

Anomalies in Flavor Physics

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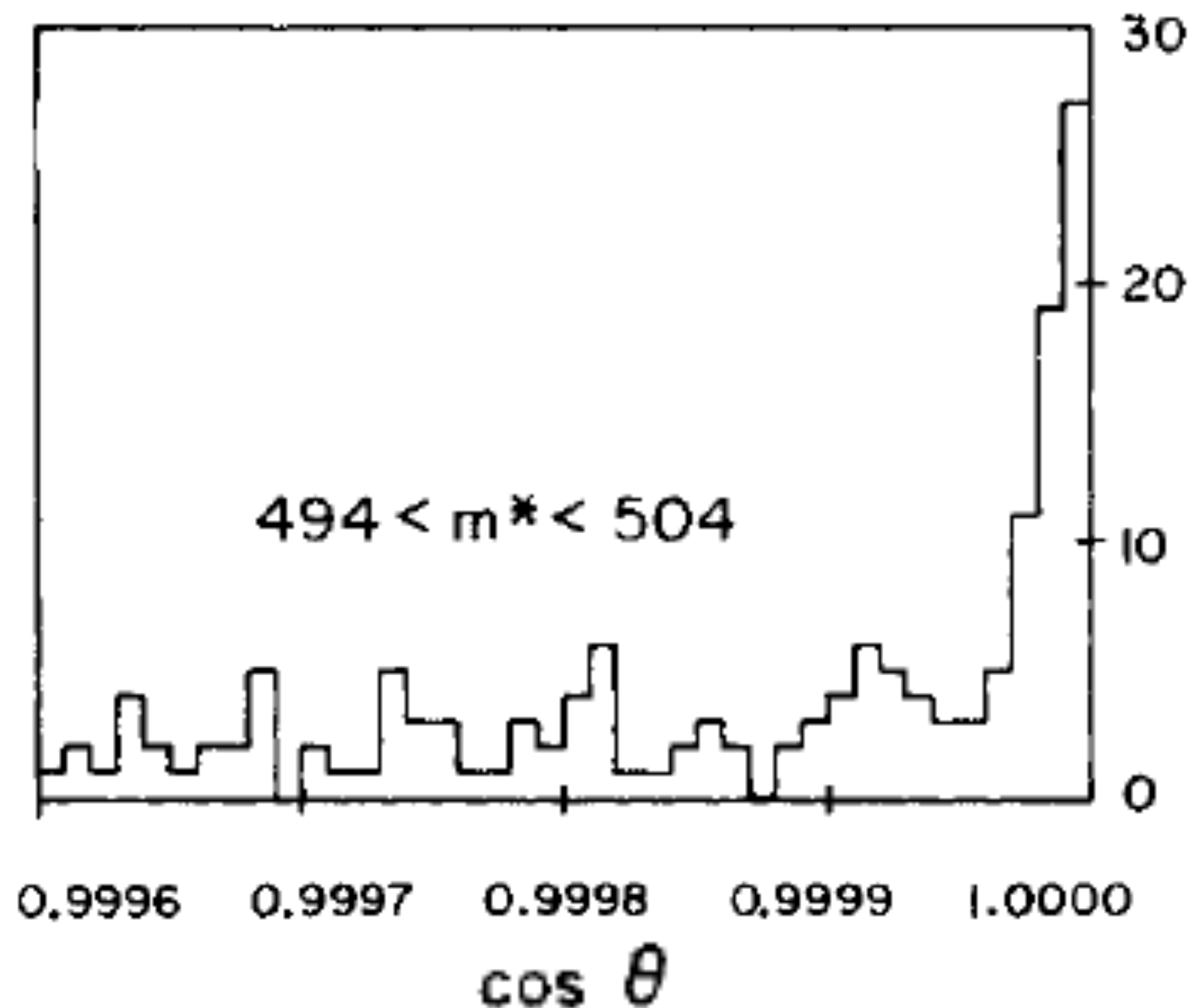
The 4th KMI school

- Statistical Data Analysis and Anomalies
in Particle Physics and Astrophysics -

Nagoya University, December 17, 2022



A historic flavor anomaly



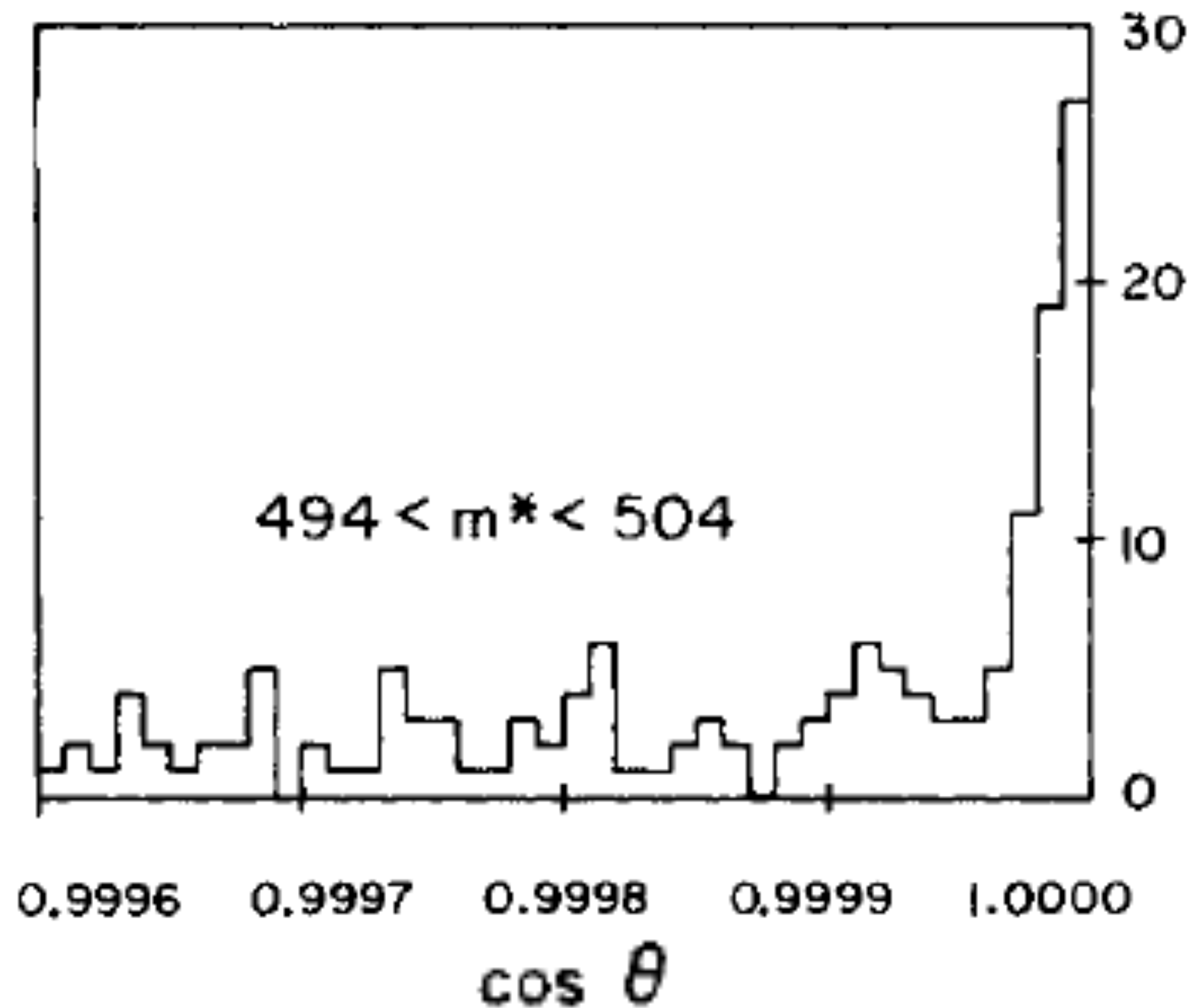
The relative efficiency for detection of the three-body K_2^0 decays compared to that for decay to two pions is 0.23. We obtain 45 ± 9 events in the forward peak after subtraction of background out of a total corrected sample of 22 700 K_2^0 decays.

22700 events \rightarrow event selection
 \rightarrow 45 signal with ± 9 uncertainty

$45/9 = 5\sigma$ peak in the last several bins

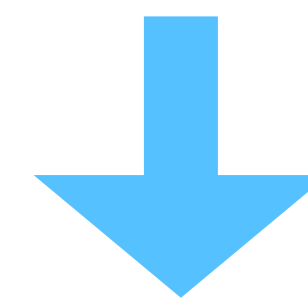
Then, what?

A historic flavor anomaly



[Christenson, Cronin, Fitch, Turlay. '64, PRL]

“Discovery of $K_L^0 \rightarrow \pi^+ \pi^-$ decay”
 corresponding to “discovery of CP violation”
 inconsistent with Weinberg-Salam theory



Kobayashi and Maskawa
 introduced the CKM matrix

prediction of c, b, t + CPV

... and this building was built

Thus, *Anomaly* had provided
 us great breakthroughs!



Kobayashi-Maskawa Institute

Statistical fluctuation

Let us consider **1,000,000** different experiments

2,700 experiments will provide 3σ deviation

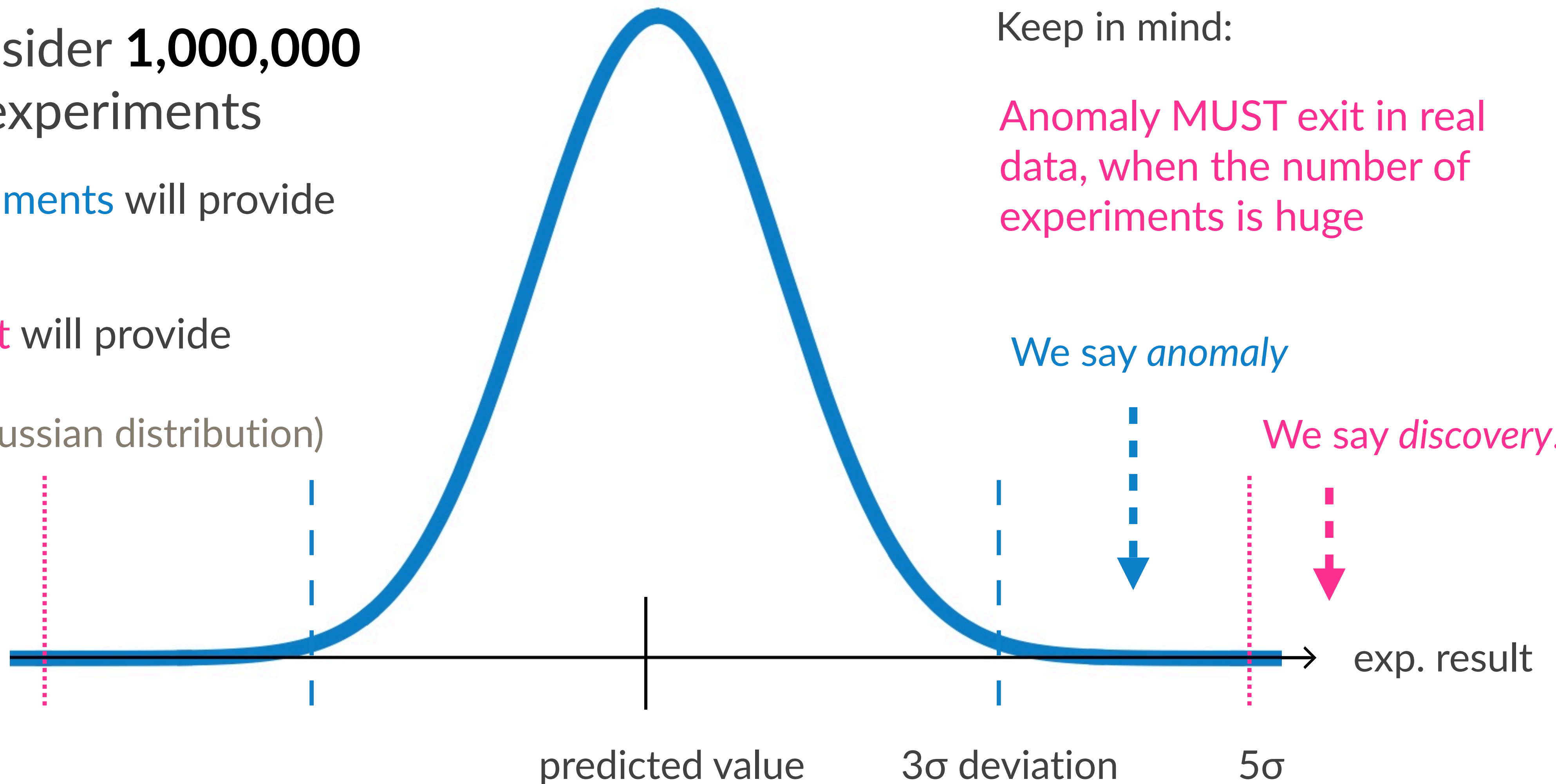
1 experiment will provide 5σ deviation
(assuming Gaussian distribution)

Keep in mind:

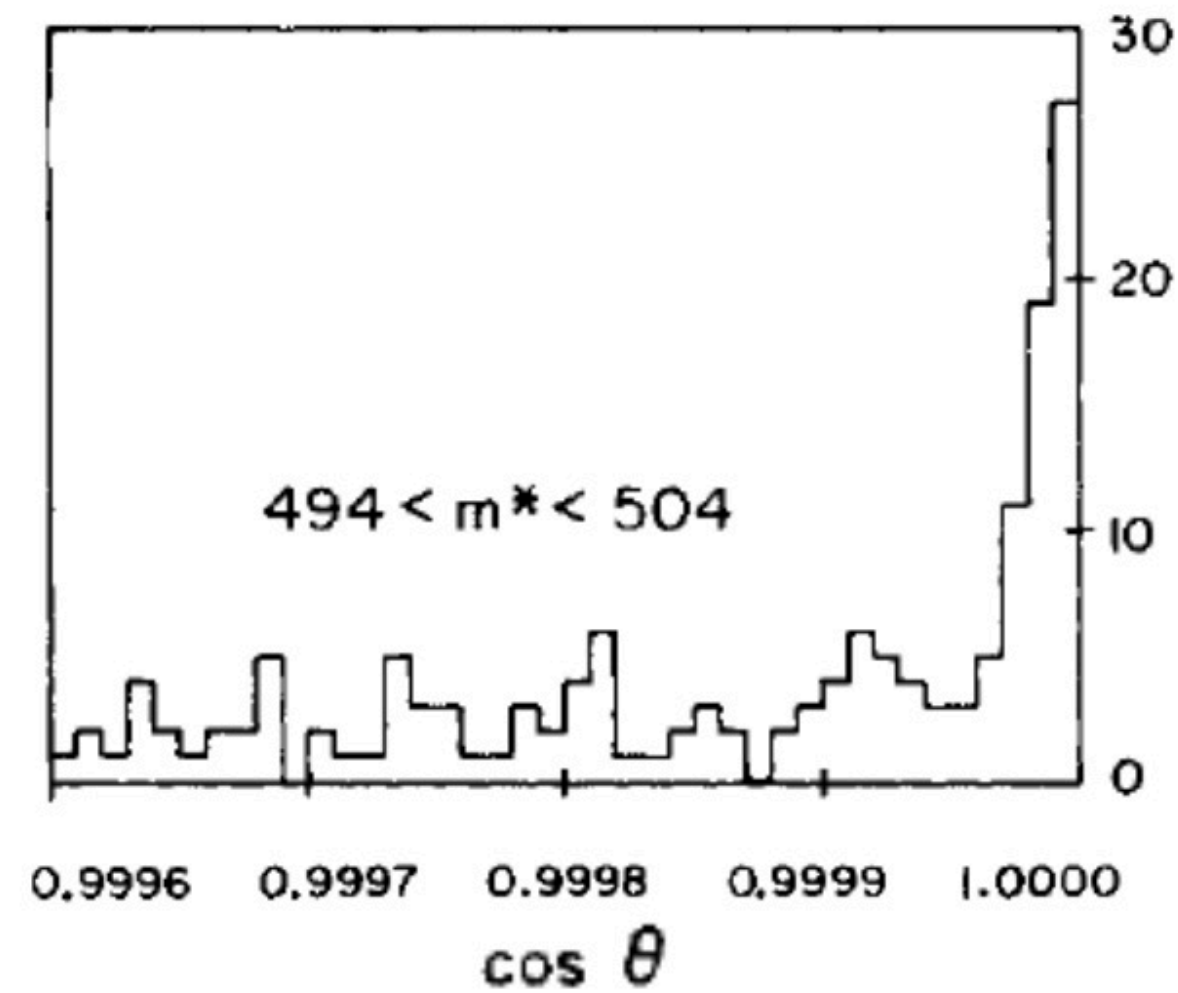
Anomaly **MUST** exist in real data, when the number of experiments is huge

We say *anomaly*

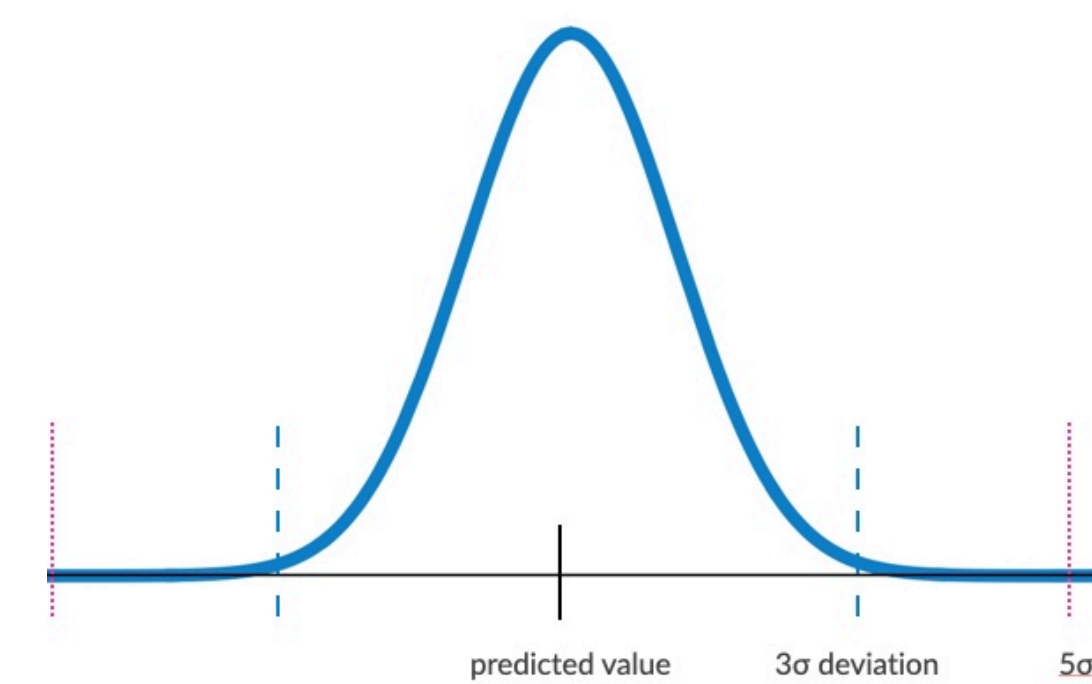
We say *discovery...*



Q. How to distinguish “new physics signal” from “fake anomaly”?



or



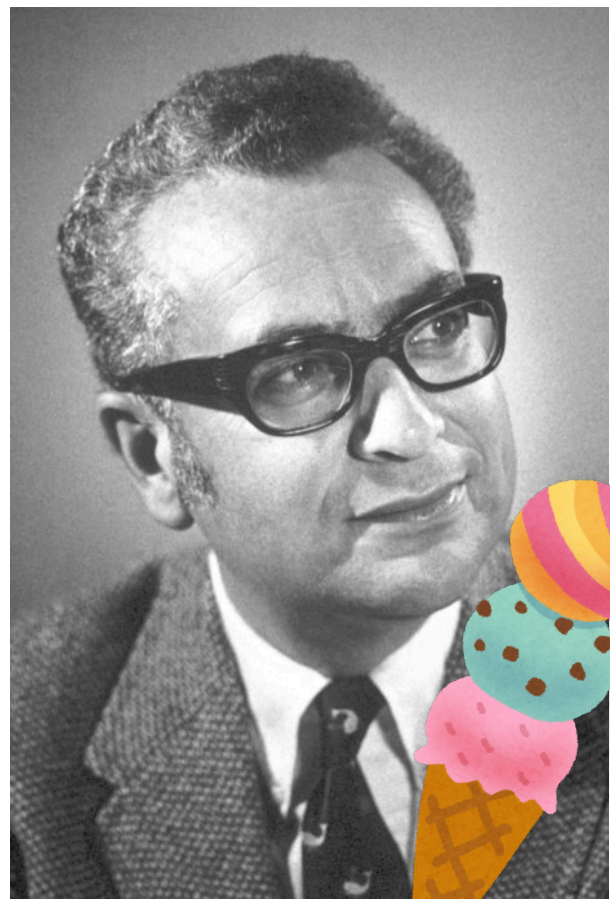
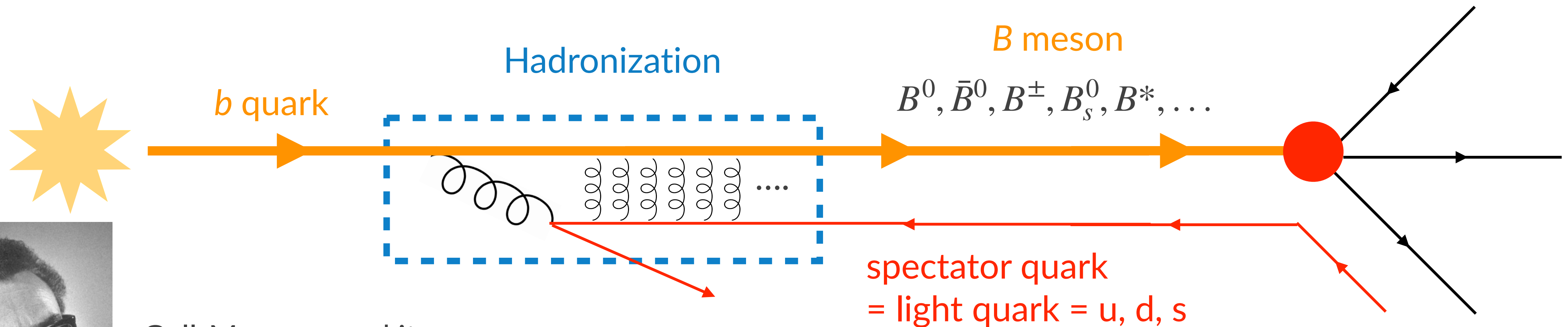
better strategies:

- 1, [exp-side] cross-checked by different collaborations or methods
- 2, [th-side] hidden theoretical correlation among several anomalies

What is flavor physics?

- ◆ Quarks cannot become the asymptotic field but must be contained in hadron=meson (or baryon) ***b* ... *B* meson**, ***c* ... *D* meson**, ***s* ... *K* meson**

decay by weak force



Gell-Mann named it “flavor” at an ice-cream store, just as ice-cream has both color and quark (cheese) flavor

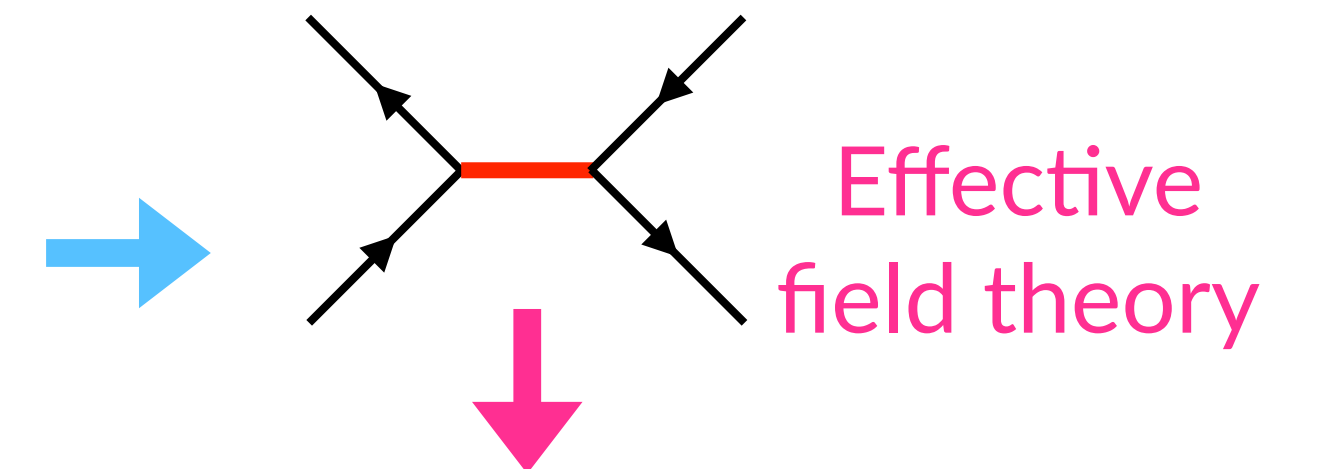
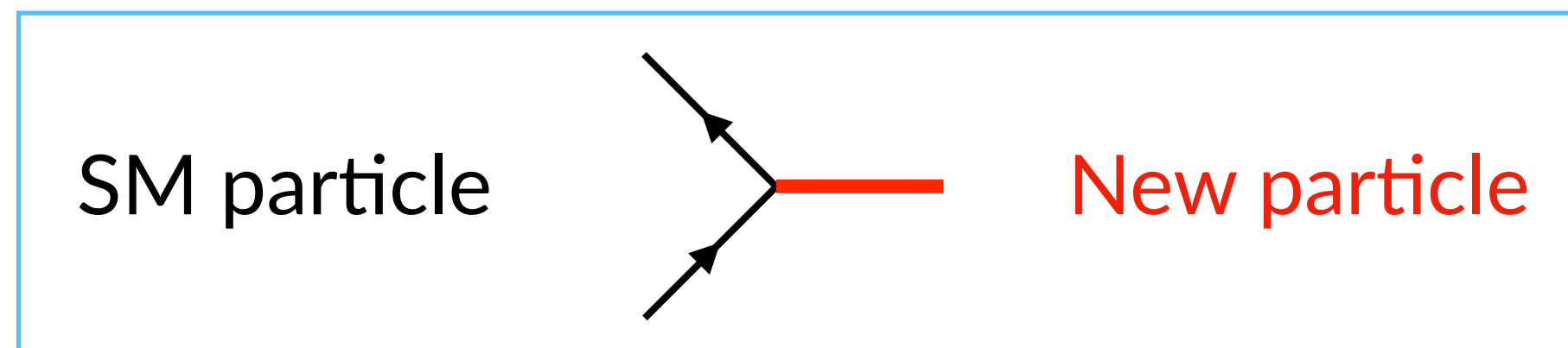
Quark flavor physics means physics of meson (or baryon) transition;

$$B \rightarrow K + X (b \rightarrow s), D \rightarrow \pi + X (c \rightarrow u), K \rightarrow \pi + X (s \rightarrow d), \text{ etc.}$$

High-energy vs. High-precision

- ◆ High-energy experiments and high-precision experiments can probe new physics (NP) by different and complementary ways

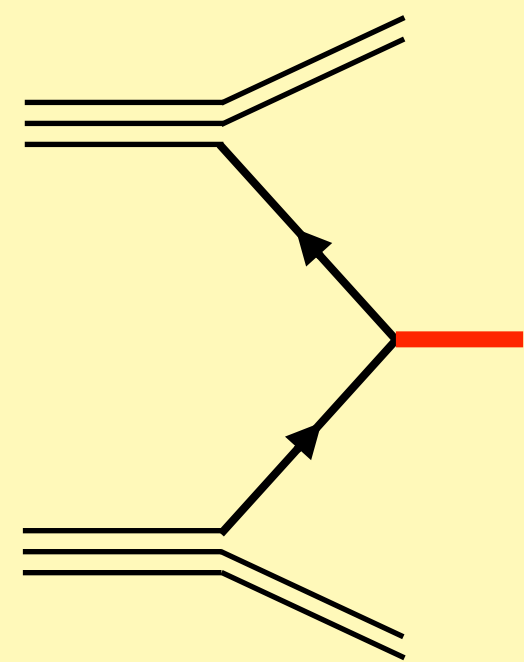
hunt a new interaction



Collider physics

High-energy frontier

$$\sqrt{s} > m_{NP}$$



complementary

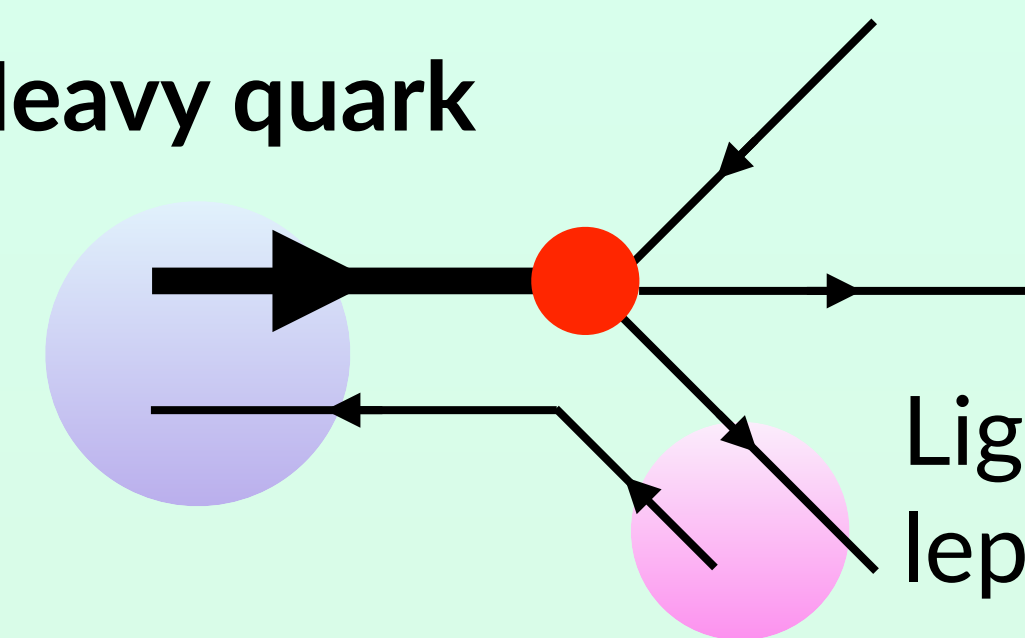
Precision measurement

High-intensity frontier



Small theoretical uncertainty

Heavy quark



Light meson, lepton

Good sensitivity to NP

B physics in B factory

- ◆ Rich phenomenology; CKM matrix, flavor-changing neutral current (FCNC), CP violation, tau lepton, **Lepton-flavor universality (LFU)**, Hadron spectroscopy, dark sector, etc.



BaBar experiment @ **SLAC**, physics run finished at **2008**

$$e^+e^- \rightarrow \Upsilon \rightarrow B\bar{B} \quad 10^8 B\bar{B} \text{ per year}$$



Belle and Belle II experiments @ **KEK**, Belle II started at **2019**

$$e^+e^- \rightarrow \Upsilon \rightarrow B\bar{B} \quad 10^{10} B\bar{B} \text{ per year}$$



LHCb experiment @ **CERN**, Run 3 started at **2022**

$$pp \rightarrow b\bar{b} \rightarrow B\bar{B} \quad 10^{12} b\bar{b} \text{ per year} \quad (\text{large event but large bkg})$$

newcomer!



CMS experiment will become B factory at Run 3 (called **B-parking**),
Run 2 data [$10^{10} (b \rightarrow \mu X)\bar{b}$] will be shown near future

CKM matrix

- ◆ Cabibbo-Kobayashi-Maskawa (CKM) matrix arises the relative misalignment between the Yukawa matrices and gauge interactions:

$$\mathcal{L} \supset -\frac{g}{\sqrt{2}} \bar{u}_L^i \gamma^\mu d_L^j W_\mu^+ \xrightarrow{\text{mass-eigenbasis}} -\frac{g}{\sqrt{2}} \bar{u}_L^i \gamma^\mu (U_u^\dagger U_d)^{ij} d_L^j W_\mu^+ \\ = -\frac{g}{\sqrt{2}} \bar{u}_L^i \gamma^\mu V_{\text{CKM}}^{ij} d_L^j W_\mu^+$$

- ◆ In the SM, the CKM matrix appears only through weak force

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

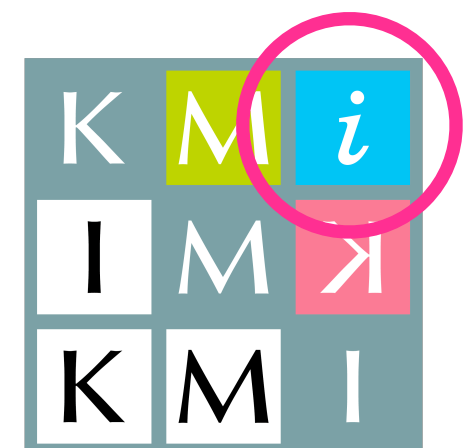
SM (Kobayashi-Maskawa) prediction:

must be **unitary matrix**

3 mixing angles and

1 CP-violating (CPV) phase

phase is here



Kobayashi-Maskawa Institute

Unitarity of CKM matrix

- ◆ Each component of the CKM matrix can be measured without assuming the unitarity
 - ➔ One can test the CKM unitarity conditions from data

$$V_{\text{CKM}} = \begin{pmatrix} \text{\color{red} β decays} & \text{K meson decays} & \text{B meson decays} \\ V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ \text{D meson decays} & V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

K and B mesons mixing,
K and B mesons FCNC

$$VV^\dagger = \mathbb{I}_3 \text{ or } \neq \mathbb{I}_3?$$

SM NP?



