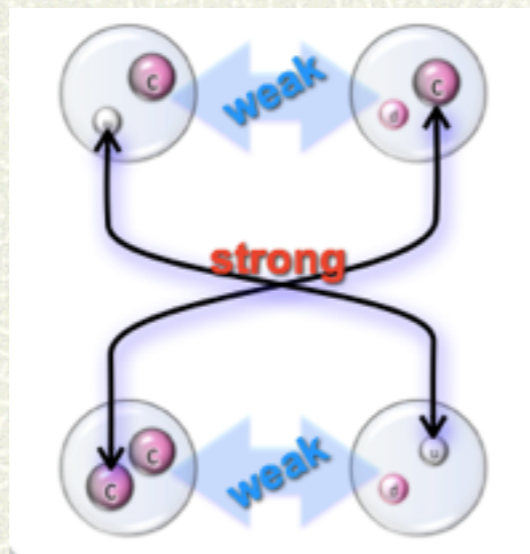


by A. Hosaka



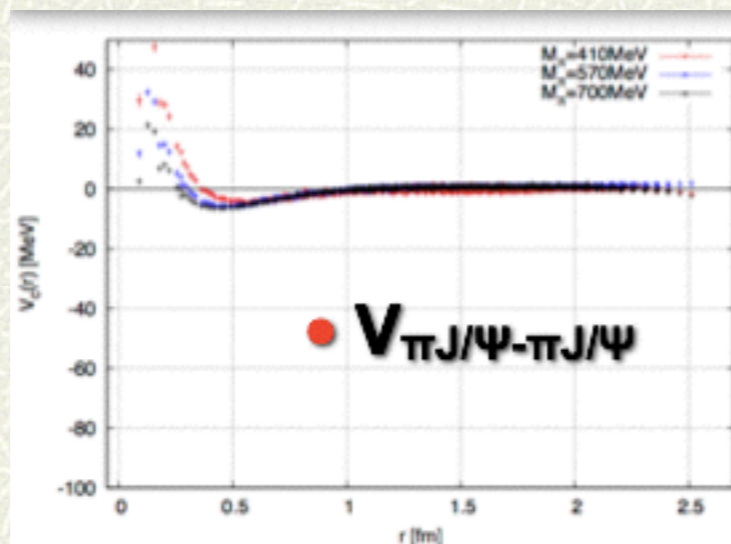
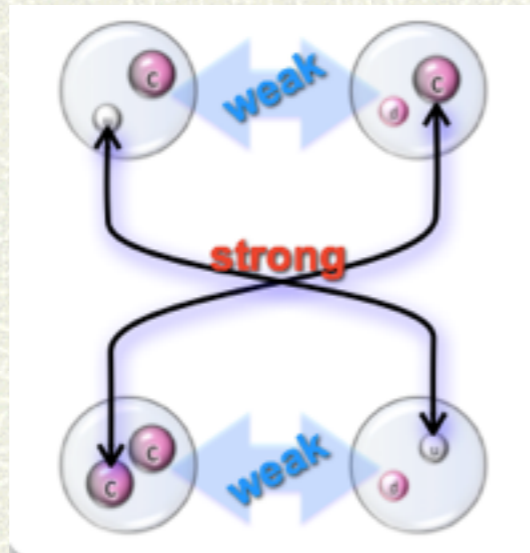
# Exotic States on Lattice

- #  $Z_c(3900)$  v.s.  $(D^{\text{bar}}D^*) + (\pi J/\psi)$  using the HAL QCD method  
Y. Ikeda for HALQCD @ NSTAR2015 (in preparation)

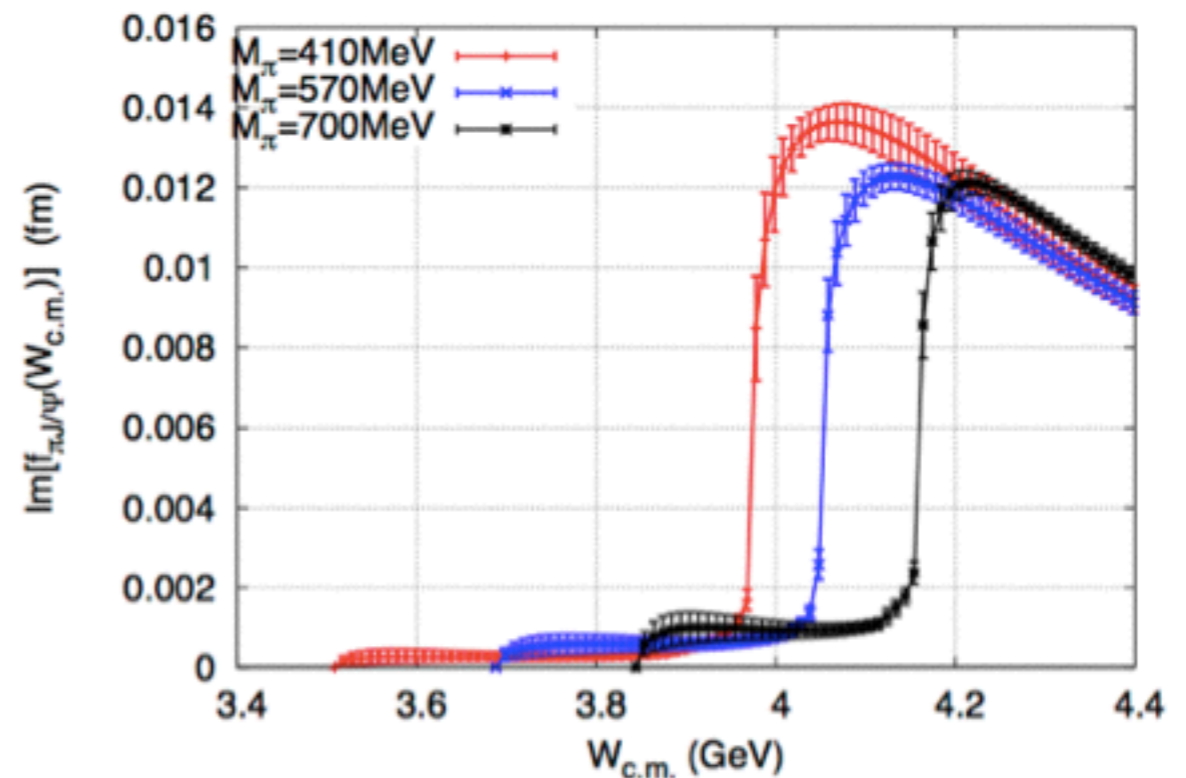


# Exotic States on Lattice

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## • $\pi J/\psi$ invariant mass



