

New predictions for $R(D^{(*)})$

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**Mini-workshop on $D^{(*)}\tau\bar{\nu}$ and related topics
Nagoya University, March 27–28, 2017**

F. Bernlochner, ZL, D. Robinson, M Papucci, 1703.05330

D. Robinson, ZL, M Papucci, JHEP 1701 (2017) 083 [1610.02045]

M. Freytsis, ZL, J. Ruderman, PRD 92 (2015) 054018 [1506.08896]

+ works in progress ...

Flavor anomalies: (subjective) status

- Several measurements are in intriguing tensions with the SM

Key roles of Δm_K and ϵ_K remain, to constrain NP vs. flood of LHCb data, exploring Higgs flavor, etc.

- **Guaranteed** to probe and understand the SM much better (e.g., “new” hadronic states)

We'll at least understand inclusive vs. exclusive better...

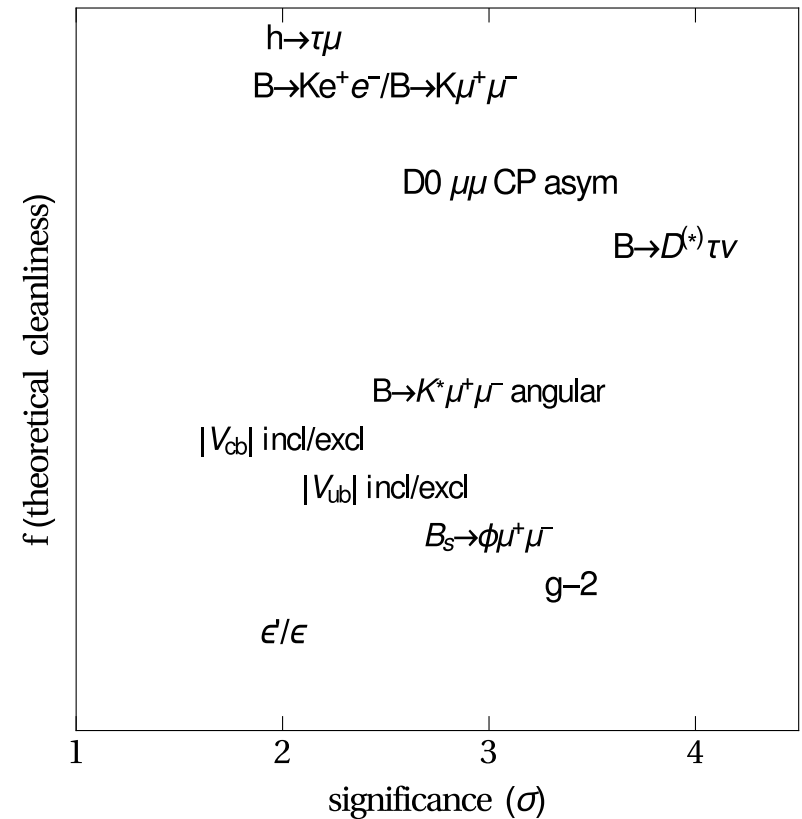
Hope of discovering BSM phenomena

- **Exp.:** NA62 taking data, by 2019 measure $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ to $< 10\%$ (at SM level)

Belle II approaching, time to make genuine **predictions** is shrinking

LHCb 300/fb upgrade planning

+ improving EDM, CLFV, DM, sensitivities



Outline

- $B \rightarrow D^{(*)}\tau\bar{\nu}$ is currently the most significant deviation from the SM (at colliders)

1. Use $B \rightarrow D^{(*)}l\bar{\nu}$ to refine $R(D^{(*)})$, lattice independent, improvable

[F. Bernlochner, ZL, Papucci, Robinson, 1703.05330]

Refine $|V_{cb}|$, test HQET, test fitting, test lattice, test measurements... [soon]

2. MFV models, leptoquarks

[M. Freytsis, ZL, J. Ruderman, PRD 92 (2015) 054018, arXiv:1506.08896]

Suppress e & μ instead of enhancing τ ?

[M. Freytsis, ZL, J. Ruderman, to appear]

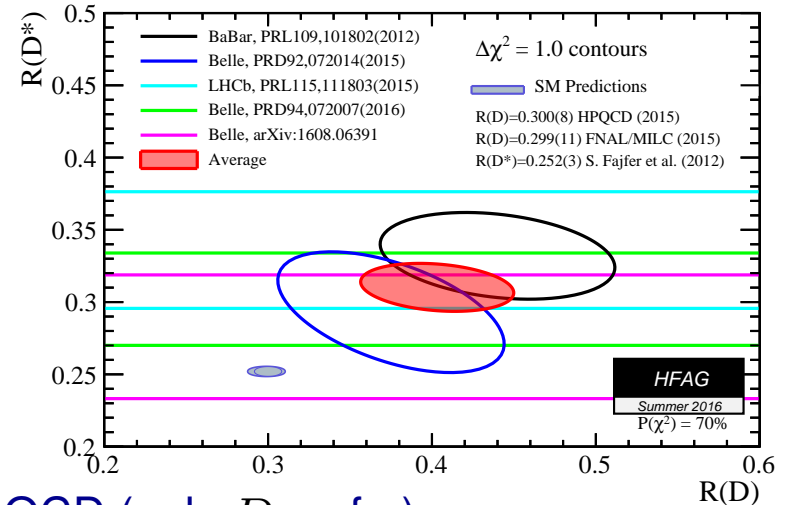
“When you think you can finally forget something, it’s about to become important”

The tension with the SM

- BaBar / Belle / LHCb: $R(X) = \frac{\Gamma(B \rightarrow X\tau\bar{\nu})}{\Gamma(B \rightarrow Xl\bar{\nu})}$
 $l = e, \mu$

World average: 3.9σ from the SM

	$R(D)$	$R(D^*)$
World average	0.403 ± 0.047	0.310 ± 0.017
my SM expectation	0.299 ± 0.005	0.257 ± 0.005
Belle II	± 0.010	± 0.005



Reliable SM predictions: heavy quark symmetry + lattice QCD (only D so far)