CKM unitarity triangle

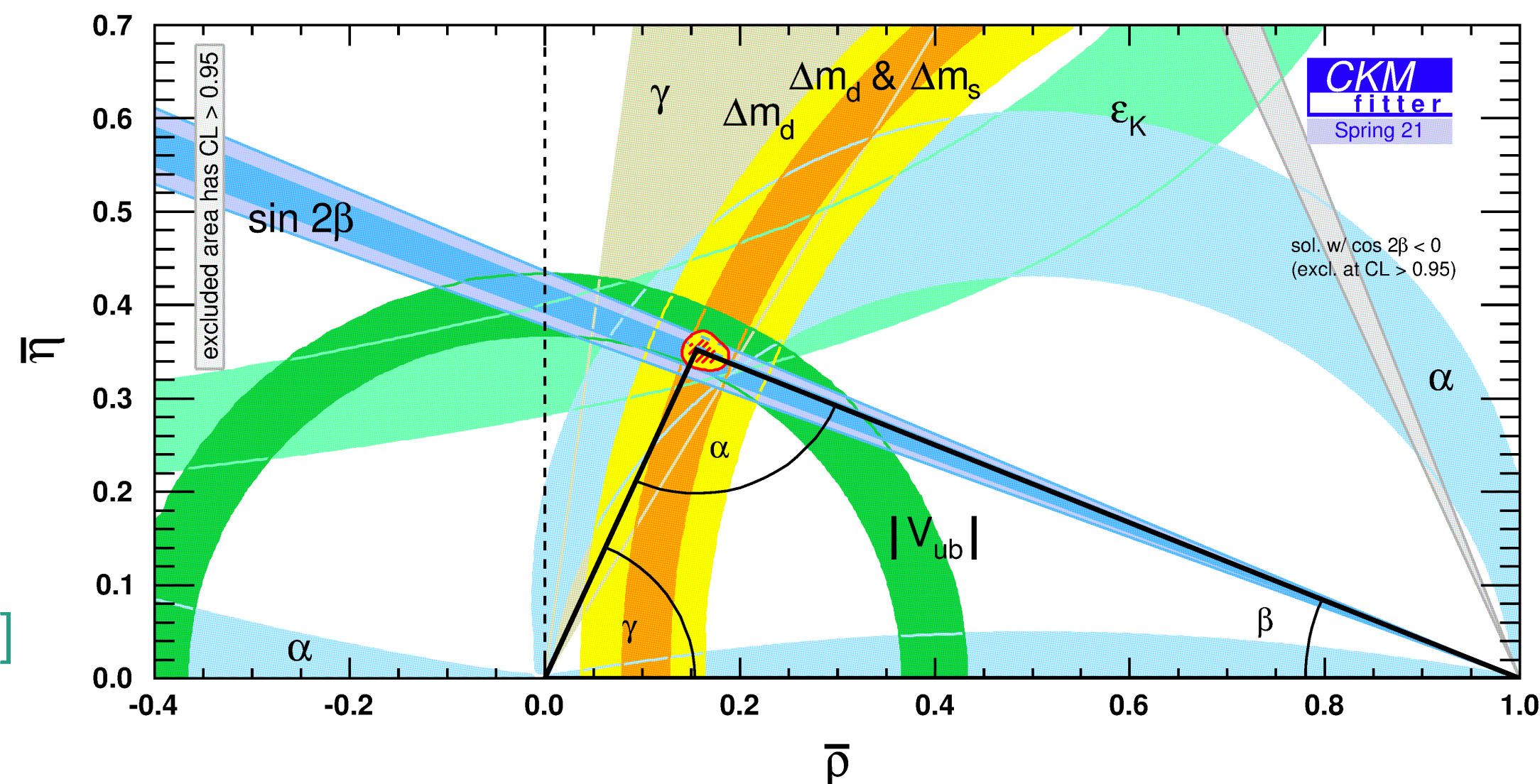
$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Unitarity condition

$$V^\dagger V = \mathbb{I}_3$$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

A triangle can be drawn on a complex plane



[CKM fitter 2021]

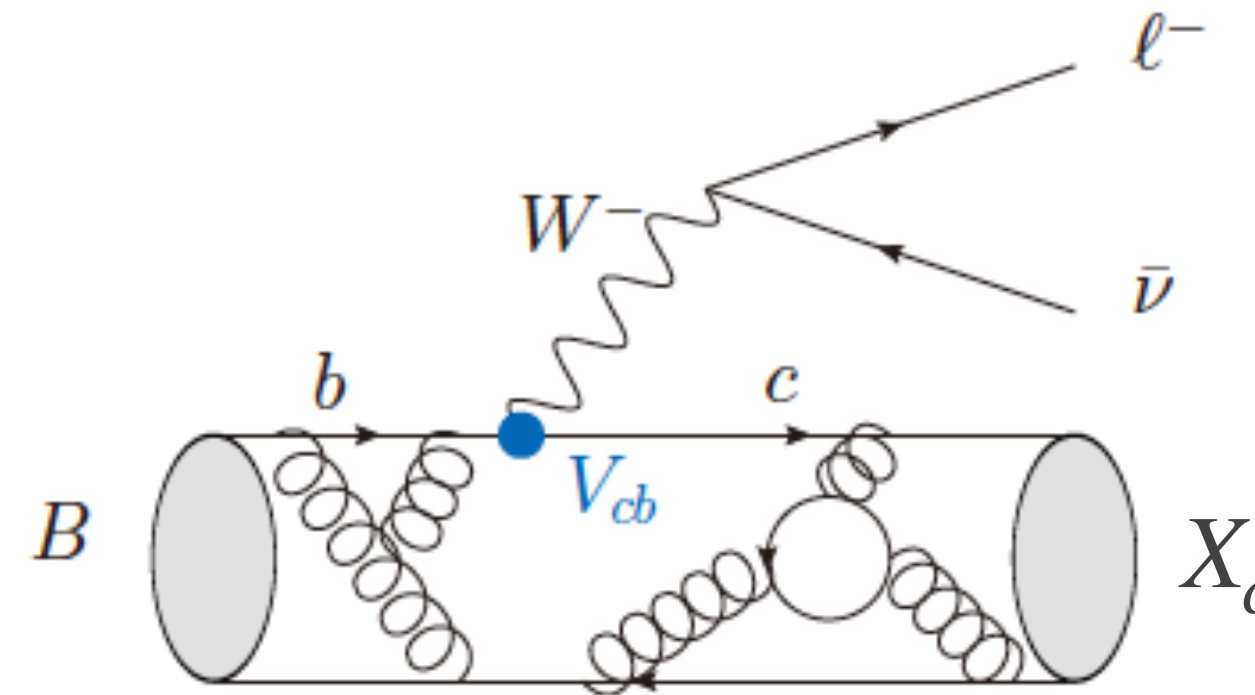
B triangle

$$\begin{array}{ccc} V_{ud}V_{ub}^* \sim \lambda^3 & \alpha & V_{td}V_{tb}^* \sim \lambda^3 \\ & \gamma & \beta \\ V_{cd}V_{cb}^* \sim \lambda^3 & & \end{array}$$

Many data are available! Currently, they are consistent with the triangle

$b \rightarrow c$ [$B \rightarrow X_c, D, D^*$] semileptonic decays

- ◆ Comparing measured BR to the theoretical formulae **determines** $|V_{cb}|$



$$\ell = e, \mu + \tau$$

- ◆ Inclusive decays: $B \rightarrow X_c \ell \nu$

Inclusive hadron states
 $X_c = D^{**}, D^*, D, D\pi,$
 $D\pi\pi\dots$

- ◆ The heavy quark effective theory: $b \rightarrow c \ell \nu + \mathcal{O}(\alpha_s, \Lambda_{\text{QCD}}/m_b)$ with non-perturbative elements
- ◆ Last data in 2010 (BaBar) & no lattice \rightarrow Belle II result coming soon [Belle II, 2205.06372], the first lattice study [Gambino, Hashimoto, '20]

- ◆ Exclusive decays: $B \rightarrow D \ell \nu, B \rightarrow D^* \ell \nu$

- ◆ Hadronization is relevant; channel-dependent form factor, difficult SM prediction
- ◆ Many data and many lattice results are available

Exclusive decays: $B \rightarrow D\ell\nu, B \rightarrow D^*\ell\nu$ [HFLAV 2021; based on CLN]

$B \rightarrow D\ell\nu$

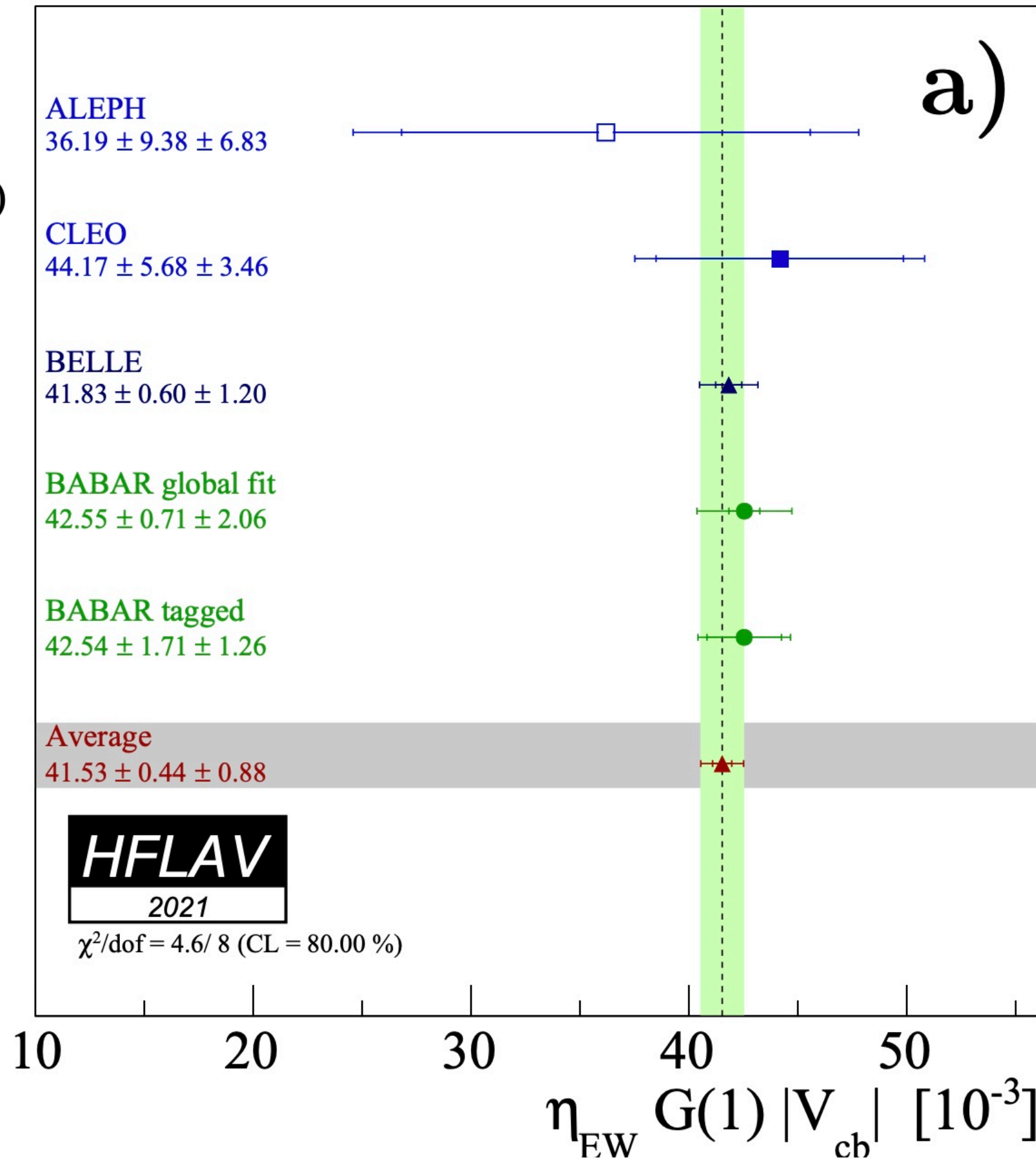
$B \rightarrow D^*\ell\nu$

$\chi^2/\text{dof} = 4.6/8$ (CL = 80.00 %)

9 input data
(D^0 and D^\pm)
1 parameter fit
→ dof = 9-1=8

total $\chi^2 = 4.6$

P value = 0.80

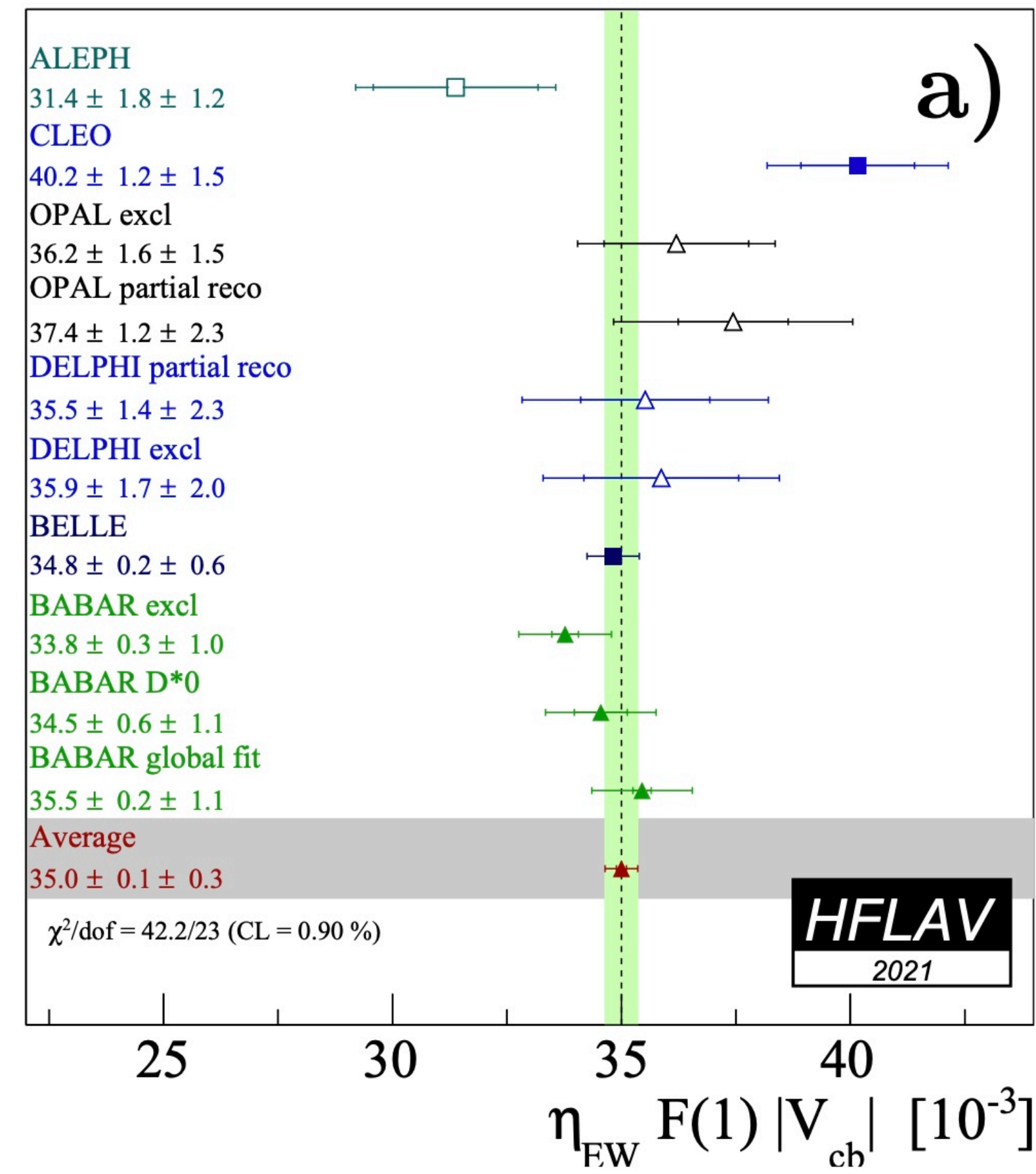


$\chi^2/\text{dof} = 42.2/23$ (CL = 0.90 %)

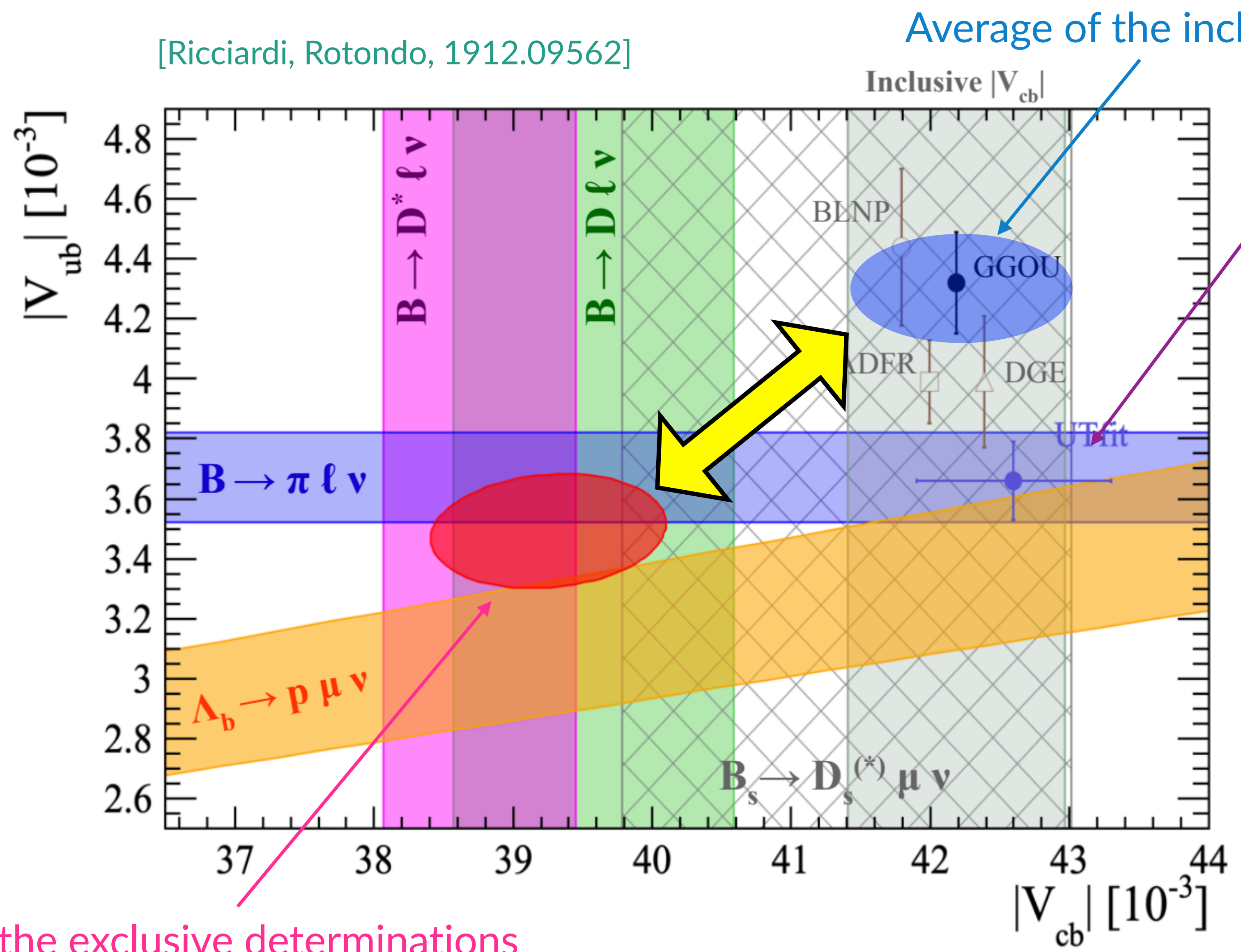
24 input data
(D^{*0} and $D^{*\pm}$)
→ dof = 23

total $\chi^2 = 42.2$

P value = 0.009



[Ricciardi, Rotondo, 1912.09562]



CKM unitarity

Kaon physics prefers inclusive V_{cb}

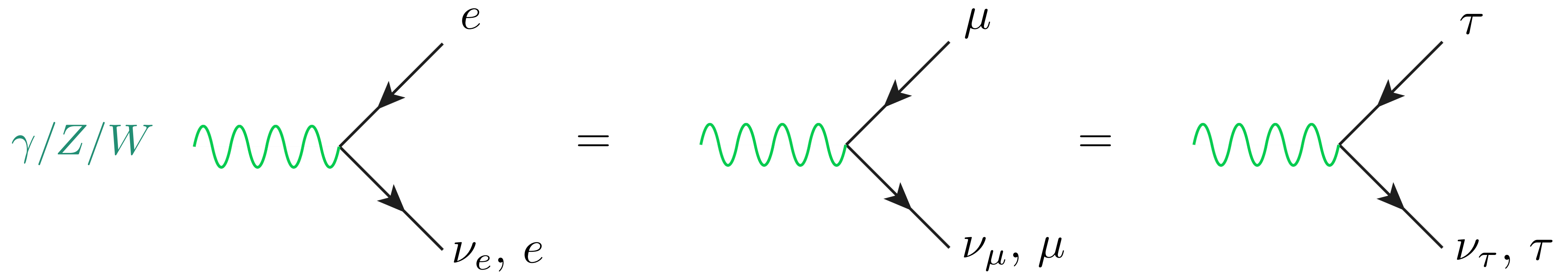
3.3 σ tension between inclusive vs exclusive determinations of V_{cb} and V_{ub} (exclusive violates the CKM unitarity condition)

But, NP interpretation is not easy

Average of the exclusive determinations

Test of Lepton Flavor Universality (LFU)

- ◆ Gauge symmetry predicts lepton flavor universal (LFU) phenomena:



- ◆ Only charged-lepton mass violates the LFU within the SM

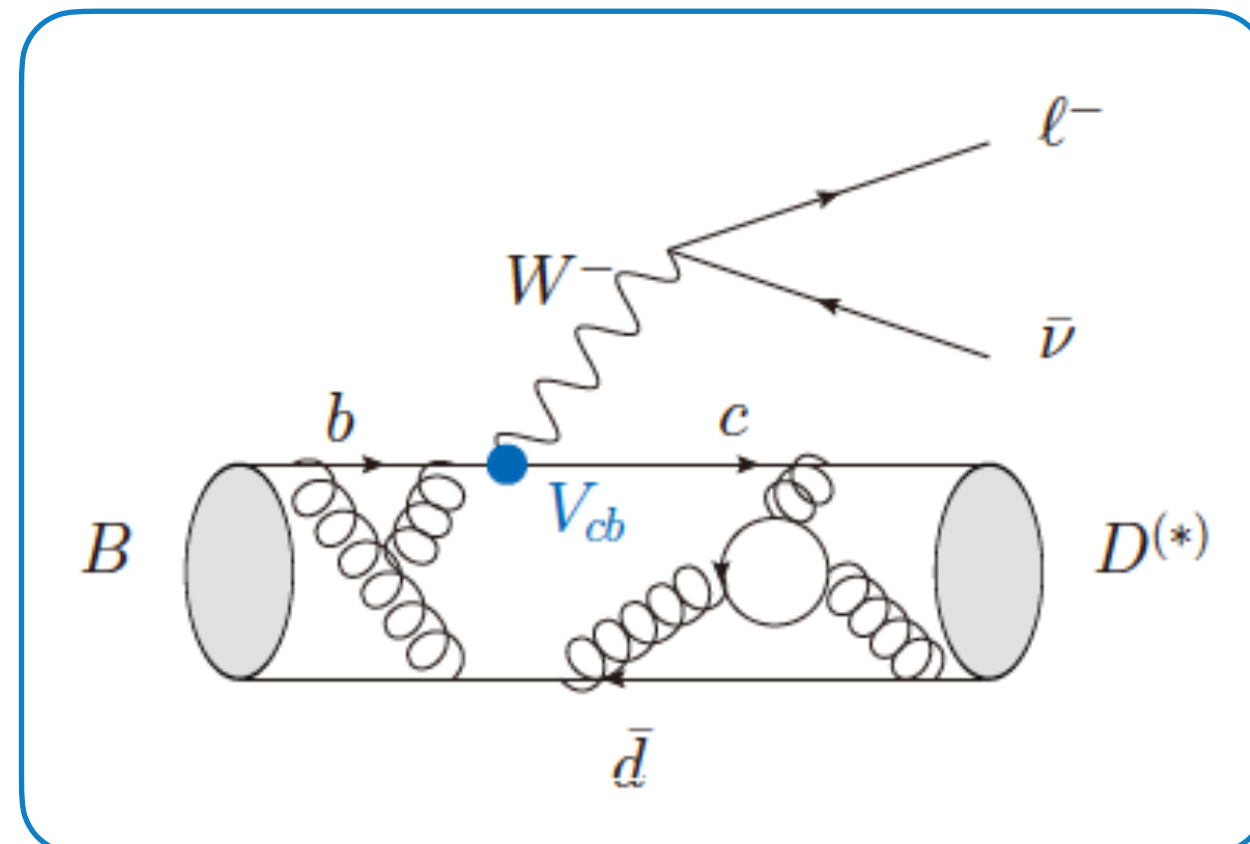
$$m_e = 0.5 \text{ MeV}, \quad m_\mu = 105 \text{ MeV}, \quad m_\tau = 1776 \text{ MeV}$$

Lepton-flavor-universality observables $R(D)$ and $R(D^*)$

[HFLAV 2022+, [Iguro, TK, Watanabe, 2210.10751]]

$$R(D^{(*)}) = \frac{\text{BR}(B \rightarrow D^{(*)} \bar{\tau} \nu_{\tau})}{\text{BR}(B \rightarrow D^{(*)} \bar{\ell} \nu_{\ell})}$$

($\ell = e, \mu$)



Experiment	R_{D^*}	R_D	Correlation
BaBar	$0.332 \pm 0.024 \pm 0.018$	$0.440 \pm 0.058 \pm 0.042$	-0.27
Belle	$0.293 \pm 0.038 \pm 0.015$	$0.375 \pm 0.064 \pm 0.026$	-0.49
Belle	$0.270 \pm 0.035^{+0.028}_{-0.025}$	-	-
Belle	$0.283 \pm 0.018 \pm 0.014$	$0.307 \pm 0.037 \pm 0.016$	-0.51
LHCb	$0.280 \pm 0.018 \pm 0.029$	-	-
LHCb	$0.281 \pm 0.018 \pm 0.024$	$0.441 \pm 0.060 \pm 0.066$	-0.43
World average	$0.285 \pm 0.010 \pm 0.008$	$0.358 \pm 0.025 \pm 0.012$	-0.29

10 measurements with correlations and 2 parameter fit

→ dof = 10 - 2 = 8

total $\chi^2 = 9.2$

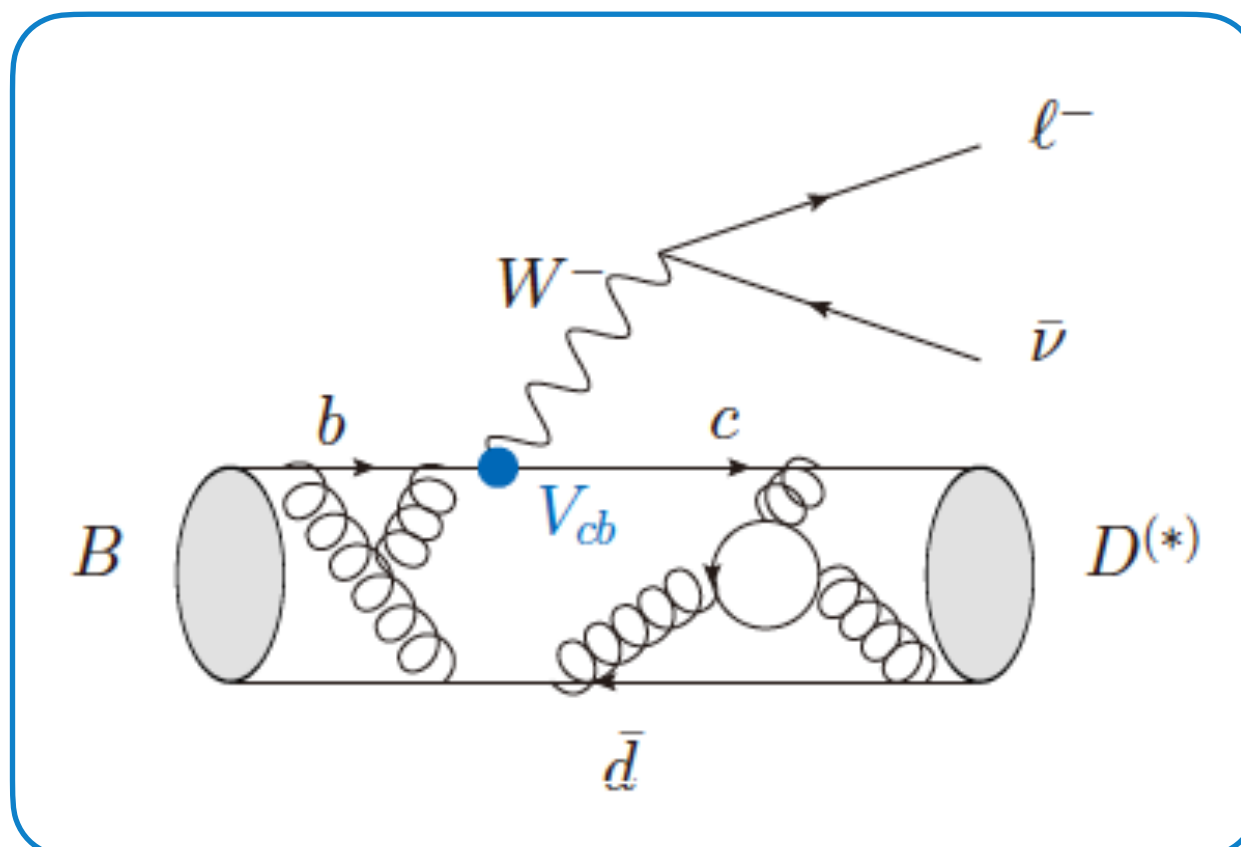
P value = 0.32; means data are consistent

