

# 3サイトヒッグスレス模型への $Z \rightarrow b \bar{b}$ からの制限

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collaborate with

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**arXiv:0902.3910** [hep-ph]

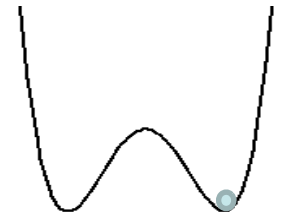
タウ・レプトン物理研究センター研究報告会 (3.26.2009)

# Introduction

Standard Model describes the phenomenology of elementary particles.

Higgs particle

- SSB of EW symmetry (the origin of mass)
- Unitarize the scattering amplitude of gauge bosons.



$$i\mathcal{M}(W_L^a W_L^b \rightarrow W_L^c W_L^d) = \text{[t-channel diagram]} + \text{[W boson exchange diagram]} + \text{[Higgs exchange diagram]} + \text{crossed.}$$

- The precision test indicates  $M_h \leq 200 \text{ GeV}$

### 標準模型

$$i\mathcal{M}(W_L^a W_L^b \rightarrow W_L^c W_L^d) =$$

+crossed.

### ヒッグスレス模型

$$i\mathcal{M}(W_L^a W_L^b \rightarrow W_L^c W_L^d) =$$

+ ...

# Introduction

Higgs has not appeared yet. (  $M_h \geq 114 \text{ GeV}$  )

=SSB of EW symmetry remains unsolved.

- If Higgs exists
  - naturalness problem  $\delta M_H^2 \sim \Lambda^2$
- If Higgs does not exist
  - unitarity problem
  - consistency with EWPT

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Are there any models compatible with EWPT without Higgs ?

 **Higgsless model** is one of the candidate.

# Contents

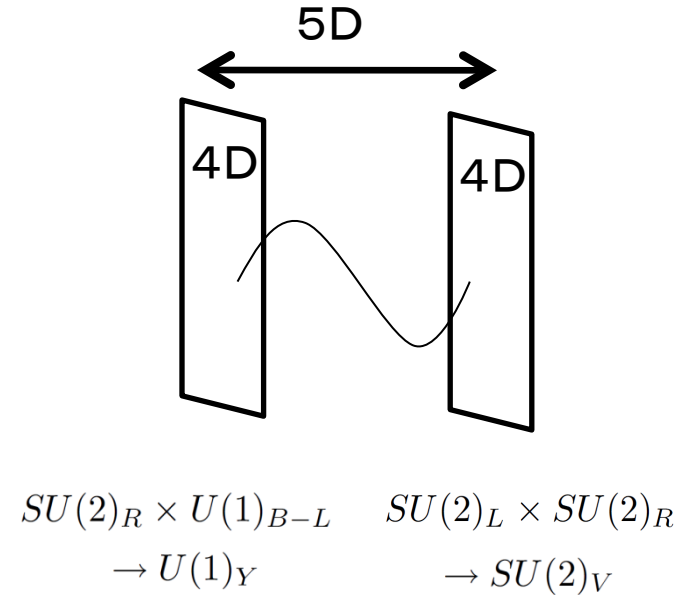
- ✓ 1. Introduction
- 2. Higgsless model
  - 3. Z b bbar coupling
  - 4. Summary

# Introduction

## Higgsless model

- is based on 5D gauge theory.
- breaks EW sym. by the boundary conditions for 5th direction.

$$SU(2)_L \times SU(2)_R \times U(1)_{B-L} \rightarrow U(1)_{em}$$



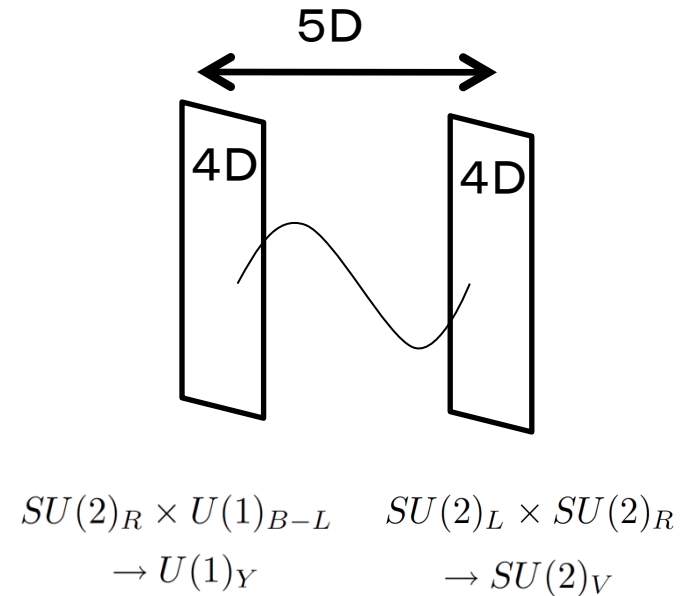
- Massive particles appear as Kaluza-Klein mode (KK mode)

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- Massive particles appear as Kaluza-Klein mode (KK mode)

→ these play the role of Higgs in SM.

- unitarity conservation
- consistency with EWPT



# Introduction

## Kaluza-Klein mode (KK mode) の説明

- 4次元で見たら質量がある
- 簡単のため、スカラー場で説明

5次元 massless スカラー場

$$(\partial_\mu \partial^\mu - \partial_5 \partial_5) \phi(x, y) = 0$$

変数分離：4次元+5次元目

$$\phi(x, y) = \phi(x) f(y)$$

$$\square \phi(x) = \text{const} \times \phi(x)$$

$$\partial_5 \partial_5 f(y) = \text{const} \times f(y)$$

← const が質量に相当

# Introduction

$$\square\phi(x) = \text{const} \times \phi(x)$$
$$\partial_5\partial_5 f(y) = \text{const} \times f(y)$$

$$\phi(x, y) = \phi(x)f(y)$$

例えば次のような境界条件を課す(両端ともにディレクレ条件)

$$f(0) = 0$$

$$f(\pi R) = 0$$

すると

$$f_n(y) = A \sin\left(\frac{ny}{R}\right)$$

$$\partial_5\partial_5 f_n(y) = -\left(\frac{n}{R}\right)^2 f_n(y)$$

$$n = 1, 2, 3 \dots \quad n = 0 \text{ は、} f(y)=0 \text{ となるので除く}$$

よって

$$\left(\square + \left(\frac{n}{R}\right)^2\right) \phi_n(x) = 0$$



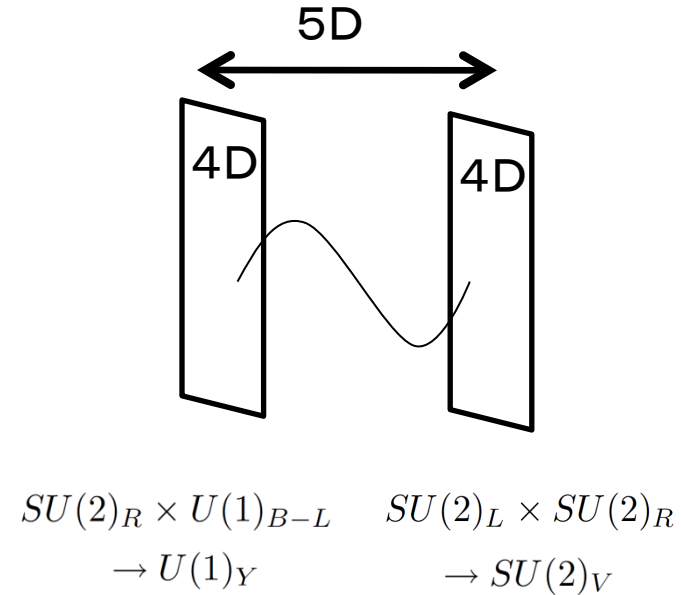
- $n$  に応じた質量をもつ
- 質量をもったモードが無  
限個現れる(KK モード)