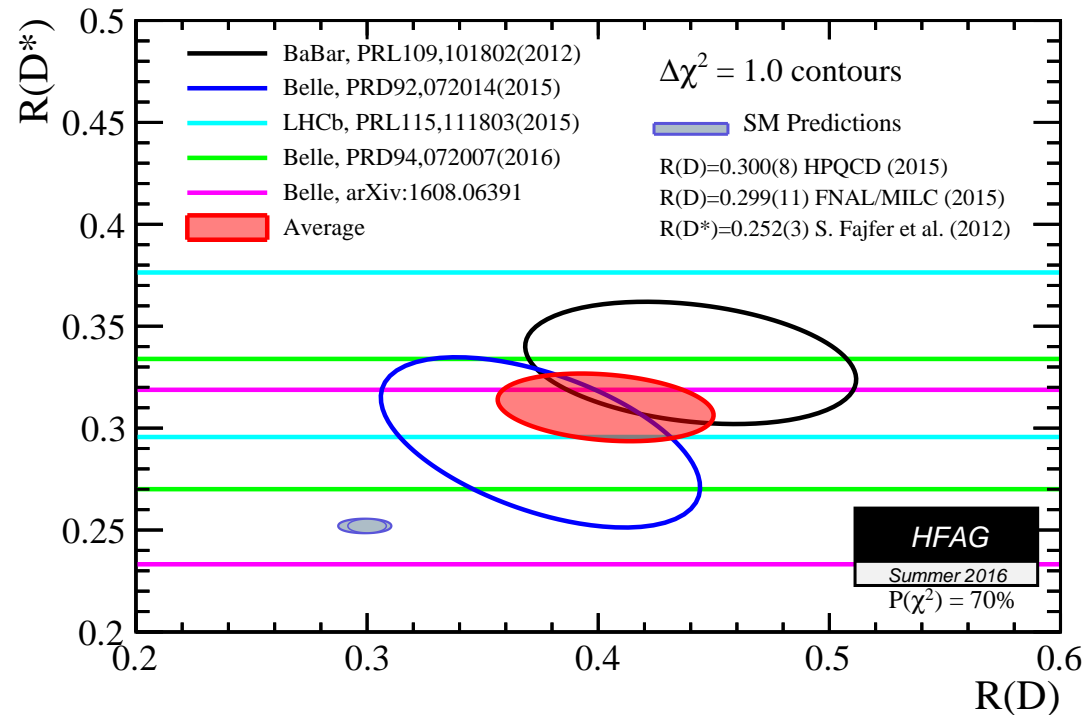
- Model indep. 2σ tension: $R(D^{(*)})$ vs. $R(X_c) = 0.223 \pm 0.004$ in SM [Freysis, ZL, Ruderman]

No $\mathcal{B}(B \rightarrow X\tau\bar{\nu})$ measurement since LEP, $\mathcal{B}(b \rightarrow X\tau^+\nu) = (2.41 \pm 0.23)\%$

Imply NP at a fairly low scale (leptoquarks, W' , etc.), likely visible at the LHC

- Next: LHCb result with hadronic τ decays, measure $R(D)$, B_c & Λ_b decays
- Experimental precision will improve a lot + theory uncertainty also improvable

Refining SM predictions



Can it be a theory issue?

Basics of $B \rightarrow D^{(*)} \ell \bar{\nu}$

- Only Lorentz invariance: 6 functions of q^2 , only 4 measurable with e, μ final states

$$\langle D | \bar{c} \gamma^\mu b | \bar{B} \rangle = f_+(q^2) (p_B + p_D)^\mu + [f_0(q^2) - f_+(q^2)] \frac{m_B^2 - m_D^2}{q^2} q^\mu$$

$$\langle D^* | \bar{c} \gamma^\mu b | \bar{B} \rangle = -ig(q^2) \epsilon^{\mu\nu\rho\sigma} \epsilon_\nu^* (p_B + p_{D^*})_\rho q_\sigma$$

$$\langle D^* | \bar{c} \gamma^\mu \gamma^5 b | \bar{B} \rangle = \epsilon^{*\mu} f(q^2) + a_+(q^2) (\epsilon^* \cdot p_B) (p_B + p_{D^*})^\mu + a_-(q^2) (\epsilon^* \cdot p_B) q^\mu$$

Two form factors involving $q^\mu = p_B^\mu - p_{D^{(*)}}^\mu$ do not contribute for $m_l = 0$

- HQET constraints: 6 functions \Rightarrow 1 in $m_{c,b} \gg \Lambda_{\text{QCD}}$ limit + 3 at $\mathcal{O}(\Lambda_{\text{QCD}}/m_{c,b})$

$$\langle D | \bar{c} \gamma^\mu b | \bar{B} \rangle = \sqrt{m_B m_D} [h_+(v + v')^\mu + h_-(v - v')^\mu] \quad w = v_B \cdot v'_{D^{(*)}}$$

$$\langle D^* | \bar{c} \gamma^\mu b | \bar{B} \rangle = i\sqrt{m_B m_{D^*}} h_V \epsilon^{\mu\nu\alpha\beta} \epsilon_\nu^* v'_\alpha v_\beta$$

$$\langle D^* | \bar{c} \gamma^\mu \gamma^5 b | \bar{B} \rangle = \sqrt{m_B m_{D^*}} [h_{A_1} (w + 1) \epsilon^{*\mu} - h_{A_2} (\epsilon^* \cdot v) v^\mu - h_{A_3} (\epsilon^* \cdot v) v'^\mu]$$

$m_{c,b} \gg \Lambda_{\text{QCD}}$ limit: $h_+ = h_V = h_{A_1} = h_{A_3} = \xi(w)$ and $h_- = h_{A_2} = 0$

- Constrain all 4 functions from $B \rightarrow D^{(*)} \ell \bar{\nu} \Rightarrow \mathcal{O}(\Lambda_{\text{QCD}}^2/m_{c,b}^2, \alpha_s^2)$ uncertainties

Form factor expansion details

- Expand form factors to order $\varepsilon_{c,b} = \Lambda_{\text{QCD}}/(2m_{c,b})$ and α_s (new results for tensor ff)

$$f_i(w) = \xi(w) \left[1 + \varepsilon_c f_i^{(c,1)}(w) + \varepsilon_b f_i^{(b,1)}(w) + \alpha_s f_i^{(\alpha_s)}\left(\frac{m_c}{m_b}, w\right) + \mathcal{O}(\varepsilon_{c,b}^2, \alpha_s^2) \right]$$

The $\alpha_s \varepsilon_{c,b}$ terms are known, should be included if NP established

Expect that fit readjusts subleading Isgur-Wise functions \Rightarrow modest impacts

Known for SM terms since the early 90s, but not written down for others before

Absorbed $\xi(w) \rightarrow \xi(w) + 2(\varepsilon_c + \varepsilon_b)\chi_1(w)$, so only $\chi_{2,3}$ and $\eta = \xi_3/\xi$ remain

- Calculated in QCD sum rules — may parametrize them: [Ligeti, Neubert, Nir, '92-'93]