Lepton-flavor-universality observables $R(D)$ and $R(D^*)$

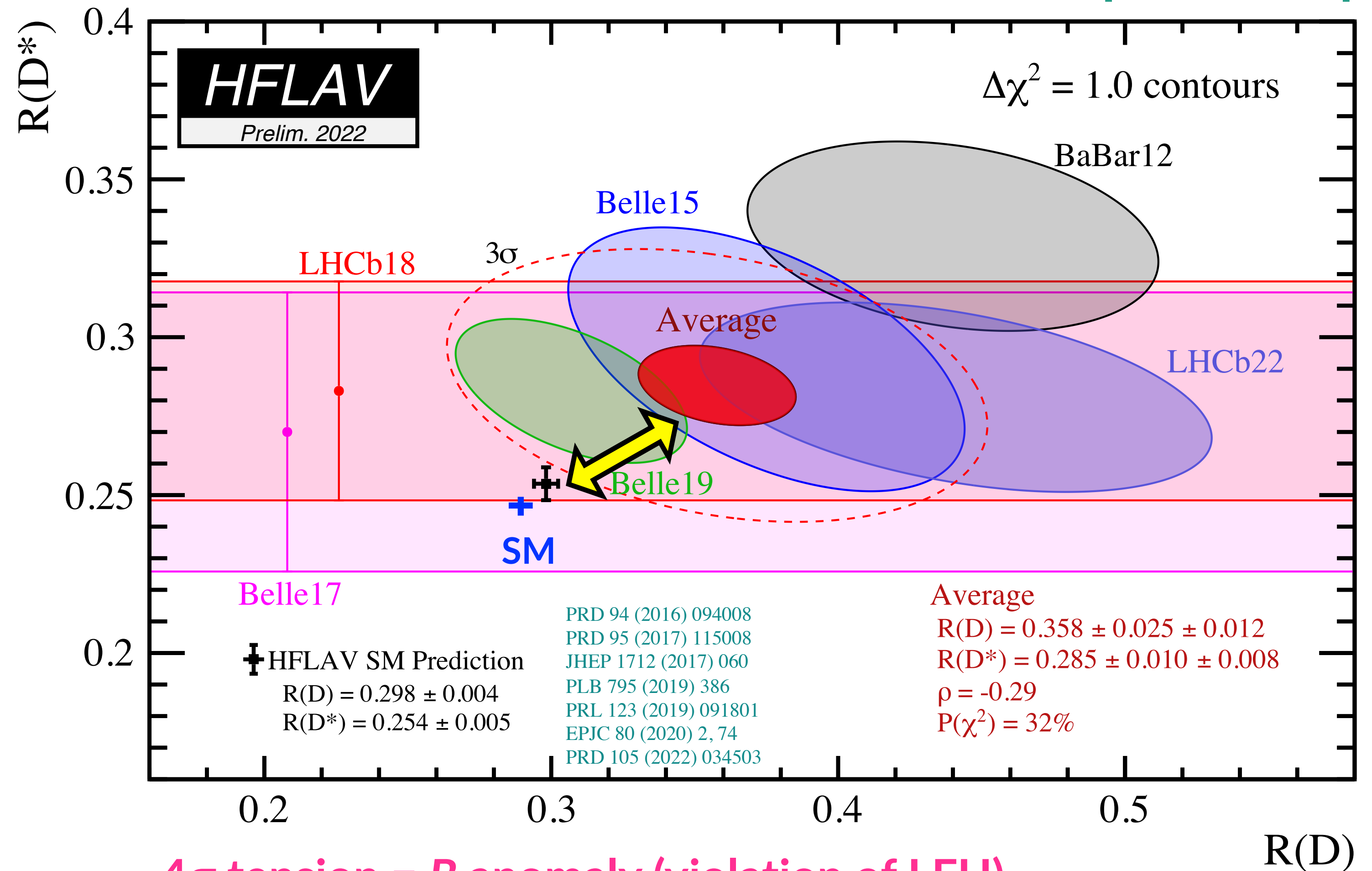
[HFLAV 2022+]

$$R(D^{(*)}) = \frac{\text{BR}(B \rightarrow D^{(*)} \bar{\tau} \nu_{\tau})}{\text{BR}(B \rightarrow D^{(*)} \bar{\ell} \nu_{\ell})}$$

($\ell = e, \mu$)



$b \rightarrow c \tau \nu$ anomaly

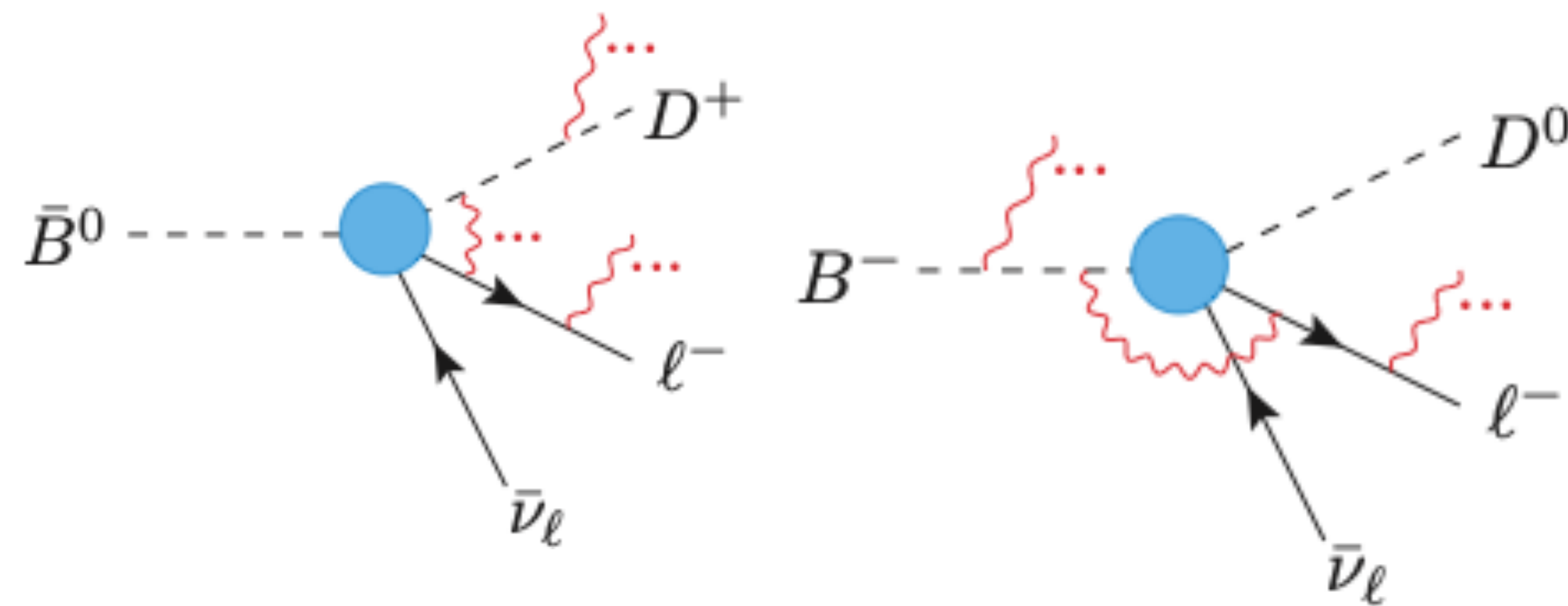


$\sim 4\sigma$ tension = B anomaly (violation of LFU)

QED correction within the SM

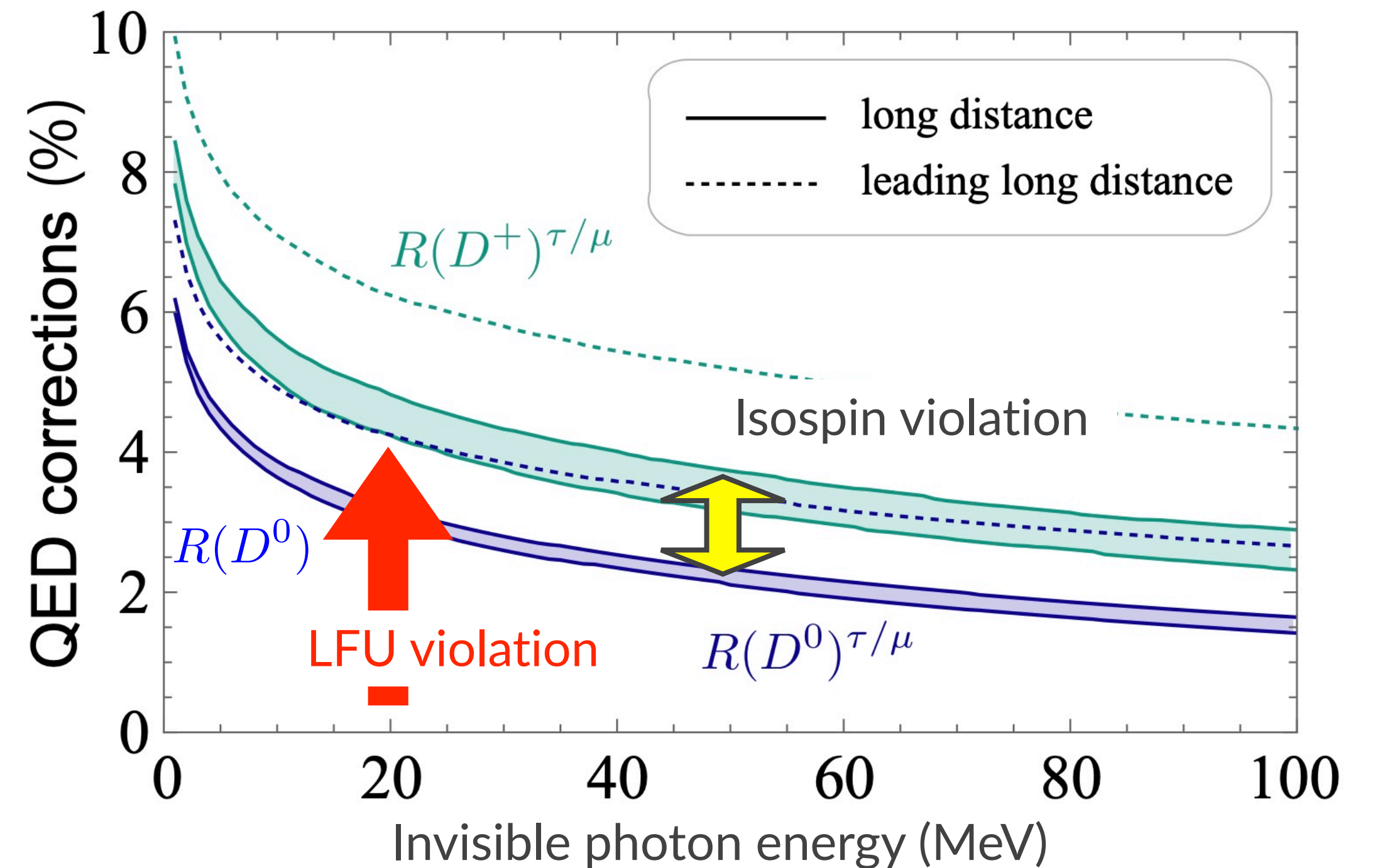
- ◆ Long-distance QED correction could violate the lepton flavor universality

[de Boer, TK, Nisandzic, Phys.Rev.Lett. '18] + [Calí, Klaver, Rotondo, Sciascia, '19; Isidori, Nabeebaccus, Zwicky, '20]



We found that the QED corrections depend on the lepton velocities; non-rela τ vs relativistic μ

Improvement on theory (SM) prediction



[de Boer, TK, Nisandzic, Phys.Rev.Lett. '18]

Single new-particle interpretations

- ◆ W'
- ◆ **Severely constrained** from ΔM_s , $W' \rightarrow \tau\nu$ search [Abdullah, Calle, Dutta, Flores, Restrepo, [1805.01869](#)] and $Z' \rightarrow \tau\tau$ search [Faroughy, Greljo, Kamenik, [1609.07138](#)]
- ◆ **Charged-Higgs with generic flavor structure**
- ◆ **Constrained** from $B_c \rightarrow \tau\nu$ and $H^\pm \rightarrow \tau\nu$ search **but still allowed** [Iguro, Tobe, [1708.06176](#); Iguro, [2201.06565](#)]
- ◆ **Leptoquark**
- ◆ Collider bound comes from $gg \rightarrow LQ LQ^*$, and **broad parameter regions are still allowed**

Single new-particle interpretations

[Iguro, TK, Watanabe, [2210.10751](https://arxiv.org/abs/2210.10751)]

	Spin	Charge	Operators	R_D	R_{D^*}	LHC	Flavor
	0	$(\mathbf{1}, \mathbf{2}, 1/2)$	O_{S_L}	✓	✓	$b\tau\nu$	$B_c \rightarrow \tau\nu, F_L^{D^*}, P_\tau^D, M_W$
LQ	0	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	O_{V_L}, O_{S_L}, O_T	✓	✓	$\tau\tau$	$\Delta M_s, P_\tau^D, B \rightarrow K^{(*)}\nu\nu$
LQ	0	$(\mathbf{3}, \mathbf{2}, 7/6)$	$O_{S_L}, O_T, (O_{V_R})$	✓	✓	$b\tau\nu, \tau\tau$	$R_{\Upsilon(nS)}, P_\tau^{D^*}, M_W$
LQ	1	$(\mathbf{3}, \mathbf{1}, 2/3)$	O_{V_L}, O_{S_R}	✓	✓	$b\tau\nu, \tau\tau$	$R_{K^{(*)}}, R_{\Upsilon(nS)}, B_s \rightarrow \tau\tau$
LQ	1	$(\bar{\mathbf{3}}, \mathbf{2}, 5/6)$	O_{S_R}	✓	2σ	$\tau\tau$	$B_s \rightarrow \tau\tau, M_W$

One can distinguish each model by these channels

New idea: LFU violation in Υ (Upsilon) decay

- ◆ $\Upsilon(nS)$ [$n=1,2,3$] leptonic decays can provide new LFU observable ($b\bar{b} \rightarrow \tau\bar{\tau}$)

$$R_{\Upsilon(nS)} = \frac{\mathcal{B}(\Upsilon(nS) \rightarrow \tau^+\tau^-)}{\mathcal{B}(\Upsilon(nS) \rightarrow \ell^+\ell^-)},$$

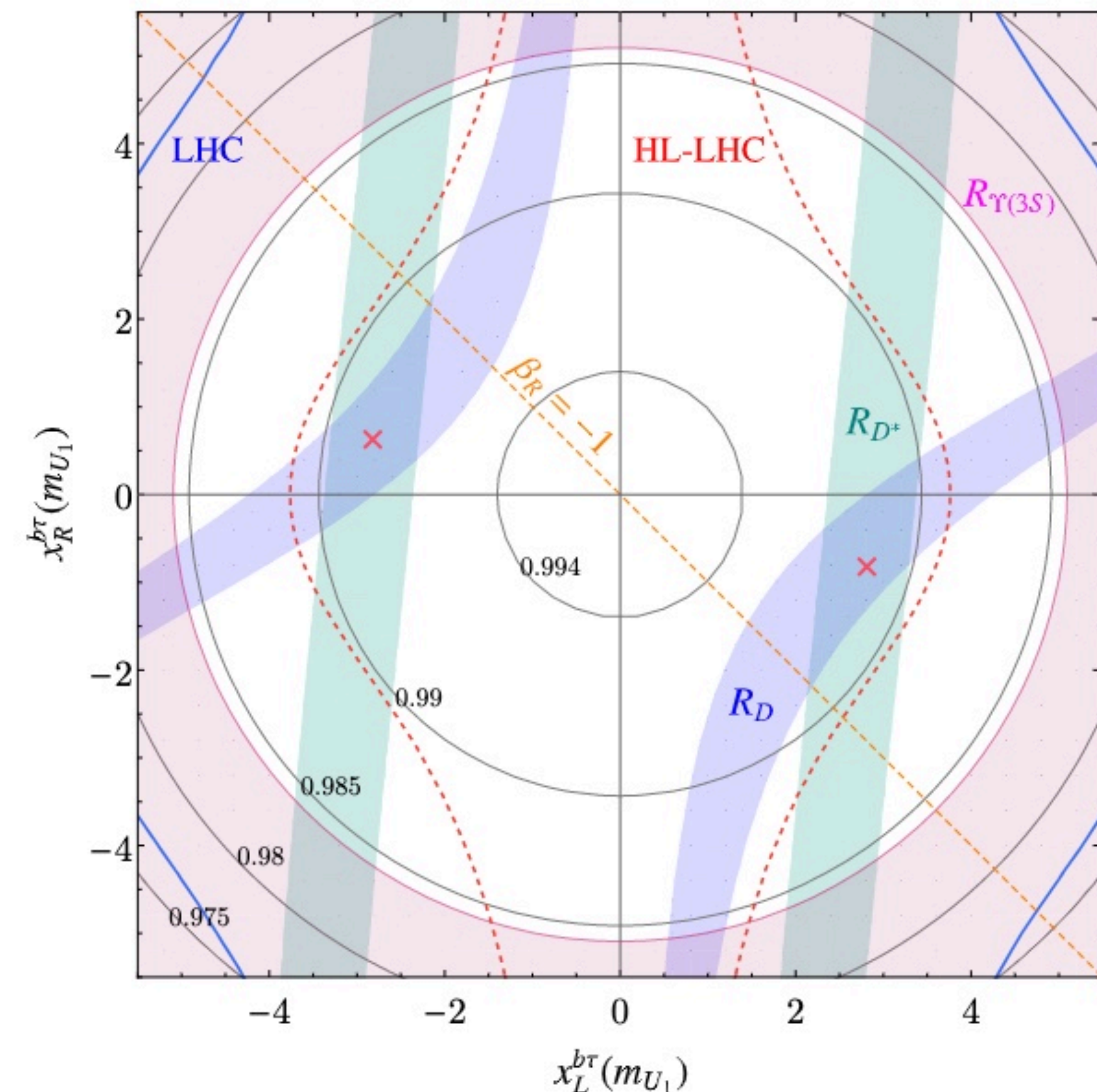
$$R_{\Upsilon(3S)}^{\text{SM}} = 0.9948 \pm \mathcal{O}(10^{-5}),$$

$$R_{\Upsilon(3S)}^{\text{exp}} = 0.968 \pm 0.016. \quad [\text{CLEO+BaBar data}]$$

- ◆ Belle II will measure it [$n=2$] very precisely
- ◆ less than 1% accuracy is needed

Correlation in the U_1 LQ scenario

[Iguro, TK, Watanabe, [2210.10751](https://arxiv.org/abs/2210.10751)]



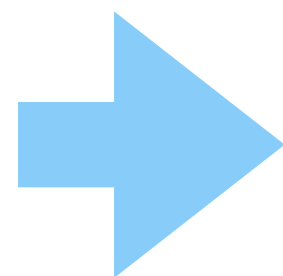
Sum rule between $R(\Lambda_c)$ and $R(D)$, $R(D^*)$

- ◆ Baryonic counterpart ($b \rightarrow c\tau\nu$): $\mathcal{R}(\Lambda_c) = \frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda_c^+ \ell^- \bar{\nu}_\ell)}$
- ◆ There is a **model-independent sum rule** for $R(D)$, $R(D^*)$, and $R(\Lambda_c)$, through new physics form factor analysis (originated from heavy quark symmetry)

$$\frac{R(\Lambda_c)}{R(\Lambda_c)_{\text{SM}}} \simeq 0.26 \frac{R(D)}{R(D)_{\text{SM}}} + 0.74 \frac{R(D^*)}{R(D^*)_{\text{SM}}} \quad [\text{Fedele, Blanke, Crivellin, Iguro, TK, Nierste, Watanabe, [2211.14172](#)}]$$

It can crosscheck of $R(D^{(*)})$ anomaly by coherent amplification of $R(\Lambda_c)$

$R(D^{(*)})$
anomaly



$$R(\Lambda_c) = 0.380 \pm 0.012 R(D^{(*)}) \pm 0.005_{\text{FF}}$$

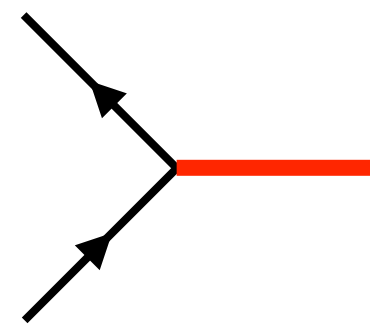
$$R(\Lambda_c)_{\text{SM}} = 0.324 \pm 0.004$$

$$R(\Lambda_c)_{\text{exp}} = 0.242 \pm 0.075 \quad [\text{LHCb: 2201.03497}]$$

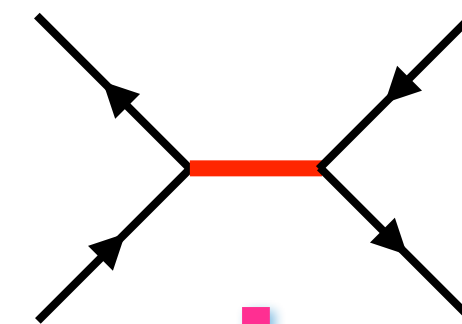
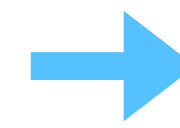
A slight ($\sim 2\sigma$)
inconsistency appeared

hunt a new interaction

SM particle



New particle

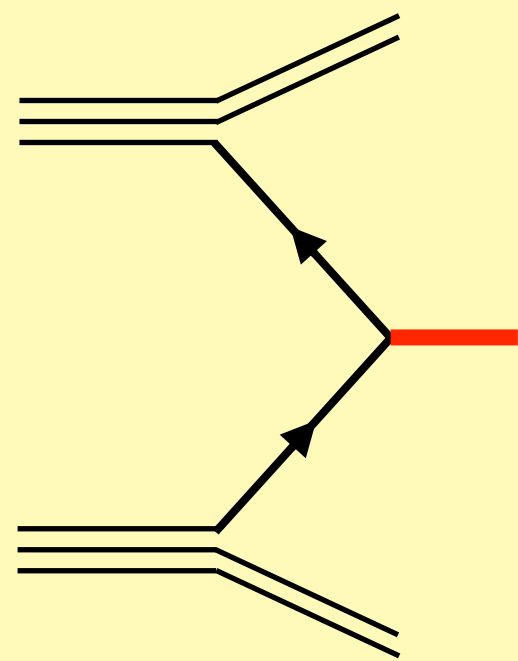


Effective field theory



Collider physics

$$\sqrt{s} > m_{NP}$$

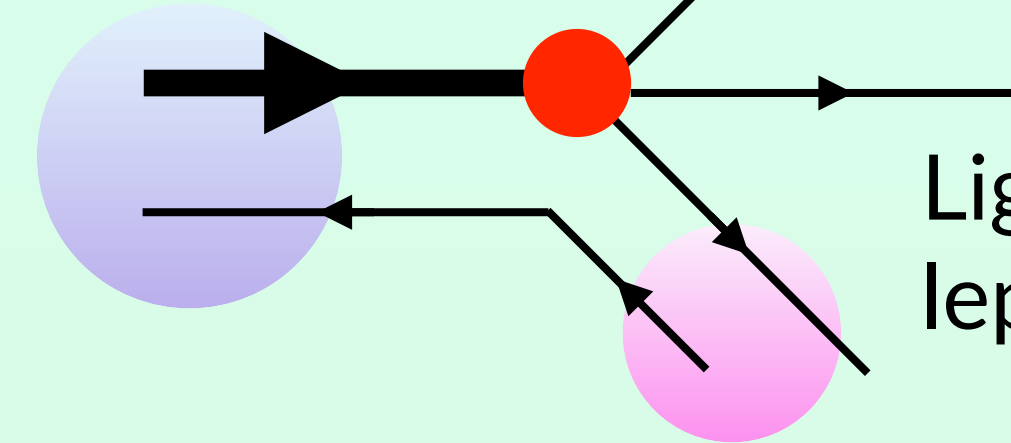


complementary

Precision measurement

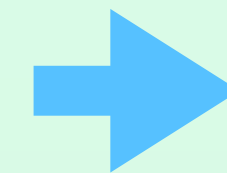


Heavy quark

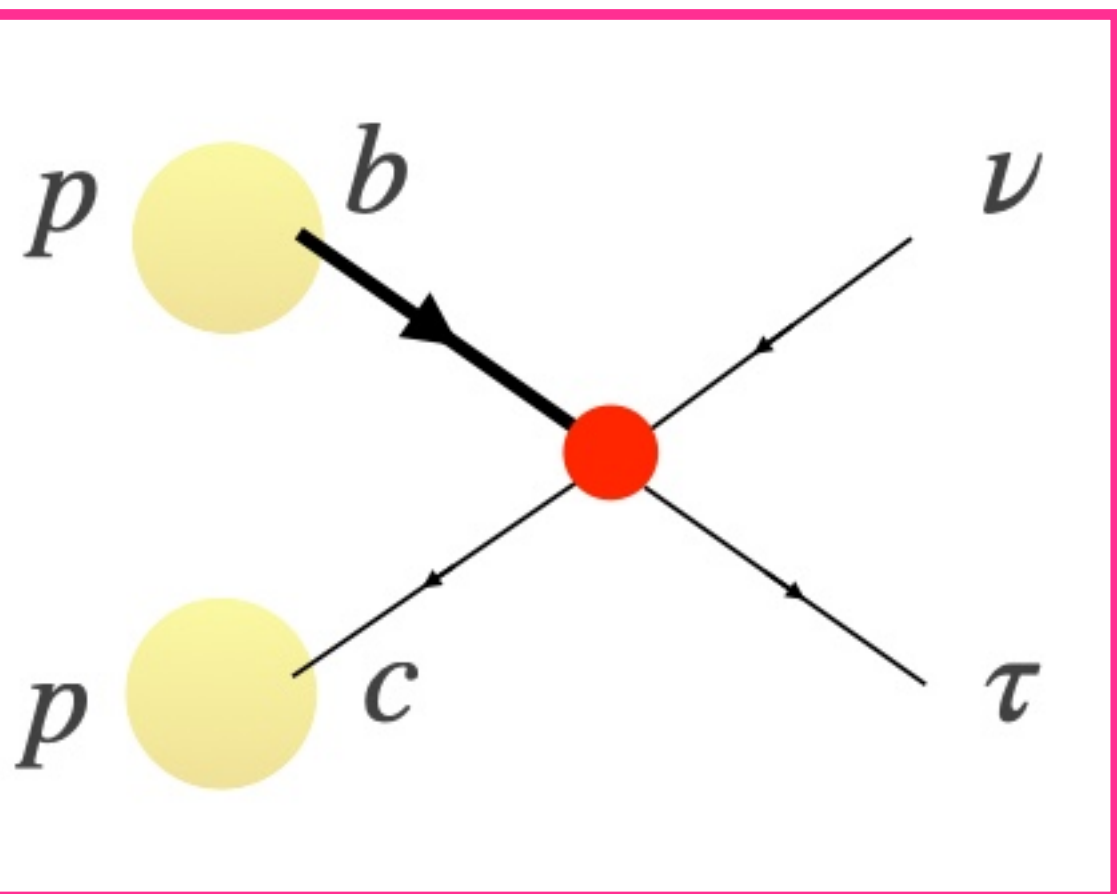


Light meson, lepton

Small theoretical uncertainty



Good new physics sensitivity

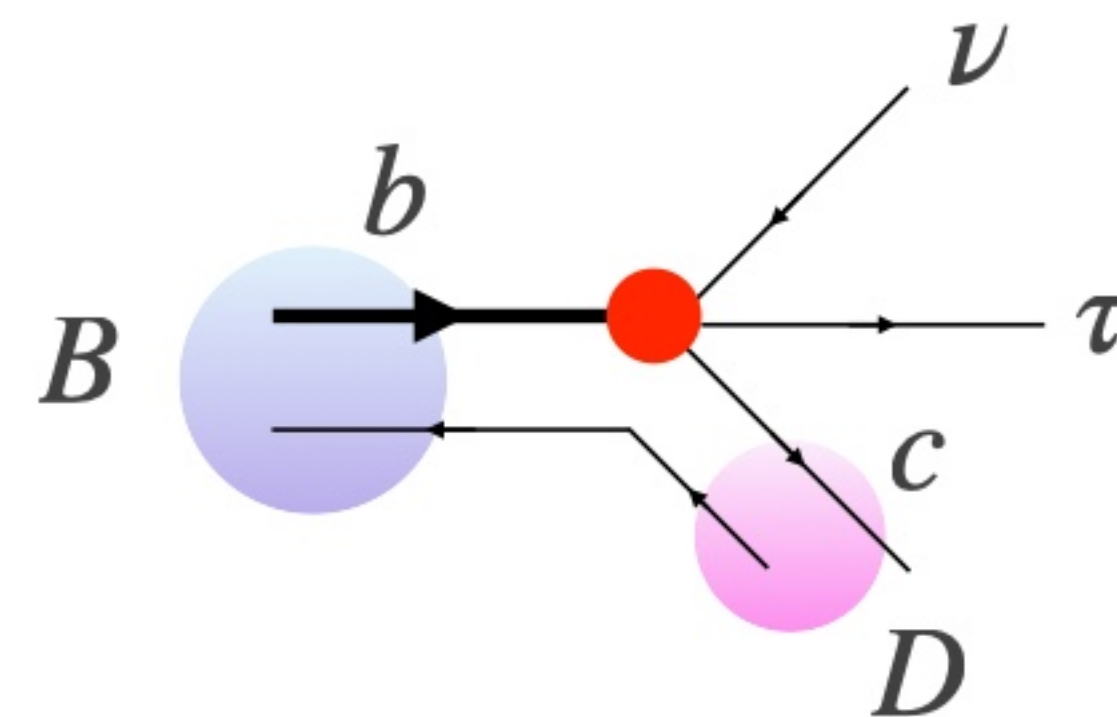


non-resonance search
→ new study direction

Crossing symmetry



Direct connection



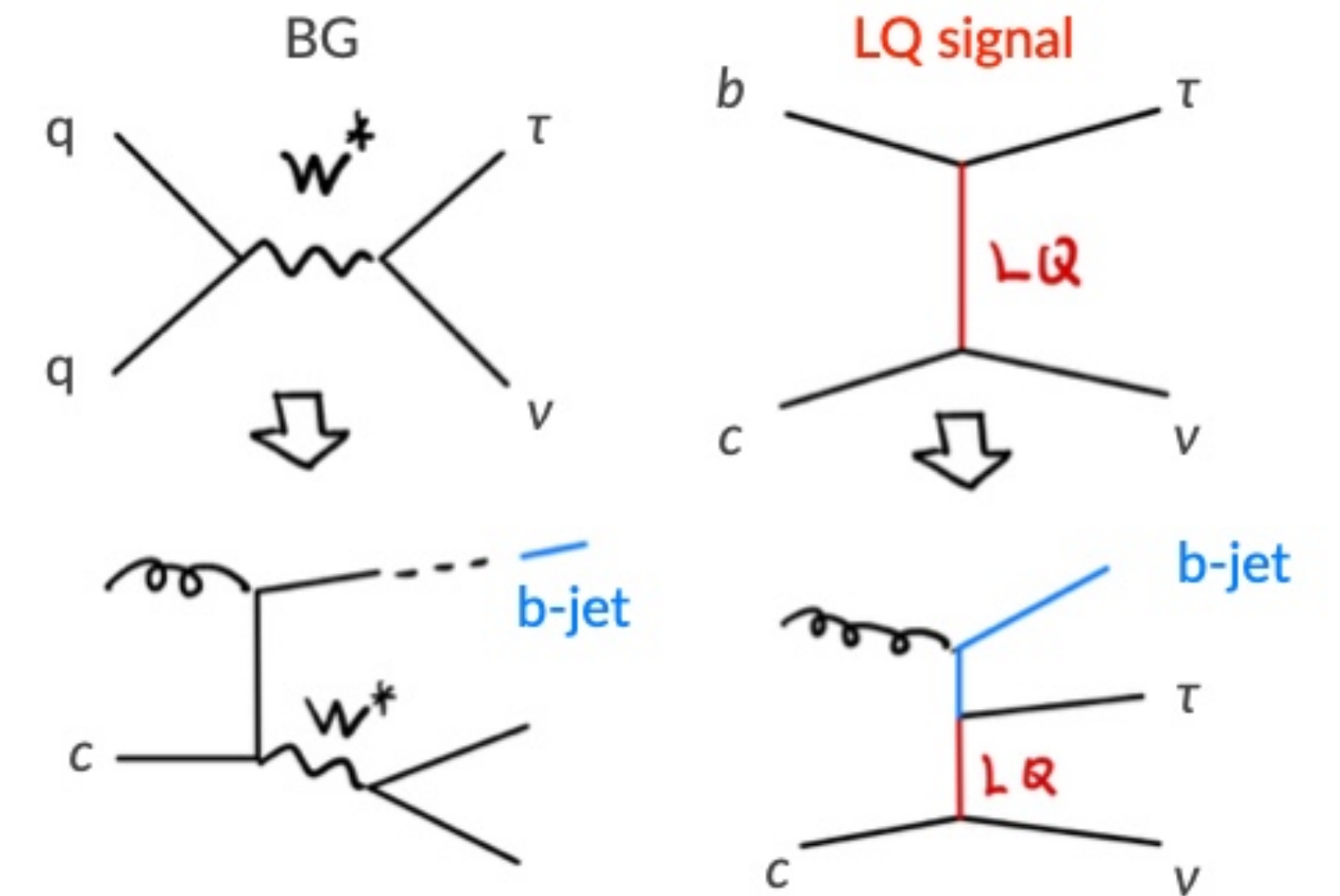
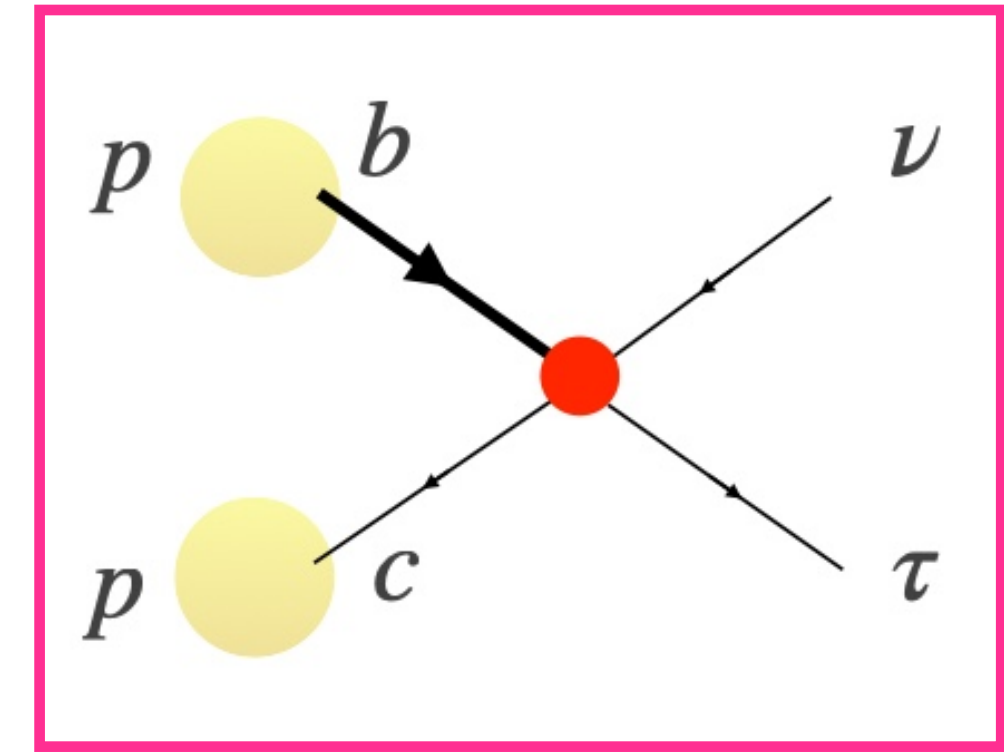
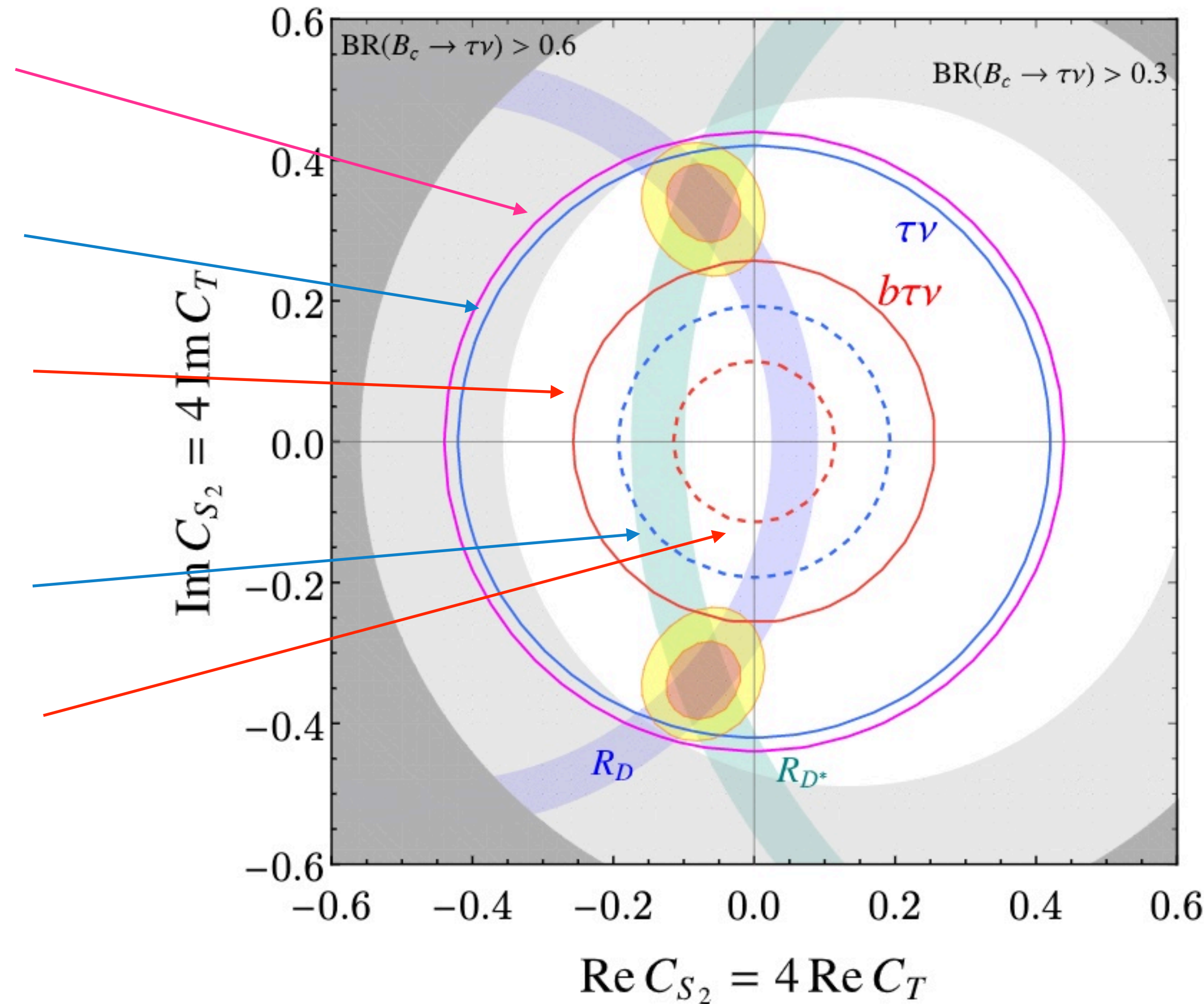
B anomaly!

