

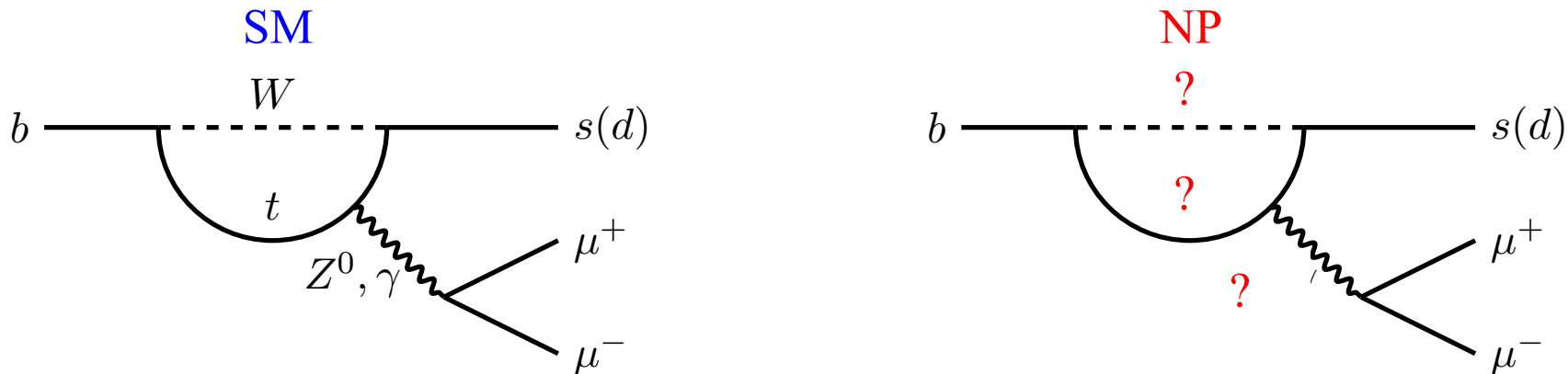
Electroweak penguin decays: $b \rightarrow s \ell \ell$

FPCP 2015, Nagoya

Christian Linn, CERN

on behalf of the LHCb collaboration,
including results from other experiments

FCNC as $b \rightarrow sll$ transitions in the SM only possible via loop and box diagrams
 → highly suppressed / new particles can enter the loop and modify observables



$b \rightarrow sll$ decays can theoretically be described by effective hamiltonian:

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i)$$

↑

left-handed part

↑

right-handed part
suppressed in SM

i=1,2	Tree
i=3-6,8	Gluon penguin
i=7	Photon penguin
i=9,10	Electroweak penguin
i=S, P	Scalar / Pseudoscalar penguin