Strong (cusp) enhancement above the  $D^{\text{bar}}D^*$  threshold





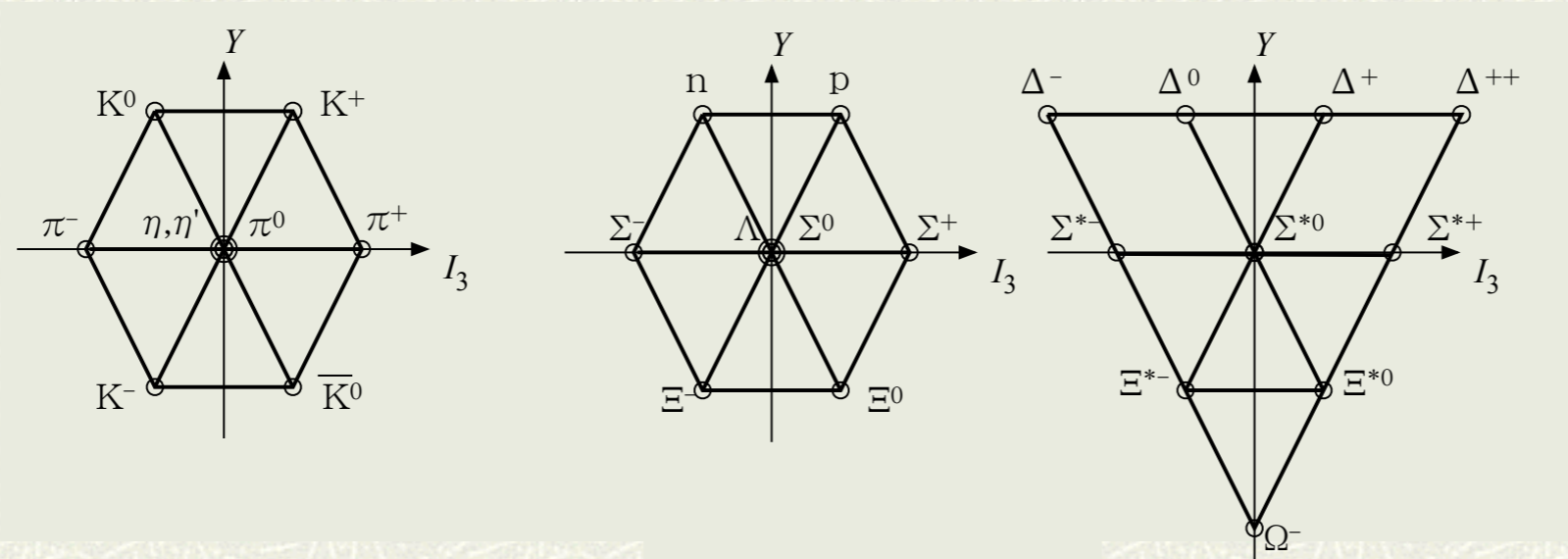
# Light Exotic Hadrons

# Light Hadrons

## # Light hadrons

The low-lying hadrons with u, d, s quarks form complete patterns of the  $SU(3)_f$  representations.