LQ indirect collider search

[Endo, Iguro, TK, Takeuchi, Watanabe [2111.04748](#)]

$$M_{R_2 LQ} = 2.5 \text{ TeV}$$

- τ +MET search
36fb⁻¹ exclusion
- τ +MET search
139fb⁻¹ sensitivity
- τ +MET+b search
139fb⁻¹ sensitivity
- τ +MET search
3000fb⁻¹ sensitivity
- τ +MET+b search
3000fb⁻¹ sensitivity



+b jet suppresses only bkg

R₂ LQ scenario can be probed by $b\tau$ +MET search with Run 2 data

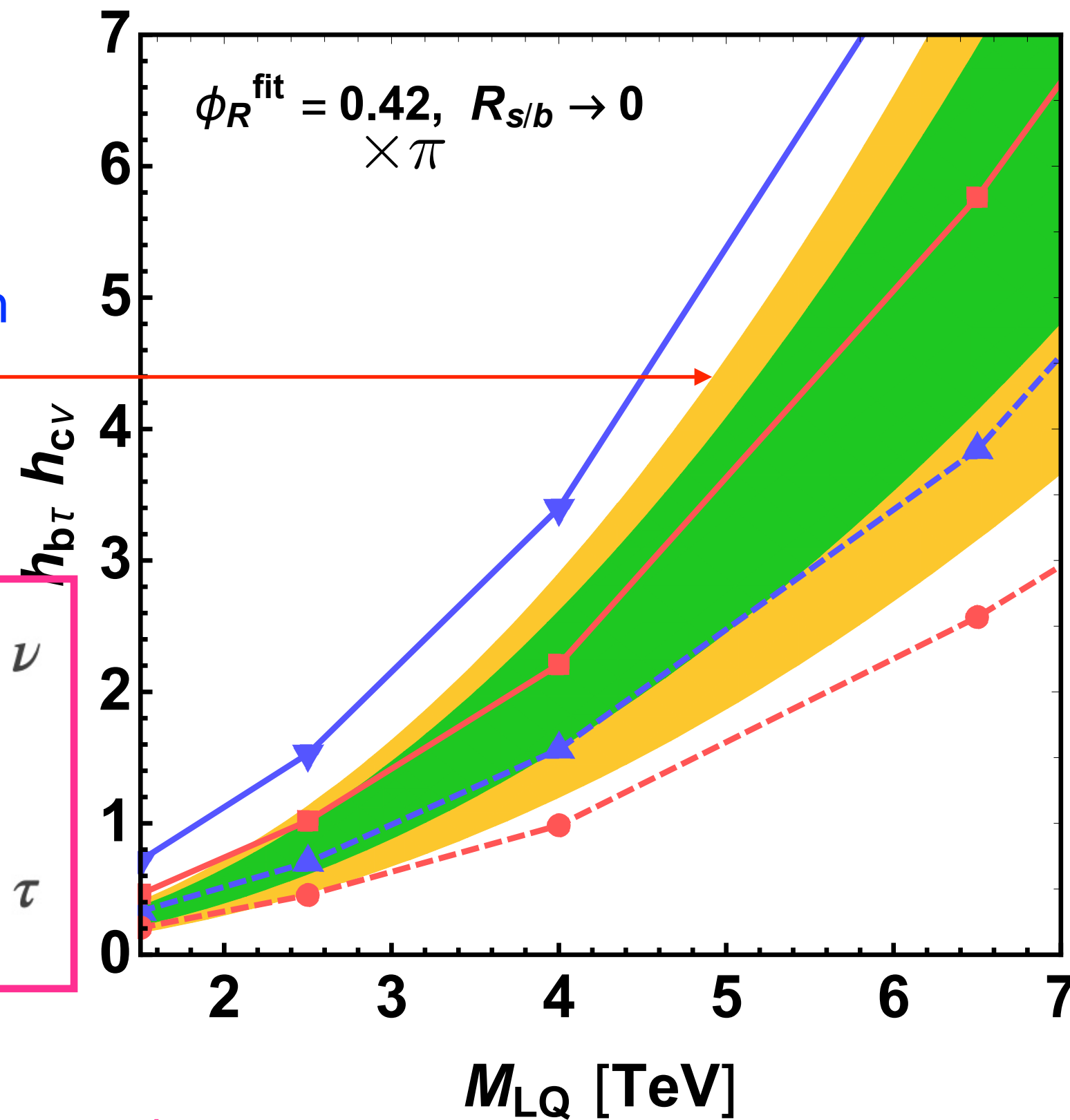
U₁ Leptoquark scenario: comparison

See also Nobe-san's talk

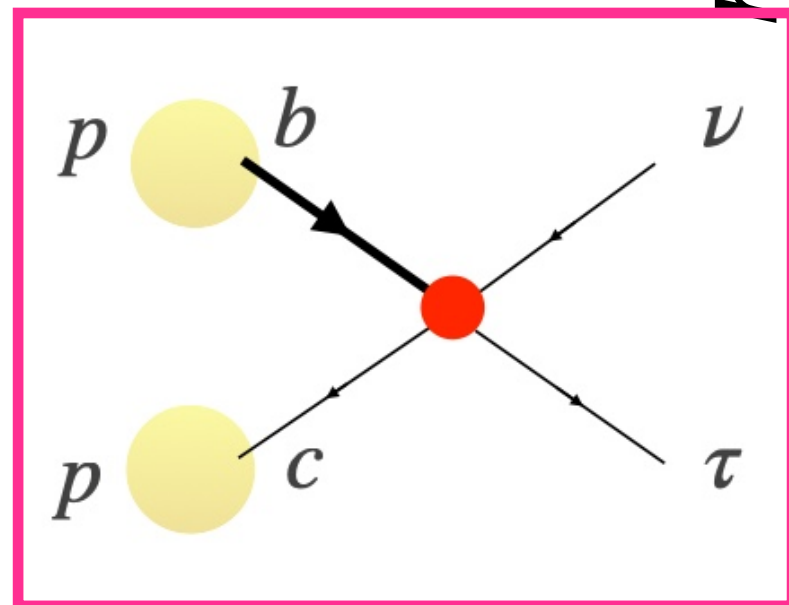
[Endo, Iguro, TK, Takeuchi, Watanabe, [2111.04748](#)]

[CMS, CMS PAS HIG-21-001]

$$U_1 \text{ LQ: } C_{S_1} = -2 e^{i\phi_R} C_{V_1}$$

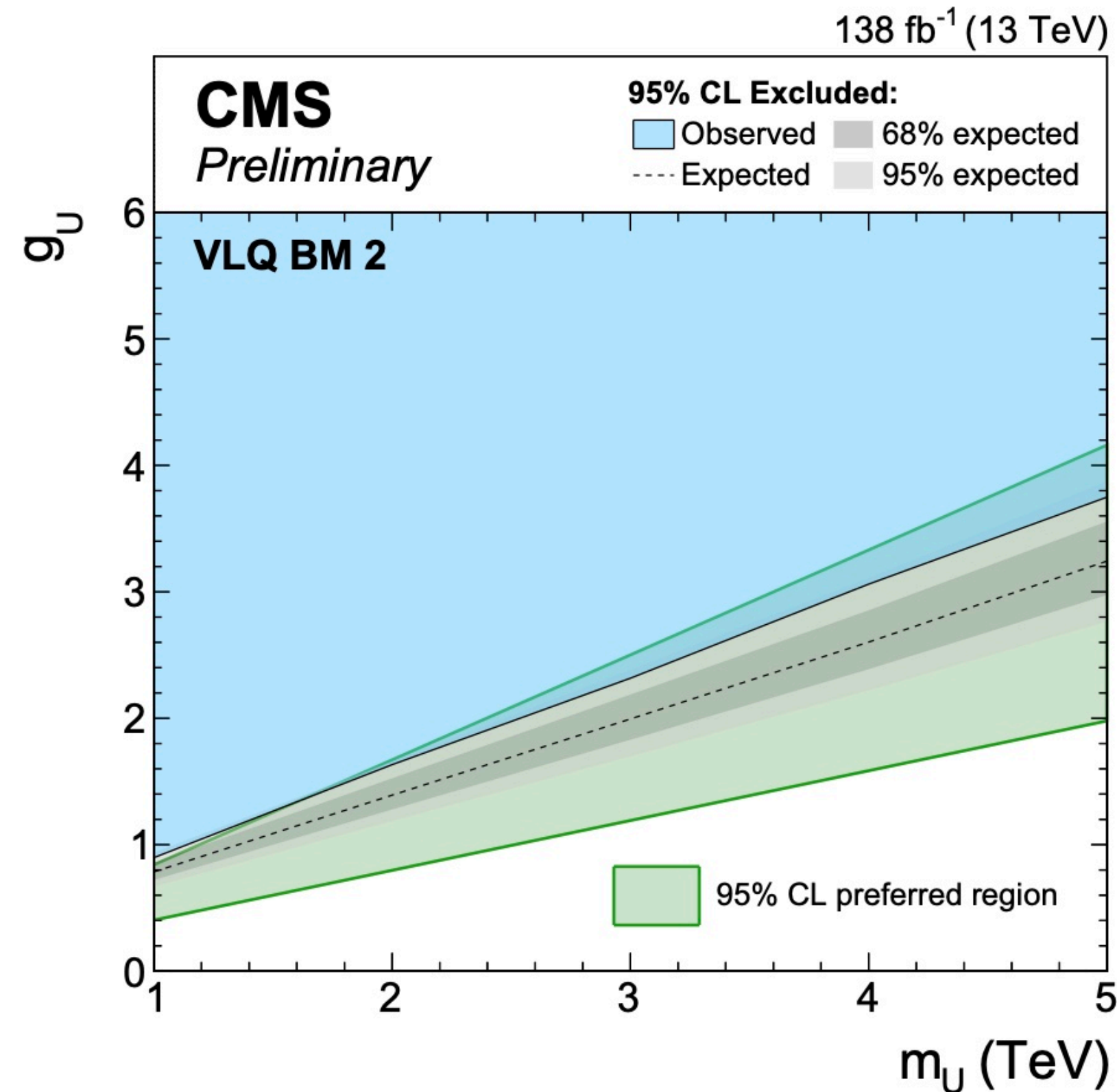


$\tau + \text{MET} + b$ search
 139 fb⁻¹
 sensitivity



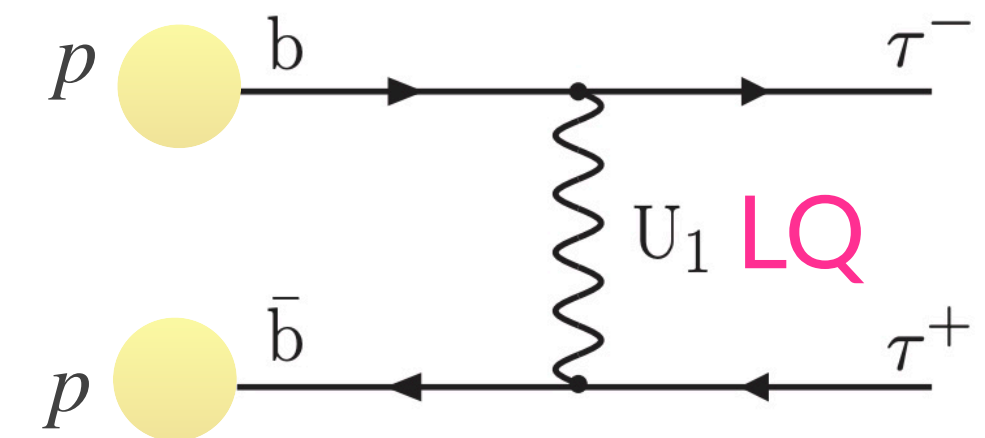
direct bound
 via crossing symmetry

$\tau b + \text{MET} (139 \text{ fb}^{-1})$



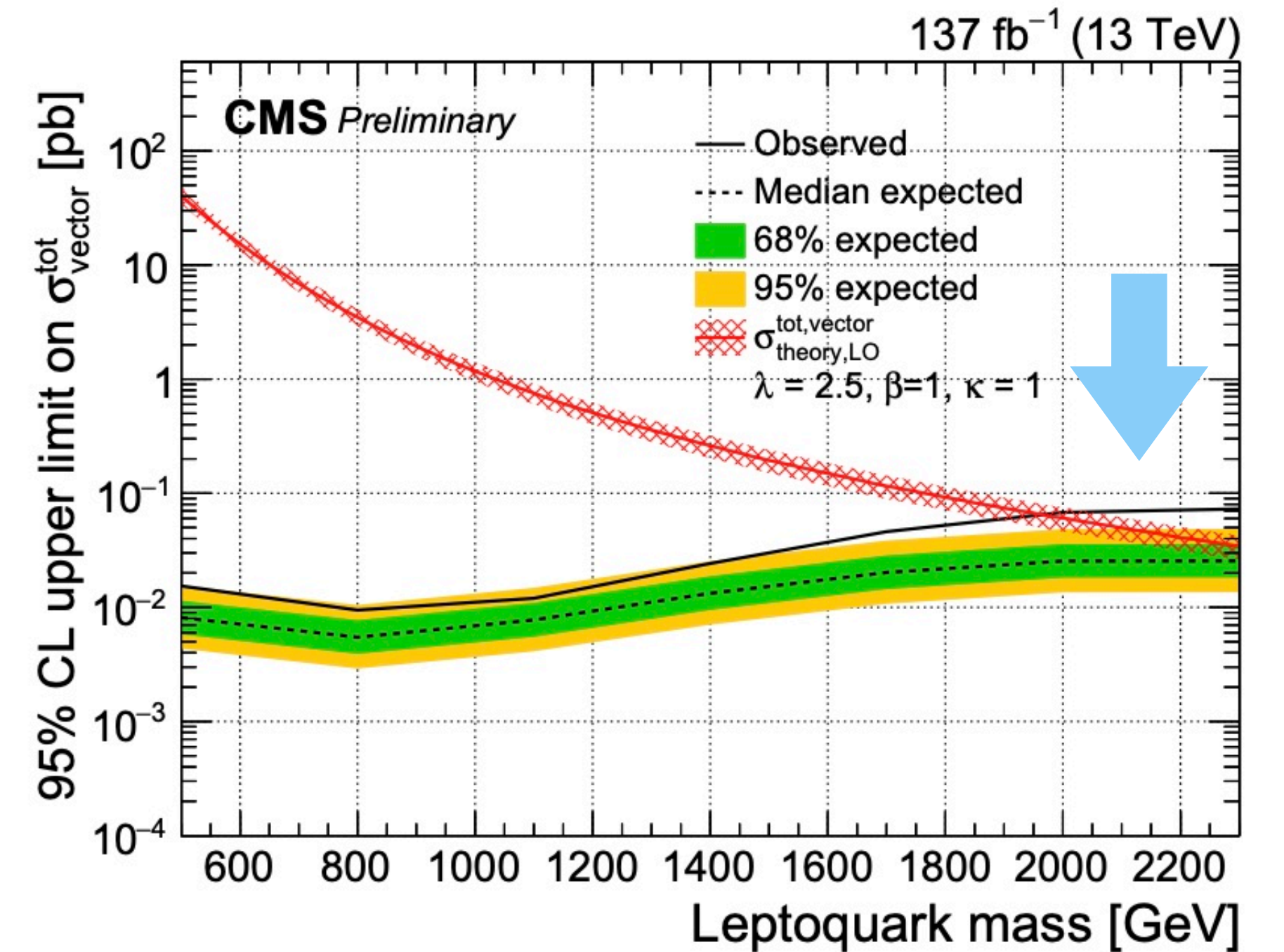
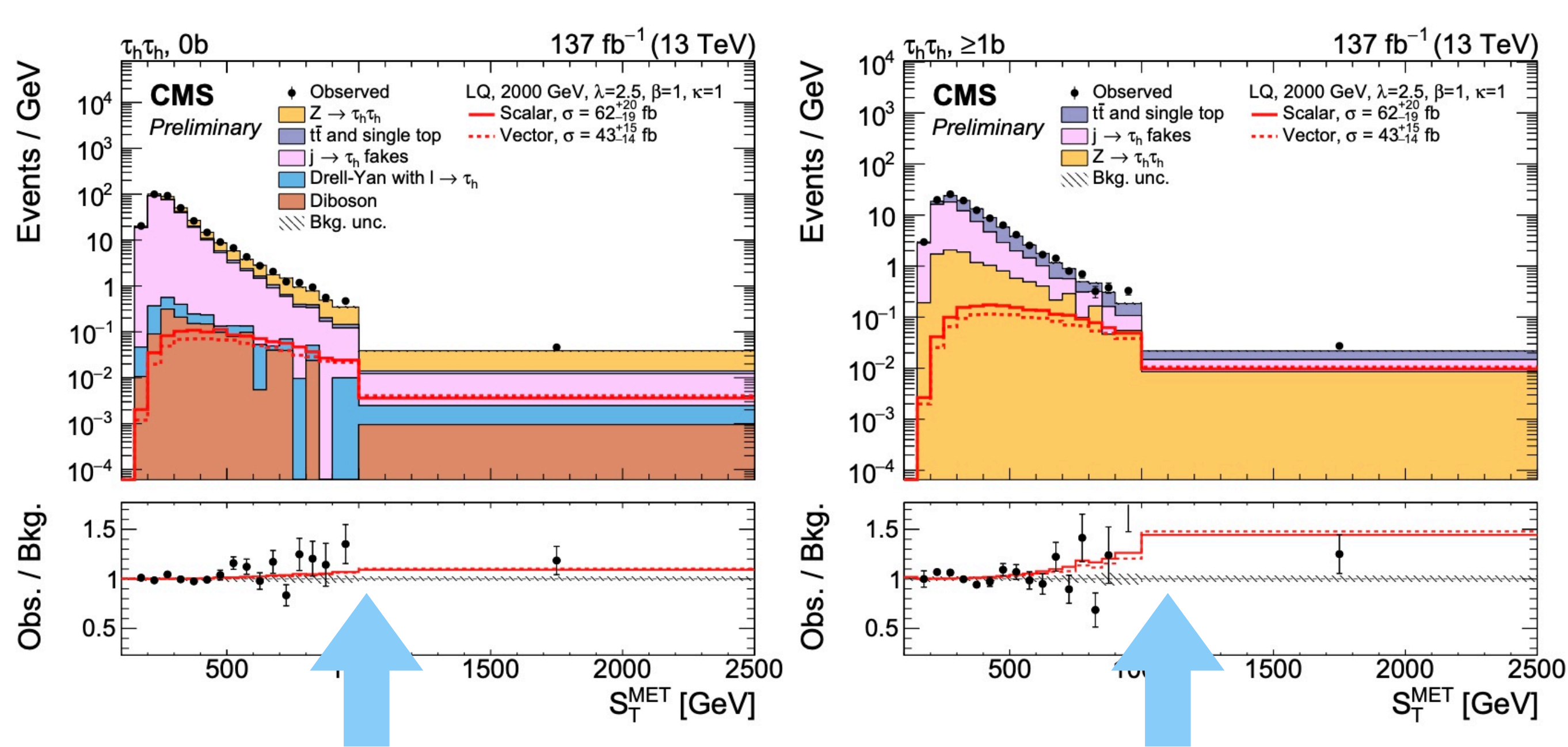
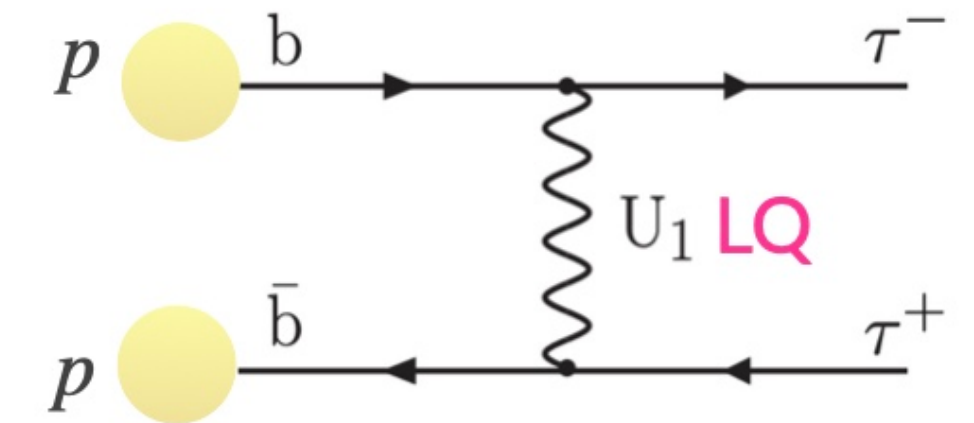
$\tau\tau (138 \text{ fb}^{-1}) (+b \text{ is included})$

Both are comparable sensitivity



model-dependent bound

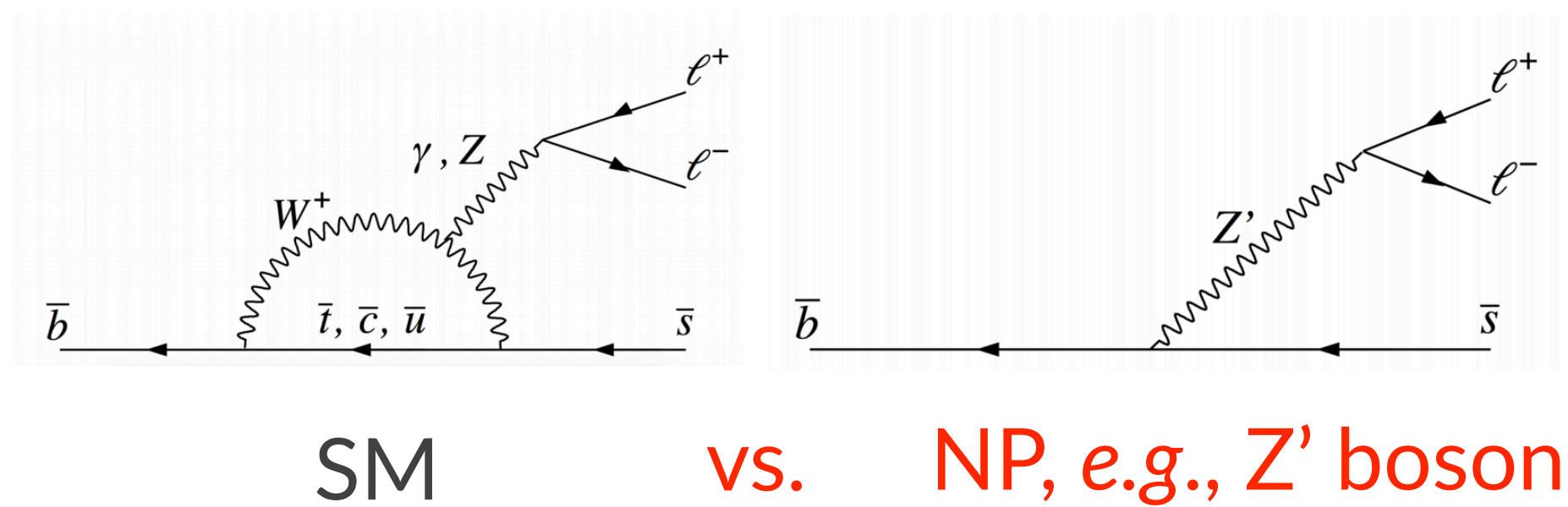
New LQ anomaly from CMS @ICHEP2022



3.4σ level excess at $M_{LQ} \sim 2 \text{ TeV}$ was reported from CMS [CMS, CMS-PAS-EXO-19-016]

Other LFU observables: $R(K)$ and $R(K^*)$

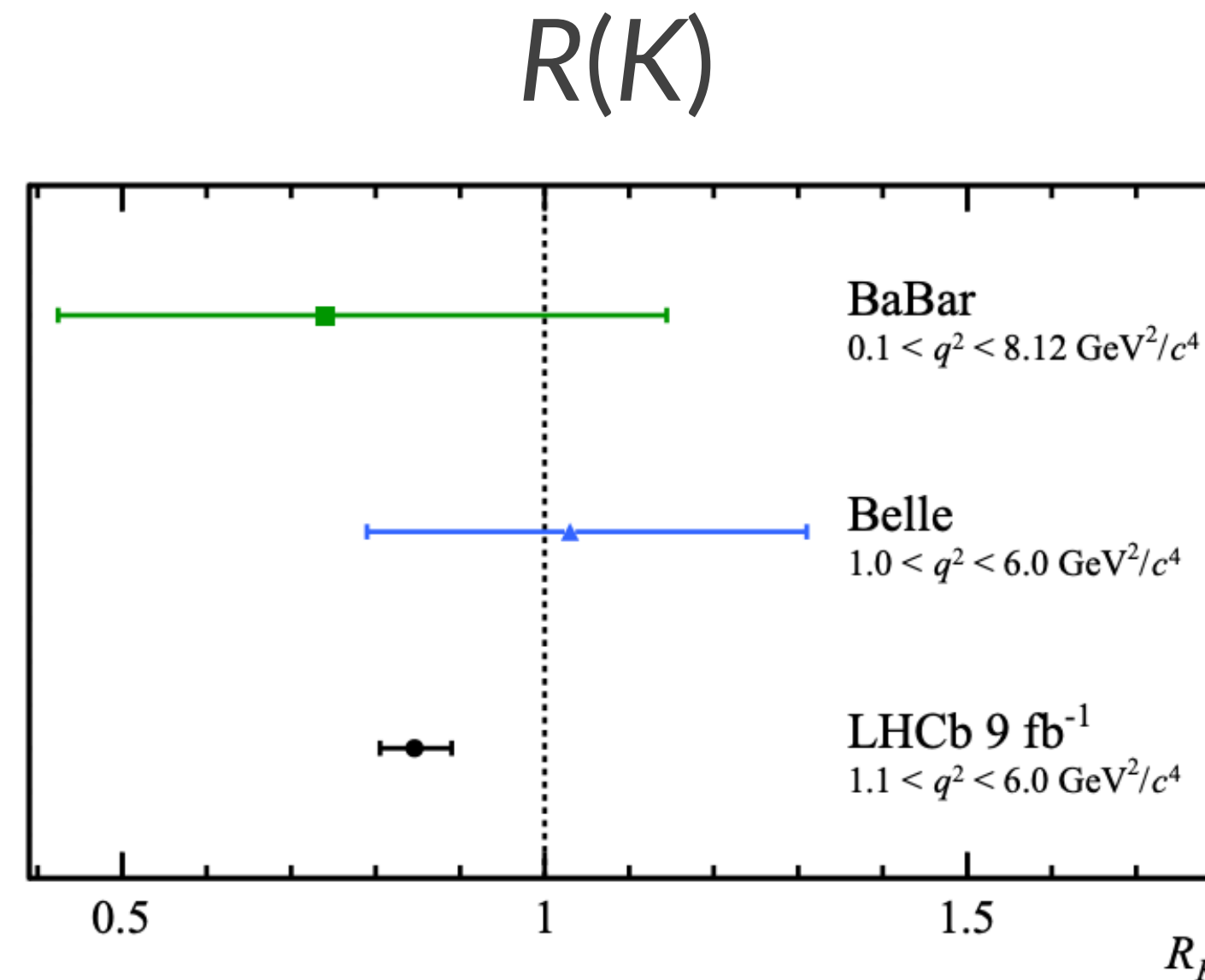
$$R(K^{(*)}) = \frac{\text{BR}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\text{BR}(B \rightarrow K^{(*)} e^+ e^-)}$$