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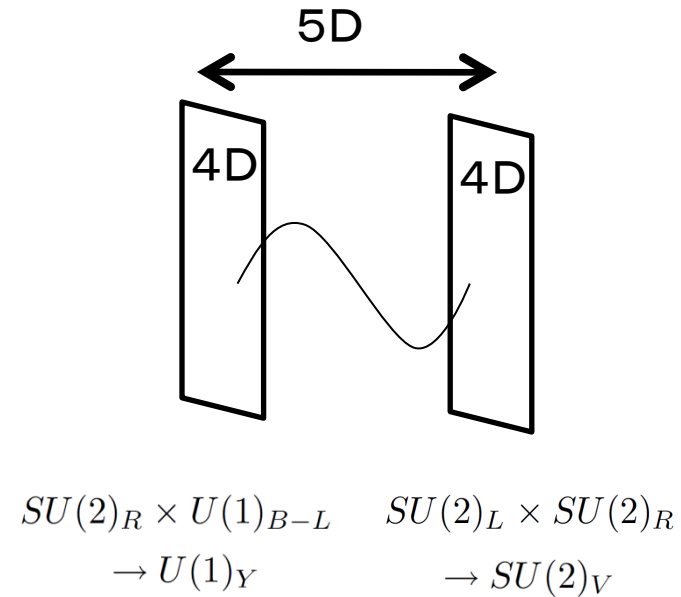
$$\begin{array}{ccccccc}
 \frown & \sim & \text{wavy} & \text{wavy} & \dots & & \\
 W, & W', & W'', & W'''' & \dots & & 
 \end{array}$$

# Introduction

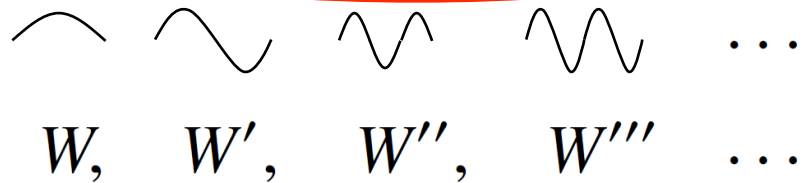
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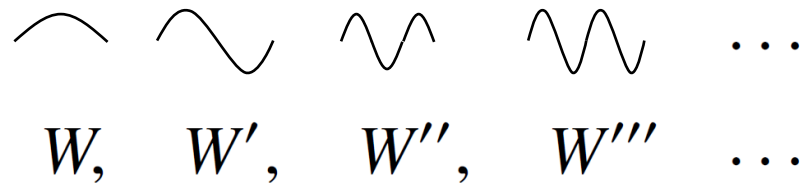


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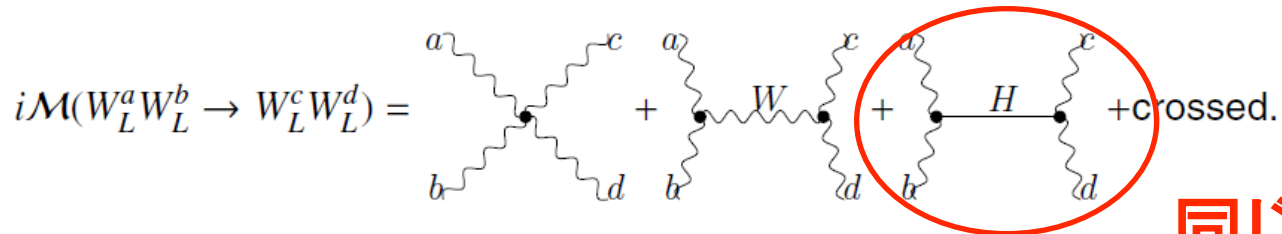


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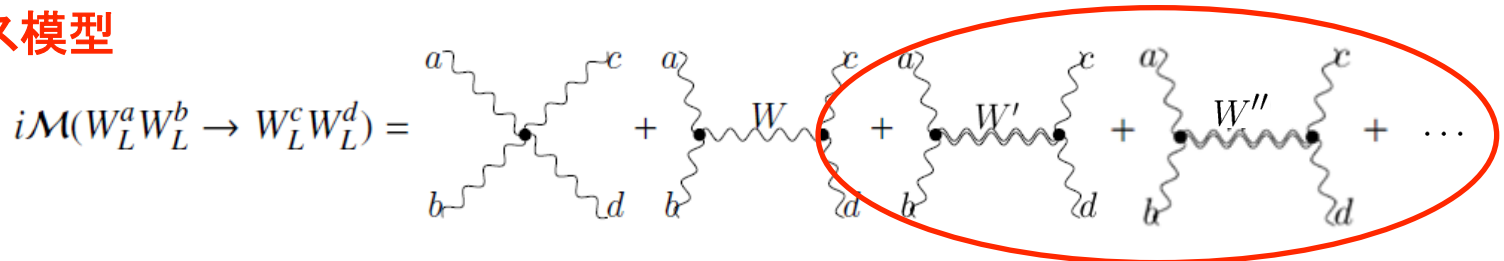


標準模型



同じ役割

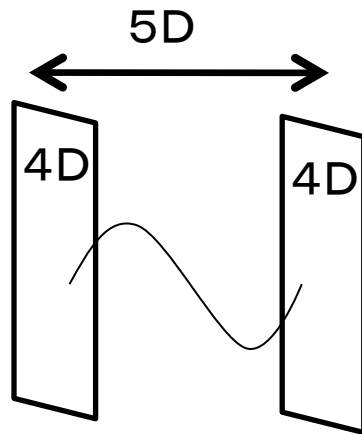
ヒッグスレス模型



# Introduction

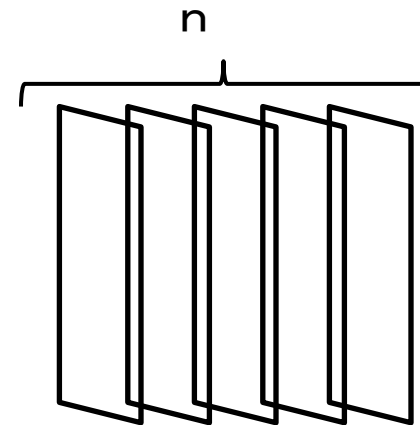
## Higgsless model

- deconstruction : discretion for 5th dim.  
→ we can treat it as 4D model.