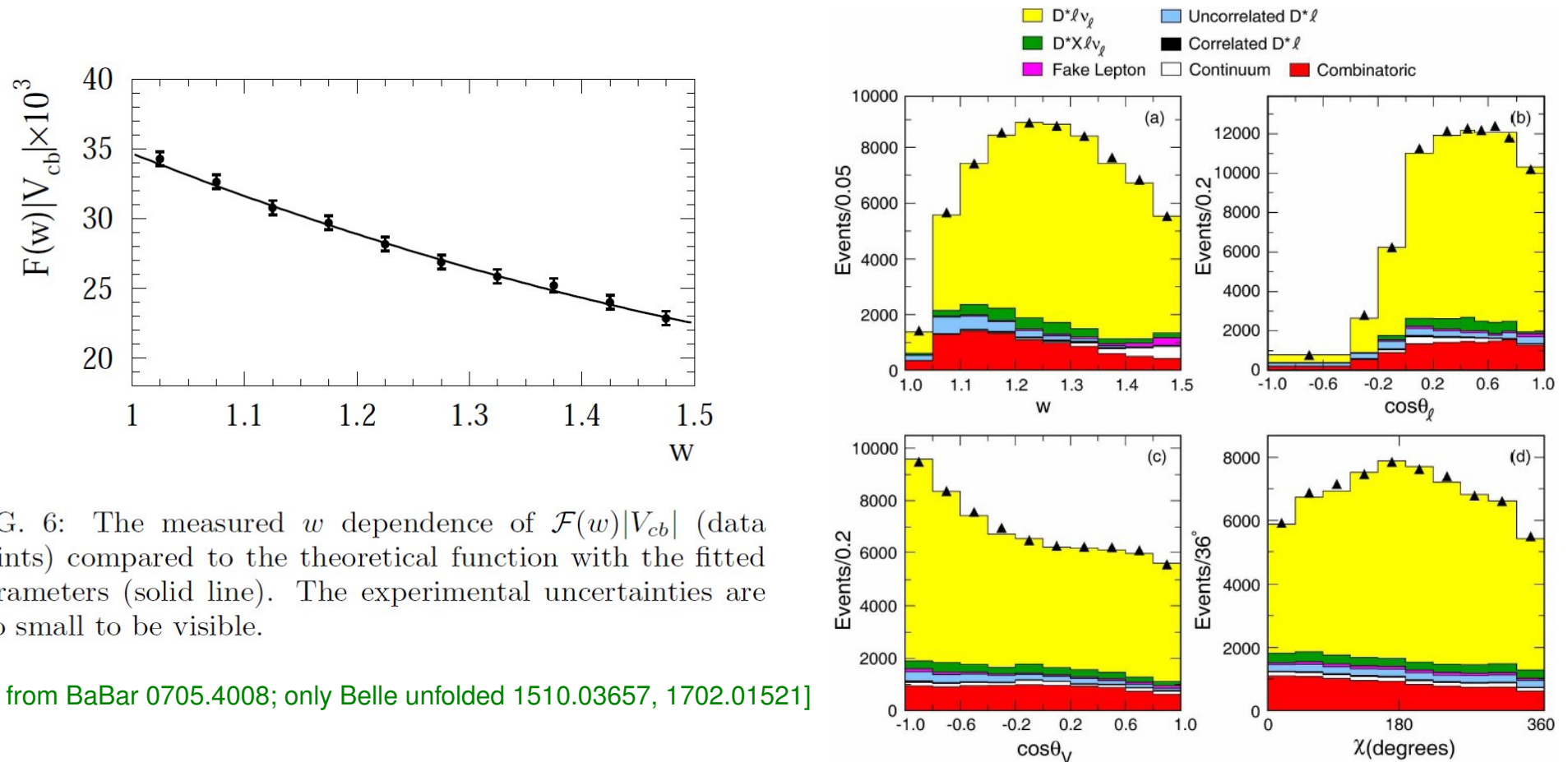
Lagrangian: $\hat{\chi}_2^{\text{ren}}(1) = -0.06 \pm 0.02$ $\hat{\chi}'_2^{\text{ren}}(1) = 0 \pm 0.02$ $\hat{\chi}'_3^{\text{ren}}(1) = 0.04 \pm 0.02$

Current: $\eta(1) = 0.62 \pm 0.2$, $\eta'(1) = 0 \pm 0.2$ (Luke: $\hat{\chi}_3(1) = 0$)

Central values match what CLN used, these uncertainties $>$ in original papers

Measured spectra for e & μ final states

- 4 functions: two q^2 spectra in $D^{(*)}$ + two q^2 -dependent angular distributions in D^*
- All form factors = Isgur-Wise function + $\Lambda_{\text{QCD}}/m_{c,b}$ + α_s corrections



Consider 7 different fit scenarios

- All calculations of subleading $\Lambda_{\text{QCD}}/m_{c,b}$ Isgur-Wise functions model dependent
Only $R(D)$ calculated in LQCD — all others did not include uncertainties properly

- Theory [CLN] & exp papers: $R_{1,2}(w) = \underbrace{R_{1,2}(1)}_{\text{fit}} + \underbrace{R'_{1,2}(1)}_{\text{fixed}}(w - 1) + \underbrace{R''_{1,2}(1)}_{\text{fixed}}(w - 1)^2/2$

In HQET: $R_{1,2}(1) = 1 + \mathcal{O}(\Lambda_{\text{QCD}}/m_{c,b}, \alpha_s)$ $R_{1,2}^{(n)}(1) = 0 + \mathcal{O}(\Lambda_{\text{QCD}}/m_{c,b}, \alpha_s)$

Sometimes calculations using QCD sum rule predictions for $\Lambda_{\text{QCD}}/m_{c,b}$ corrections are called the HQET predictions

- Our fits:

Fit	QCDSR	Lattice QCD			Belle Data
		$\mathcal{F}(1)$	$f_{+,0}(1)$	$f_{+,0}(w > 1)$	
$L_{w=1}$	—	+	+	—	+
$L_{w=1} + \text{SR}$	+	+	+	—	+
NoL	—	—	—	—	+
NoL + SR	+	—	—	—	+
$L_{w \geq 1}$	—	+	+	+	+
$L_{w \geq 1} + \text{SR}$	+	+	+	+	+
th: $L_{w \geq 1} + \text{SR}$	+	+	+	+	—

Fit details

- Standard choice to minimize range of expansion param' z_* in unitarity constraints:

$$z_*(w) = \frac{\sqrt{w+1} - \sqrt{2}a}{\sqrt{w+1} + \sqrt{2}a}, \quad a = \left(\frac{1+r_D}{2\sqrt{r_D}} \right)^{1/2}$$

- Parametrize similar to CLN — wanted to start with fit comparable to prior results

$$\frac{\mathcal{G}(w)}{\mathcal{G}(w_0)} \simeq 1 - 8a^2\rho_*^2 z_* + (V_{21}\rho_*^2 - V_{20})z_*^2$$

Translate this to $\xi(w)/\xi(w_0)$ to be able to simultaneously fit $B \rightarrow D$ and $B \rightarrow D^*$

Uncertainty in z_*^2 term may be sizable — we checked that fit results are stable if constraint between the slope and the curvature is relaxed

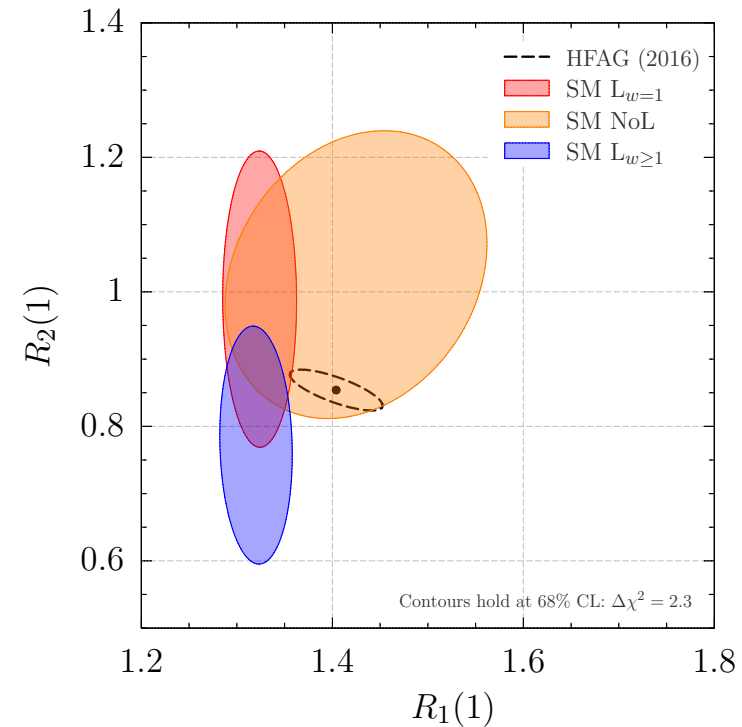
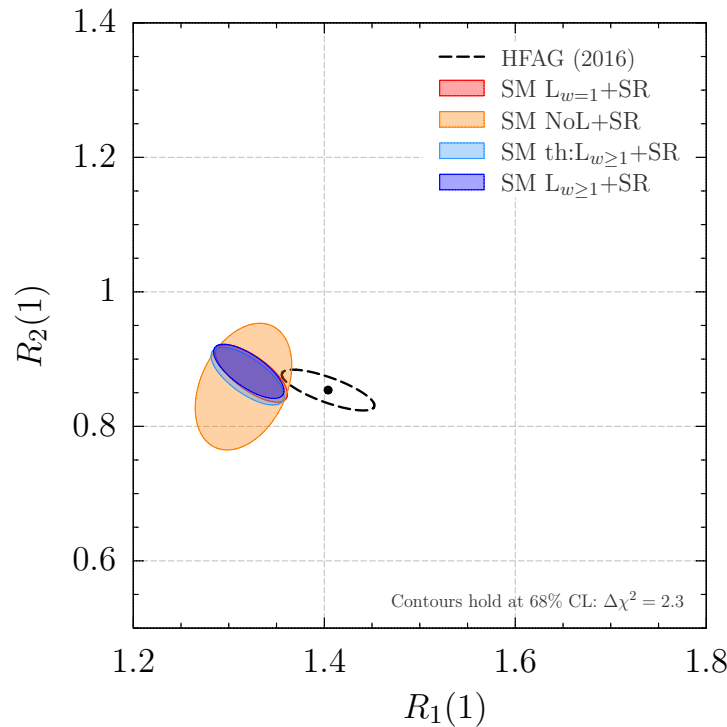
Keep uncertainties and correlations in form factor ratios (Λ_{QCD}/m Isgur-Wise fn's)