SM vs. NP, e.g., Z' boson

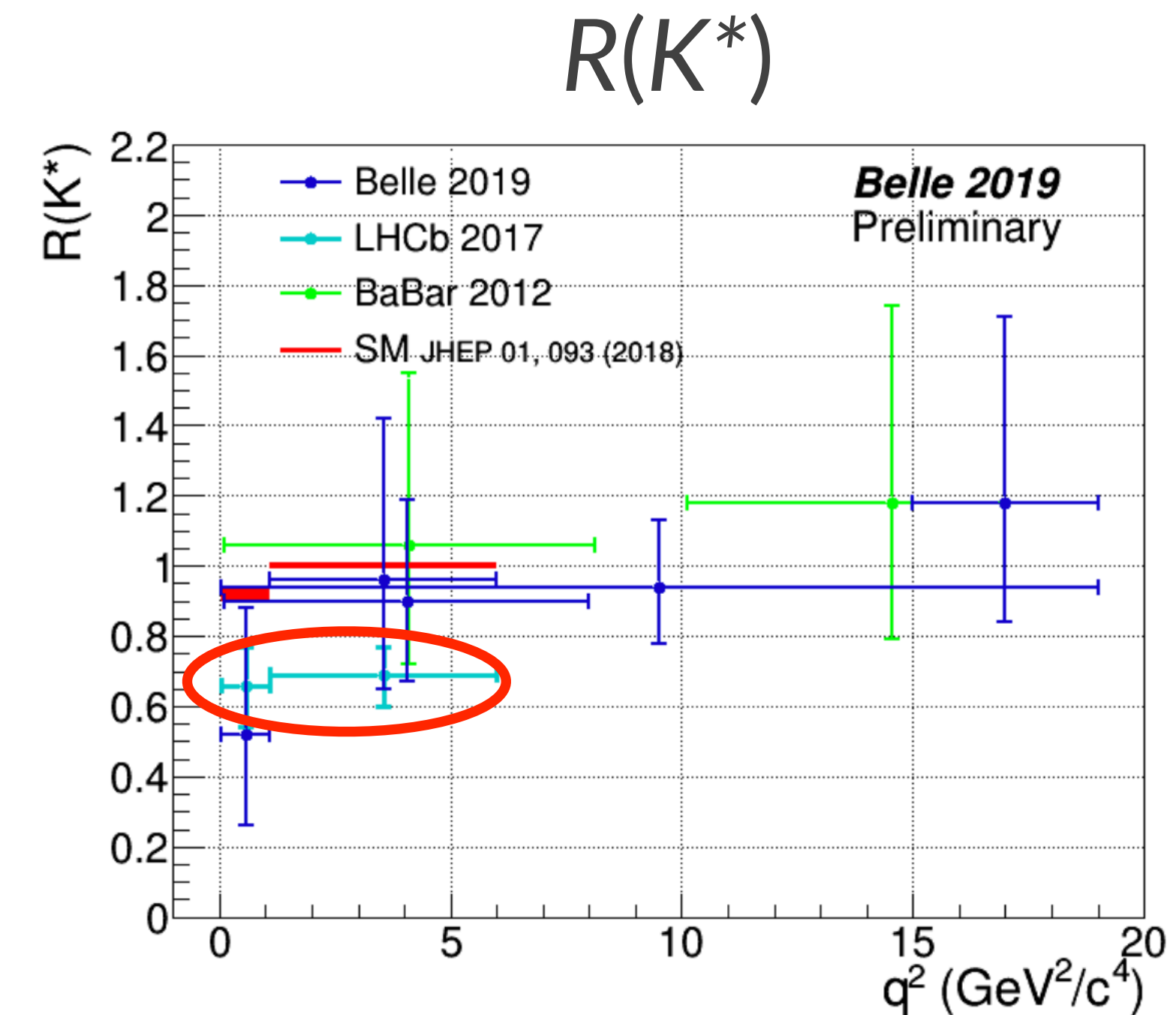
SM: $R(K) \simeq R(K^*) \simeq 1$

data: $R(K) \simeq R(K^*) \approx 0.8$



$\sim 3.1\sigma$ below the SM

$b \rightarrow s\mu\mu$ anomaly

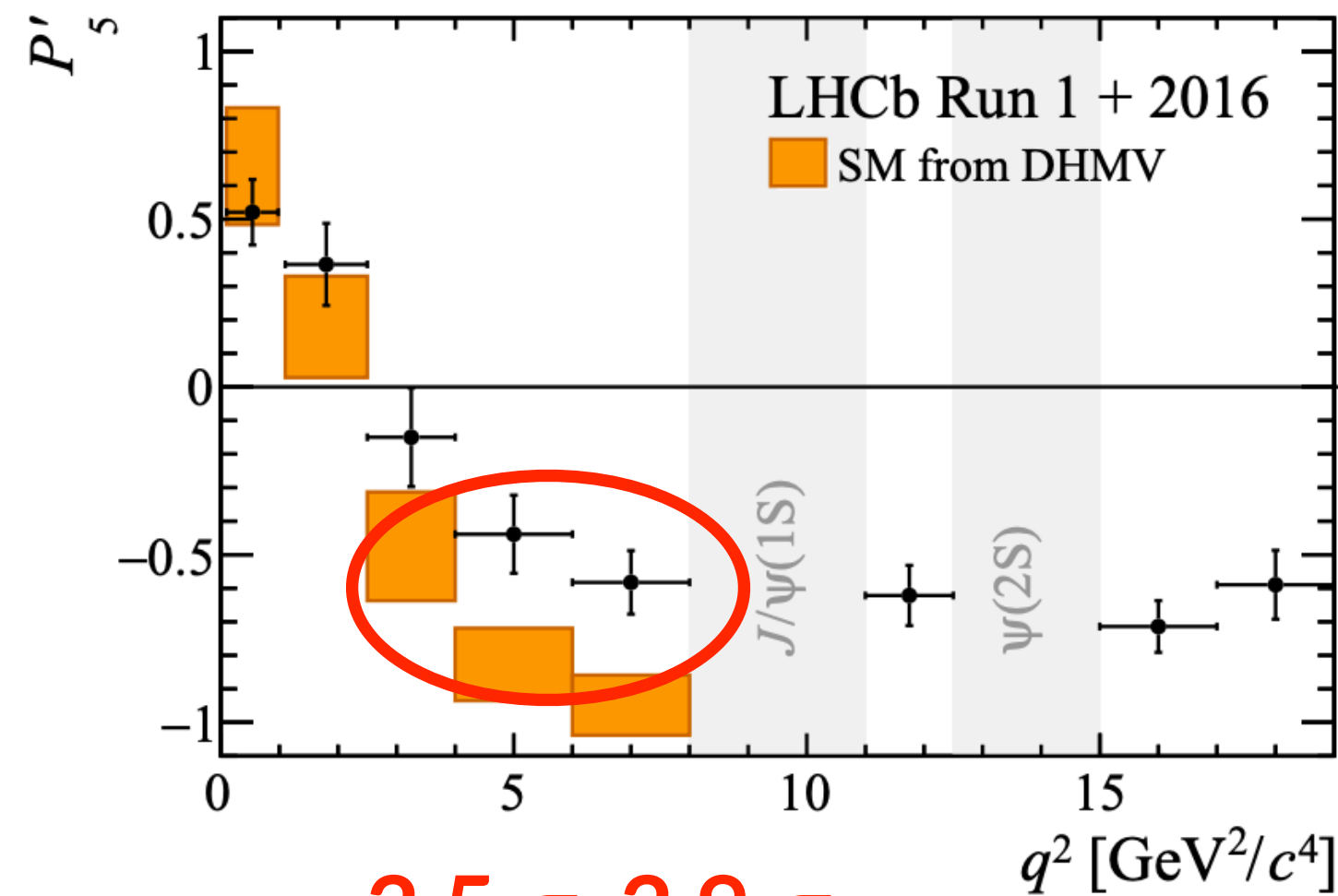


$\sim 2.5\sigma$ below the SM

$b \rightarrow s\mu^+\mu^-$ anomalies

$$B \rightarrow K^*\mu^+\mu^-$$

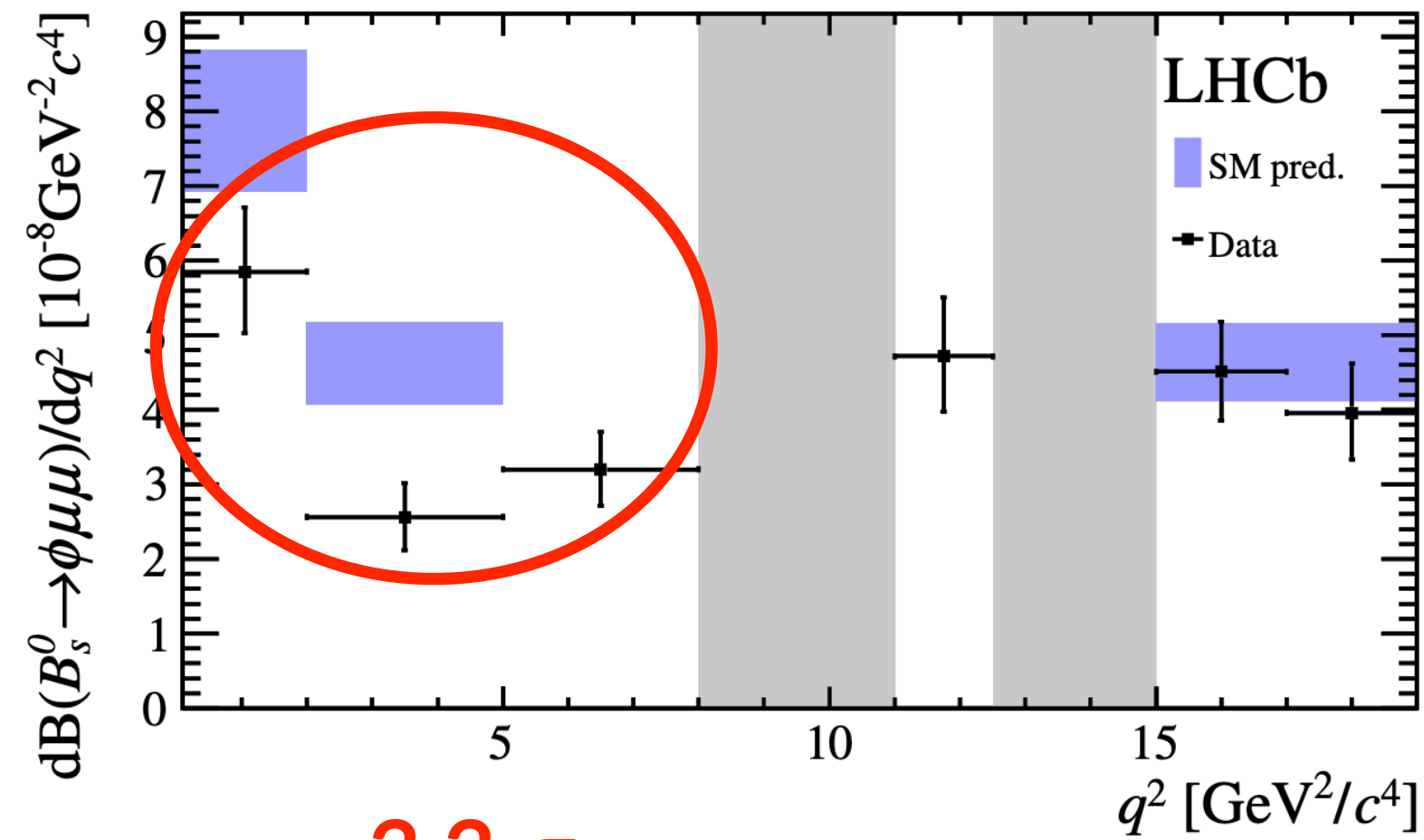
[LHCb, 2003.04831]



2.5 σ , 2.9 σ

$$B_s \rightarrow \phi\mu^+\mu^-$$

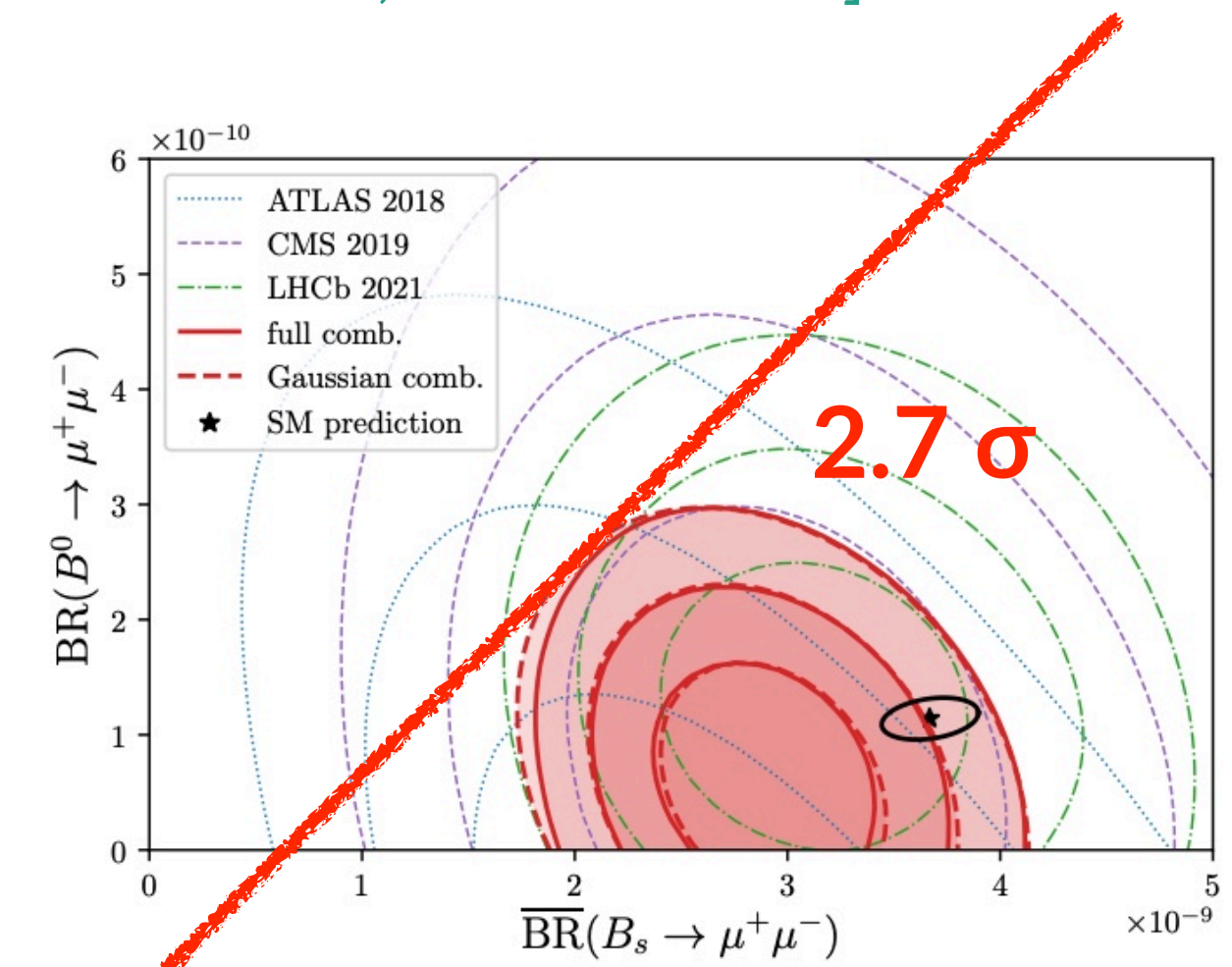
[LHCb, 1506.08777]



3.3 σ

$$B_s \rightarrow \mu^+\mu^-$$

[Altmannshofer, Stangl, 2103.13370;
Buras, 2205.01118]



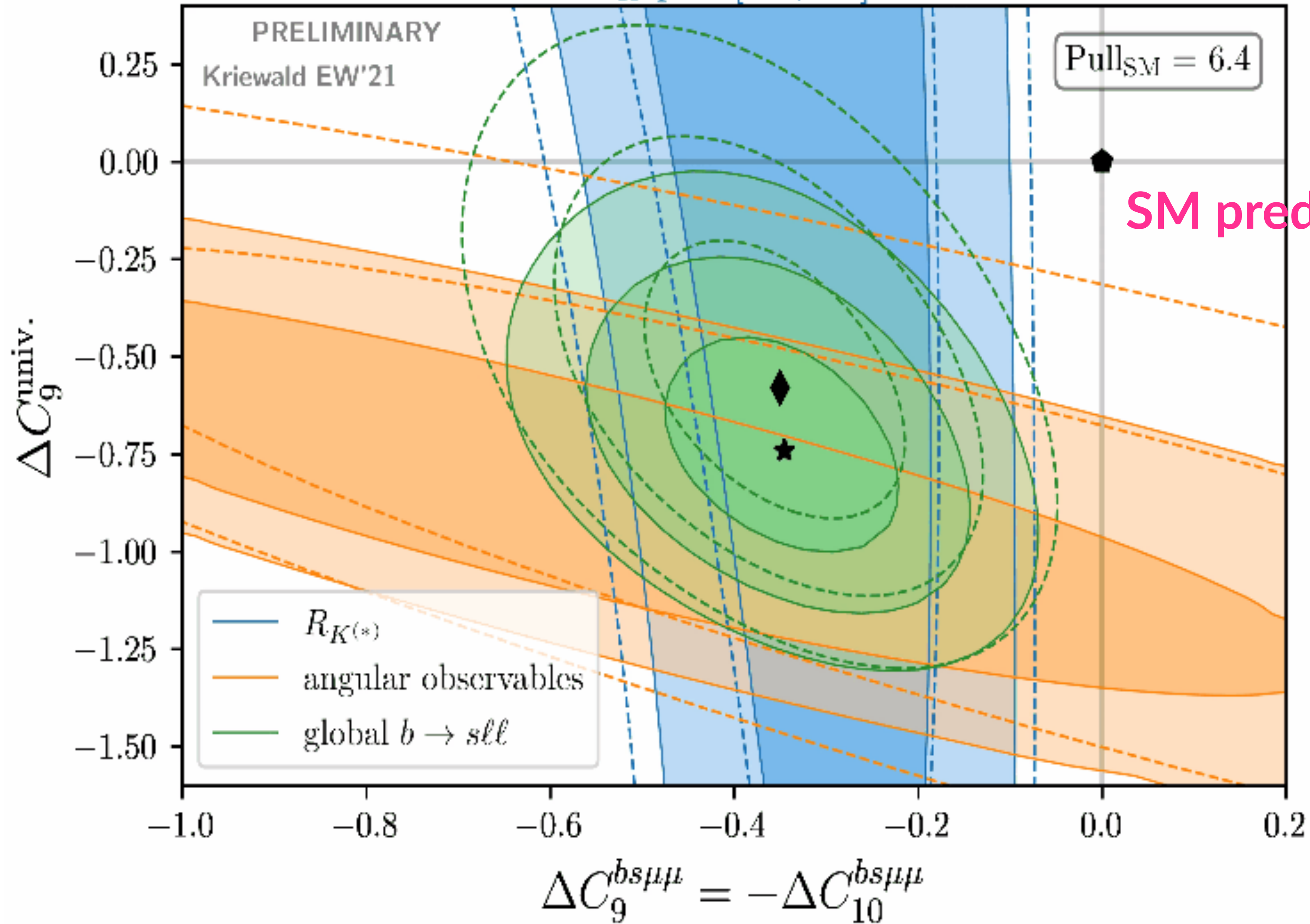
gone [CMS, ICHEP2022]

- ◆ Global significance of $b \rightarrow s\mu\mu$ anomaly is **4.3 σ level** taking into account the **look-elsewhere effect** (evaluated via pseudo-experiment) [Isidori, Lancierini, Owen, Serra [2104.05631](#)]

Moriond'21: LHCb $R_K q^2 \in [1.1, 6.0] \text{ GeV}^2$

[Kriewald, et al, [2104.00015](#)]

New physics operator



$$C_{bs\mu\mu} \approx (39 \text{ TeV})^{-2}$$

Assuming all dimensionless interactions = 1

New physics operator


New result will be presented next Tuesday! You cannot miss it.

LHC Seminar

Measurements of $R(K)$ and $R(K^*)$ with the full LHCb Run 1 and 2 data

by Renato Quagliani (EPFL - Ecole Polytechnique Federale Lausanne (CH))

 Tuesday Dec 20, 2022, 11:00 AM → 12:00 PM Europe/Zurich

 500/1-001 - Main Auditorium (CERN)

Description In this seminar we present the first simultaneous test of muon-electron universality in $B^+ \rightarrow K^+ \ell^+ \ell^-$ and $B^0 \rightarrow K^{*0} \ell^+ \ell^-$ decays, known as $R(K)$ and $R(K^*)$, in two regions of di-lepton invariant mass squared.

The analysis operates at a higher signal purity compared with previous analyses and implements a data-driven treatment of residual hadronic backgrounds. The analysis uses the full LHCb Run 1 and 2 data recorded in 2011-2012 and 2015-2018, corresponding to an integrated luminosity of 9 fb^{-1} . This analysis is the most sensitive lepton universality test in rare b-decays and the results obtained supersede the previous LHCb measurements of $R(K)$ and $R(K^{*0})$.

Organized by Michelangelo Mangano, Jan Fiete Grosse-Oetringhaus and Pedro Silva.....Refreshments will be served at 10h30

Videoconference



LHC seminar - 20 December - LHCb

 Join



Webcast



There is a live webcast for this event

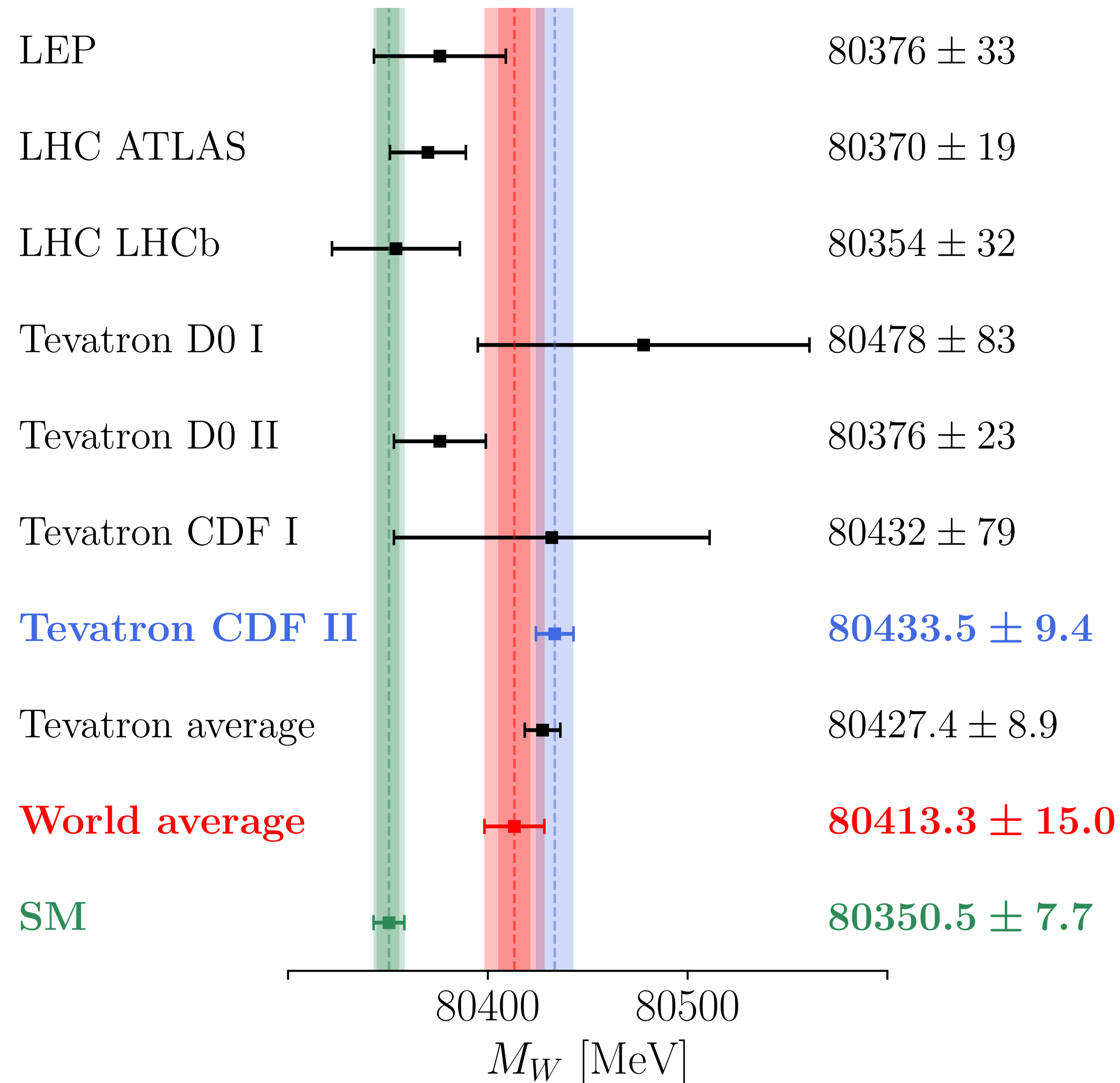
 Watch

W boson mass anomaly

Review [Endo, TK, Yagyu, High Energy News, 2022, [Link](#)]



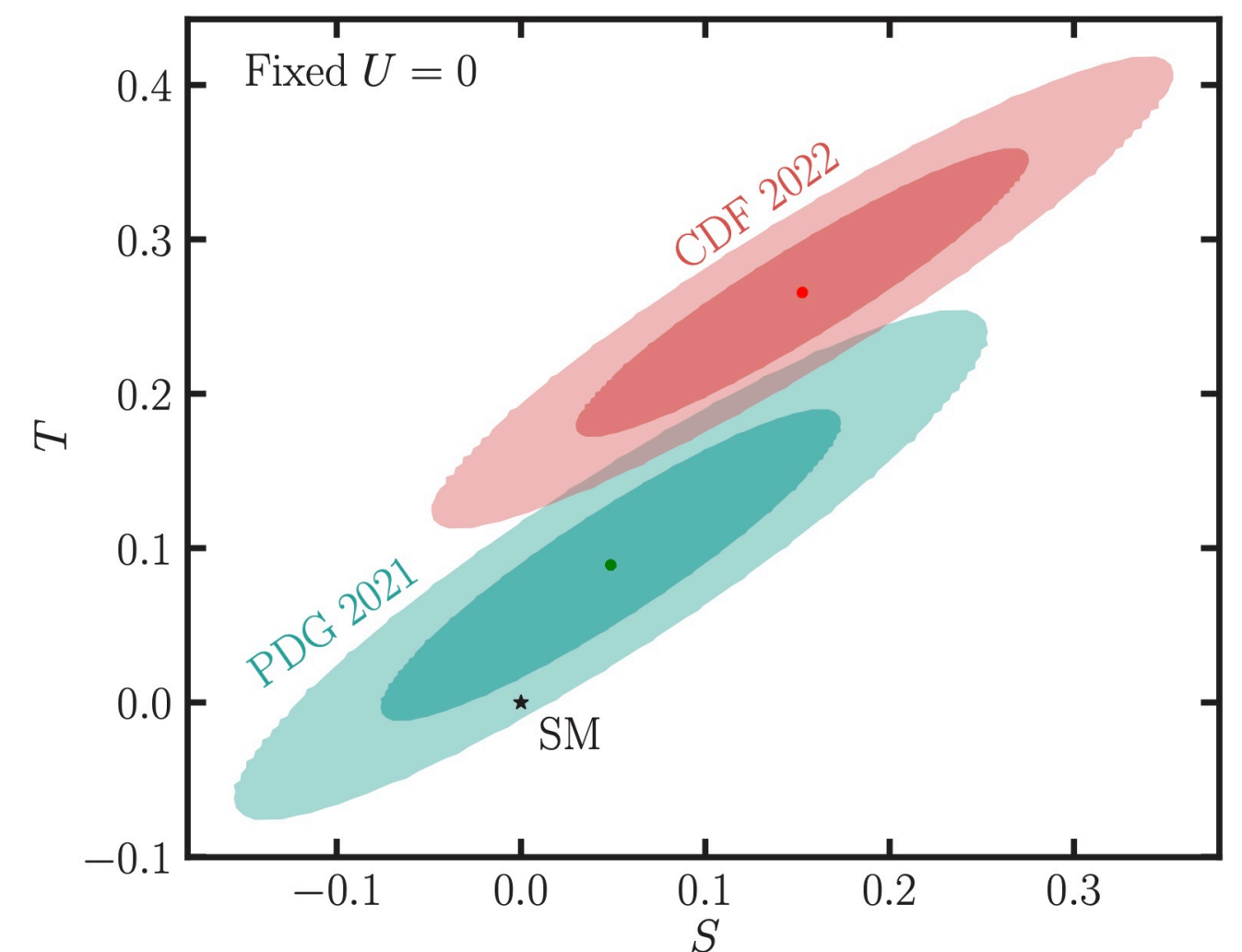
[CDF Collaboration, Science 376 (2022)].



“Scale factor” is included in the world average

Most conservatively, the tension is 3.7σ

Oblique parameter fit

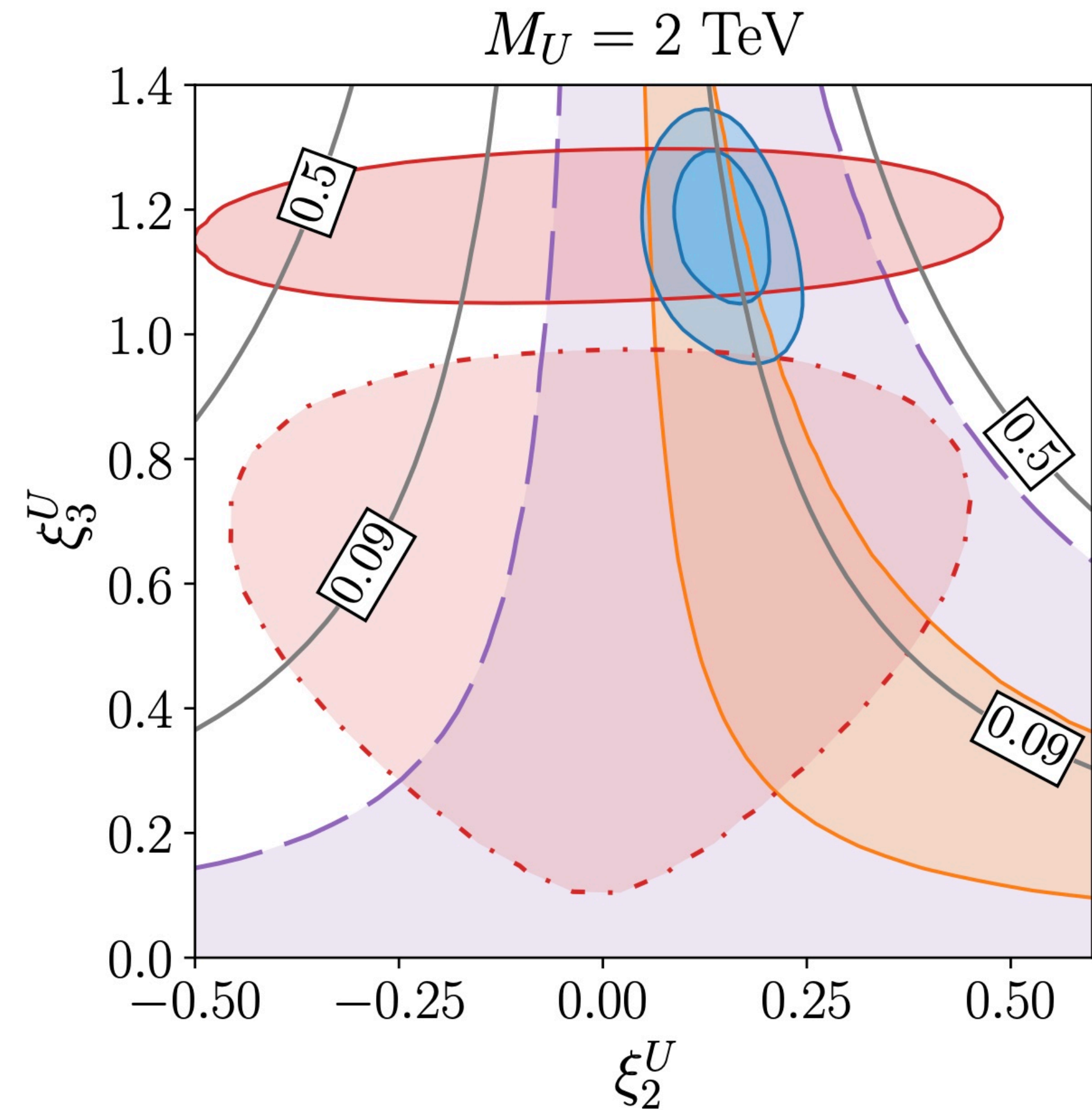
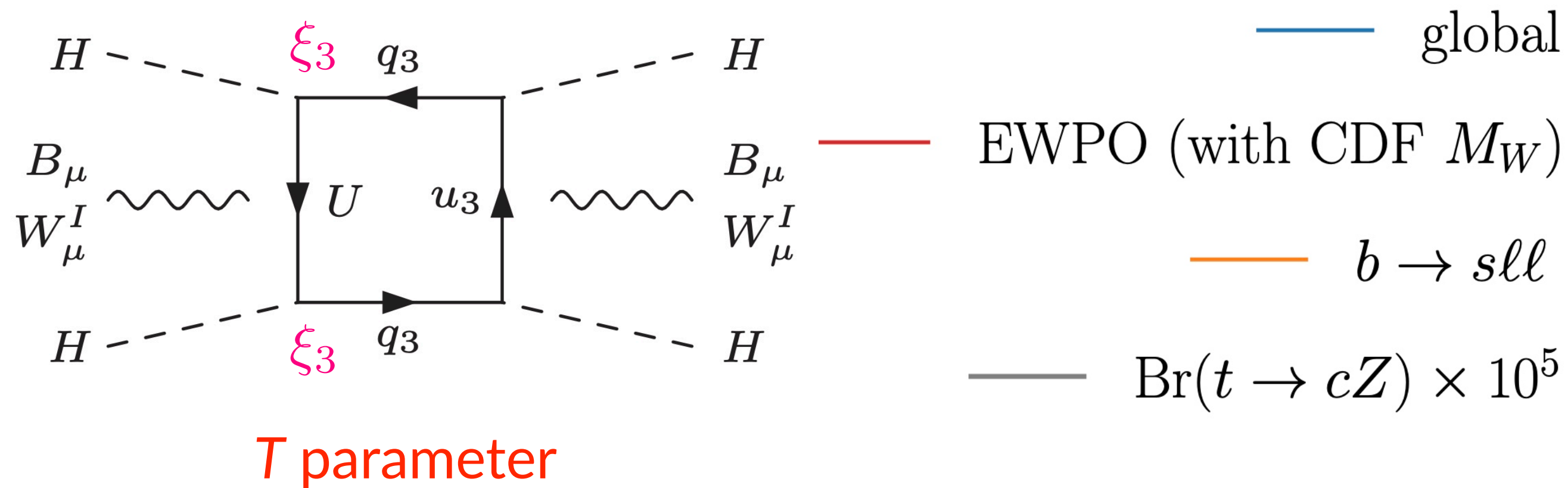


[Lu, Wu, Wu, Zhu, [2204.03796](#)]

B anomaly ($b \rightarrow s\mu\mu$) vs W boson mass

[Crivellin, Kirk, TK, Mescia, [2204.05962](#)]

- ◆ SM + vector-like quark model can explain (a part of) B anomaly ($b \rightarrow s\mu\mu$) and recent measured W mass anomaly
- ◆ Predict unique signal in $t \rightarrow Zc$ channel, which can be probed by future 100 TeV collider



Leptoquark catalogue

[cf. Angelescu, Bečirević, Faroughy, Jaffredo, Sumensari, [2103.12504](#); Athron, Balazs, Jacob, Kotlarski, Stockinger, Stockinger-Kim, [2104.03691](#)]

- ◆ Leptoquarks that do not lead to proton decay and can contribute precision measurements
[LQ* requires additional symmetry that forbids the proton decay, see [1603.04993](#)]

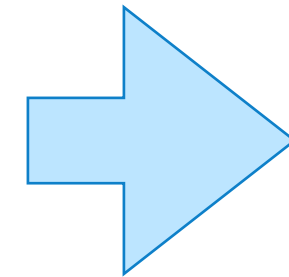
Label	Spin	Charge	R(D ^(*))	R(K ^(*))	muon g-2	M _W
S ₁ LQ ^(*)	0	$(\bar{3}, 1, 1/3)$	✓	Loop	✓	With S ₃
U ₁ LQ	1	$(3, 1, 2/3)$	✓	✓	✗	✗
R ₂ LQ	0	$(3, 2, 7/6 [1/6])$	✓	Loop	✓	✓
V ₂ LQ ^(*)	1	$(\bar{3}, 2, 5/6)$	Small	⚠	Small	✓
S ₃ LQ ^(*)	0	$(\bar{3}, 3, 1/3)$	✗	✓	✗	With S ₁
U ₃ LQ	1	$(3, 3, 2/3)$	✗	✓	✗	?