#  $SU(3)_f$  symmetry is the basis of the constituent quark model.



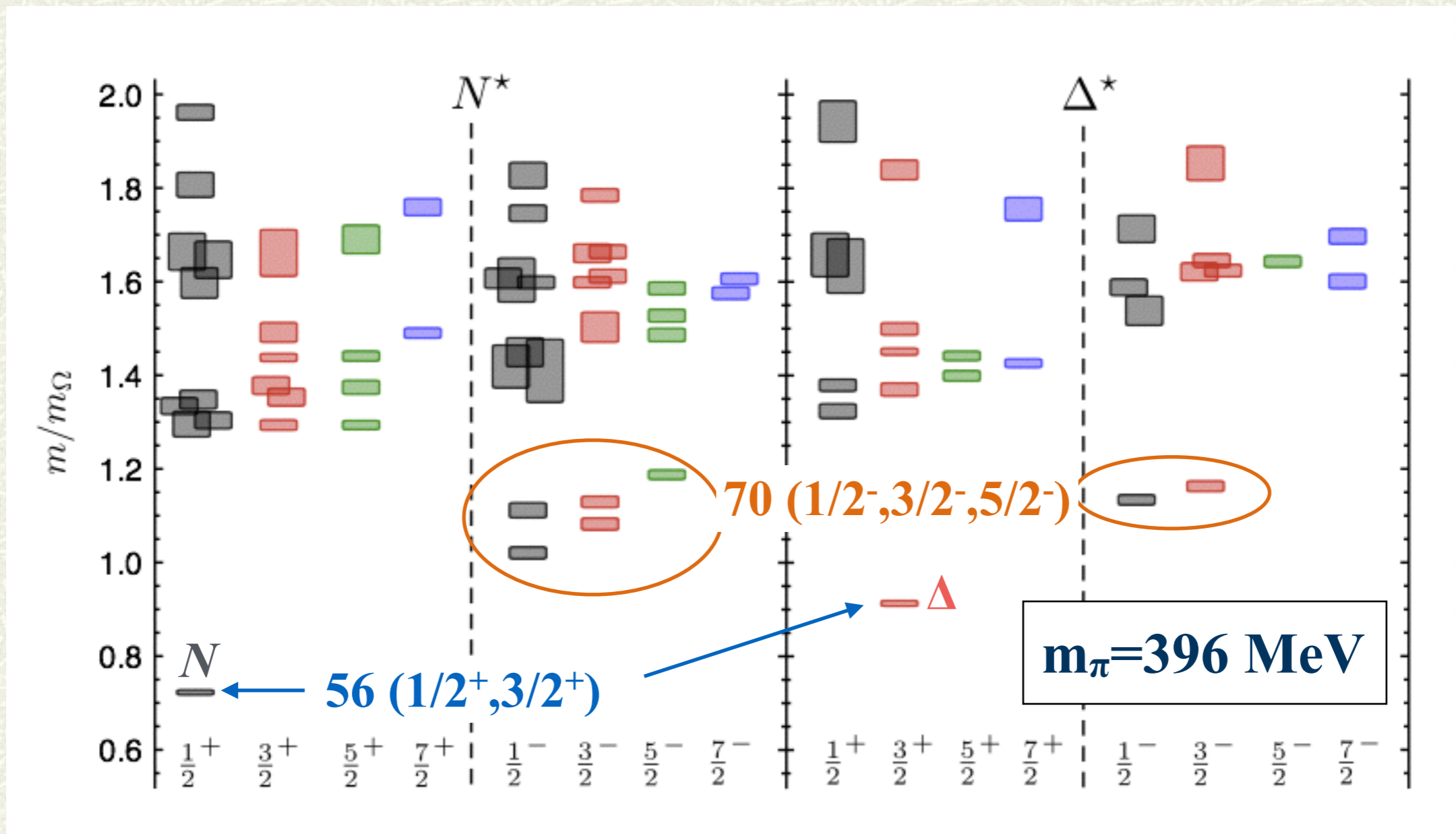
mesons with  $qq^{\text{bar}}$

baryons with  $qqq$



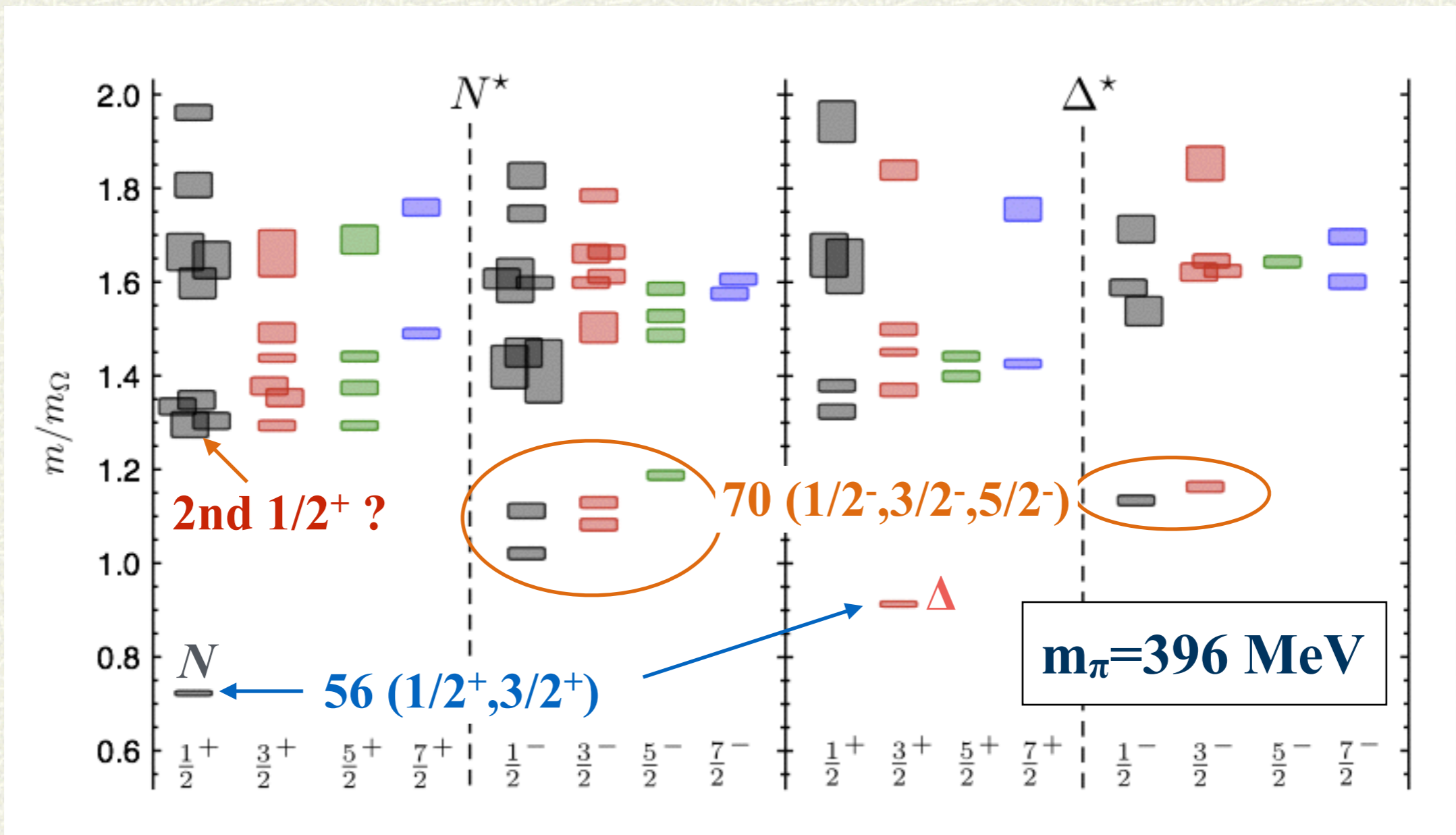
# Light Hadrons

- # Light baryon spectra by R.G. Edwards et al., PRD84 (2011) 074508, are consistent with the  $SU(6) \times O(3)$  quark model.



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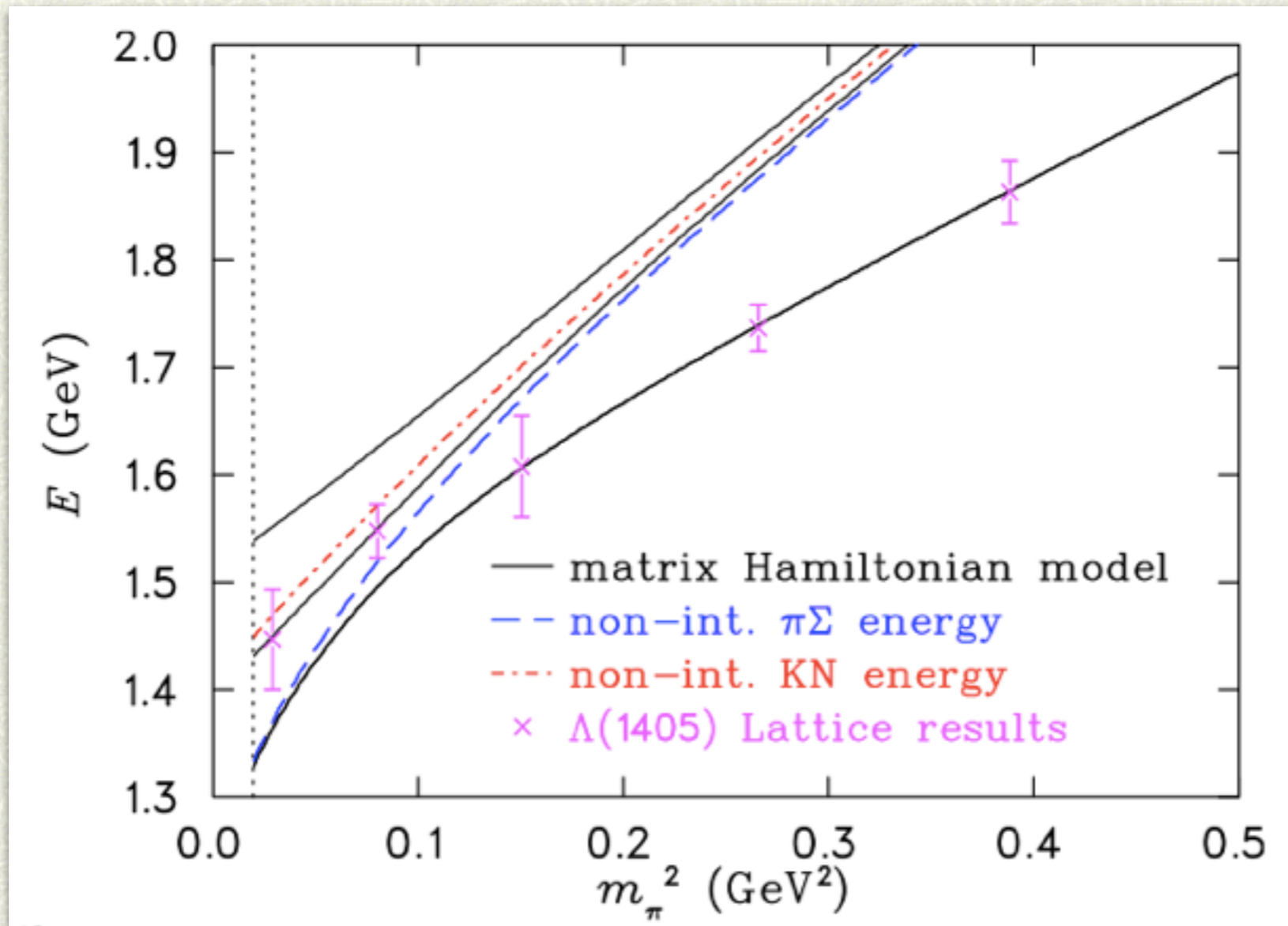


# Light Hadrons

- # Lattice QCD has confirmed that the overall features of the low-lying hadron spectrum are given consistently as the constituent quark model.
- # Yet, there are some (exotic) hadrons which are not reproduced in LQCD by simple  $qq^{\text{bar}}$  or  $qqq$  operators.
- # A few prominent examples:  
Light scalar mesons, Roper resonance(s),  $\Lambda(1405)$ , . .
- # Recent analyses have “confirmed” the exotic properties of  $\Lambda(1405)$ .

# $\Lambda(1405)$

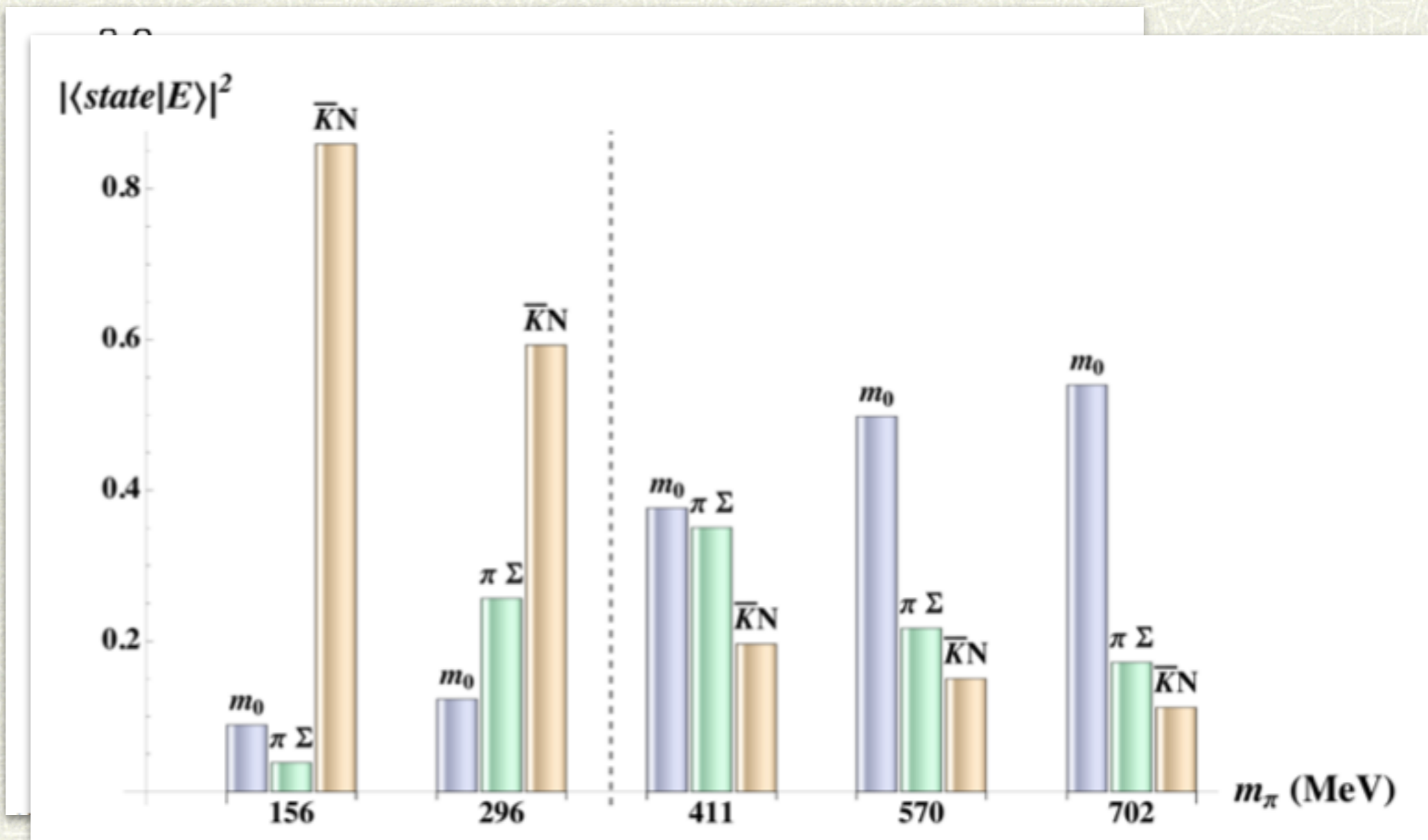
- Recent LQCD analysis by J.M.M. Hall et al. *PRL* 114, 132002 (2015) (ArXiv:1411.3402), claims  $K^{\text{bar}}N$  dominance.