- In progress: study systematically orders/constraints in fit, HQET corrections, etc.

Experimental inputs and self-consistency

- Experimental inputs: $B \rightarrow Dl\bar{\nu} : d\Gamma/dw$ (Only Belle published fully corrected distributions)
- $B \rightarrow D^*l\bar{\nu} : d\Gamma/dw, R_1(w), R_2(w)$

Model-dependent inputs in SM predictions for $R_{1,2}$ in all exp. fits & theory papers



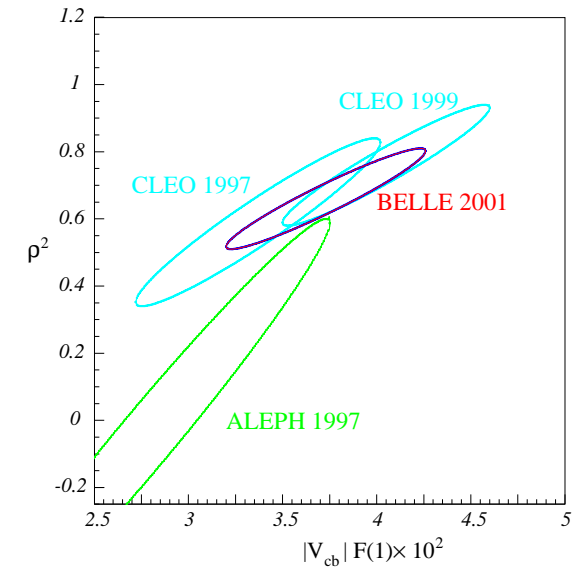
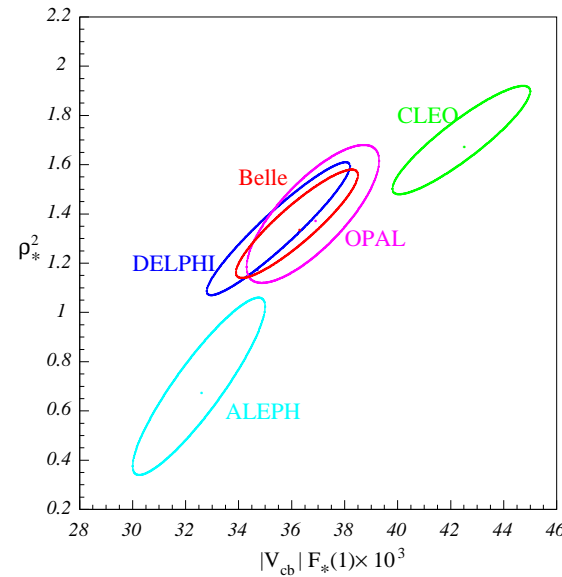
- Mild tension for $R_1(1)$ — may affect $|V_{cb}|$ from $B \rightarrow D^{(*)}l\bar{\nu}$, long standing issues
- In 1S scheme: $R_1(1) \simeq 1.34 - 0.12 \eta(1)$, $R_2(1) \simeq 0.98 - 0.42 \eta(1) - 0.54 \hat{\chi}_2(1)$

Other place where $\Lambda_{\text{QCD}}/m_{c,b}$ matters

- At EPS 2001, Ben and I got puzzled by surprising plots...

So we considered corrections up to $\Lambda_{\text{QCD}}/m_{c,b}$ and $\alpha_s^2\beta_0$ to the slopes, curvatures, $R_{1,2} \dots$

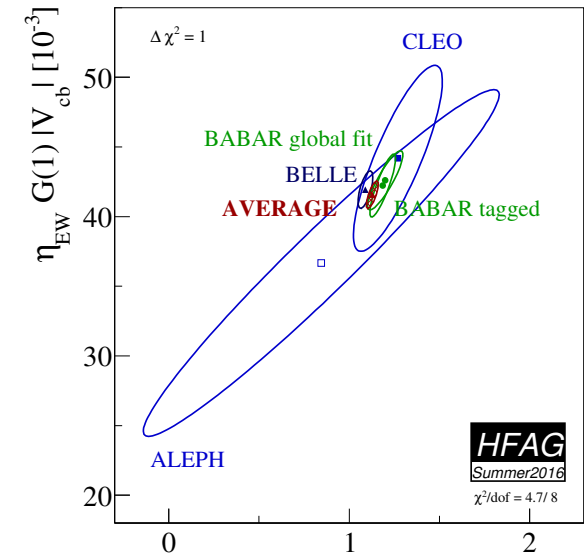
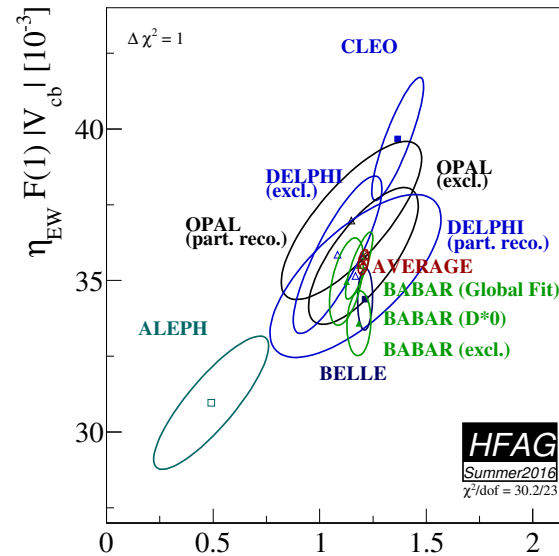
[PLB 526 (2002) 345 (2002), hep-ph/0111392]



- Current plots from HFAG 2016:

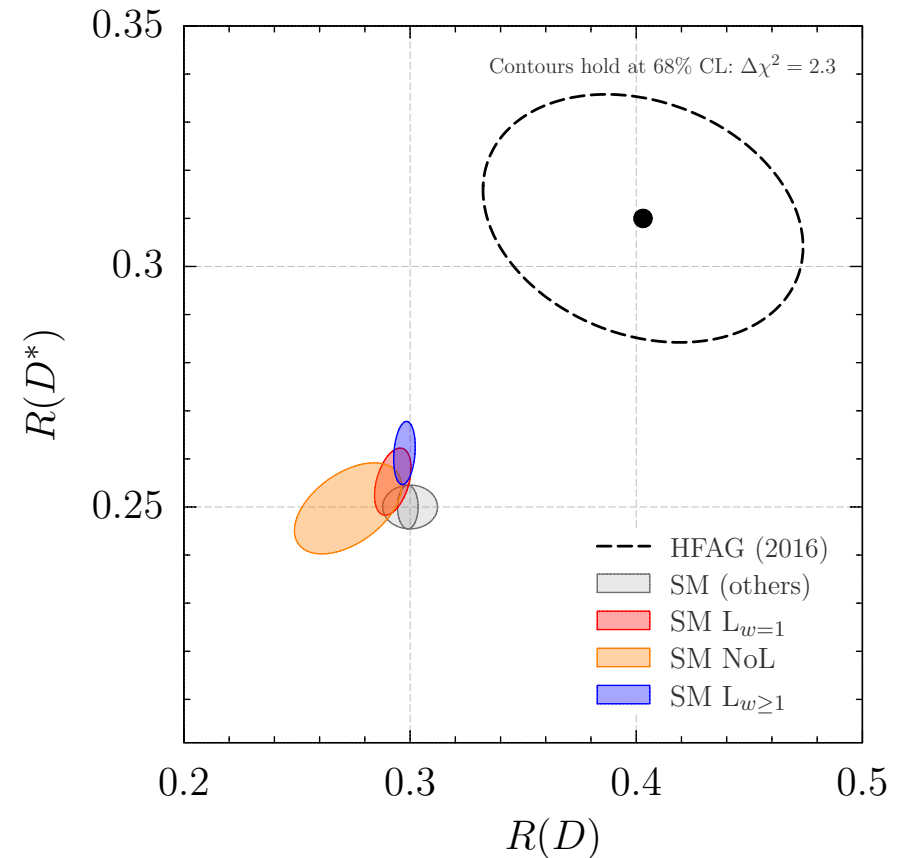
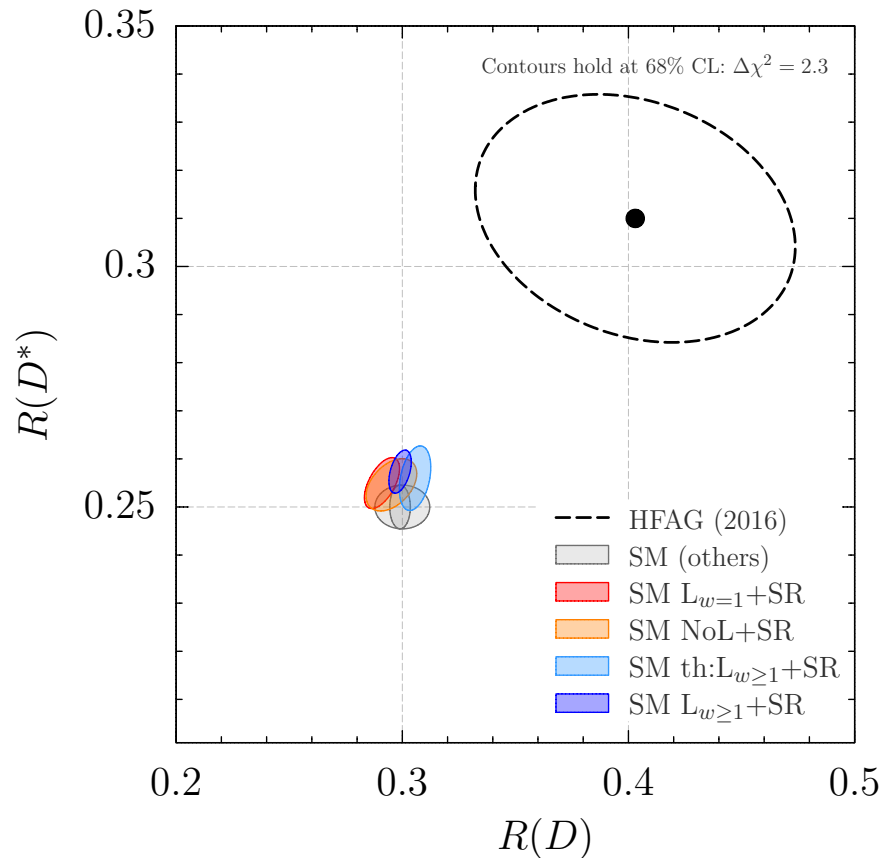
$\rho_G^2 \simeq \rho_{A_1}^2$, as expected

All this is folded into our fits



Our SM predictions for $R(D)$ and $R(D^*)$

- Significance of the tension is (surprisingly) stable across our fit scenarios:



- Fit just a quadratic polynomial in z_* : consistent results

Summary of SM predictions

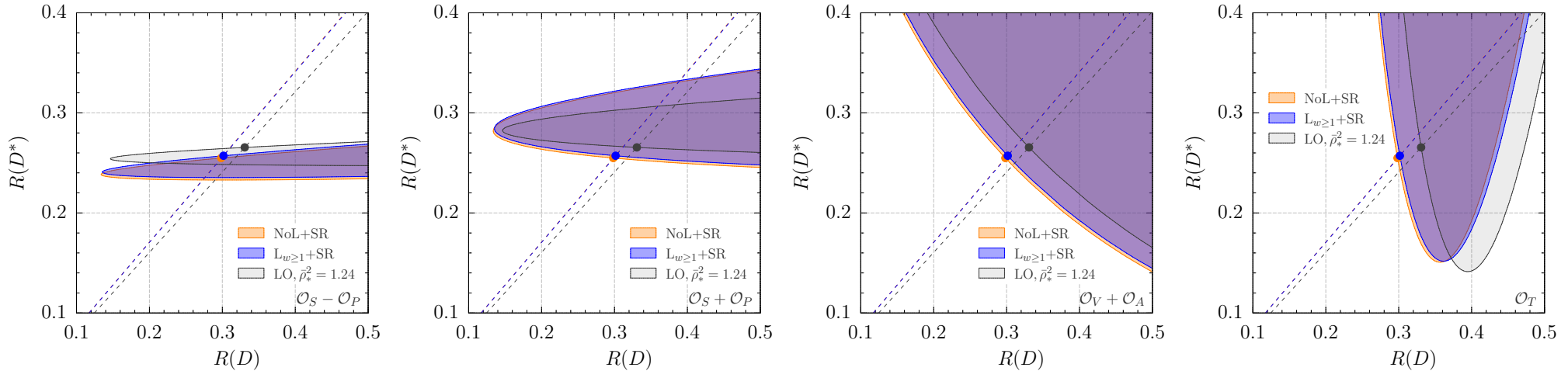
- Small variations: heavy quark symmetry & phase space leave little wiggle room