$$SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

deconstruction



$$[SU(2)_L \times SU(2)_R \times U(1)_{B-L}]^n$$

# Introduction

## Higgsless model

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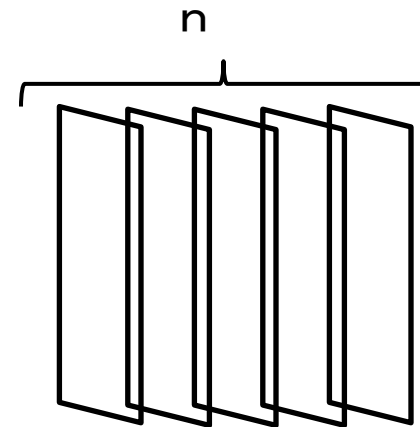
It is enough to analyze as a low energy effective theory



Integrate out of heavy gauge bosons



rough discretion



Boundary conditions

$$\begin{aligned} & SU(2)_L \times U(1)_Y \\ & \times [SU(2)_L \times SU(2)_R \times U(1)_{B-L}]^{n-2} \\ & \times SU(2)_V \times U(1)_{B-L} \\ & \rightarrow U(1)_{em} \end{aligned}$$

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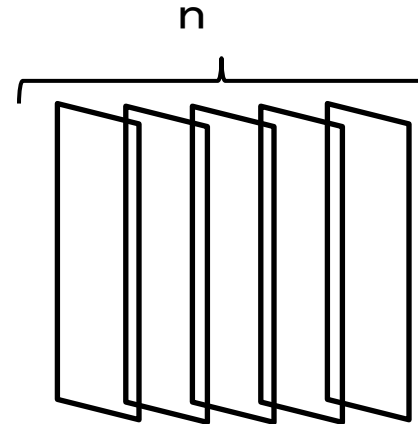


rough discretion



### 3site Higgsless model

$$SU(2)_0 \times SU(2)_1 \times U(1)_2 \rightarrow U(1)_{em}$$



Boundary conditions

$$\begin{aligned} & SU(2)_L \times U(1)_Y \\ & \times [SU(2)_L \times SU(2)_R \times U(1)_{B-L}]^{n-2} \\ & \times SU(2)_V \times U(1)_{B-L} \\ & \rightarrow U(1)_{em} \end{aligned}$$

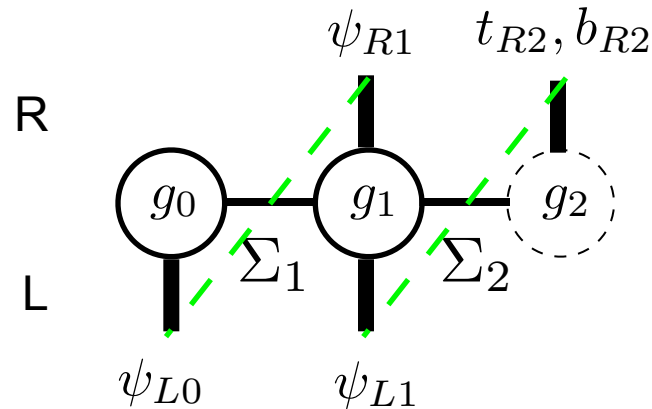


# 3site Higgsless model

R.S.Chivukula et.al Phys.Rev.D74:075011 (2006)  
 M.Bando et.al Nucl.Phys. B259 (1985) 493  
 R.Casalbuoni et.al Phys.Lett.B155(1985) 95

Minimal deconstructed model

$$SU(2)_0 \times SU(2)_1 \times U(1)_2 \rightarrow U(1)_{em}$$



NG bosons  $\Sigma_i = \exp\left(2i\frac{\pi_i}{f_i}\right)$

gauge bosons  $\gamma, W, W', Z, Z'$

fermions  $f_{SM} = \{t, b, c, \dots\}, F_{heavy} = \{T, B, C \dots\}$

## 3site Higgsless model

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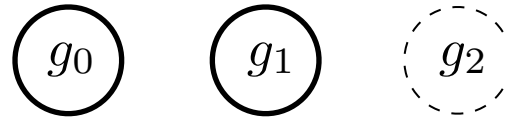
$$SU_0(2) \times SU_1(2) \times U_2(1)$$

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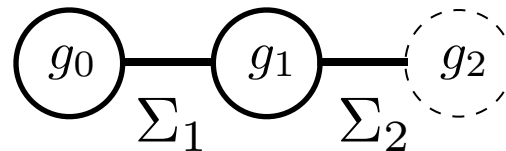


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Minimal deconstructed model

$$SU(2)_0 \times SU(2)_1 \times U(1)_2 \rightarrow U(1)_{em}$$



NG bosons  
(Non-linear rep.)

$$\Sigma_i = \exp \left( 2i \frac{\pi_i}{f_i} \right)$$

$$\Sigma_1 \rightarrow \exp \left( i \frac{\sigma^a}{2} \theta_0^a \right) \Sigma_1 \exp \left( -i \frac{\sigma^a}{2} \theta_1^a \right)$$

$$\Sigma_2 \rightarrow \exp \left( i \frac{\sigma^a}{2} \theta_1^a \right) \Sigma_2 \exp \left( -i \frac{\sigma^a}{2} \theta_2^a \right)$$

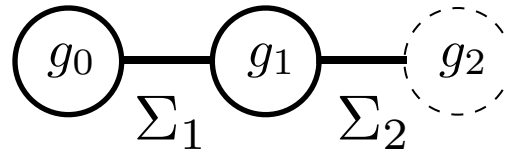
$$\frac{1}{v^2} = \frac{1}{f_1^2} + \frac{1}{f_2^2} \quad (v = 246 \text{ GeV})$$

# 3site Higgsless model

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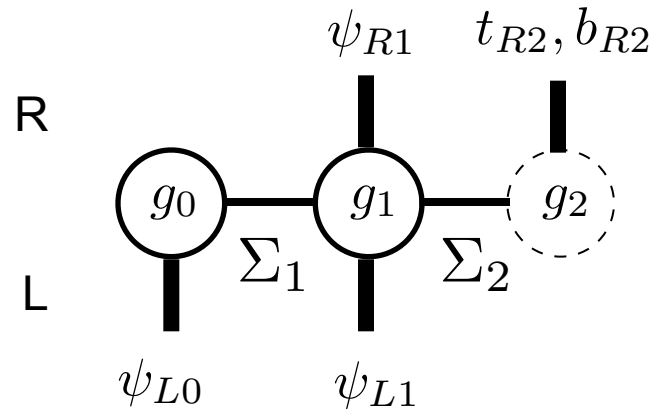