# $\Lambda(1405)$

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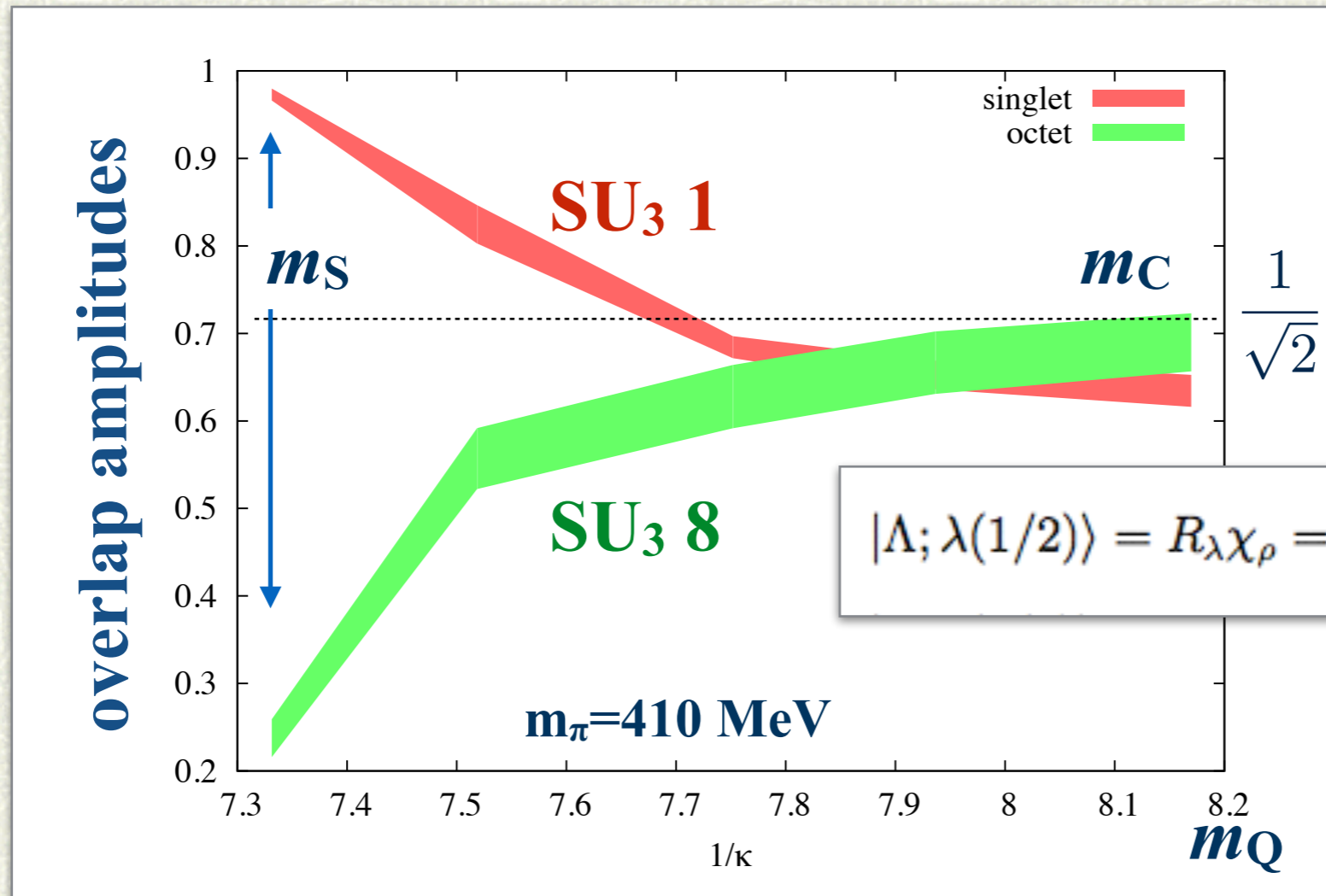




# $\Lambda(1405)$

- # HQ mass dependence:  $m_Q = m_S \rightarrow m_C$   
transition from SU(3) to HQ symmetry