Test of unitarity in CKM matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

Unitarity condition

$$VV^\dagger = \mathbb{I}_3$$

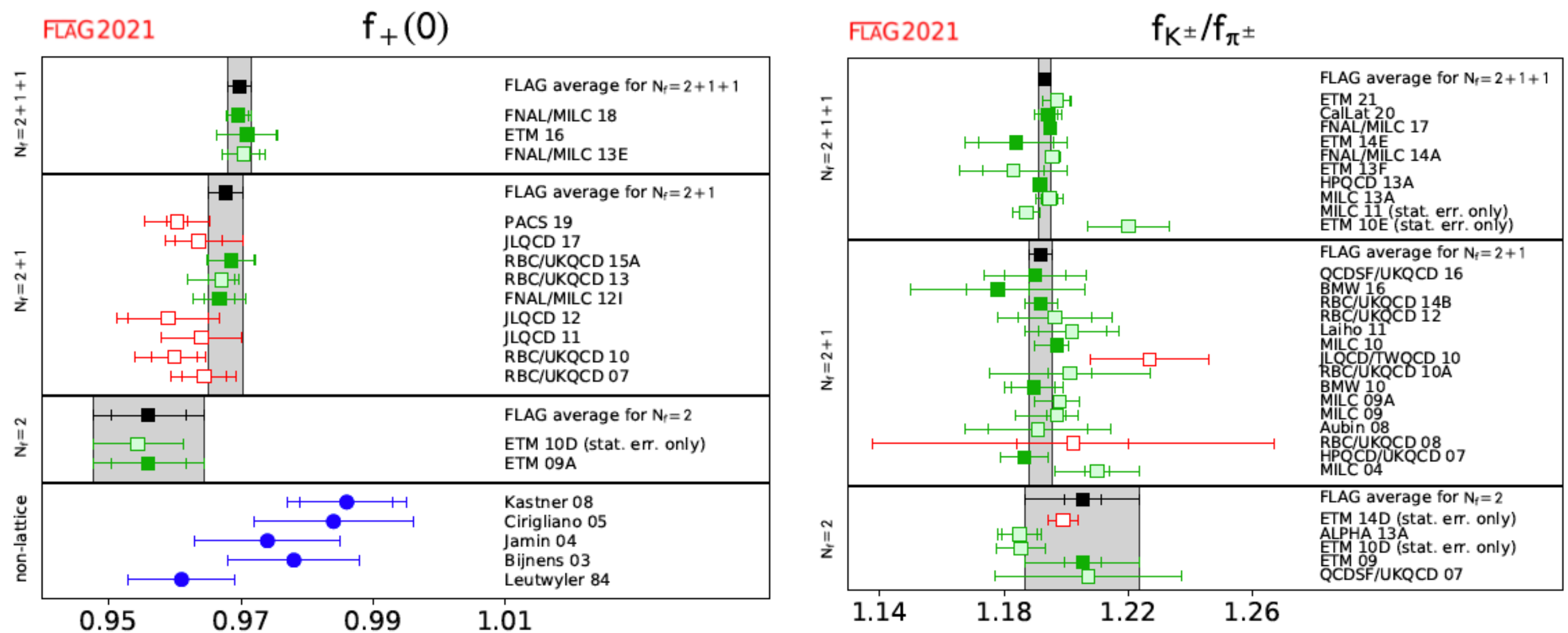


1st row unitarity condition

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

Sum of the absolute values must become 1

- ◆ Why these components?
 - ◆ Leading uncertainties from kaon form factors have been improved significantly
- [FLAG2021, [2111.09849](https://arxiv.org/abs/2111.09849)]

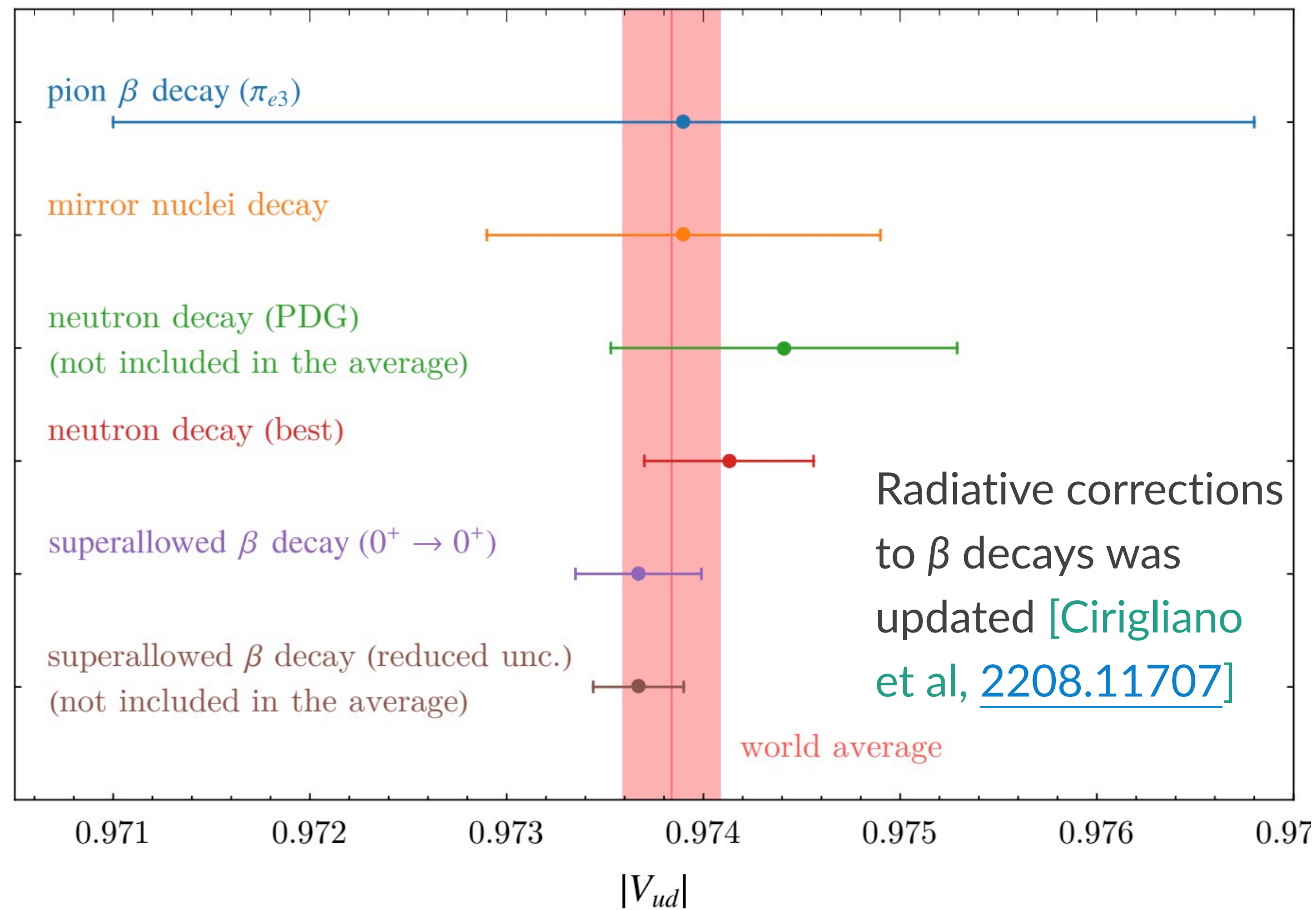


time ↑

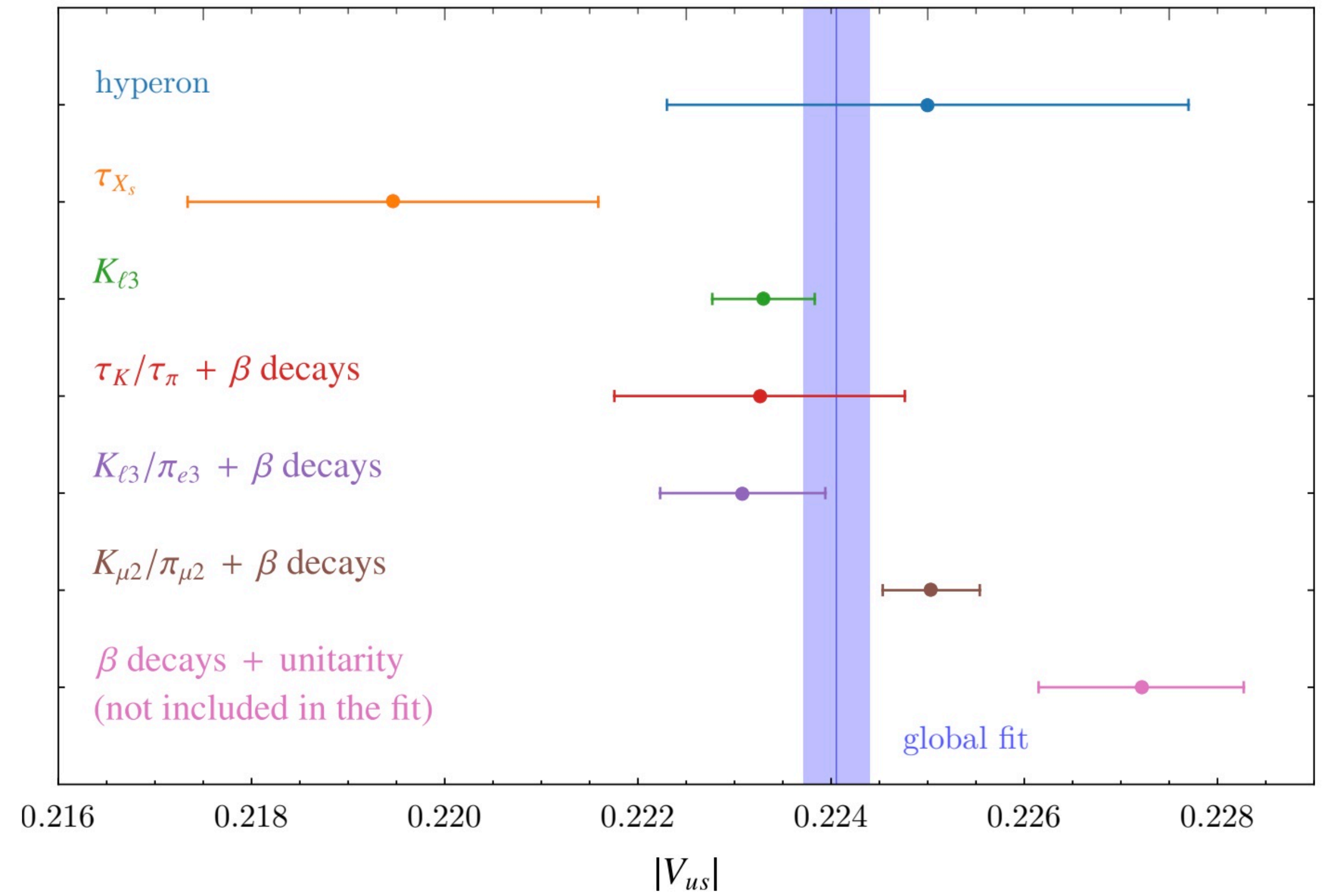
Vud and Vus determinations

See also Young-san's talk

[Crivellin, Kirk, TK, Mescia, [2212.06862](#)]

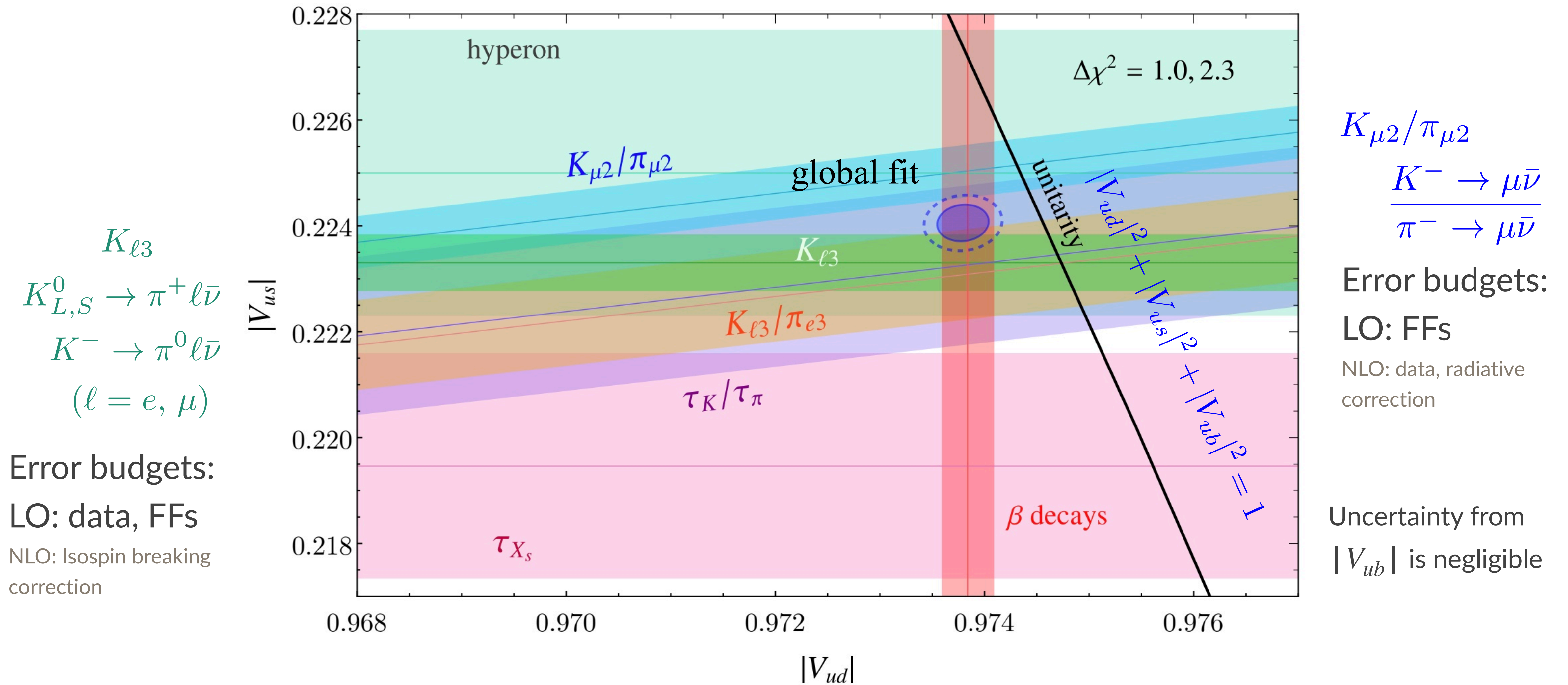


All data are consistent



One can see several tensions

Cabibbo-angle anomaly (CAA) [Crivellin, Kirk, TK, Mescia, [2212.06862](#)]



$K_{\ell 3}$
 $K_{L,S}^0 \rightarrow \pi^+ \ell \bar{\nu}$
 $K^- \rightarrow \pi^0 \ell \bar{\nu}$
 $(\ell = e, \mu)$

Error budgets:
LO: data, FFs
NLO: Isospin breaking correction

Significance of CAA

- ◆ Global fit (including with some correlations of uncertainties) [Crivellin, Kirk, TK, Mescia, [2212.06862](#)]

$$\begin{aligned} |V_{ud}|_{\text{global}} &= 0.973\,79(25), & \rho(V_{ud}, V_{us}) &= 0.09 \\ |V_{us}|_{\text{global}} &= 0.224\,05(35), \end{aligned}$$


$$\Delta_{\text{CKM}}^{\text{global}} \equiv |V_{ud}|_{\text{global}}^2 + |V_{us}|_{\text{global}}^2 + |V_{ub}|^2 - 1 = -0.001\,51(53),$$

2.8 σ level deviation from the unitarity condition

- ◆ Another precise combination (1st column unitarity)

$$\Delta_{\text{CKM}}^{\text{1st column}} \equiv |V_{ud}|_{\text{global}}^2 + |V_{cd}|^2 + |V_{td}|^2 - 1 = -0.0028(18),$$

Uncertainty is predominated by **data of $D \rightarrow \mu\nu$, being probed precisely** by Belle II and BES III

EFT fitting

[Crivellin, Kirk, TK, Mescia, [2212.06862](#)]

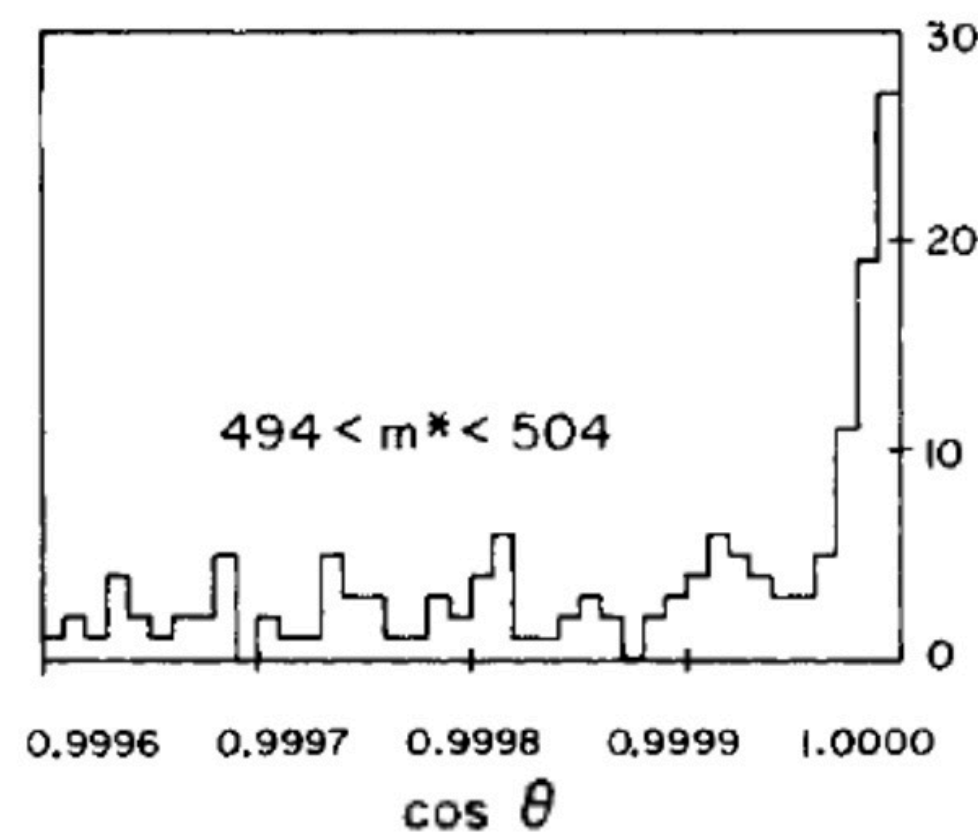
- ◆ EFT global fitting implies that right-handed W-u-d and W-u-s new physics is preferred

EFT Scenario	Best fit point	$-\Delta\chi^2$	Pull
$[C_{Hq}^{(3)}]_{11}$	-0.49	3.3	1.8σ
$[C_{Hq}^{(3)}]_{11} = [C_{Hq}^{(3)}]_{22}$	-0.26	1.1	1.1σ
$[C_{Hq}^{(3)}]_{11} = [C_{Hq}^{(1)}]_{11}$	-0.53	3.6	1.9σ
$[C_{Hud}]_{11}$	-1.1	3.3	1.8σ
$[C_{Hud}]_{12}$	-2.5	8.2	2.9σ
$([C_{Hud}]_{11}, [C_{Hud}]_{12})$	(-1.6, -3.1)	15	3.5σ
$([C_{Hq}^{(3)}]_{11}, [C_{Hud}]_{12})$	(-0.59, -2.7)	12	3.1σ
$([C_{Hq}^{(3)}]_{11}, [C_{Hud}]_{11}, [C_{Hud}]_{12})$	(0.25, -2.1, -3.2)	16	3.2σ
$([C_{Hq}^{(3)}]_{11}, [C_{Hq}^{(3)}]_{22}, [C_{Hud}]_{11}, [C_{Hud}]_{12})$	(0.59, 0.78, -2.8, -3.3)	18	3.3σ
$([C_{Hq}^{(3)}]_{11}, [C_{Hq}^{(1)}]_{11}, [C_{Hud}]_{11}, [C_{Hud}]_{12})$	(0.27, 0.11, -2.1, -3.2)	16	2.9σ

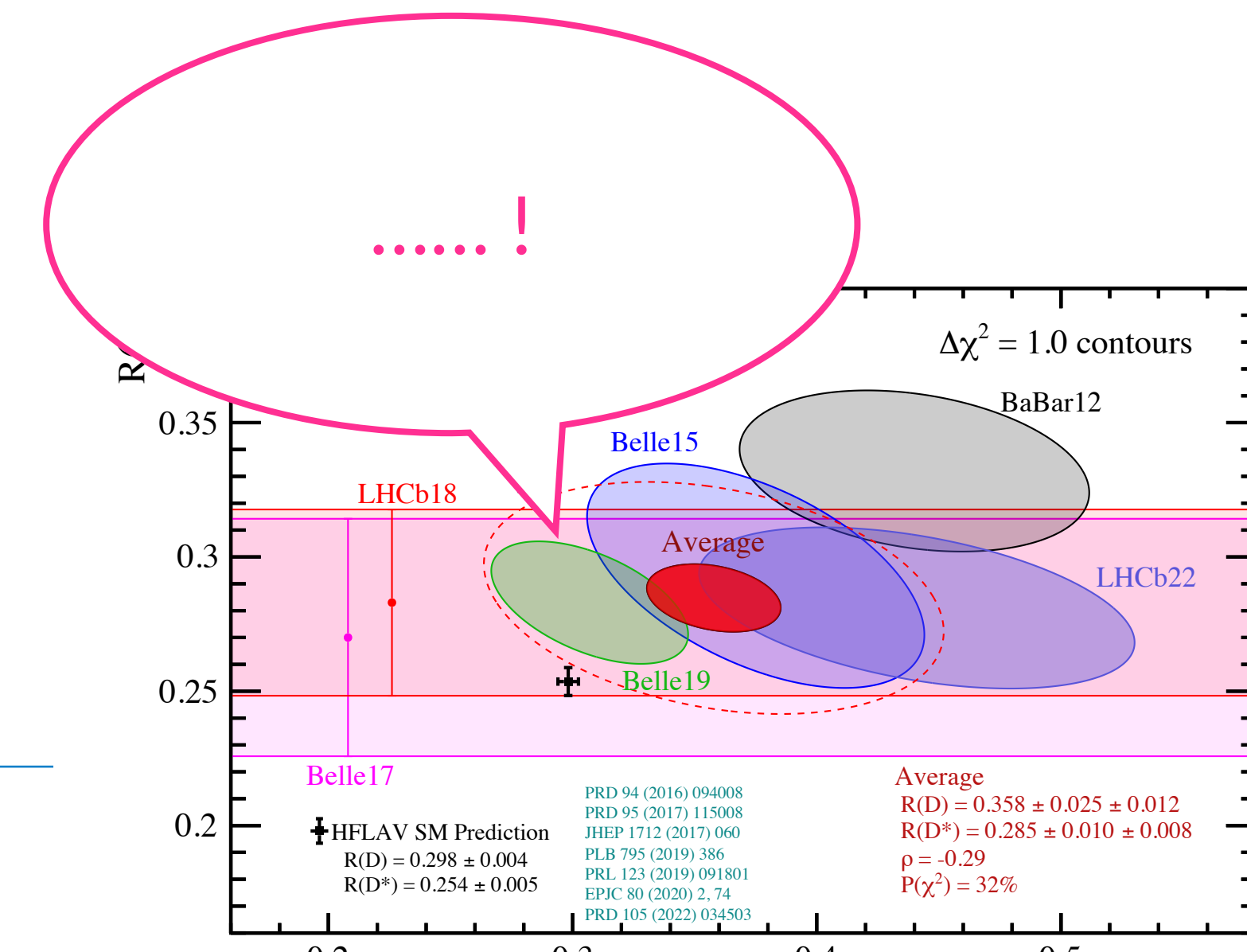
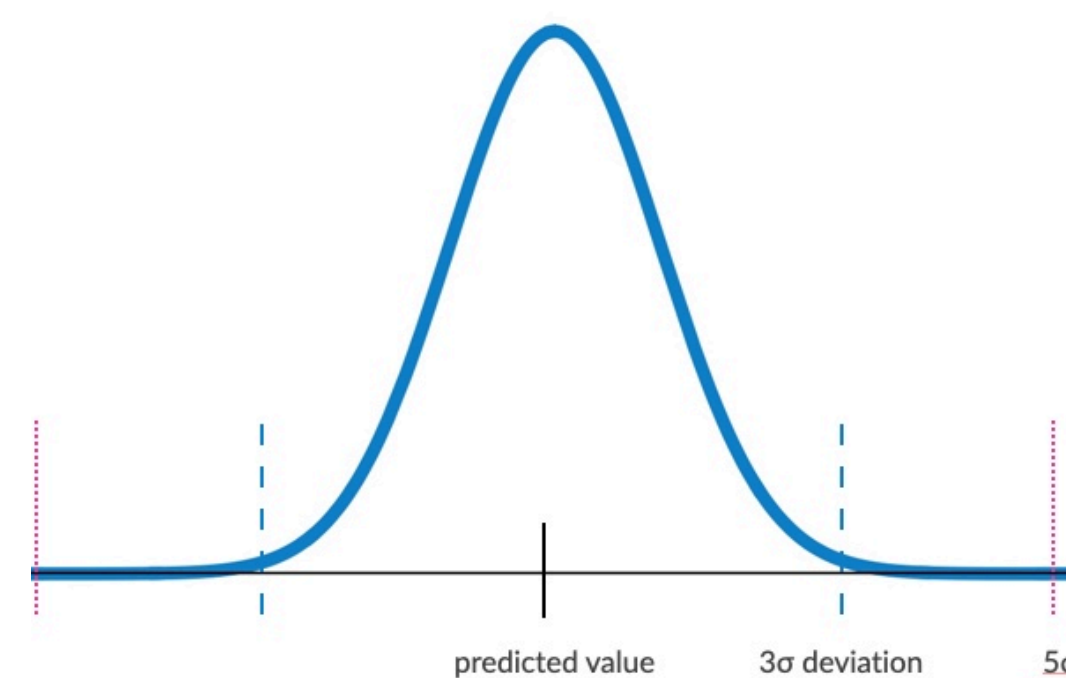
nice pull

Conclusions

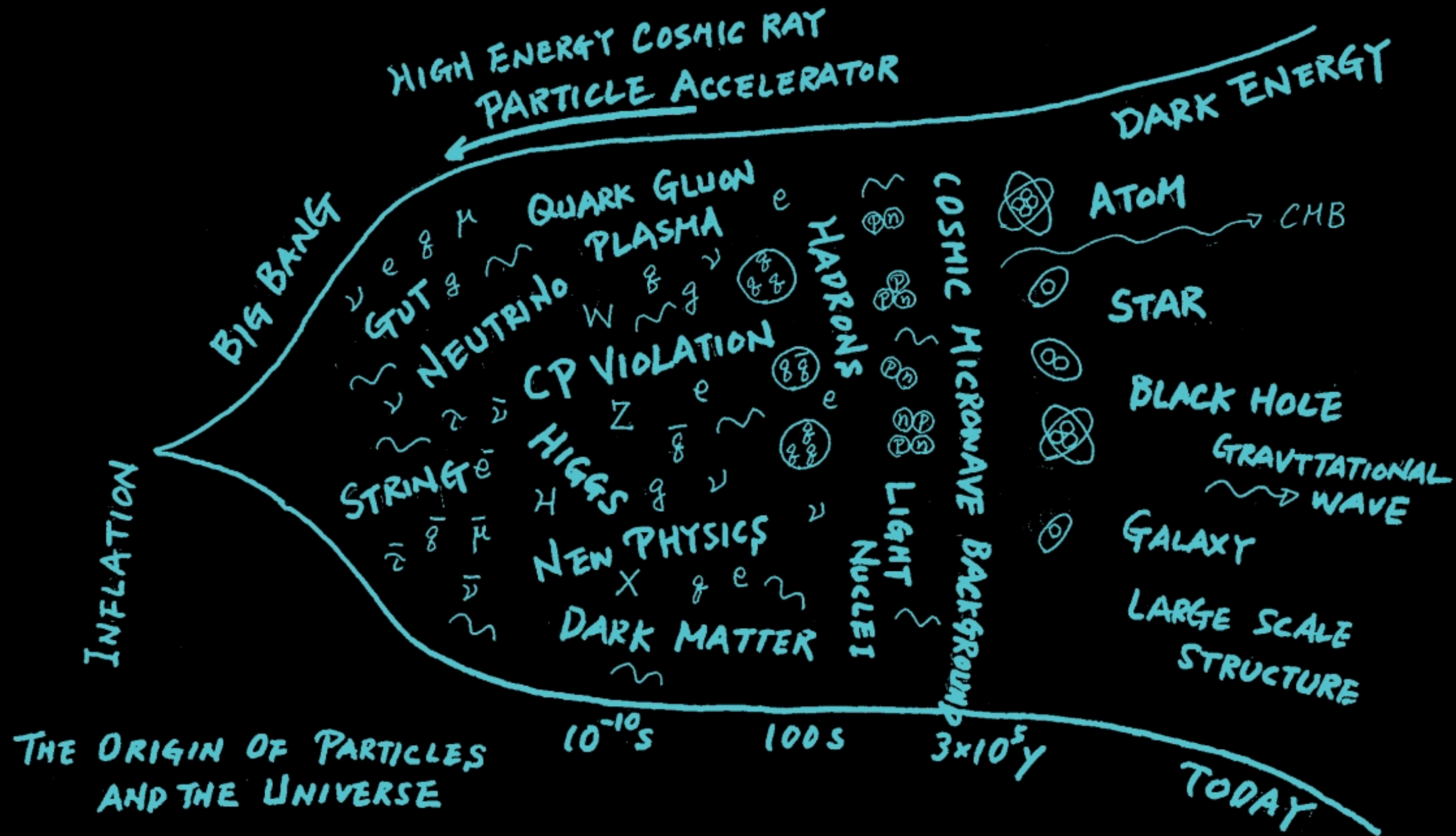
- ◆ Flavor physics is an essential approach to investigate new physics beyond the SM
- ◆ Currently, several flavor anomalies are found. There, **the statistical data analysis plays an important role**
- ◆ Beyond the statistical data analysis, **it is important to investigate *hidden theoretical correlation among several observables***



or



Backup slides



Operators for CAA

$$\begin{aligned}
 Q_{Hq}^{(1)ij} &= (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{q}_i \gamma^\mu P_L q_j), & Q_{Hq}^{(3)ij} &= (H^\dagger i \overleftrightarrow{D}_\mu^I H) (\bar{q}_i \tau^I \gamma^\mu P_L q_j), \\
 Q_{Hu}^{ij} &= (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{u}_i \gamma^\mu P_R u_j), & Q_{Hd}^{ij} &= (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{d}_i \gamma^\mu P_R d_j), \\
 Q_{Hud}^{ij} &= i(\tilde{H}^\dagger D_\mu H) (\bar{u}_i \gamma^\mu P_R d_j).
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{L}_{W,Z} &= -\frac{g_2}{\sqrt{2}} W_\mu^+ \bar{u}_i \gamma^\mu \left([V \cdot (\mathbb{1} + v^2 C_{Hq}^{(3)})]_{ij} P_L + \frac{v^2}{2} [C_{Hud}]_{ij} P_R \right) d_j + \text{h.c.} \\
 &\quad -\frac{g_2}{6c_W} Z_\mu \bar{u}_i \gamma^\mu \left([(3 - 4s_W^2)\mathbb{1} + 3v^2 V \cdot \{C_{Hq}^{(3)} - C_{Hq}^{(1)}\} \cdot V^\dagger]_{ij} P_L \right. \\
 &\quad \quad \left. - [4s_W^2\mathbb{1} + 3v^2 C_{Hu}]_{ij} P_R \right) u_j \\
 &\quad -\frac{g_2}{6c_W} Z_\mu \bar{d}_i \gamma^\mu \left([(2s_W^2 - 3)\mathbb{1} + 3v^2 \{C_{Hq}^{(3)} + C_{Hq}^{(1)}\}]_{ij} P_L \right. \\
 &\quad \quad \left. + [2s_W^2\mathbb{1} + 3v^2 C_{Hd}]_{ij} P_R \right) d_j,
 \end{aligned}$$