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|  | $SU(2)_0$ | $SU(2)_1$ | $U(1)_2$  | $SU(3)_c$ |
|--|-----------|-----------|---|-----------|
| $\Psi_{L0}$  | 2         | 1         | $\frac{1}{6} \begin{pmatrix} -\frac{1}{2} \\ -\frac{1}{2} \end{pmatrix}$                          | 3 (1)     |
| $\Psi_{L1}$  | 1         | 2         | $\frac{1}{6} \begin{pmatrix} -\frac{1}{2} \\ -\frac{1}{2} \end{pmatrix}$                          | 3 (1)     |
| $\Psi_{R1}$  | 1         | 2         | $\frac{1}{6} \begin{pmatrix} -\frac{1}{2} \\ -\frac{1}{2} \end{pmatrix}$                          | 3 (1)     |
| $\Psi_{R2} = \begin{pmatrix} u_{R2} \\ d_{R2} \end{pmatrix}$ | 1         | 1         | $\begin{pmatrix} \frac{2}{3} \\ -\frac{1}{3} \end{pmatrix} \begin{pmatrix} 0 \\ -1 \end{pmatrix}$ | 3 (1)     |

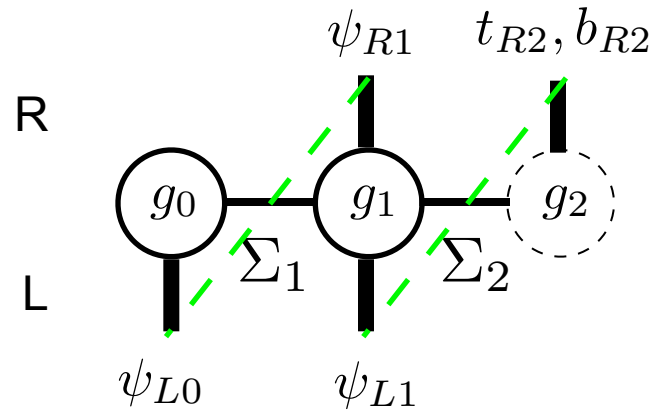
$\begin{pmatrix} \end{pmatrix}$  means lepton.

# 3site Higgsless model

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Minimal deconstructed model

$$SU(2)_0 \times SU(2)_1 \times U(1)_2 \rightarrow U(1)_{em}$$



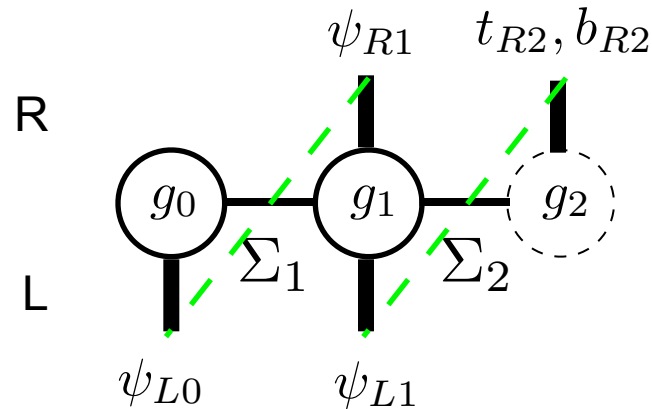
$$-m_1 \bar{\psi}_{L0} \Sigma_1 \psi_{R1} - M \bar{\psi}_{R1} \psi_{L1} - \bar{\psi}_{L1} \Sigma_2 \begin{pmatrix} m'_t & 0 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} t_{R2} \\ b_{R2} \end{pmatrix} + (h.c.)$$

# 3site Higgsless model

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NG bosons

$$\Sigma_i = \exp \left( 2i \frac{\pi_i}{f_i} \right)$$

gauge bosons

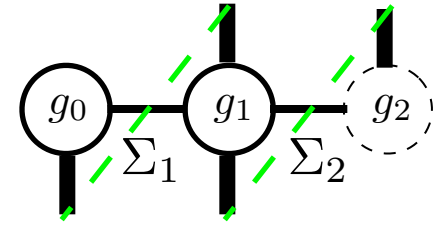
$$\gamma, W, W', Z, Z'$$

fermions

$$f_{SM} = \{t, b, c, \dots\}, F_{heavy} = \{T, B, C \dots\}$$

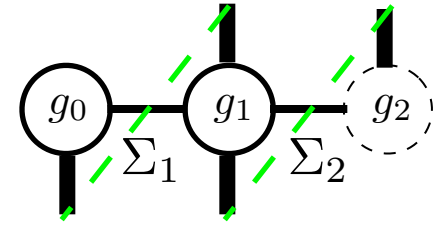


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- ➔ 3. Z b bbar coupling
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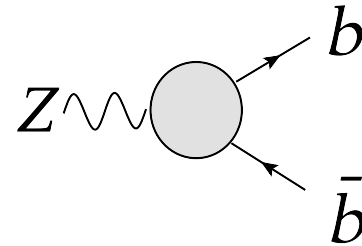
# Z b bbar coupling



## Z b bbar coupling

- We calculated flavor dependent correction.

$$g_Z \left( -\frac{1}{2} + \delta g_L^{b\bar{b}} + \frac{1}{3} \sin^2 \theta_W \right)$$



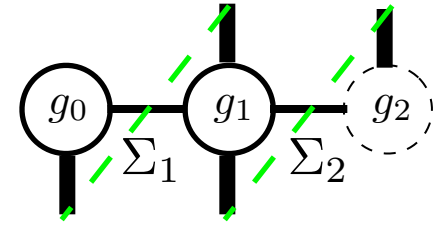
$$(\delta g_L^{b\bar{b}})_{sm} = \frac{m_t^2}{16\pi^2 v^2} \quad (\text{SM correction})$$

- We used  $R_b$  to find the constraint on this model.

$$R_b \equiv \frac{\Gamma(Z \rightarrow b\bar{b})}{\Gamma(Z \rightarrow \text{hadrons})}$$

$$\delta R_b^{\text{obs}} \equiv R_b^{\text{obs}} - R_b^{\text{SM}} = (4.5 \pm 6.6) \times 10^{-4}$$

# Z b bbar coupling



- The correction in 3site Higgsless model

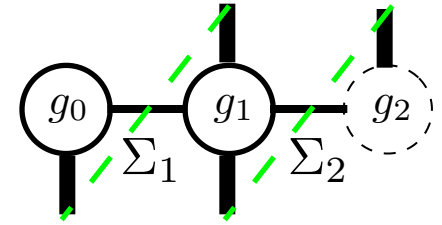
$$\delta g_L^{b\bar{b}} = \frac{m_t^2}{(4\pi)^2 v^2} \left[ 1 + \frac{f_1^2 f_2^2}{2(f_1^2 + f_2^2)^2} \log \left( \frac{\Lambda^2}{M^2} \right) \right]$$

$\Lambda$  : Cut off scale of this model  
 $M$  : Dirac mass (Heavy fermion mass)

- We can calculate this by RGE

$$j_L^{a\mu} \supset \left( 1 - \frac{\epsilon_L^2 f_2^2}{f_1^2 + f_2^2} \right) \bar{\psi}_L \gamma^\mu \frac{\sigma^a}{2} \psi_L \quad : \text{current coupled to Z boson}$$