*P. Gubler, T.T. Takahashi, M.O., in preparation*



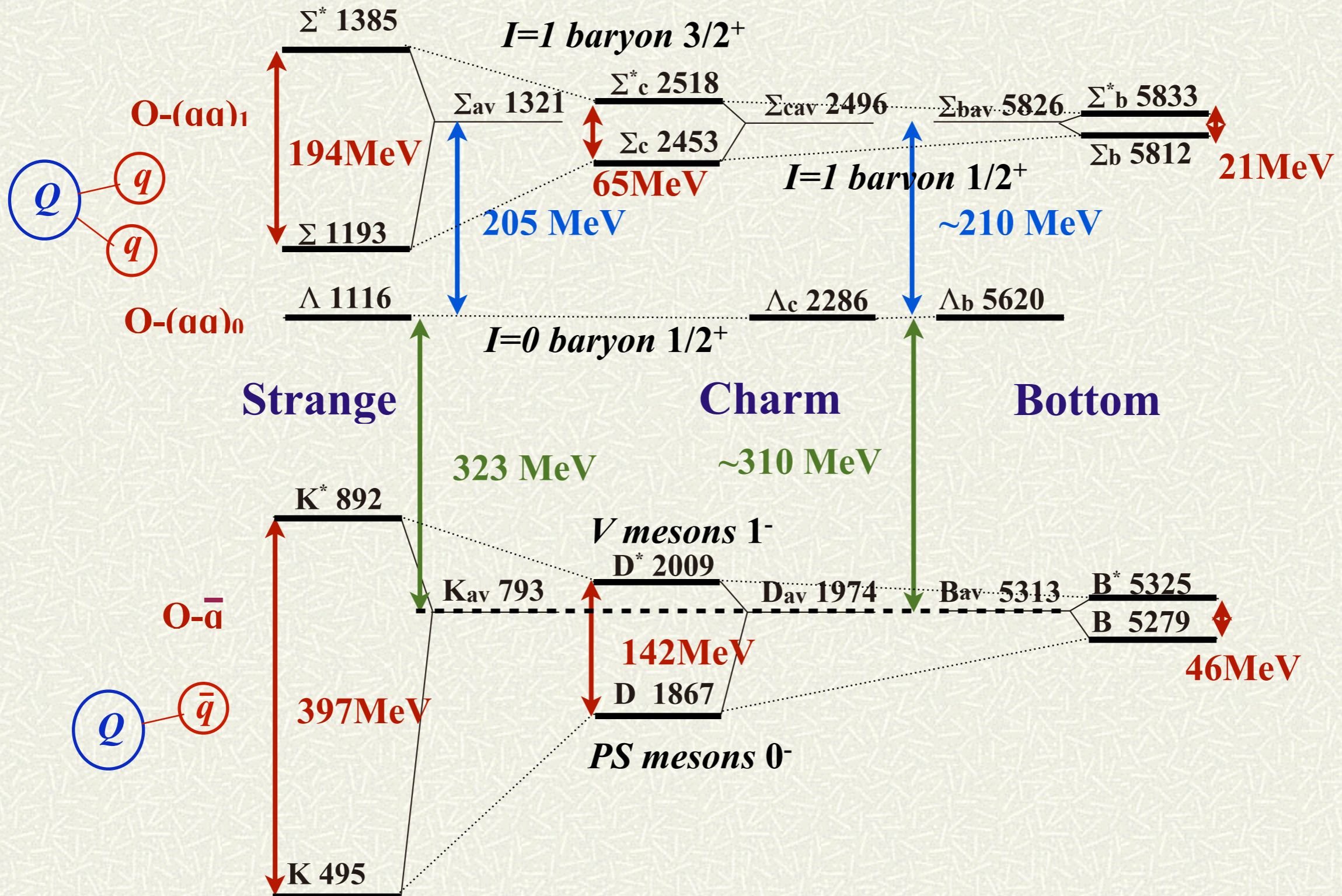


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# Diquarks in Heavy Baryons

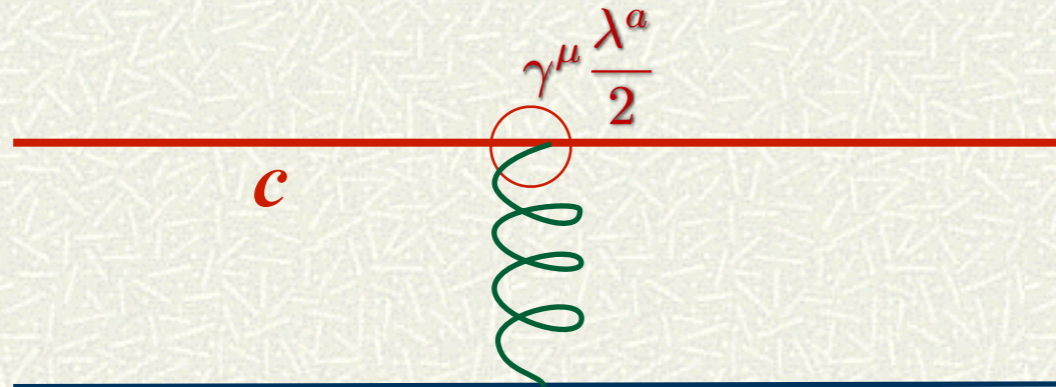


# Strange v.s. Charm/Bottom



# Heavy Quark Spin Symmetry

Magnetic gluon coupling is suppressed



$$\bar{\Psi} \gamma^\mu \frac{\lambda^a}{2} \Psi A_\mu^a \sim \underbrace{\Psi^\dagger \frac{\lambda^a}{2} \Psi A_0^a}_{\text{Color Electric coupling}} - \underbrace{\Psi^\dagger \sigma \frac{\lambda^a}{2} \Psi \cdot \frac{1}{m_Q} (\nabla \times A^a)}_{\text{Color Magnetic coupling}}$$

**(Color Electric coupling)  $\gg$  (Color Magnetic coupling)**

**HQ spin-flip amplitudes are suppressed by  $(1/m_Q)$ .**

$\Rightarrow$  **Heavy Quark Spin Symmetry**

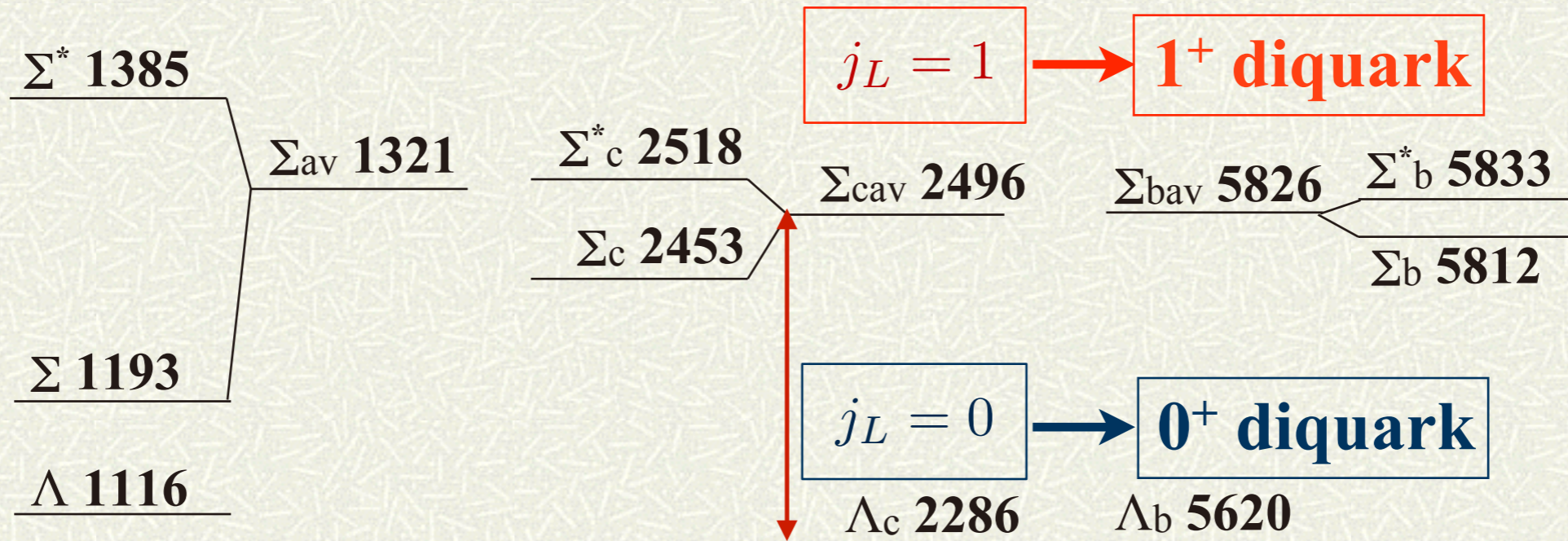


# Heavy Quark Spin Symmetry

HQ spin symmetry  $[S_Q, H] = O\left(\frac{1}{m_Q}\right)$

$$\left. \begin{array}{l} Q \\ \hline qq \end{array} \right\} \vec{J} = \vec{S}_Q + \vec{j}_L \quad \vec{j}_L = \vec{S}_q + \vec{L}_q$$

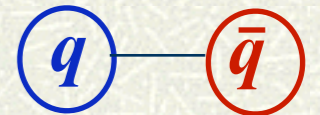
$J = j_L \pm \frac{1}{2}$  states are degenerate in the HQ limit.



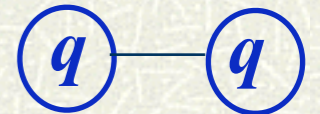
# Diquark

# The Scalar ( $0^+$ ) diquark is an analogue of the PS meson:

PS meson  $qq^{\text{bar}}$  : color 1,  $J^\pi=0^-$ , flavor 1+8



**S diquark**  $[qq]_0$  : color  $3^{\text{bar}}$ ,  $J^\pi=0^+$ ,



flavor SU(3)  $3^{\text{bar}}$  :  $[ud]_0$ ,  $[ds]_0$ ,  $[sd]_0$

■ Color magnetic interaction (CMI) of the OGE is attractive for the scalar diquark.