Operators for R(D^(*)) anomaly

$$\mathcal{H}_{\text{eff}} = 2\sqrt{2}G_F V_{cb} \left[(1 + C_{V_L})O_{V_L} + C_{V_R}O_{V_R} + C_{S_L}O_{S_L} + C_{S_R}O_{S_R} + C_T O_T \right],$$

with

$$O_{V_L} = (\bar{c}\gamma^\mu P_L b)(\bar{\tau}\gamma_\mu P_L \nu_\tau),$$

$$O_{V_R} = (\bar{c}\gamma^\mu P_R b)(\bar{\tau}\gamma_\mu P_L \nu_\tau),$$

$$O_{S_L} = (\bar{c}P_L b)(\bar{\tau}P_L \nu_\tau),$$

$$O_{S_R} = (\bar{c}P_R b)(\bar{\tau}P_L \nu_\tau),$$

$$O_T = (\bar{c}\sigma^{\mu\nu} P_L b)(\bar{\tau}\sigma_{\mu\nu} P_L \nu_\tau),$$

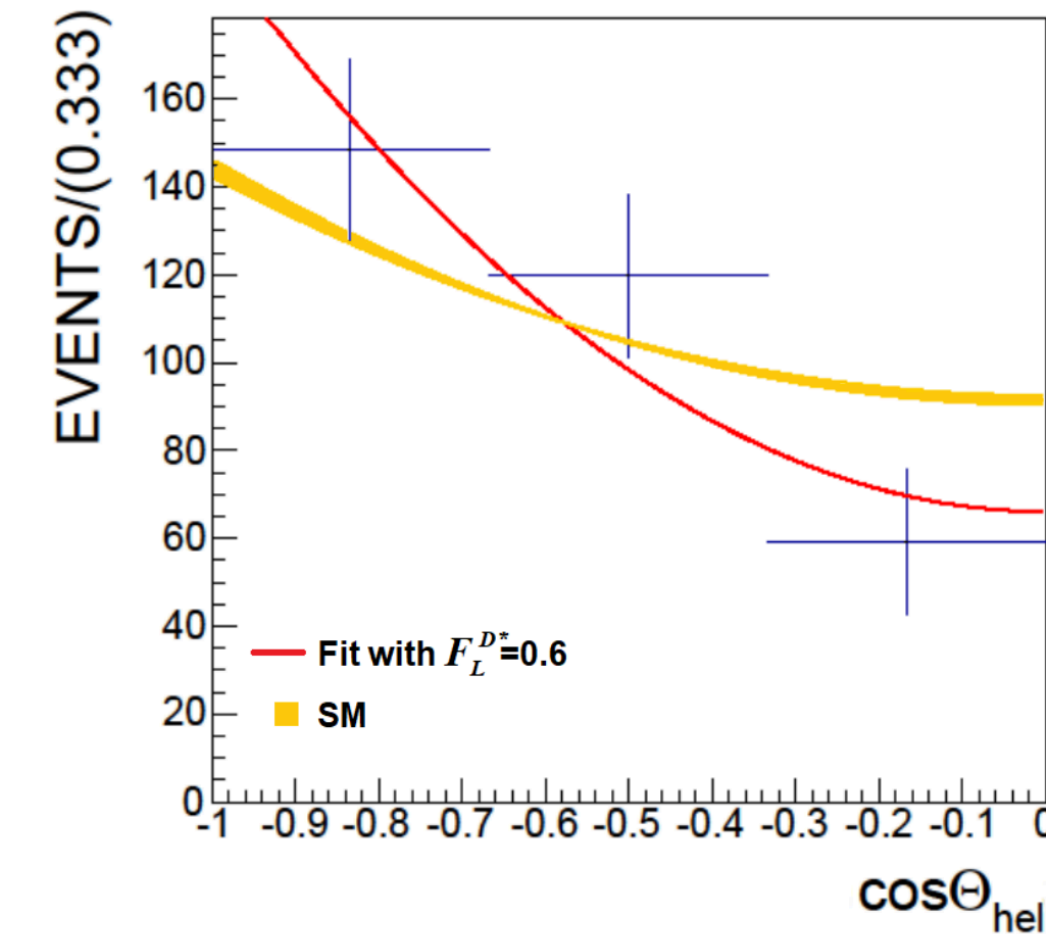
Polarization observables in $b \rightarrow c\tau\nu$

- ◆ The following two polarization observables could be important to confirm/distinguish new physics

- ◆ Longitudinal D^* polarization ($D^* \rightarrow D\pi$)

$$F_L(D^*) = \frac{\Gamma(B \rightarrow D_L^* \tau \nu)}{\Gamma(B \rightarrow D^* \tau \nu)}$$

θ_{hel} is the angle
between D and B in the
 D^* rest frame



[Belle, 1903.03102]

1.4 σ consistent

- ◆ τ polarization asymmetry along the longitudinal directions of τ ($\tau \rightarrow \pi\nu, \rho\nu$) [Tanaka, ZPC '95]

$$P_\tau(D^{(*)}) = \frac{\Gamma(B \rightarrow D^{(*)} \tau^{\lambda=+1/2} \nu) - \Gamma(B \rightarrow D^{(*)} \tau^{\lambda=-1/2} \nu)}{\Gamma(B \rightarrow D^{(*)} \tau \nu)}$$

Fit of an angle dependence:
between π, ρ and $W^*(\tau\nu)$ in τ
rest frame

B anomaly prediction

Charged Higgs

SU(2)_L-singlet scalar LQ (S_1)

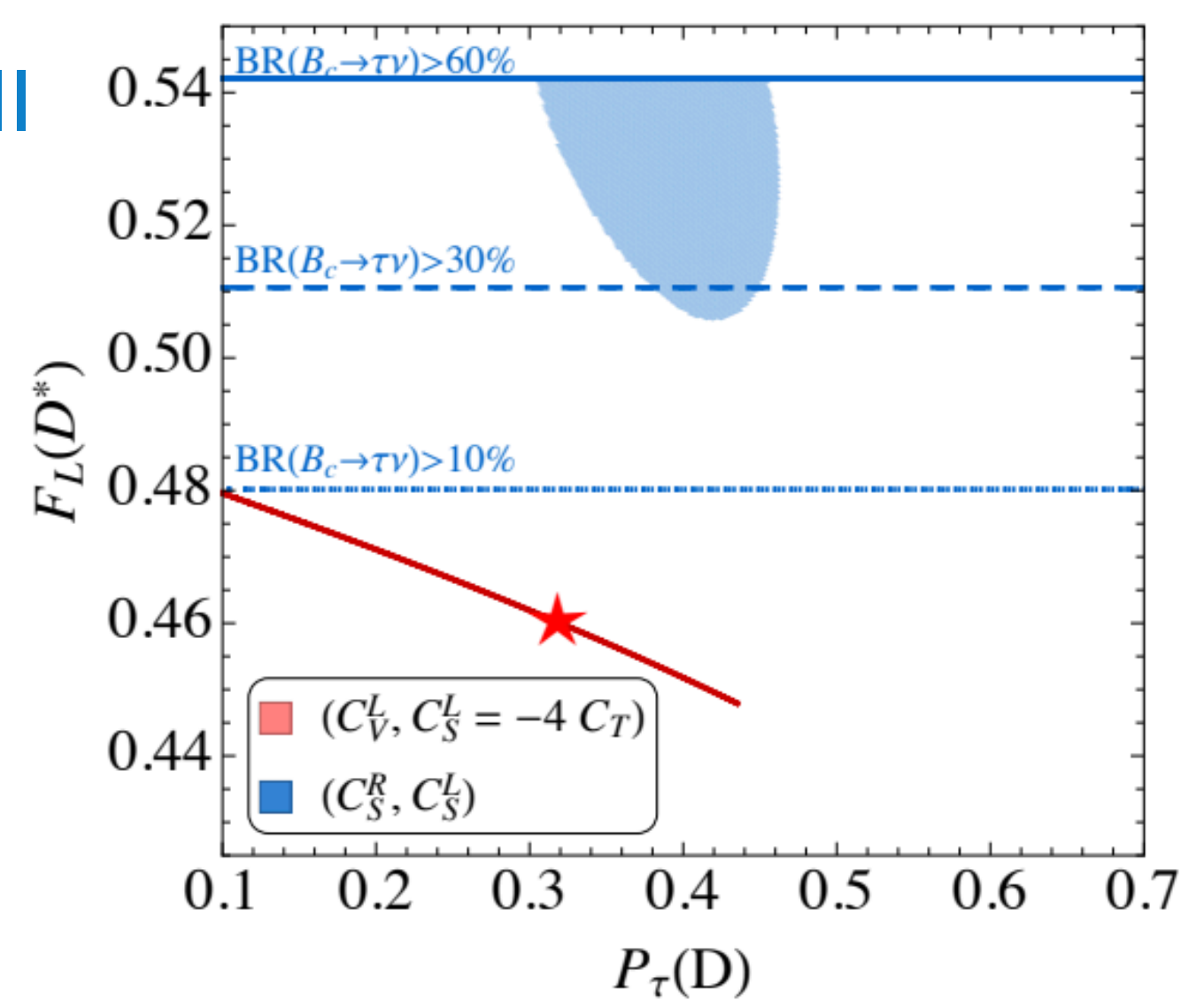
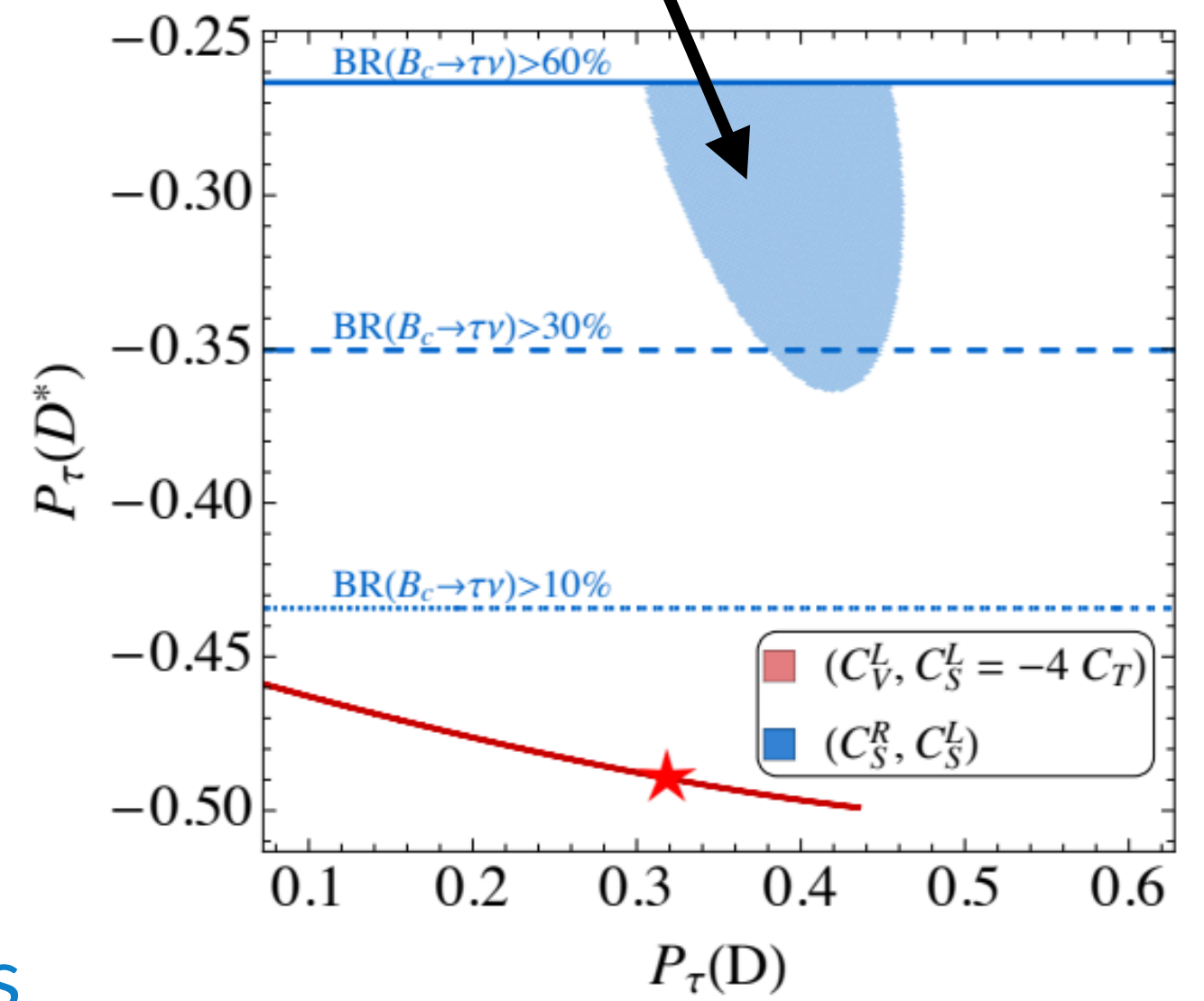
$P_\tau(D)$ vs. $P_\tau(D^*)$



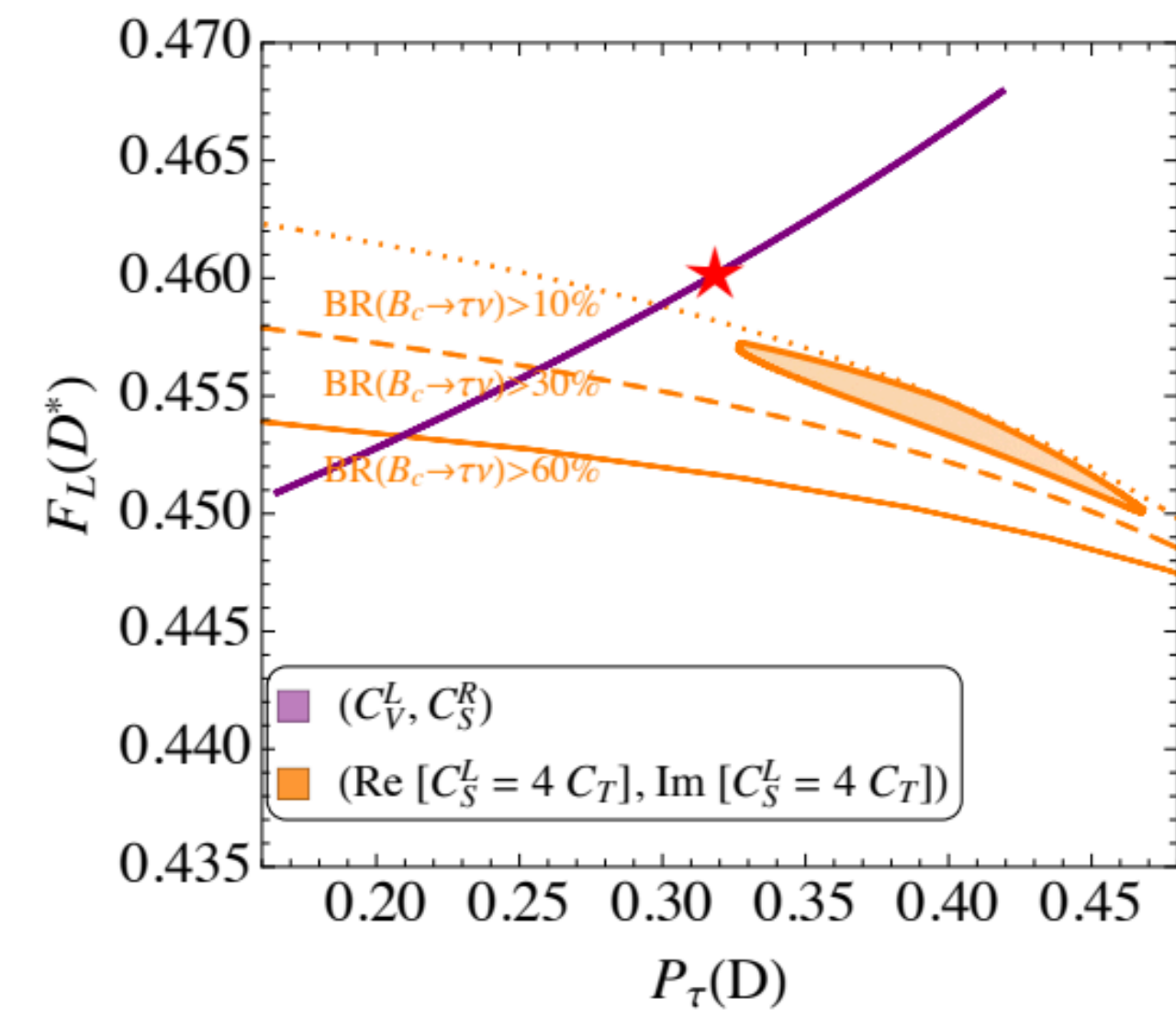
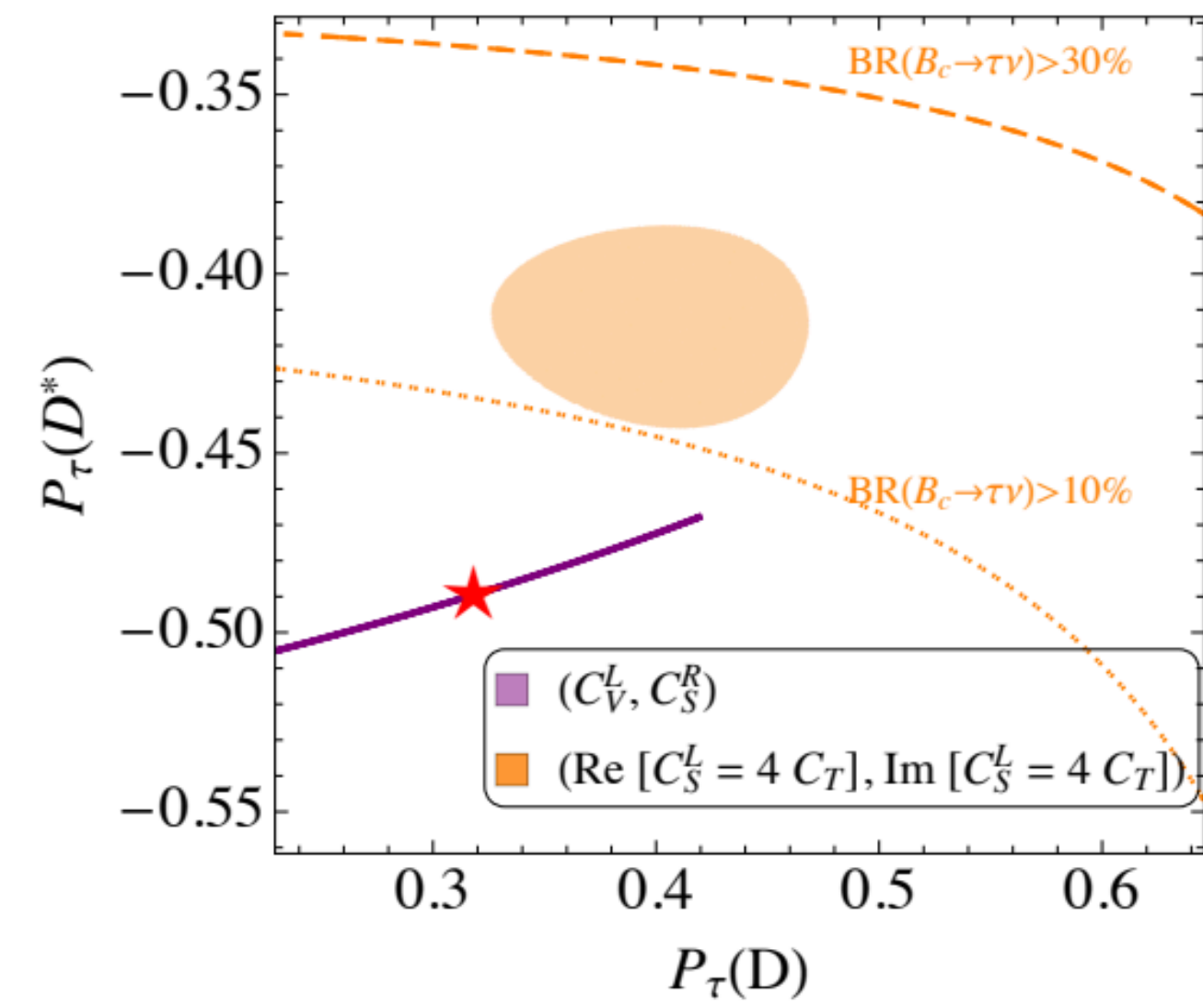
Polarization observables in $B \rightarrow D^{(*)}\tau\nu$, which will be probed by Belle II



$P_\tau(D)$ vs. $F_L(D^*)$



[Blanke, Crivellin, TK, Moscati, Nierste, Nisandzic '19]



SU(2)_L-doublet scalar LQ (R_2)

SU(2)_L-singlet vector LQ (U_1)

$P_\tau(D)$ can discriminate the new physics

$P_\tau(D^*)$ could discriminate the new physics

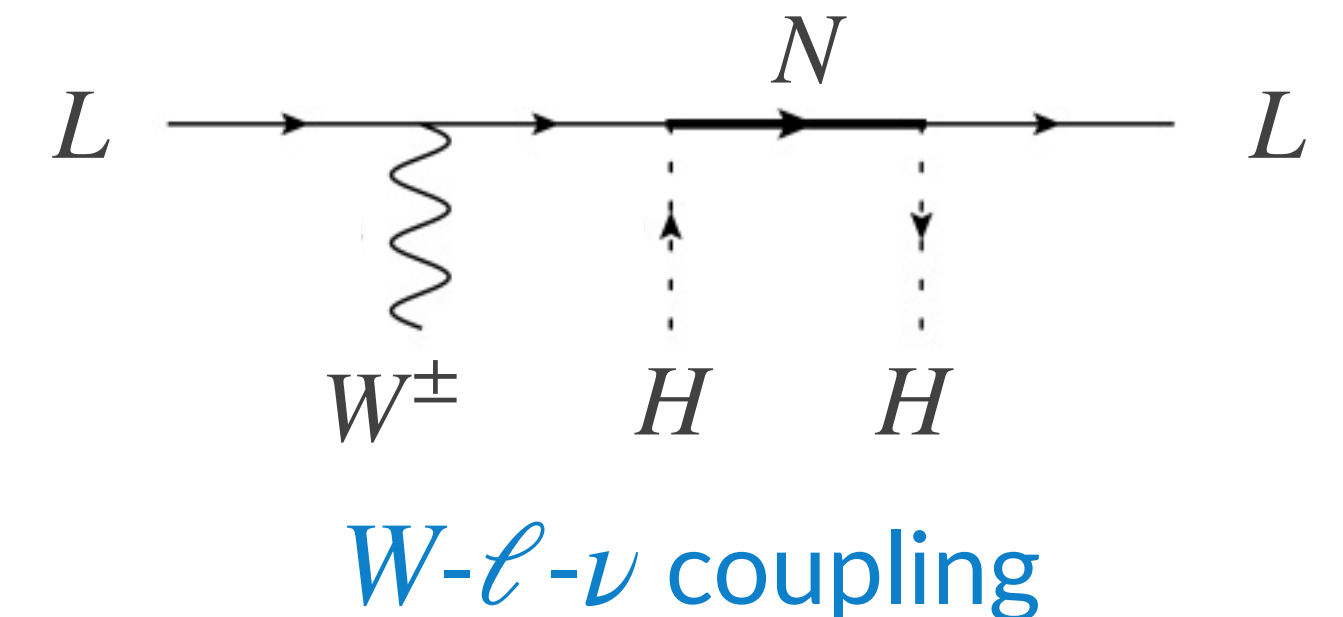
One can distinguish each new physics scenario

New physics interpretations of CAA

- ◆ EFT fittings: $(H^\dagger iD_\mu^L H)(\bar{L}\gamma^\mu \tau^I L)$ fit [Coutinho, et al, [1912.08823](#)]; right-handed current fit [Grossman, et al, [1911.07821](#), Cirigliano, et al, [2112.02087](#)]; $W-\ell-\nu$ fit [Crivellin, et al, [2002.07184](#)]; G_F fit [Crivellin, et al, [2102.02825](#)]
- ◆ Heavy $SU(2)_L$ vector boson (~ 10 TeV) [Capdevila, et al, [2005.13542](#)]
- ◆ Leptoquark (~ 5 TeV) [Marzocca, Trifinopoulos, [2104.05730](#)]
- ◆ Vector-like Quark (1-5 TeV) [Belfatto, et al, [1906.02714](#), [2103.05549](#); Cheung, et al, [2001.02853](#); Branco, et al, [2103.13409](#)]
- ◆ Vector-like Lepton (1-2 TeV) [Endo, Mishima, [2005.03933](#); Crivellin, et al, [2008.01113](#); Kirk, [2008.03261](#)]

◆ **Heavy right-handed neutrino** (type I seesaw) can not explain the tension, but the unphysical region [$(\text{mixing})^2 < 0$] is favored

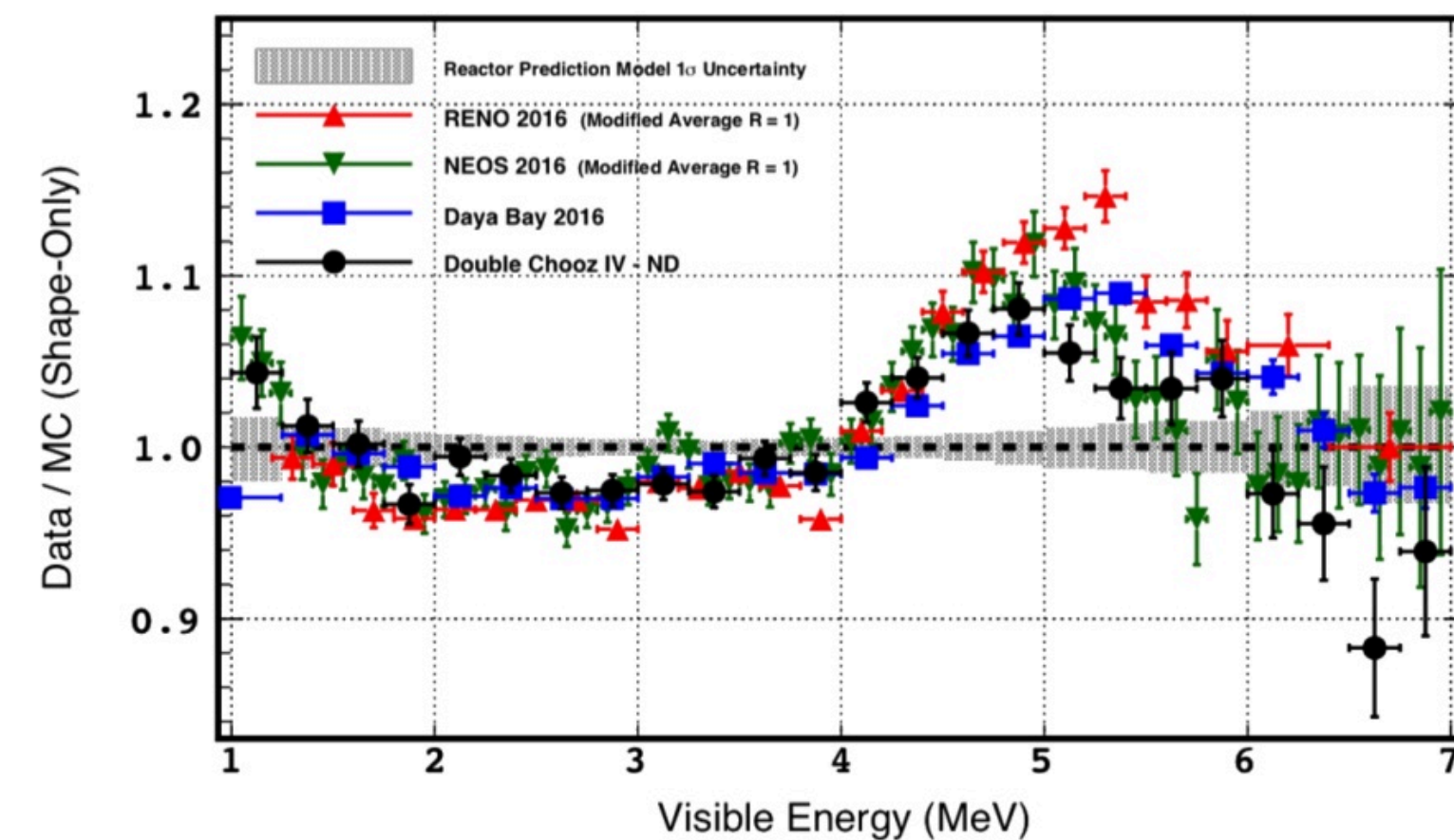
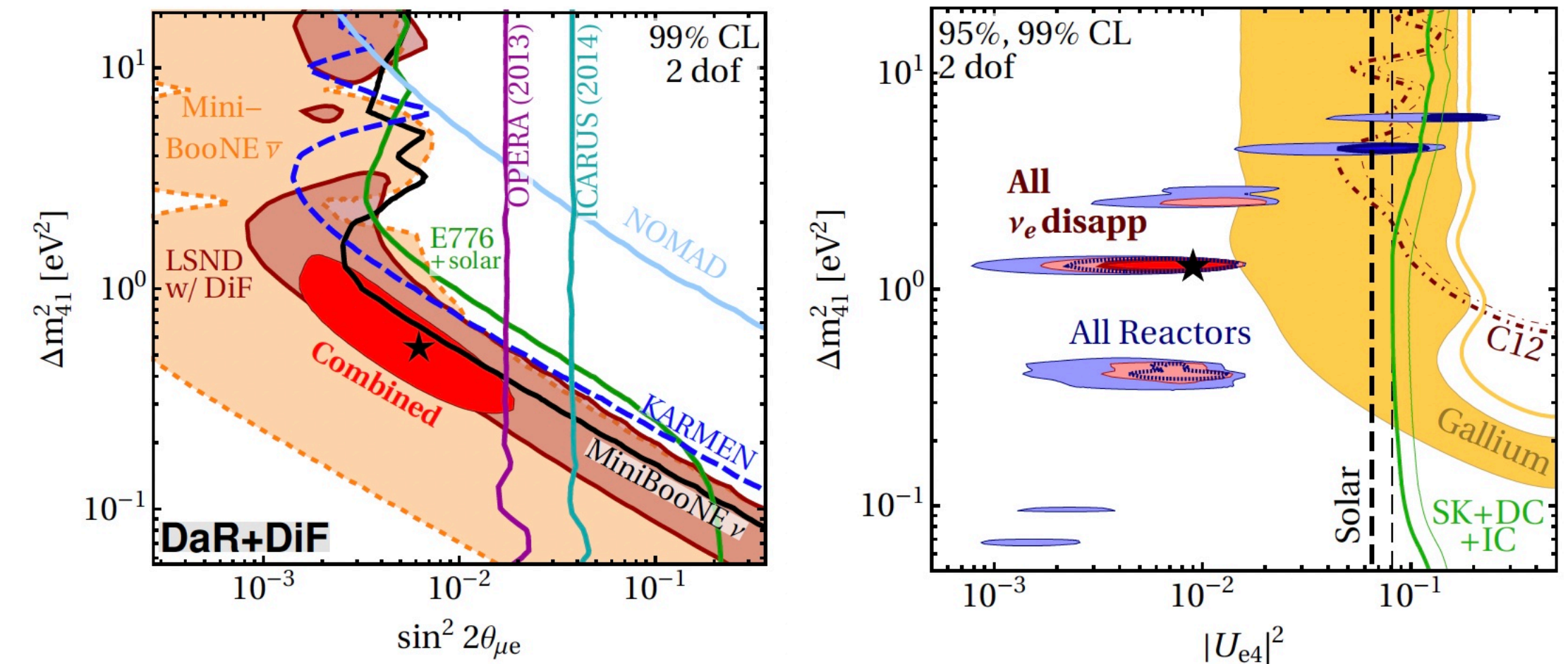
◆ **How about a light sterile neutrino?**