Scenario	$R(D)$	$R(D^*)$	Correlation
$L_{w=1}$	0.292 ± 0.005	0.255 ± 0.005	41%
$L_{w=1} + \text{SR}$	0.291 ± 0.005	0.255 ± 0.003	57%
NoL	0.273 ± 0.016	0.250 ± 0.006	49%
NoL+SR	0.295 ± 0.007	0.255 ± 0.004	43%
$L_{w \geq 1}$	0.298 ± 0.003	0.261 ± 0.004	19%
$L_{w \geq 1} + \text{SR}$	0.299 ± 0.003	0.257 ± 0.003	44%
th: $L_{w \geq 1} + \text{SR}$	0.306 ± 0.005	0.256 ± 0.004	33%
Data [HFAG]	0.403 ± 0.047	0.310 ± 0.017	-23%
Lattice [FLAG]	0.300 ± 0.008	—	—
Bigi, Gambino '16	0.299 ± 0.003	—	—
Fajfer et al. '12	—	0.252 ± 0.003	—

- Tension between our “ $L_{w \geq 1} + \text{SR}$ ” fit and data is 3.9σ , with $p\text{-value} = 11.5 \times 10^{-5}$
(close to HFAG: 3.9σ , with $p\text{-value} = 8.3 \times 10^{-5}$)

Impact on new physics effects

- Add only one NP operator to the SM at a time: $O_S - O_P$, $O_S + O_P$, $O_V + O_A$, O_T



- Not all $1/m$ corrections in literature, some $\mathcal{O}(1/m)$ form factors had 100% uncert.
- Shifts from gray regions non-negligible — if one seriously wanted to fit a NP model

Few comments on new physics

Consider redundant set of operators

- Fits to different fermion orderings convenient to understand allowed mediators

Usually only the first 5 operators considered, related by Fierz

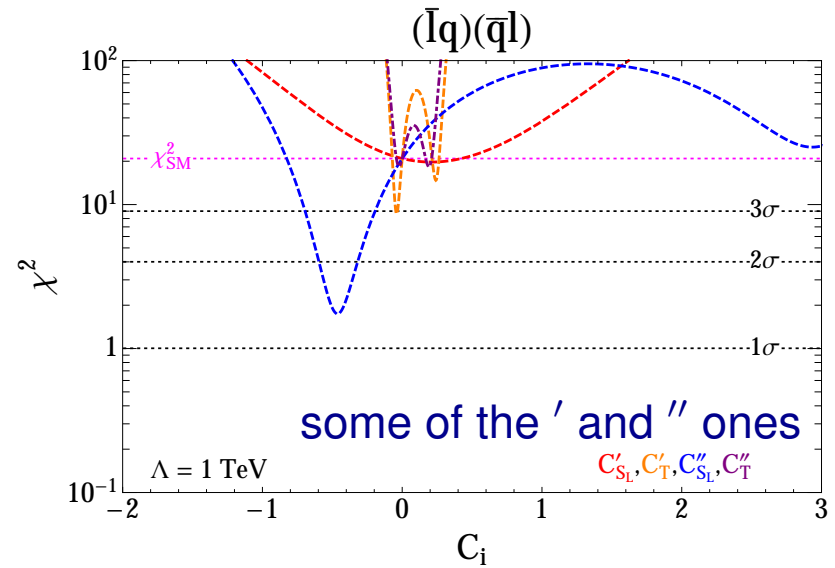
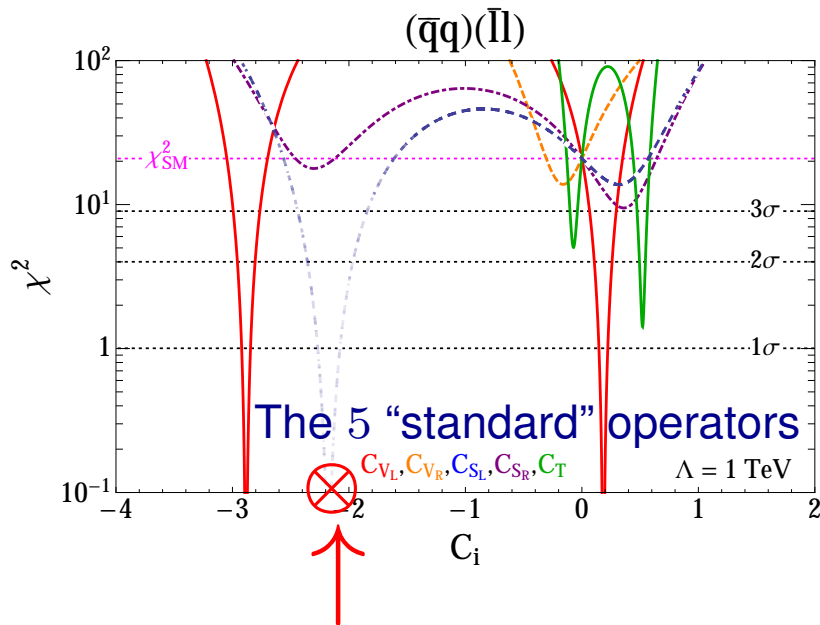
from dim-6 terms, others from dim-8 only



	Operator	Fierz identity	Allowed Current	$\delta\mathcal{L}_{\text{int}}$
\mathcal{O}_{V_L}	$(\bar{c}\gamma_\mu P_L b)(\bar{\tau}\gamma^\mu P_L \nu)$		$(1, 3)_0$	$(g_q \bar{q}_L \tau \gamma^\mu q_L + g_e \bar{\ell}_L \tau \gamma^\mu \ell_L) W'_\mu$
\mathcal{O}_{V_R}	$(\bar{c}\gamma_\mu P_R b)(\bar{\tau}\gamma^\mu P_L \nu)$		$\left. \begin{array}{l} (1, 2)_{1/2} \\ (3, 1)_{2/3} \\ (3, 2)_{7/6} \end{array} \right\}$	$(\lambda_d \bar{q}_L d_R \phi + \lambda_u \bar{q}_L u_R i \tau_2 \phi^\dagger + \lambda_e \bar{\ell}_L e_R \phi)$
\mathcal{O}_{S_R}	$(\bar{c} P_R b)(\bar{\tau} P_L \nu)$			
\mathcal{O}_{S_L}	$(\bar{c} P_L b)(\bar{\tau} P_L \nu)$			
\mathcal{O}_T	$(\bar{c} \sigma^{\mu\nu} P_L b)(\bar{\tau} \sigma_{\mu\nu} P_L \nu)$			
\mathcal{O}'_{V_L}	$(\bar{\tau}\gamma_\mu P_L b)(\bar{c}\gamma^\mu P_L \nu) \longleftrightarrow \mathcal{O}_{V_L}$	$\left\langle \begin{array}{l} (3, 3)_{2/3} \\ (3, 1)_{2/3} \end{array} \right\rangle$		
\mathcal{O}'_{V_R}	$(\bar{\tau}\gamma_\mu P_R b)(\bar{c}\gamma^\mu P_L \nu) \longleftrightarrow -2\mathcal{O}_{S_R}$		$(\lambda \bar{q}_L \gamma_\mu \ell_L + \tilde{\lambda} \bar{d}_R \gamma_\mu e_R) U^\mu$	
\mathcal{O}'_{S_R}	$(\bar{\tau} P_R b)(\bar{c} P_L \nu) \longleftrightarrow -\frac{1}{2}\mathcal{O}_{V_R}$			
\mathcal{O}'_{S_L}	$(\bar{\tau} P_L b)(\bar{c} P_L \nu) \longleftrightarrow -\frac{1}{2}\mathcal{O}_{S_L} - \frac{1}{8}\mathcal{O}_T$		$(3, 2)_{7/6}$	$(\lambda \bar{u}_R \ell_L + \tilde{\lambda} \bar{q}_L i \tau_2 e_R) R$
\mathcal{O}'_T	$(\bar{\tau} \sigma^{\mu\nu} P_L b)(\bar{c} \sigma_{\mu\nu} P_L \nu) \longleftrightarrow -6\mathcal{O}_{S_L} + \frac{1}{2}\mathcal{O}_T$			
\mathcal{O}''_{V_L}	$(\bar{\tau}\gamma_\mu P_L c^c)(\bar{b}^c \gamma^\mu P_L \nu) \longleftrightarrow -\mathcal{O}_{V_R}$		$\left. \begin{array}{l} (\bar{3}, 2)_{5/3} \\ (\bar{3}, 3)_{1/3} \\ (\bar{3}, 1)_{1/3} \end{array} \right\}$	$(\lambda \bar{d}_R^c \gamma_\mu \ell_L + \tilde{\lambda} \bar{q}_L^c \gamma_\mu e_R) V^\mu$ $\lambda \bar{q}_L^c i \tau_2 \tau \ell_L S$
\mathcal{O}''_{V_R}	$(\bar{\tau}\gamma_\mu P_R c^c)(\bar{b}^c \gamma^\mu P_L \nu) \longleftrightarrow -2\mathcal{O}_{S_R}$			
\mathcal{O}''_{S_R}	$(\bar{\tau} P_R c^c)(\bar{b}^c P_L \nu) \longleftrightarrow \frac{1}{2}\mathcal{O}_{V_L}$			
\mathcal{O}''_{S_L}	$(\bar{\tau} P_L c^c)(\bar{b}^c P_L \nu) \longleftrightarrow -\frac{1}{2}\mathcal{O}_{S_L} + \frac{1}{8}\mathcal{O}_T$			
\mathcal{O}''_T	$(\bar{\tau} \sigma^{\mu\nu} P_L c^c)(\bar{b}^c \sigma_{\mu\nu} P_L \nu) \longleftrightarrow -6\mathcal{O}_{S_L} - \frac{1}{2}\mathcal{O}_T$			