■ Instanton Induced Interaction (III) is attractive in the flavor antisymmetric states

■ Rough estimate:  $S(0^+)$  v.s.  $\Lambda(1^+)$

$$M(1^+) - M(0^+) = (2/3) [M(\Delta) - M(N)] \sim 200 \text{ MeV}$$



# Diquark

## # Heavy Baryons, $\Lambda_Q, \Sigma_Q = Q + (qq)$

Because the spin dependent interaction is suppressed between the heavy Q and light quarks, **the heavy baryon spectrum will reflect the light diquark (qq) *spin-dependent* correlation.**

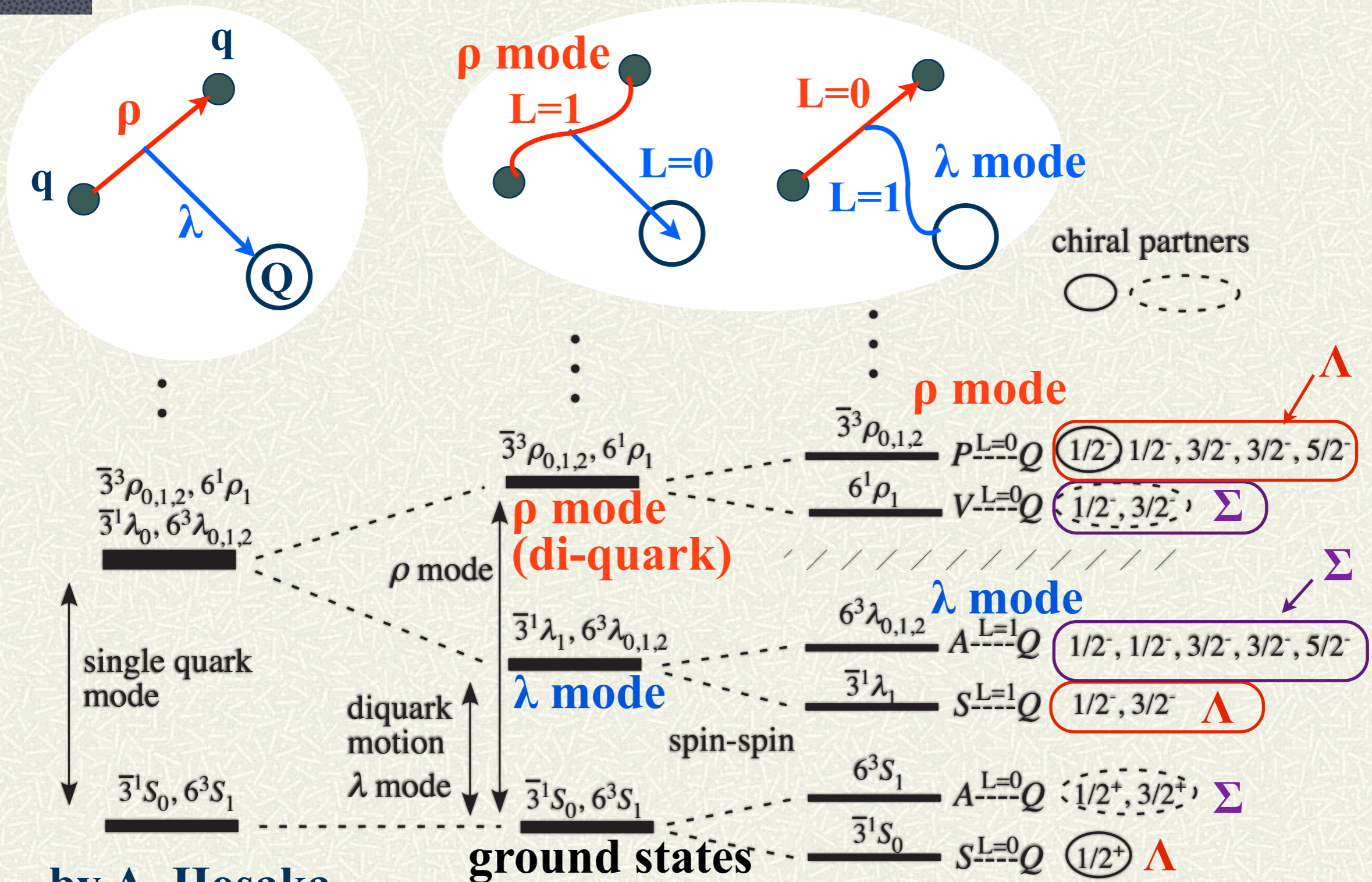
		$J^\pi$	color	flavor
<b>Pseudoscalar</b>	$\epsilon_{abc}(u_a^T C d_b)$	$0^-$	$\bar{3}$	$\bar{3} (I = 0)$
<b>Scalar</b>	$\epsilon_{abc}(u_a^T C \gamma^5 d_b)$	$0^+$	$\bar{3}$	$\bar{3} (I = 0)$
<b>Vector</b>	$\epsilon_{abc}(u_a^T C \gamma^\mu \gamma^5 d_b)$	$1^-$	$\bar{3}$	$\bar{3} (I = 0)$
<b>Axial Vector</b>	$\epsilon_{abc}(u_a^T C \gamma^\mu d_b)$	$1^+$	$\bar{3}$	$6 (I = 1)$
	$\epsilon_{abc}(u_a^T C \sigma^{\mu\nu} d_b)$	$1^+, 1^-$	$\bar{3}$	$6 (I = 1)$
<b>color 6 only in Exotic Hadrons</b>	$(u_a^T C d_b) + (a \leftrightarrow b)$	$0^-$	6	$6 (I = 1)$
	$(u_a^T C \gamma^5 d_b) + (a \leftrightarrow b)$	$0^+$	6	$6 (I = 1)$
	$(u_a^T C \gamma^\mu \gamma^5 d_b) + (a \leftrightarrow b)$	$1^-$	6	$6 (I = 1)$
	$(u_a^T C \gamma^\mu d_b) + (a \leftrightarrow b)$	$1^+$	6	$\bar{3} (I = 0)$
	$(u_a^T C \sigma^{\mu\nu} d_b) + (a \leftrightarrow b)$	$1^+, 1^-$	6	$\bar{3} (I = 0)$

# Diquark

- # **Diquarks in (quenched) lattice calculations**
  - Hess, Karsch, Laermann, Wetzorke, PR D58, 111502 (1998)  
 $M(0^+) \sim 694 \text{ MeV}, M(1^+) \sim 810 \text{ MeV}$  (Landau gauge)
  - Alexandrou, de Forcrand, Lucini, PRL 97, 222002 (2006)  
gauge invariant calculation in a  $Qqq$  system  
 $M(1^+) - M(0^+) \sim 100\text{-}150 \text{ MeV}$
  - Babich, et al., PR D76, 074021 (2007)  
 $M(1^+) - M(0^+) \sim 162 \text{ MeV}$  (Landau gauge)
  - DeGrand, Liu, Schaefer, PR D77, 034505 (2008)  
S: strongly attractive, PS: attractive for small  $m_q$
  