# Z b bbar coupling



- The correction in 3site Higgsless model

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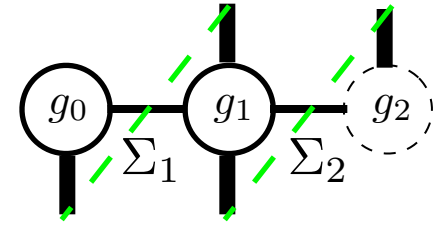
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Only this term has the flavor dependence

$$\Delta \epsilon_L^2 \equiv \left( \frac{m_1}{M} \right)_{3rd}^2 \Big|_{\mu=M} - \left( \frac{m_1}{M} \right)_{1st}^2 \Big|_{\mu=M} = \frac{1}{(4\pi)^2} \frac{m_t'^2}{f_2^2} \left( \frac{m_1}{M} \right)^2 \ln \frac{\Lambda^2}{M^2}$$

# Z b bbar coupling



Constraint from  $R_b$

$$R_b \equiv \frac{\Gamma(Z \rightarrow b\bar{b})}{\Gamma(Z \rightarrow \text{hadrons})}$$

$$\delta R_b = 2R_b(1 - R_b) \frac{g_{bL}}{g_{bL}^2 + g_{bR}^2} \delta g_L^{\text{NP}}$$

$$\delta g_L^{b\bar{b}} = \frac{m_t^2}{(4\pi)^2 v^2} \left[ 1 + \frac{f_1^2 f_2^2}{2(f_1^2 + f_2^2)^2} \log \left( \frac{\Lambda^2}{M^2} \right) \right]$$

$$\longrightarrow \frac{\Lambda}{M} < 4.6 \quad (95\% \text{ CL})$$

We expect a  $\Lambda$  of order 4 TeV or less;  $\Lambda \leq 4\pi f_{1,2} \sim 4\text{TeV}$

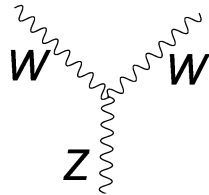
( Naive dimensional analysis )

$$\longrightarrow M \geq 1\text{TeV}$$

# Comparison with EWPT

- constraint from WWZ coupling (LEP)

$$M_{W'} \geq 380 \text{ GeV}$$



K.Hagiwara, R.D.Peccei, D.Zeppenfeld, and K.Hikasa, Nucl.Phys. B282,253(1987)

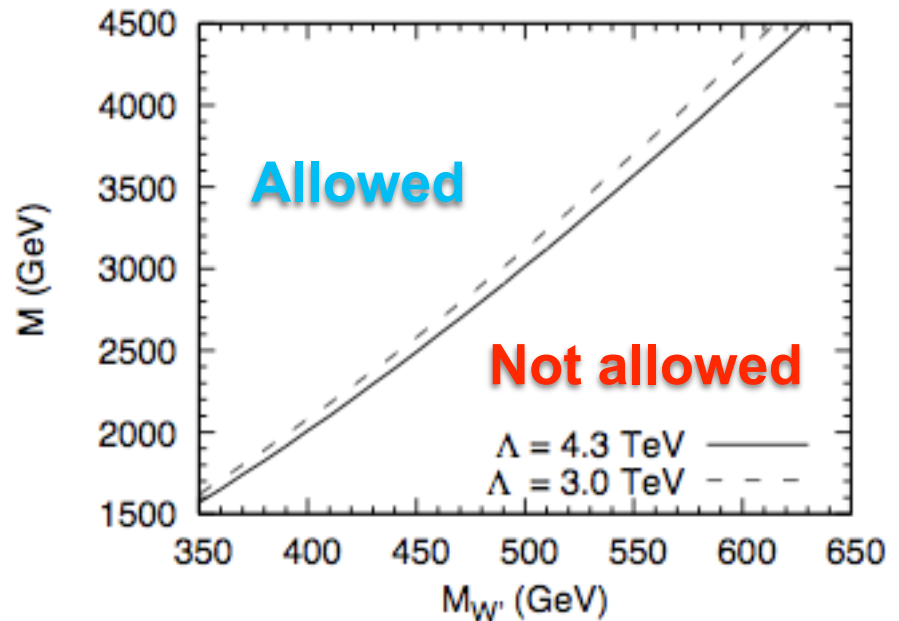
- constraint from ST fit

$$M \geq 1800 \text{ GeV}$$

- constraint from Z b bbar

$$M \geq 1000 \text{ GeV}$$

T.A, S.Matsuzaki, M.Tanabashi Phys.Rev.D78:055020,2008



➔ Z b bbar constraint is relatively mild and automatically satisfied.

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# Summary

- **Higgsless model** can break EW symmetry without Higgs particles.
- **3site Higgsless model** is a low energy effective theory of Higgsless model.
- Dirac mass is constrained by  $Z b \bar{b}$  coupling.
- Constraint from  $Z b \bar{b}$  coupling is relatively mild and automatically satisfied with EWPT.



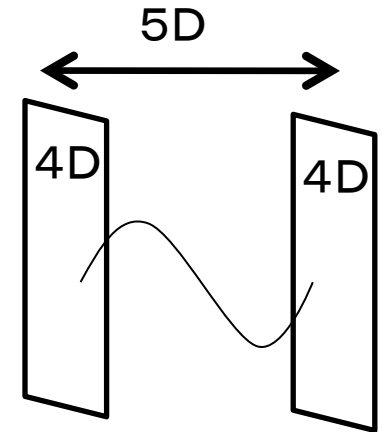
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# イントロダクション

## ヒッグスレスモデル

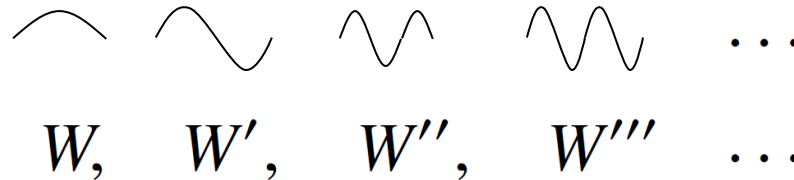
- 5次元のゲージ理論に基づいたモデル
- 電弱対称性は5次元方向の境界条件で破る

$$SU(2)_L \times SU(2)_R \times U(1)_{B-L} \rightarrow U(1)_{em}$$



- 質量をもった粒子は、カルツァクラインモード(KKモード)として現れる

例

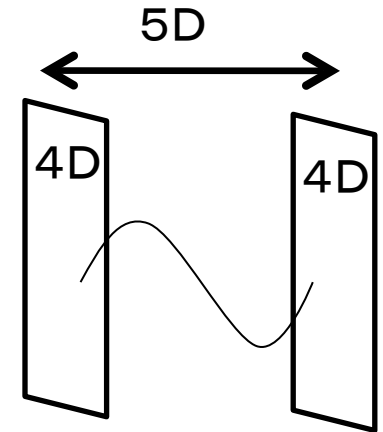


# イントロダクション

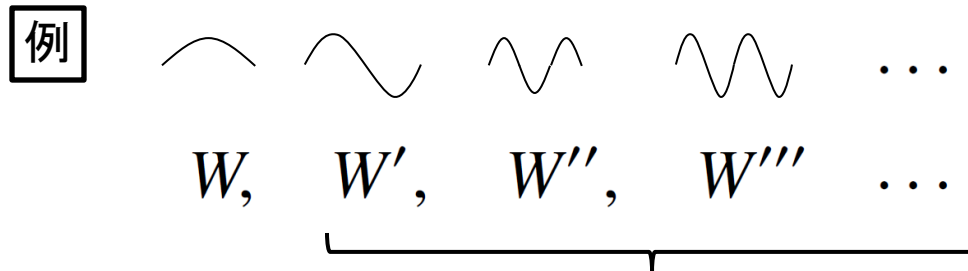
## ヒッグスレスモデル

- 5次元のゲージ理論に基づいたモデル
- 電弱対称性は5次元方向の境界条件で破る

$$SU(2)_L \times SU(2)_R \times U(1)_{B-L} \rightarrow U(1)_{em}$$



- 質量をもった粒子は、カルツァクラインモード(KKモード)として現れる



縦波W散乱のユニタリティーはヒッグスではなく重いゲージ粒子によって保たれる

# イントロダクション

標準模型

$$i\mathcal{M}(W_L^a W_L^b \rightarrow W_L^c W_L^d) =$$

+crossed.