[Freytsis, ZL, Ruderman, 1506.08896]

Fits to a single operator



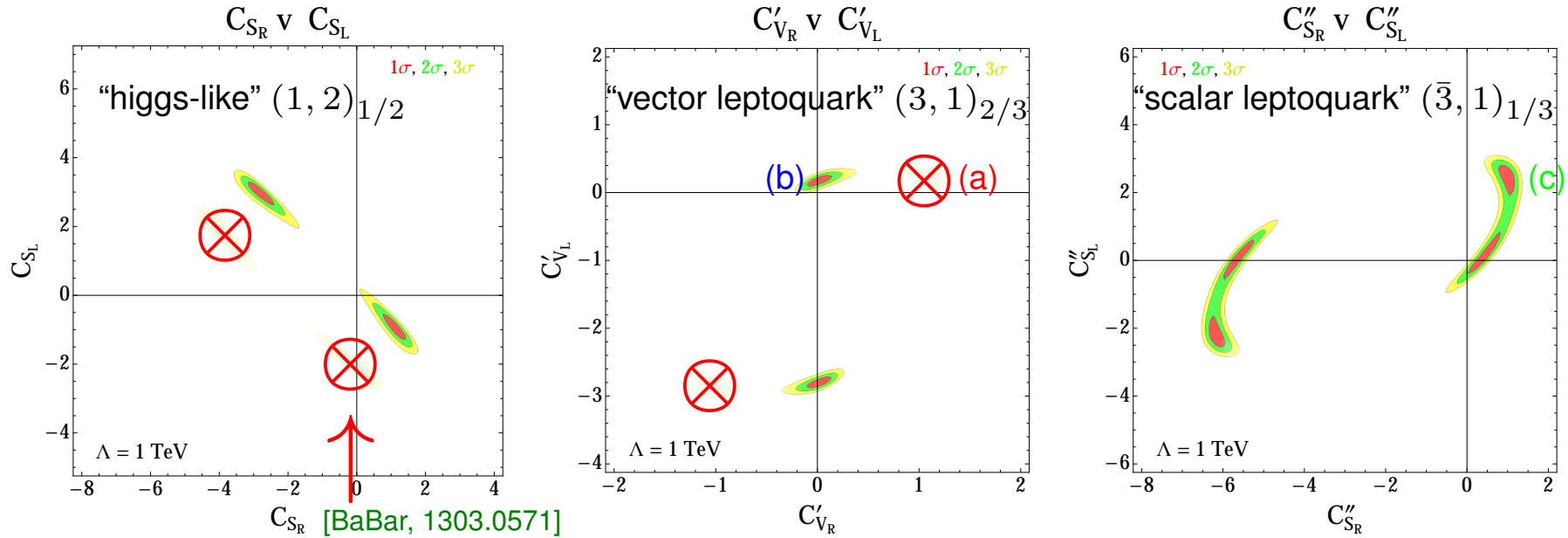
Ruled out by the BaBar q^2 spectrum [1303.0571]

- Large coefficients, $\Lambda = 1 \text{ TeV}$ in plots \Rightarrow fairly light mediators (obvious: 20–30% of a tree-level rate)

In HQET limit, we confirmed the “classic” paper

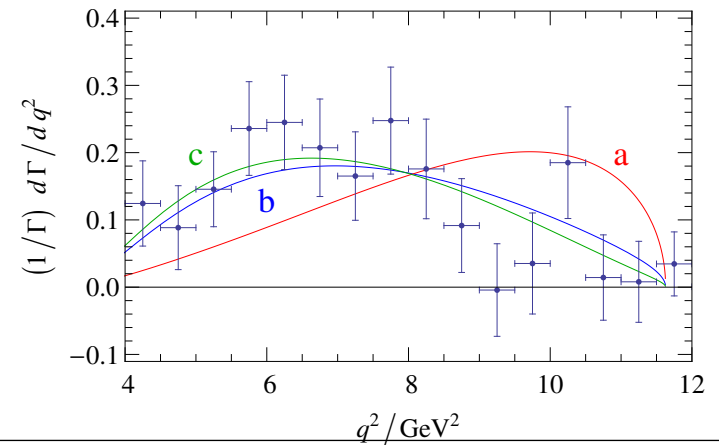
[Goldberger, hep-ph/9902311]

Fits to two operators



The \otimes solution are ruled out by the q^2 spectrum

Operator coefficients	
$C'_{V_L} = 0.24$	$C'_{V_R} = 1.10$
$C'_{V_L} = 0.18$	$C'_{V_R} = -0.01$
$C''_{S_R} = 0.96$	$C''_{S_L} = 2.41$



Operator fits \rightarrow viable MFV models?