- # **The scalar  $0^+$  diquark has a strong attractive correlation.**



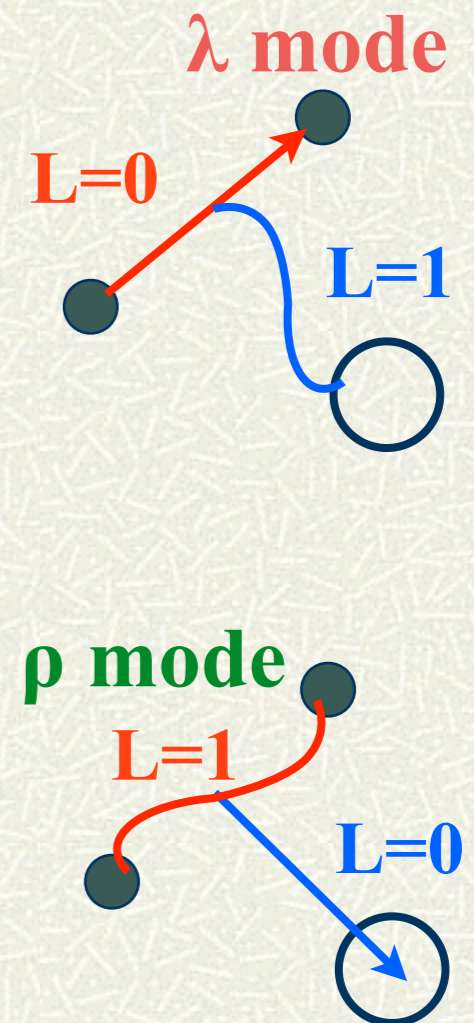
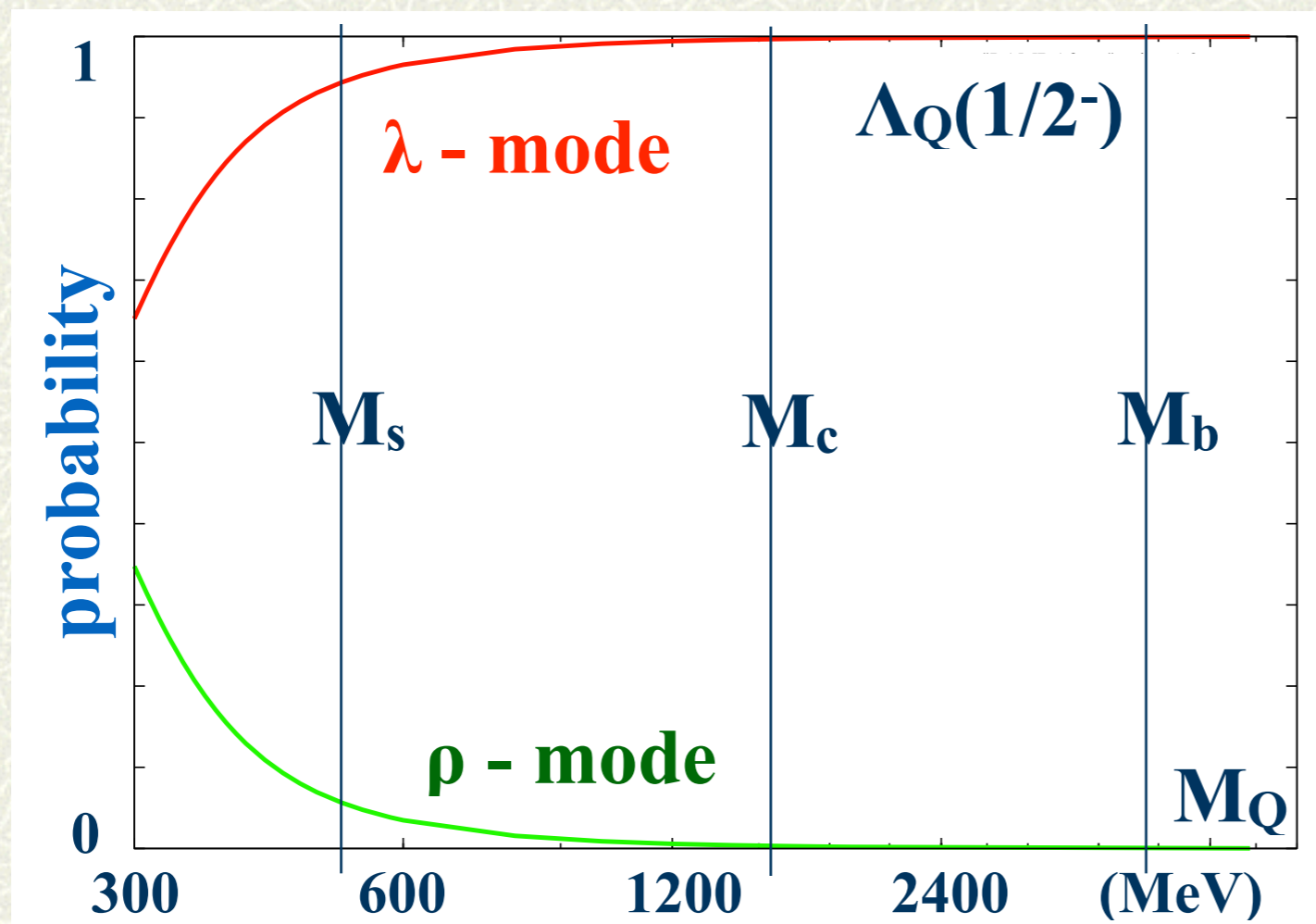
# Diquarks in P-wave Baryons



by A. Hosaka

# Diquarks in P-wave Baryons

- ▣ Probabilities of  $\lambda$  and  $\rho$  modes v.s. heavy quark mass by a Hamiltonian quark model with spin-spin, spin-orbit and tensor forces



*Yoshida, Sadato, Hosaka, Hiyama, MO, in preparation.*



# Diquarks in P-wave Baryons

**sud**  
(I=0)

$\Lambda$  (1830) 5/2

$\Lambda$  (1800) 1/2

**(S=3/2) $_{\rho}$**

$\Lambda$  (1690) 3/2

$\Lambda$  (1670) 1/2

$\Lambda$  (1520) 3/2

**(S=1/2) $_{\lambda}$**

$\Lambda$  (1405) 1/2

**sqq**  
(I=1)

**(S=1/2) $_{\rho}$**

$\Sigma$  (2000) 1/2

$\Sigma$  (1940) 3/2

$\Sigma$  (1775) 5/2

$\Sigma$  (1750) 1/2

$\Sigma$  (1670) 3/2

**(S=3/2) $_{\lambda}$**

**ssq**  
(I=1/2)

$\Xi$  (2030) ?

$\Xi$  (1950) ?

$\Xi$  (1820) 3/2

$\Xi$  (1690) ?

**cud (I=0, 1)**

$\Lambda_c$  (2880) 5/2?

$\Sigma_c$  (2800) ?

?