同じ役割

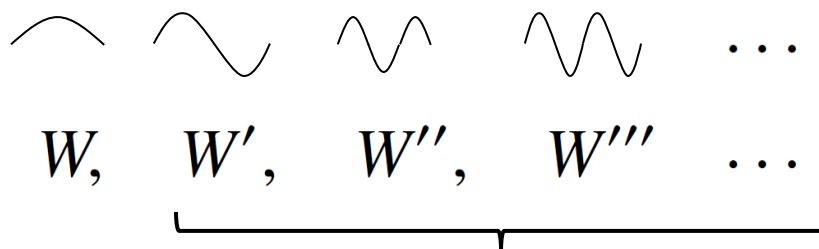
ヒッグスレス模型

$$i\mathcal{M}(W_L^a W_L^b \rightarrow W_L^c W_L^d) =$$

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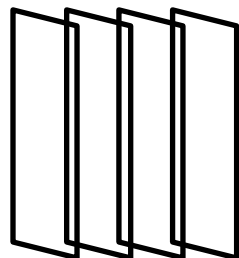
例



縦波W散乱のユニタリティーはヒッグスではなく重いゲージ粒子によって保たれる

# イントロダクション

## “スリーサイト”ヒッグスレスモデル



模式化  
(ムースダイアグラム)



$SU(2)_L$  ○○○○

$SU(2)_R$  ○○○○

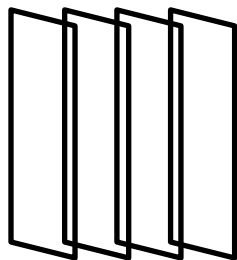
$U(1)_{B-L}$  ○○○○

○: 格子点 (ゲージ場)

—: リンク (非線形表現)

# イントロダクション

## “スリーサイト”ヒッグスレスモデル



模式化  
(ムースダイアグラム)



$SU(2)_L$  ○○○○

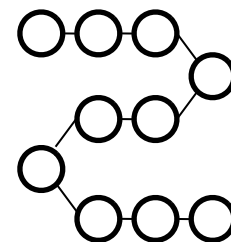
$SU(2)_R$  ○○○○

$U(1)_{B-L}$  ○○○○

境界条件



$SU(2)_R \times U(1)_{B-L}$   
 $\rightarrow U(1)_Y$



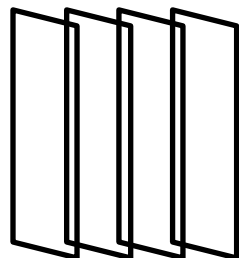
$SU(2)_L \times SU(2)_R$   
 $\rightarrow SU(2)_V$

○: 格子点 (ゲージ場)

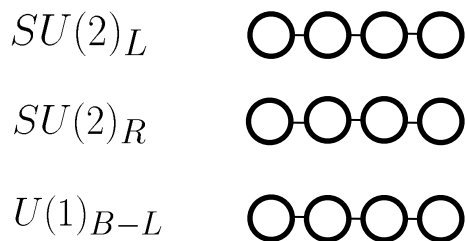
—: リンク (非線形表現)

# イントロダクション

## “スリーサイト”ヒッグスレス模型



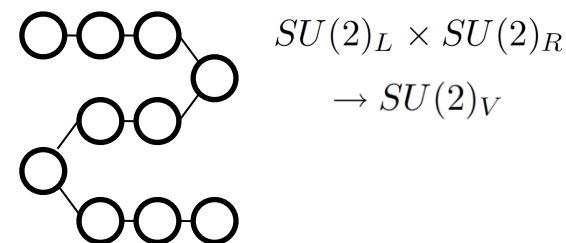
模式化  
(ムースダイアグラム)



境界条件

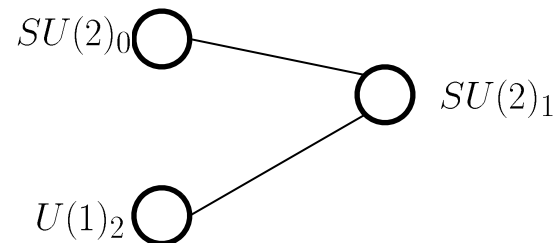


$$SU(2)_R \times U(1)_{B-L} \rightarrow U(1)_Y$$



○: 格子点 (ゲージ場)  
 —: リンク (非線形表現)

## スリーサイトヒッグスレス模型



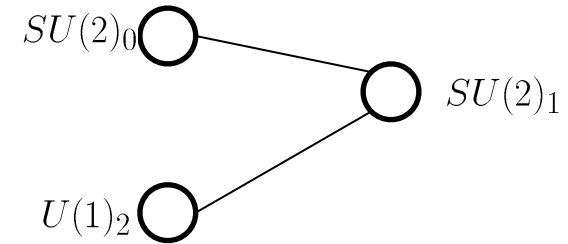
低エネルギーでは1stKK  
モードだけで十分なので

格子点(KKモード)  
を限りなく減らす



# イントロダクション

## スリーサイトヒッグスレス模型



低エネルギーでは1stKK  
モードだけで十分なので

✓ スリーサイトヒッグスレス模型のパラメータに対する1ループレベルでの制限

➤ 電弱精密測定からの  $\left\{ \begin{array}{l} \bullet \ g_{W'ff} \text{ への制限} \\ \bullet \ M_{W'} \text{ および } M_F \text{ への制限} \end{array} \right.$

( これまではトウリーレベル ← 不十分な精度 )



# スリーサイトヒッグスレスモデル

パラメータへの制限

R.S.Chivukula et.al Phys.Rev.D74:075011 (2006)

$$\mathcal{L}_f = \epsilon_L M \bar{\Psi}_{L0} \Sigma_1 \Psi_{R1} + M \bar{\Psi}_{R1} \Psi_{L1} + M \Psi_{L1} \Sigma_2 \begin{pmatrix} \epsilon_{tR} \\ \epsilon_{bR} \end{pmatrix} \begin{pmatrix} t_{R2} \\ b_{R2} \end{pmatrix} + h.c.$$