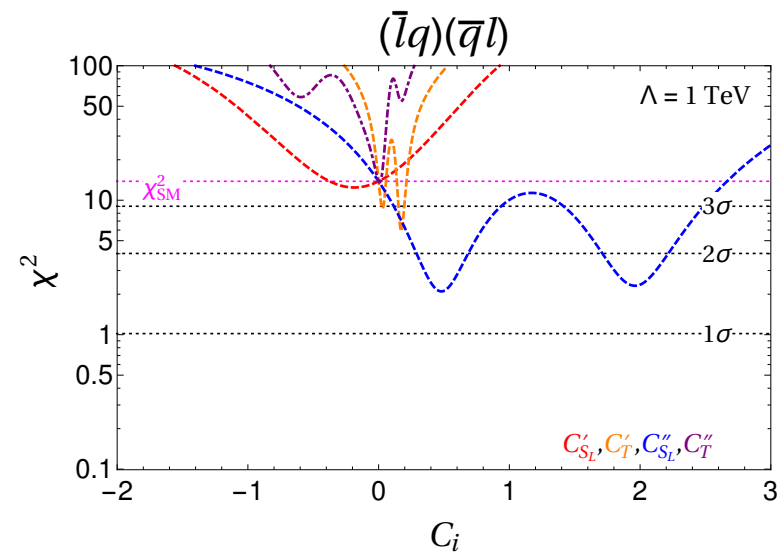
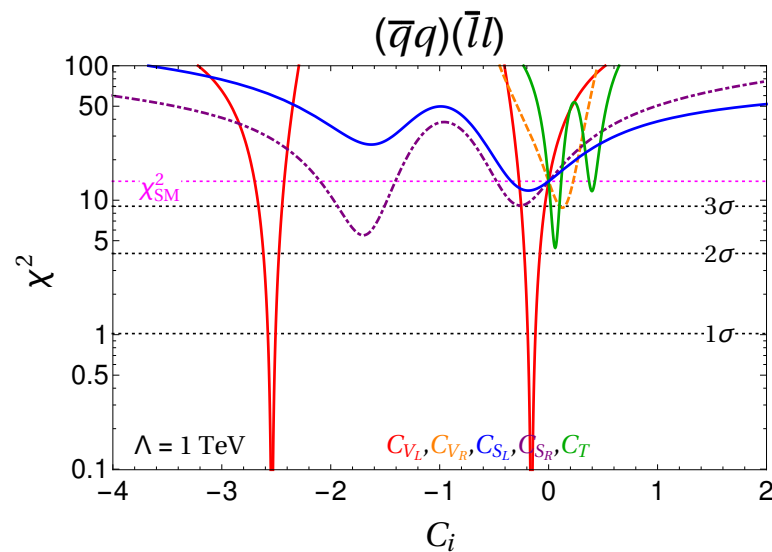
- Viable mediators: scalar, “Higgs-like” $(1, 2)_{1/2}$, vector, “ W' -like” $(1, 3)_0$
“scalar LQ” $(\bar{3}, 1)_{1/3}$ or $(\bar{3}, 3)_{1/3}$, “vector LQ” $(3, 1)_{2/3}$ or $(3, 3)_{2/3}$
- Flavor structure of TeV-scale NP cannot be generic — surprising if **only** $(\bar{b}c)(\bar{\tau}\nu)$
- New physics at LHC — MFV probably useful approximation to its flavor structure
 \Updownarrow
New physics at 10^{1-2} TeV — less strong flavor suppression, MFV less motivated
- Minimal flavor violation (MFV) is probably a useful starting point
Global $U(3)_Q \times U(3)_u \times U(3)_d$ flavor sym. broken by $Y_u \sim (\mathbf{3}, \bar{\mathbf{3}}, 1)$, $Y_d \sim (\mathbf{3}, \mathbf{1}, \bar{\mathbf{3}})$
- Which BSM scenarios can be MFV? [Freytsis, ZL, Ruderman, 1506.08896]
Not scalars or vectors, viable leptoquarks: scalar $S(\mathbf{1}, \mathbf{1}, \bar{\mathbf{3}})$ or vector $U_\mu(\mathbf{1}, \mathbf{1}, \mathbf{3})$
Bounds: $b \rightarrow s\nu\bar{\nu}$, D^0 & K^0 mixing, $Z \rightarrow \tau^+\tau^-$, LHC contact int., $pp \rightarrow \tau^+\tau^-$, etc.

How odd scenarios may be viable?

- All papers enhance the τ mode compared to the SM

Can one suppress the e and μ modes instead?

[Freysis, ZL, Ruderman, to appear]



- Unique viable option: modify the SM four-fermion operator

Good fit with: $V_{cb}^{(\text{exp})} \sim V_{cb}^{(\text{SM})} \times 0.9$ $V_{ub}^{(\text{exp})} \sim V_{ub}^{(\text{SM})} \times 0.9$

- Many relevant constraints, one of the strongest from ϵ_K

What about $e - \mu$ (non)universality?

- How well is the difference of the e and μ rates constrained?

Parameters	De sample	$D\mu$ sample	combined result
ρ_D^2	$1.22 \pm 0.05 \pm 0.10$	$1.10 \pm 0.07 \pm 0.10$	$1.16 \pm 0.04 \pm 0.08$
$\rho_{D^*}^2$	$1.34 \pm 0.05 \pm 0.09$	$1.33 \pm 0.06 \pm 0.09$	$1.33 \pm 0.04 \pm 0.09$
R_1	$1.59 \pm 0.09 \pm 0.15$	$1.53 \pm 0.10 \pm 0.17$	$1.56 \pm 0.07 \pm 0.15$
R_2	$0.67 \pm 0.07 \pm 0.10$	$0.68 \pm 0.08 \pm 0.10$	$0.66 \pm 0.05 \pm 0.09$
$\mathcal{B}(D^0 \ell \bar{\nu})(\%)$	$2.38 \pm 0.04 \pm 0.15$	$2.25 \pm 0.04 \pm 0.17$	$2.32 \pm 0.03 \pm 0.13$
$\mathcal{B}(D^{*0} \ell \bar{\nu})(\%)$	$5.50 \pm 0.05 \pm 0.23$	$5.34 \pm 0.06 \pm 0.37$	$5.48 \pm 0.04 \pm 0.22$
$\chi^2/\text{n.d.f. (probability)}$	416/468 (0.96)	488/464 (0.21)	2.0/6 (0.92)

[BaBar, 0809.0828 — similar results in Belle, 1010.5620]

- 10% difference allowed... some wrong statements...

Γ_1	$e^+ \nu_e$ anything	$(10.86 \pm 0.16)\%$
Γ_2	$\bar{p} e^+ \nu_e$ anything	$< 5.9 \times 10^{-4}$
Γ_3	$\mu^+ \nu_\mu$ anything	$(10.86 \pm 0.16)\%$
Γ_4	$\ell^+ \nu_\ell$ anything	$(10.86 \pm 0.16)\%$

- How much better can difference be constrained better?

Reaching the 1% level on ratio might be possible (but challenging) at Belle II

Final comments

Conclusions

- Amusing if NP shows up in $B \rightarrow D^{(*)}\tau\bar{\nu}$, a mode with little SM suppression
 - SM predictions can be improved with more data (with continuum methods)
 - Lattice: Calculate subleading Isgur-Wise functions and/or non-SM form factors?
 - Ongoing: consistent generator for all six $B \rightarrow D^{(*,**)}\ell\bar{\nu}$ modes, for any interaction
 - More theory progress to come, will impact measurements and sensitivity to BSM
 - With Belle II and LHCb upgrade, even if $R(D^{(*)})$ move toward SM, plenty of room to discover NP
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- There are good operator fits, and (somewhat) sensible MFV leptoquark models (Wild scenarios are also viable!)



Bonus slides