$\Lambda_c$  (2625) 3/2

$\Lambda_c$  (2595) 1/2

**(S=1/2) $_{\lambda}$**

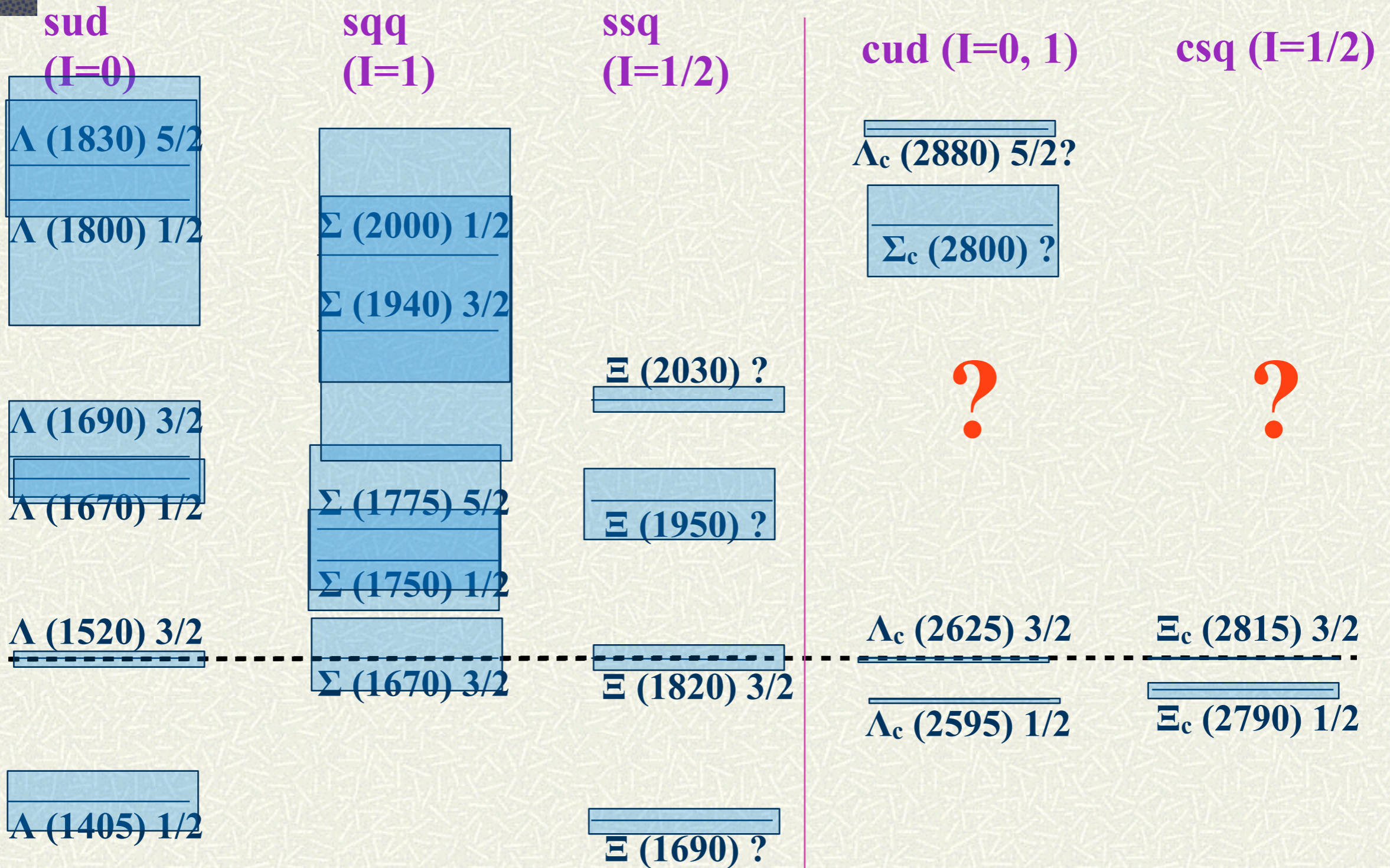
**csq (I=1/2)**

?

$\Xi_c$  (2815) 3/2

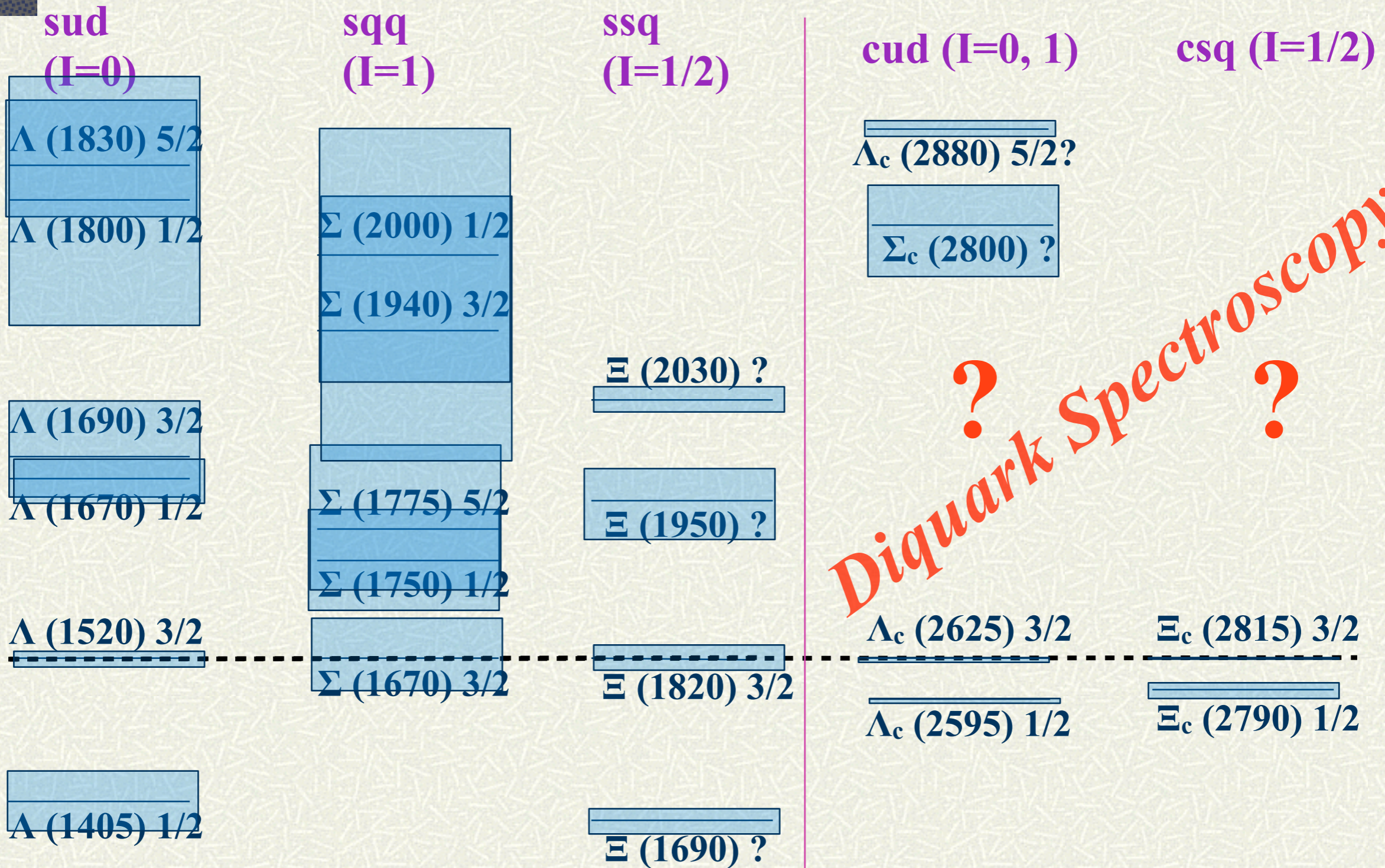
$\Xi_c$  (2790) 1/2

# Diquarks in P-wave Baryons





# Diquarks in P-wave Baryons







# Diquark

# Scalar diquark as a **new building block**.

$D^{\text{bar}} = qq$ : color  $3^{\text{bar}}$ , spin-parity  $0^+$ , flavor  $3^{\text{bar}}$  in SU(3)

$$U = [\bar{d}\bar{s}]_{C=3, J=0, F=3}, \quad D = [\bar{s}\bar{u}]_{3,0,3}, \quad S = [\bar{u}\bar{d}]_{3,0,3}$$

- diquark “meson”  $D D^{\text{bar}} \rightarrow$  tetra-quark

- di-diquark “baryon”  $D-D-q \rightarrow$  pentaquark

- tri-diquark “dibaryon”  $D^3 \rightarrow$  dibaryon

color 1, flavor 1, H dibaryon  $H = [\bar{U}\bar{D}\bar{S}]_A = [uuddss]$

- diquark matter: color superconductivity

$U^{\text{bar}} + D^{\text{bar}} + S^{\text{bar}}$  condensates: color-flavor locking (CFL)

$S^{\text{bar}}$ : 2SC (U<sup>bar</sup>: uSC D<sup>bar</sup>: dSC)



# Diquark

# Scalar diquark as a **new building block**.

$D^{\text{bar}} = qq$ : color  $3^{\text{bar}}$ , spin-parity  $0^+$ , flavor  $3^{\text{bar}}$  in SU(3)

$$U = [\bar{d}\bar{s}]_{C=3, J=0, F=3}, \quad D = [\bar{s}\bar{u}]_{3,0,3}, \quad S = [\bar{u}\bar{d}]_{3,0,3}$$

- diquark “meson”  $D D^{\text{bar}} \rightarrow$  tetra-quark

- di-diquark “baryon”  $D-D-q \rightarrow$  pentaquark

- tri-diquark “dibaryon”  $D^3 \rightarrow$  dibaryon

color 1, flavor 1, H dibaryon  $H = [\bar{U}\bar{D}\bar{S}]_A = [uuddss]$

- diquark matter: color superconductivity

$U^{\text{bar}} + D^{\text{bar}} + S^{\text{bar}}$  condensates: color-flavor locking (CFL)

$S^{\text{bar}}$ : 2SC (  $U^{\text{bar}}$ : uSC     $D^{\text{bar}}$ : dSC )



# Conclusion

- # Spectroscopy of heavy quark hadrons requires new concepts, i.e., multi-quark states, hadron molecules, heavy quark spin symmetry, diquark correlations, etc.
- # Heavy baryon spectroscopy is used for the di-quark spectroscopy.
- # In order to draw the complete picture of the heavy hadron spectrum, further experimental data are essential, both in quantity and in quality.
- # It is important to carry out various experimental methods using the facilities, such as Belle, BES ( $e^+e^-$  collider), JLab ( $e$ ), LHCb (hadron collider), J-PARC ( $p, \pi, K$ ), PANDA ( $p^{\text{bar}}$ ).