パラメータへの制限

$$0.095 \leq \epsilon_L \leq 0.30$$

$$380 \text{ GeV} \leq M_{W'} \leq 1.2 \text{ TeV}$$

$$1.8 \text{ TeV} \leq M_F \leq 46 \text{ TeV}$$

# スリーサイトヒッグスレスモデル

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- これらは、主にトウリーレベルでの解析
- 電弱精密測定による制限をつけるには不十分

# STパラメータ

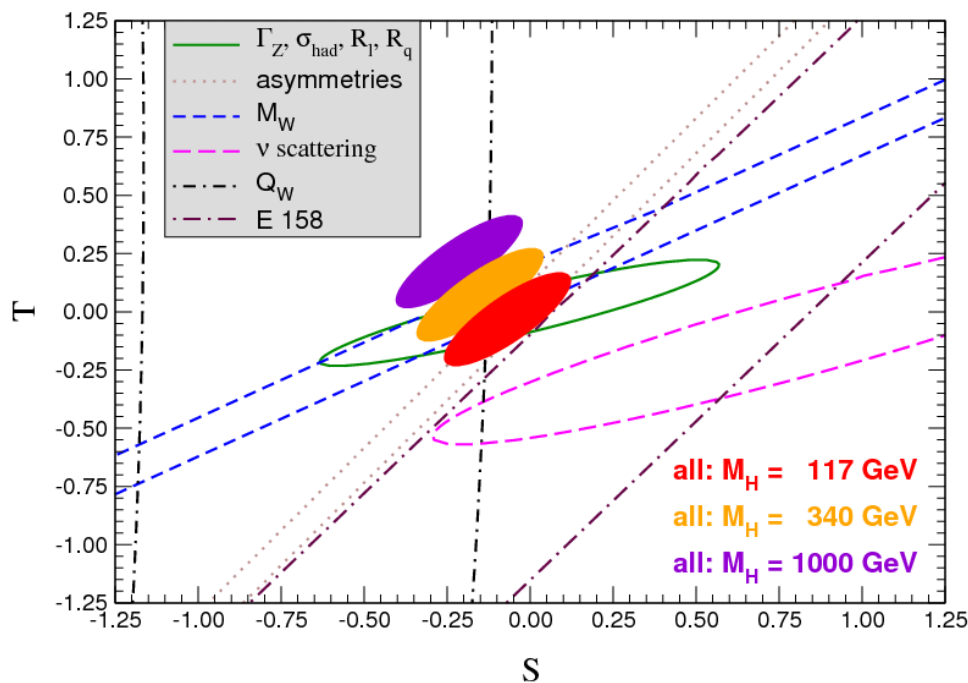
•フェルミオンの散乱  
振幅で定義

•標準模型からの  
ずれを表すのに  
用いられる

$$-\mathcal{A}_{\text{NC}} = e^2 \frac{QQ'}{-p^2} + \frac{(I_3 - s^2 Q)(I'_3 - s^2 Q')}{-\left(\frac{s^2 c^2}{e^2} - \frac{S}{16\pi}\right)p^2 + \frac{1}{4\sqrt{2}G_F}(1 - \gamma T)},$$

$$-\mathcal{A}_{\text{CC}} = \frac{(I_+ I'_- + I_- I'_+)/2}{-\left(\frac{s^2}{e^2} - \frac{S}{16\pi}\right)p^2 + \frac{1}{4\sqrt{2}G_F}}$$

$$Q = I_3 + Y$$



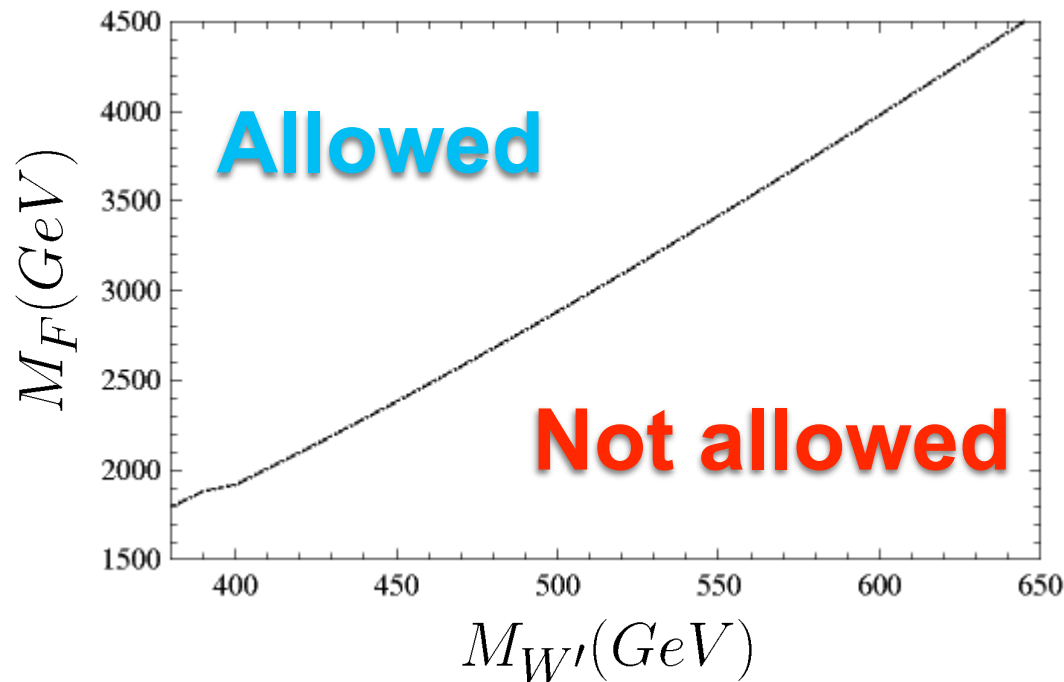
$$S \equiv S_{\text{BSM}} - S_{\text{SM}}(M_{H,\text{ref}})$$

$$T \equiv T_{\text{BSM}} - T_{\text{SM}}(M_{H,\text{ref}})$$

# 質量への制限

- 重いフェルミオンの質量の下限と  $W'$  の質量との関係

$$\alpha T = (\text{const}) \times \left( \frac{G_F M_t^4}{(4\pi)^2 M_F^2} \right) + (\text{bosonic 1-loop})$$