Neutrino anomalies on the market

- ◆ **$O(1)$ eV sterile neutrino** (neutrino oscillations from LSND, MiniBooNE, Gallium Anomaly, Reactor Antineutrino Anomaly)
- ◆ **7 keV decaying sterile neutrino** (3.5 keV photon emission from galaxy clusters)
- ◆ **5 MeV bump in antineutrino energy spectrum** (RENO, NEOS, Daya Bay, Double Chooz)
- ◆ But, no conclusive measurements yet

[Dentler et al, [1803.10661](#)]

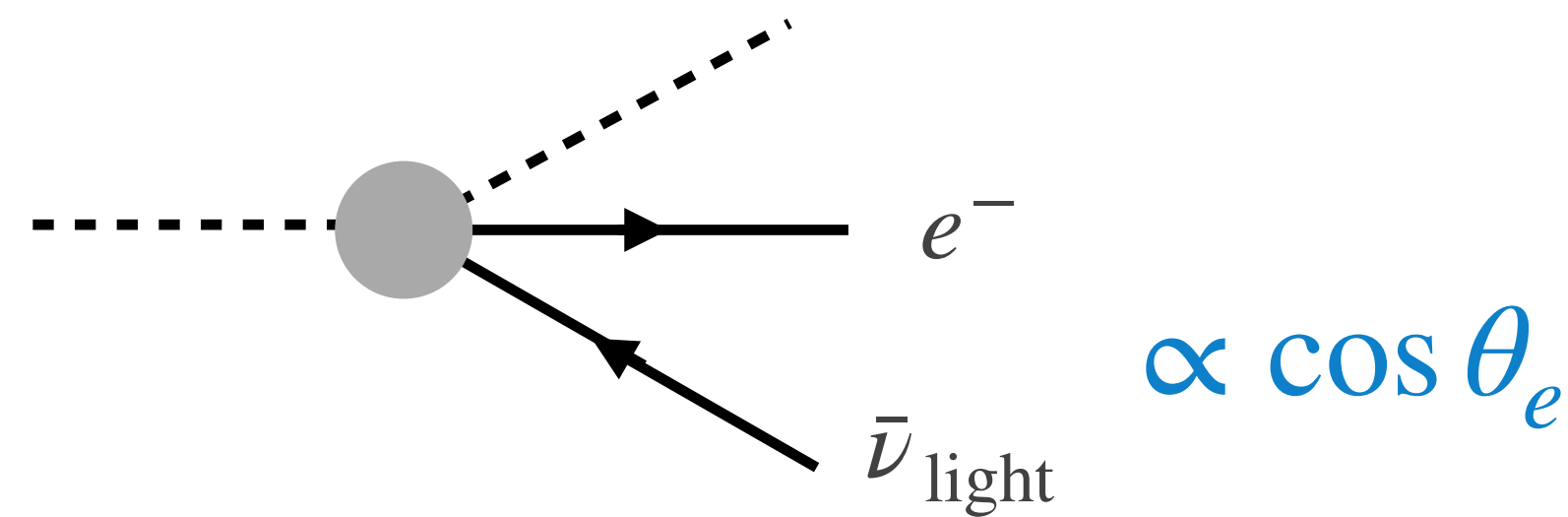


[Double Chooz, [1901.09445](#)]

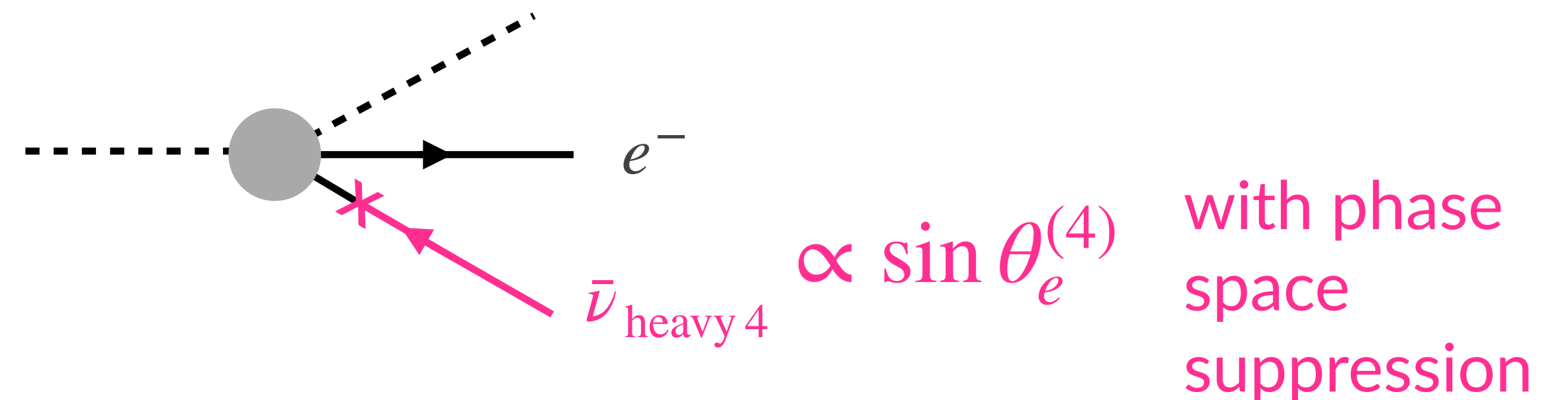
Sterile neutrino contributions

- ◆ **Two contributions** to the leptonic and semi-leptonic decays

1. modifies active neutrino coupling



2. decay into sterile neutrino if kinematically possible



- ◆ When the sterile neutrino masses are much smaller than the decay Q-value ($M_N \ll Q$), **the total contribution from 1+2 is canceled**

$$|\mathcal{M}|^2 = |\mathcal{M}_{\text{SM}}|^2 \cos^2 \theta_e + |\mathcal{M}_{\text{SM}}|^2 \sin^2 \theta_e \times f(M_N, Q)$$

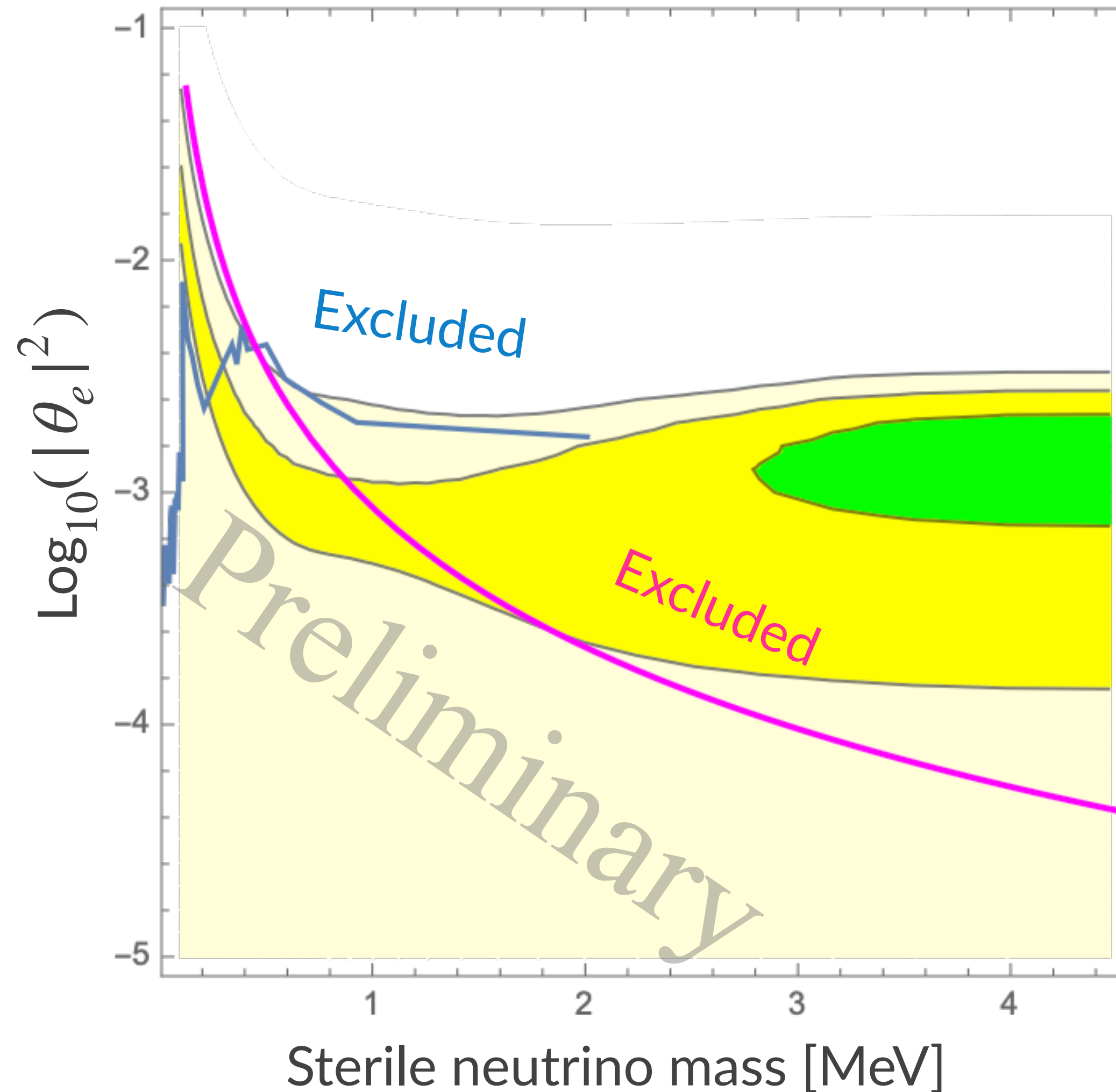
$$\simeq |\mathcal{M}_{\text{SM}}|^2 (\cos^2 \theta_e + \sin^2 \theta_e) = |\mathcal{M}_{\text{SM}}|^2$$

[Isakov, Strikman, '86;
Deutxh, Lebrun, Prieels, '90]

sterile-neutrino contributions
are suppressed when $M_N \ll Q$

Sterile neutrino fitting

Favored parameter regions ($1\sigma/2\sigma$) in a MeV sterile neutrino model with assuming CKM unitarity



[Kitahara, Tobioka, in progress]

Kink search in the energy spectrum of the isotope β decays [Bolton, et al, [1912.03058](#)]

$$E_{\text{kink}} = Q - M_N$$

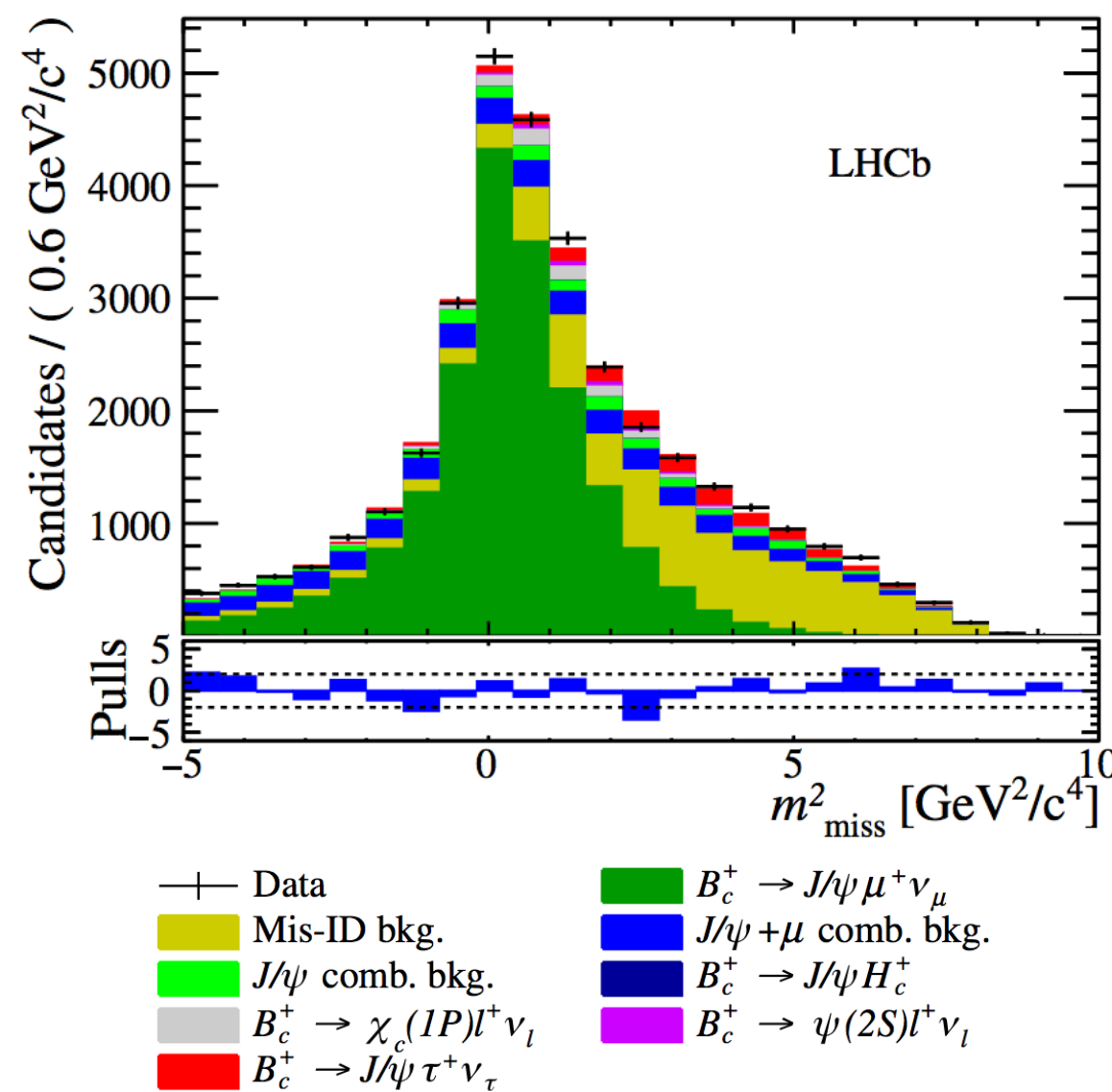
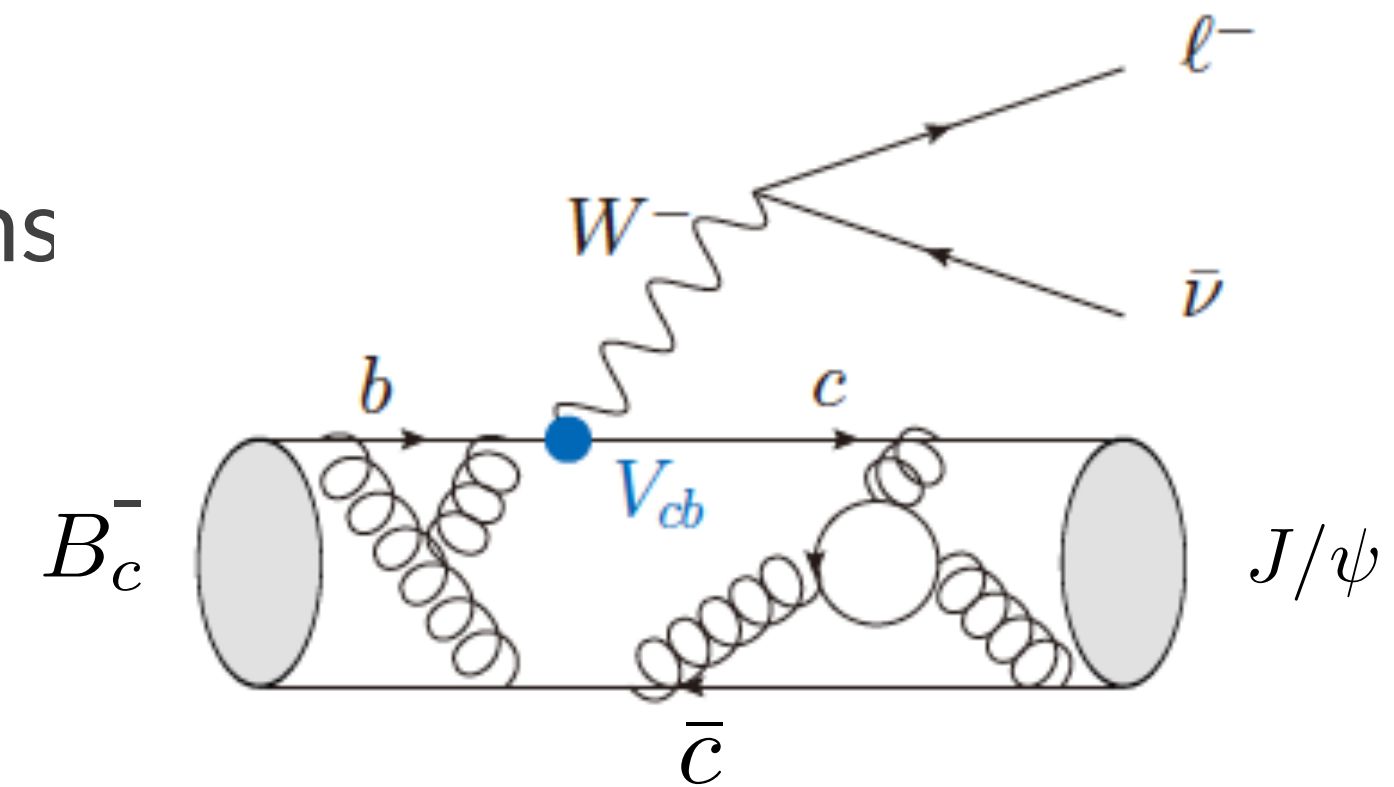
PIENU experiment: [1506.05845](#), [1909.11198](#)

$$\frac{\text{BR}(\pi^+ \rightarrow e^+ \nu_e)}{\text{BR}(\pi^+ \rightarrow \mu^+ \nu_\mu)}$$

Related channel: $R(J/\psi)$

- ◆ The LFU violation was measured in $B_c^- \rightarrow J/\psi$ transitions

$$\mathcal{R}(J/\psi) = \frac{\mathcal{B}(B_c^- \rightarrow J/\psi \tau^- \bar{\nu}_\tau)}{\mathcal{B}(B_c^- \rightarrow J/\psi \ell^- \bar{\nu}_\ell)}$$



$$R(J/\psi)_{\text{exp}} = 0.71 \pm 0.17_{\text{stat}} \pm 0.18_{\text{syst}} \quad [\text{LHCb, 1711.05623}]$$

$$R(J/\psi)_{\text{SM}} = 0.2582 \pm 0.0038 \quad \text{Based on first lattice result [HPQCD, 2007.06956]}$$

1.8 σ consistent using $N_f=2+1+1$, with “HISQ” c and heavy quark b

Same-direction tension as $R(D)$ and $R(D^*)$ anomalies

New physics study, e.g., [Watanabe, PLB '18; Alok, Kumar, Kumar, Kumbhakar, Sankar, JHEP '18]

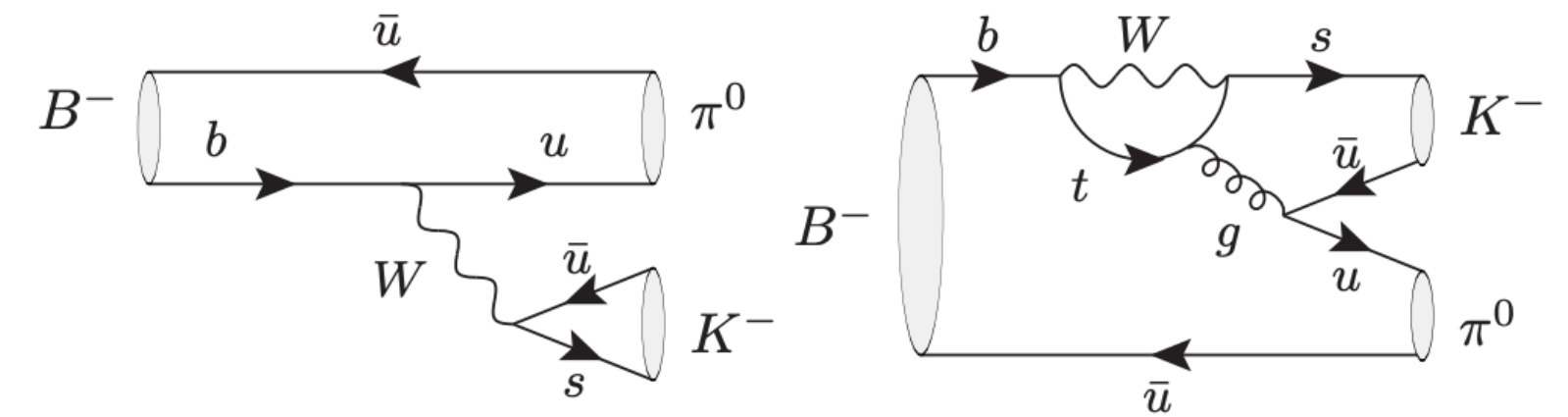
“K π puzzle”: Direct CPV in $B \rightarrow K\pi$ modes

- ◆ Direct CP asymmetry is obtained by

$$A_{CP} = \frac{\Gamma(\bar{B} \rightarrow \bar{f}) - \Gamma(B \rightarrow f)}{\Gamma(\bar{B} \rightarrow \bar{f}) + \Gamma(B \rightarrow f)}$$

- ◆ The difference between two direct CP asymmetries [note that $\mathcal{B}(B \rightarrow K\pi) = \mathcal{O}(10^{-5})$]

$$\Delta A_{CP}(K\pi) = A_{CP}(B^+ \rightarrow \pi^0 K^+) - A_{CP}(B^0 \rightarrow \pi^- K^+) = 0 \text{ @ SM leading order}$$



All data are in agreement with each other

$$A_{CP}|_{\text{BaBar}}(B^+ \rightarrow \pi^0 K^+) = (3.0 \pm 3.9 \pm 1.0) \%$$

$$A_{CP}|_{\text{Belle}}(B^+ \rightarrow \pi^0 K^+) = (4.3 \pm 2.4 \pm 0.2) \%$$

$$A_{CP}|_{\text{BaBar}}(B^0 \rightarrow \pi^- K^+) = (-10.7 \pm 1.6^{+0.6}_{-0.4}) \%$$

$$A_{CP}|_{\text{Belle}}(B^0 \rightarrow \pi^- K^+) = (-6.9 \pm 1.4 \pm 0.7) \%$$

$$A_{CP}|_{\text{CDF}}(B^0 \rightarrow \pi^- K^+) = (-8.3 \pm 1.3 \pm 0.4) \%$$

$$A_{CP}|_{\text{LHCb}}(B^0 \rightarrow \pi^- K^+) = (-8.4 \pm 0.4 \pm 0.3) \%$$

2.3σ tension



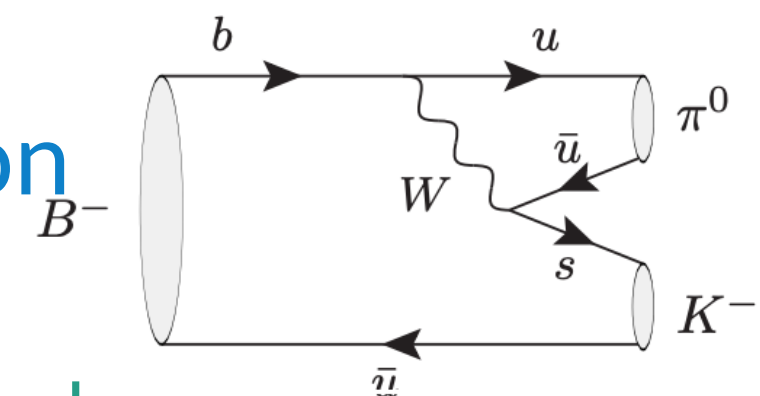
$$\Delta A_{CP}|_{\text{SM}}(K\pi) = (1.8^{+4.1}_{-3.2}) \%$$

[Hofer, Scherer, Vernazza, JHEP '11;
Crivellin, Gross, Pokorski, Vernazza, PRD '20]

$$\Delta A_{CP}|_{\text{exp}}(K\pi) = (12.4 \pm 2.1) \% \quad [\text{HFLAV averages 2019}]$$

SM explanation can be possible, if this contribution is bigger than the NLO prediction by a factor of 2

[Li, Mishima, PRD '11; Beaudry, Datta, London, Rashed, Roux, JHEP '18]

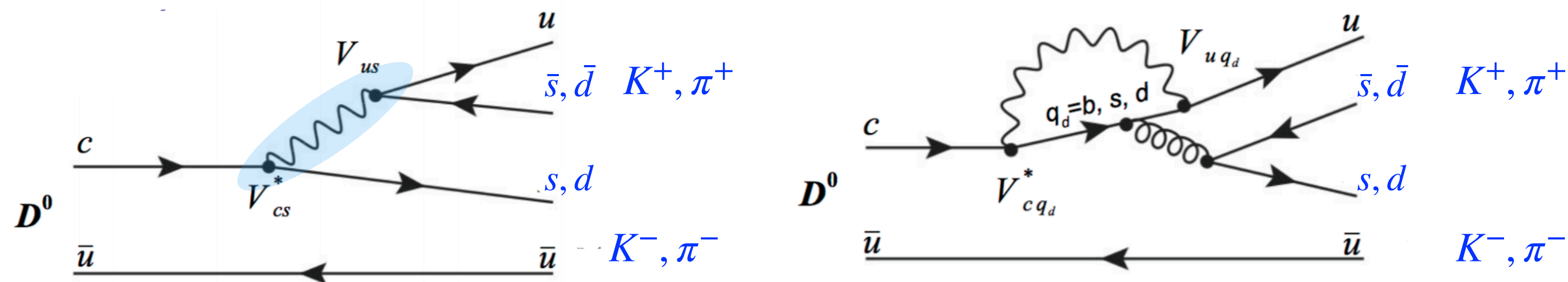


The first observation of CPV in D -meson

- ◆ Difference of Difference of $D^0 \rightarrow h^- h^+ \bar{a}$ and $D^0 \rightarrow h^- h^+$

Direct CPV $A_{CP}(D^0 \rightarrow K^- K^+) \equiv \frac{\#(D^0(t=0) \rightarrow K^- K^+) - \#(\bar{D}^0(t=0) \rightarrow K^- K^+)}{\#(D^0(t=0) \rightarrow K^- K^+) + \#(\bar{D}^0(t=0) \rightarrow K^- K^+)}$

Observable $\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^- K^+) - A_{CP}(D^0 \rightarrow \pi^- \pi^+)$

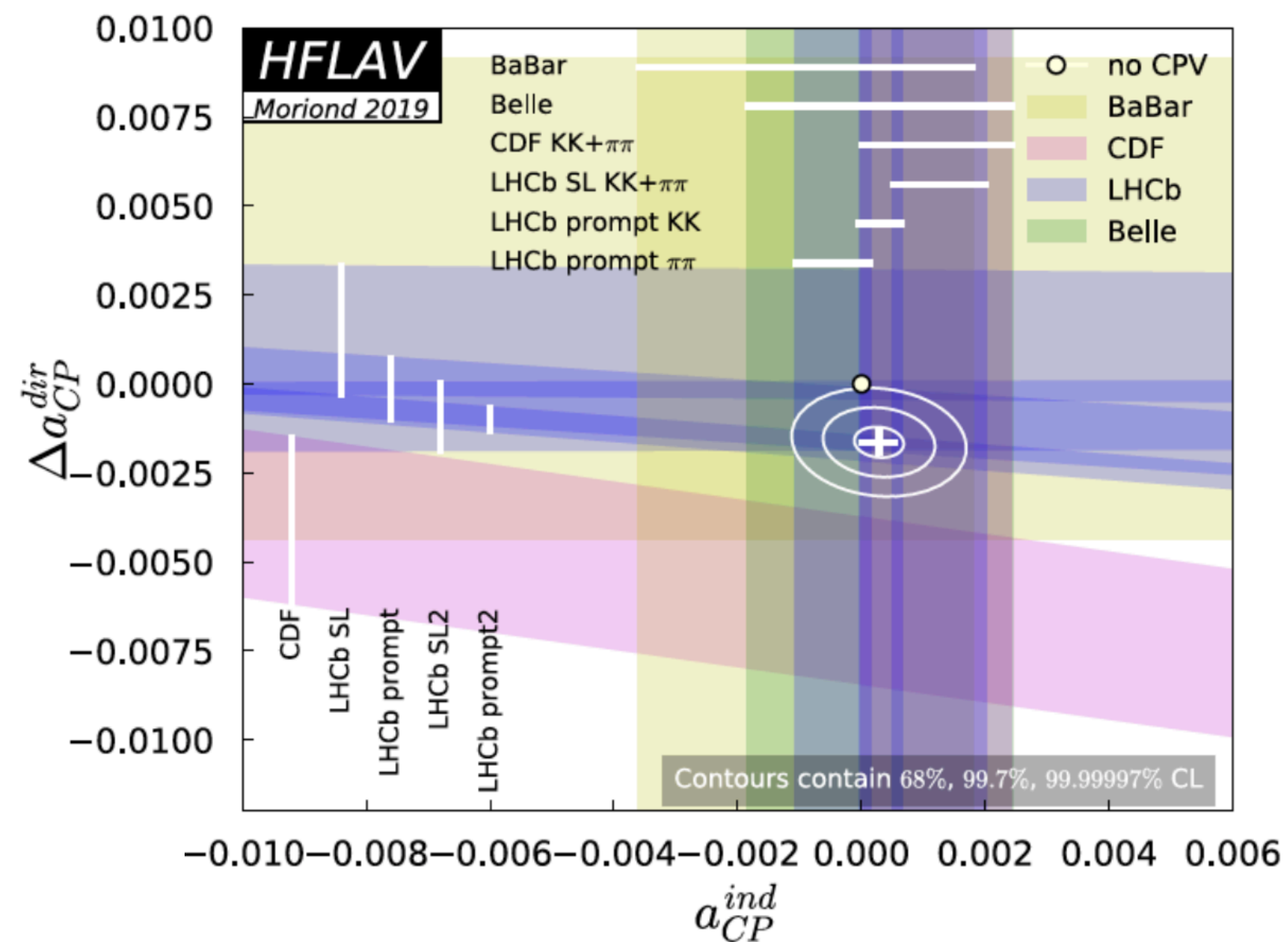


The Direct CPV is *amplified* in the difference! $V_{cd} : V_{us} \simeq -1 : 1$

Detection asymmetry and final-state independent uncertainty are dropped!

Direct CP violation in D

World average



Latest result [LHCb, 1903.08726]

$$\Delta a_{CP}^{dir} = (-15.7 \pm 2.9) \times 10^{-4} \quad 5.3\sigma \text{ discovery of CPV!}$$

But, need confirmation by Belle II

A reliable SM prediction [QCD sum rule]

$$|\Delta a_{CP}^{dir}| < (2.0 \pm 0.3) \times 10^{-4} \quad [\text{Khodjamirian, Petrov, PLB '17}]$$

Smaller than the data by a factor of 7; 4.7 σ tension

(QCD sum rule works well in B physics)

SM explanation could be possible by QCD re scattering

$$D^0 \rightarrow \pi\pi \rightarrow K^-K^+ \quad [\text{Grossman, FPCP2020}]$$

New physics implications; 2HDM, MSSM, vector-like quark

[Dery, Nir, JHEP '19]