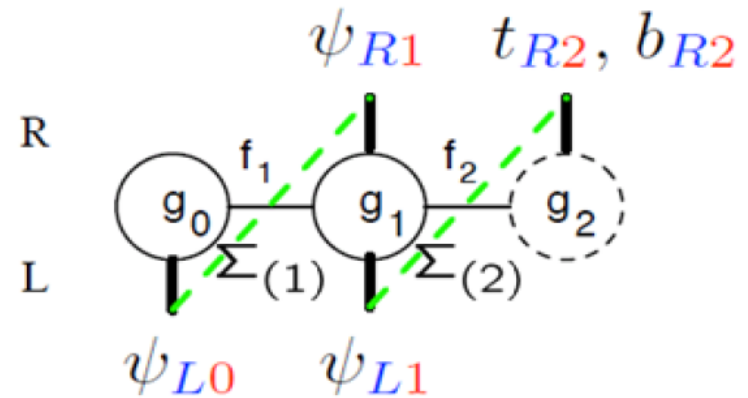
$$380 \text{ GeV} \leq M_{W'}$$

$$1.8 \text{ TeV} \leq M_F$$

# スリーサイトヒッグスレス模型

- クォークおよびNGボソンのゲージ対称性
- U(1)の()内は、レプトンの場合

$$\frac{1}{v^2} = \frac{1}{f_1^2} + \frac{1}{f_2^2}$$



|  | $SU(2)_0$ | $SU(2)_1$ | $U(1)_2$   | $SU(3)_{color}$ |
|--|-----------|-----------|--|-----------------|
| $\Psi_{L0}$  | □         | ·         | $\frac{1}{6} \begin{pmatrix} -\frac{1}{2} \\ -\frac{1}{2} \end{pmatrix}$ | □               |
| $\Psi_{L1}$  | ·         | □         | $\frac{1}{6} \begin{pmatrix} -\frac{1}{2} \\ -\frac{1}{2} \end{pmatrix}$ | □               |
| $\Psi_{R1}$  | ·         | □         | $\frac{1}{6} \begin{pmatrix} -\frac{1}{2} \\ -\frac{1}{2} \end{pmatrix}$ | □               |
| $\Psi_{R2} = \begin{pmatrix} u_{R2} \\ d_{R2} \end{pmatrix}$ | ·         | ·         | $\frac{2}{3} \begin{pmatrix} 0 \\ -1 \end{pmatrix}$                      | □               |
| $\Sigma_1$   | □         | □*        | ·  | ·               |
| $\Sigma_2$   | ·         | □         | $\begin{pmatrix} \frac{1}{2} \\ -\frac{1}{2} \end{pmatrix}^*$            | ·               |

# ゲージボソンの質量

$$\left\{ \begin{array}{l} M_W^2 = \frac{1}{4} \frac{f_1^2 f_2^2}{f_1^2 + f_2^2} g_0^2 \left( 1 - \frac{f_1^4}{(f_1^2 + f_2^2)^2} x^2 + \mathcal{O}(x^4) \right) \\ M_{W'}^2 = \frac{1}{4} (f_1^2 + f_2^2) g_1^2 \left( 1 + \frac{f_1^4}{(f_1^2 + f_2^2)^2} x^2 + \frac{f_1^6 f_2^2}{(f_1^2 + f_2^2)^4} x^4 + \mathcal{O}(x^6) \right) \end{array} \right.$$

$$\left\{ \begin{array}{l} M_Z^2 = \frac{1}{4} \frac{f_1^2 f_2^2}{f_1^2 + f_2^2} g_0^2 \left( (1 + t^2) - \frac{(f_1^2 - f_2^2 t^2)^2}{(f_1^2 + f_2^2)^2} x^2 + \mathcal{O}(x^4) \right) \\ M_{Z'}^2 = \frac{1}{4} (f_1^2 + f_2^2) g_1^2 \left( 1 + \frac{f_1^4 + f_2^4 t^2}{(f_1^2 + f_2^2)^2} x^2 + \frac{f_1^2 f_2^2 (f_1^2 - f_2^2 t^2)^2}{(f_1^2 + f_2^2)^4} x^4 + \mathcal{O}(x^6) \right) \end{array} \right.$$

$$x = \frac{g_0}{g_1} \ll 1$$

$$t = \frac{g_2}{g_0} = \frac{s}{c}$$

# スリーサイトヒッグスレスモデル

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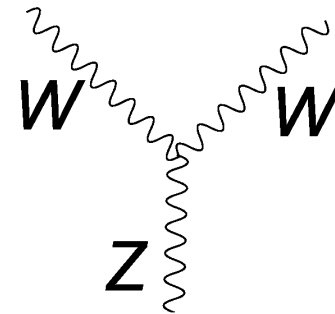
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WWZ結合定数の測定からの制限(LEP)



K.Hagiwara, R.D.Peccei, D.Zeppenfeld, and K.Hikasa, Nucl.Phys. B282,253(1987)

# スリーサイトヒッグスレス模型

## パラメータへの制限

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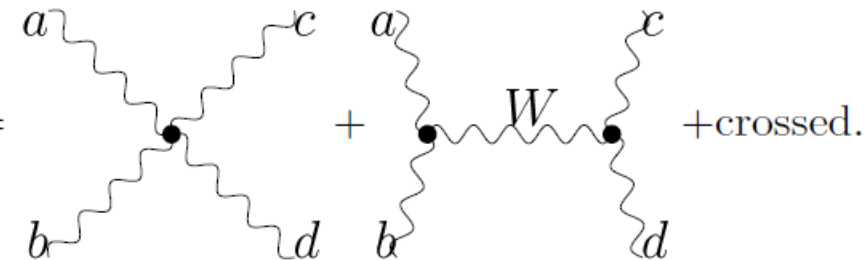
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### ユニタリティーへの制限

$$\sqrt{s} \simeq 1.2 \text{ TeV}$$

$$i\mathcal{M}(W_L^a W_L^b \rightarrow W_L^c W_L^d) =$$


+crossed.



# スリーサイトヒッグスレスモデル

## パラメータへの制限

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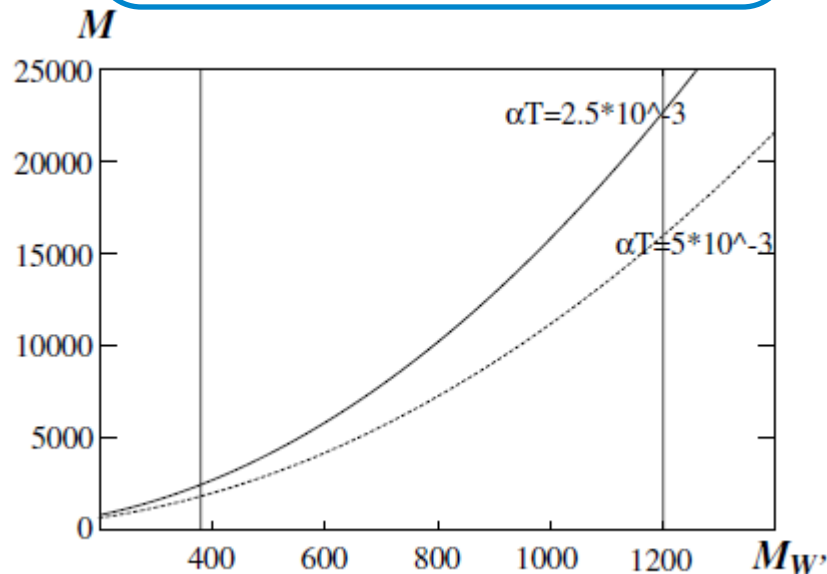
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### Tパラメータからの制限



- 考慮すべきグラフは他にもある
- 不十分な解析

# スリーサイトヒッグスレスモデル

パラメータへの制限

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ループの効果  $\leq$  トウリーレベル

であるべしという、素朴な次元解析 (NDA)