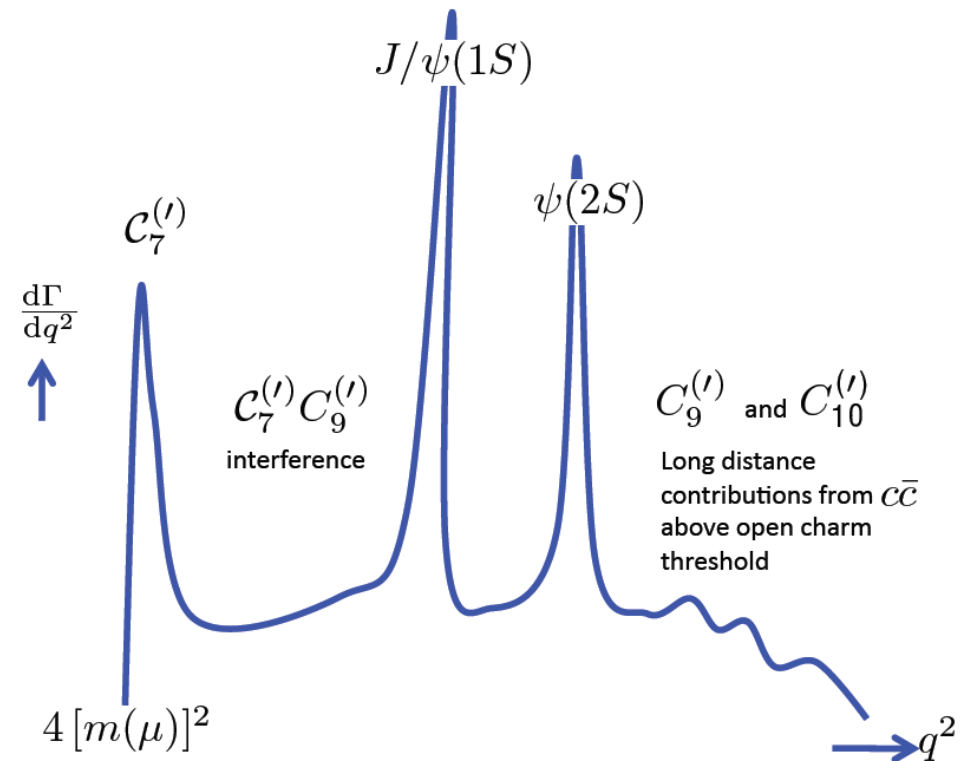
- Operators \mathcal{O}_i depend on hadronic form factors (FF) of the decay
 (FF usually dominate theoretical uncertainties)
- Wilson coefficients C_i describe short distance effects – sensitive to NP contributions
 → **observables like branching fraction, CP asymmetries, angular distributions depend on C_i**

Wilson coefficients enter many processes:

- $B \rightarrow X_s \gamma$: C_7
- $B \rightarrow (X_s, K^*) \ell \ell$: C_7, C_9, C_{10}
- $B \rightarrow \mu \mu$: C_{10}, C_S, C_P

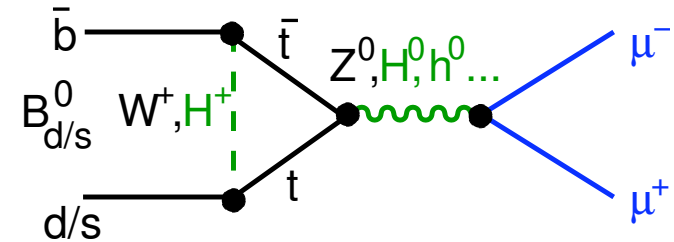
I will show today:

- Combined measurement of $B_{s/d} \rightarrow \mu \mu$ (CMS + LHCb)
- Branching fractions of $b \rightarrow s \mu \mu$ / Test of lepton universality in $b \rightarrow s \ell \ell$ decays
- Angular analysis of $B \rightarrow K^* \mu \mu$ and $B \rightarrow K^* e e$
- Branching fraction and angular analysis of $B_s \rightarrow \phi \mu \mu$ - **NEW**



rare B → μμ decays are loop, CKM and helicity suppressed in SM

→ golden channel for C₁₀ and pseudo-scalar operators
(probes models like e.g. 2HDM, MSSM, ...)



Precise theoretical predictions:

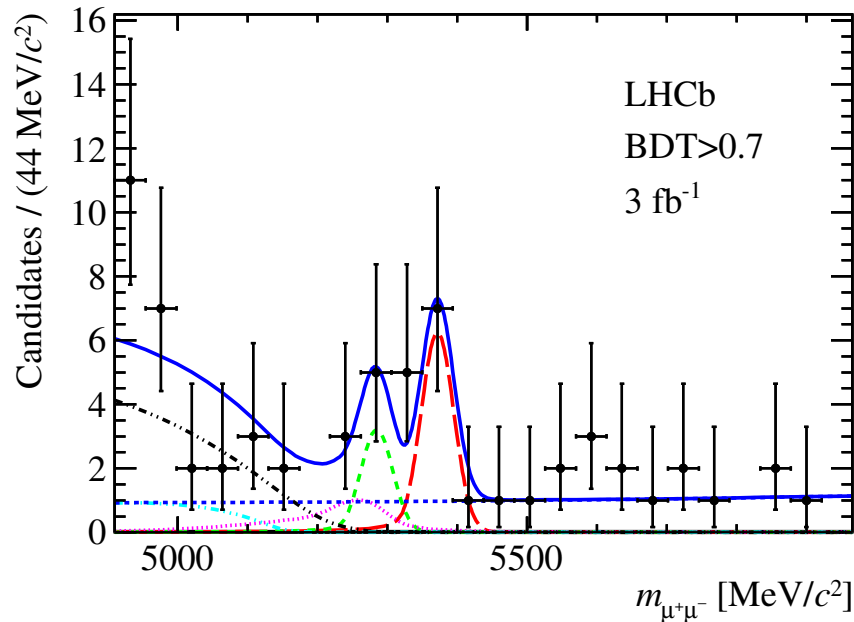
$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.66 \pm 0.23) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = (1.06 \pm 0.09) \times 10^{-10}$$

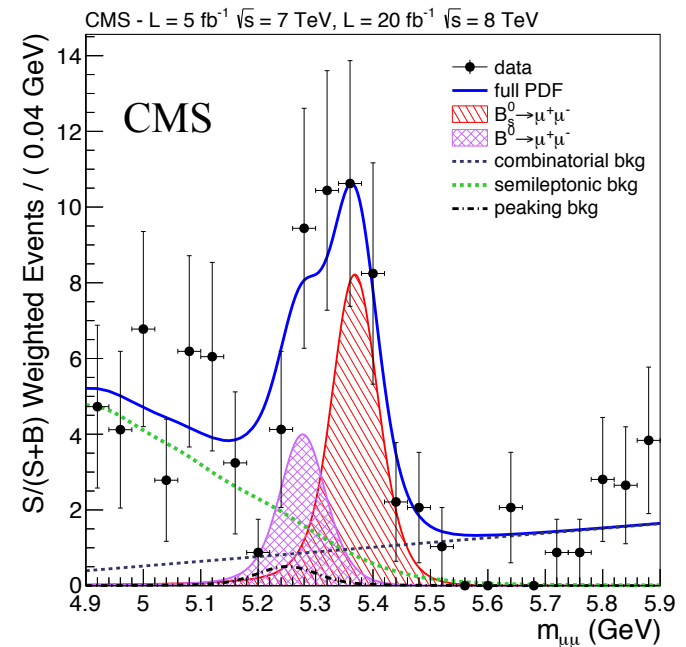
Bobeth et al, PRL 112 (2014) 101801

Measured by both LHCb and CMS with full Run 1 dataset:

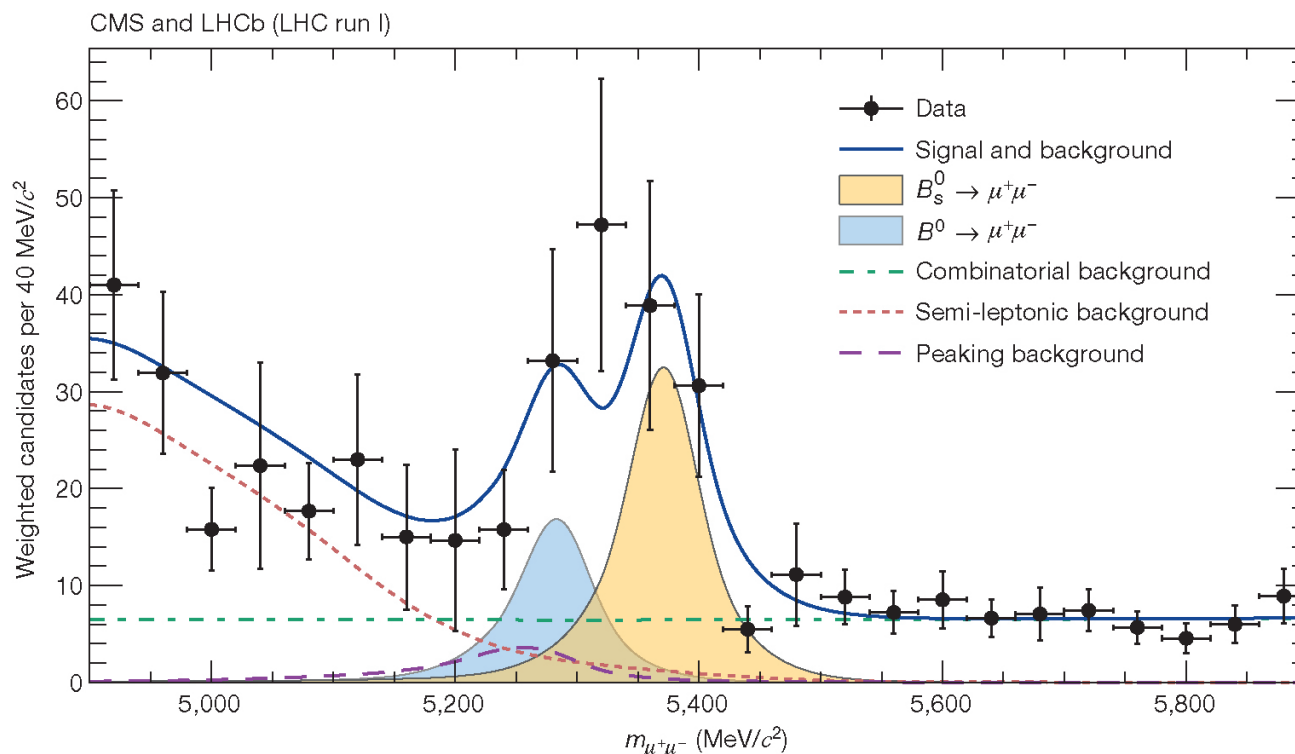
PRL 111 (2013) 101805



PRL 111 (2013) 101804



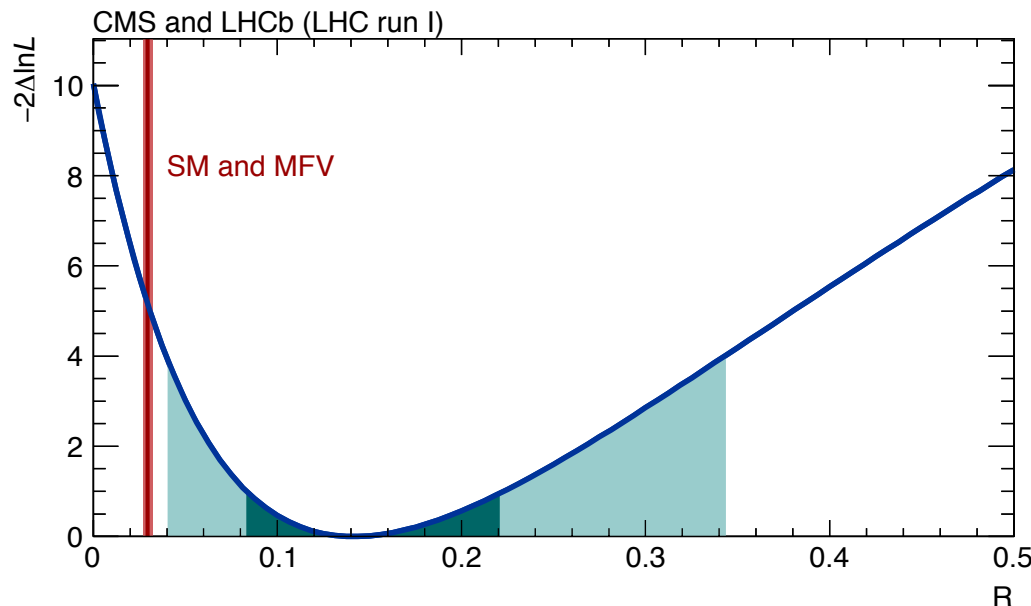
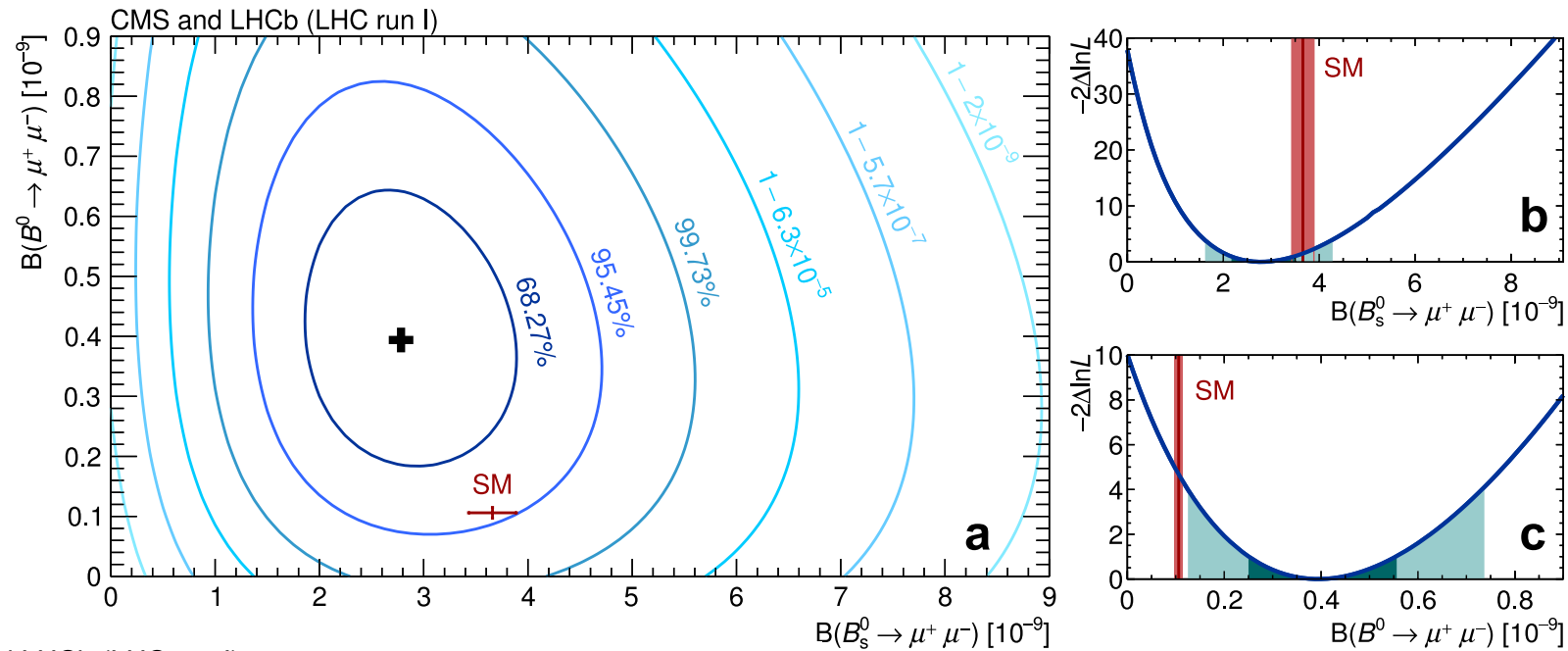
Simultaneous analysis of the LHCb and CMS datasets, with shared signal parameters and nuisance parameters:



$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (2.8_{-0.6}^{+0.7}) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = (3.9_{-1.4}^{+1.6}) \times 10^{-10}$$

- First observation of $B_s \rightarrow \mu\mu$ decay (6.2 σ significance),
- First evidence of $B^0 \rightarrow \mu\mu$ decay (3.0 σ significance)



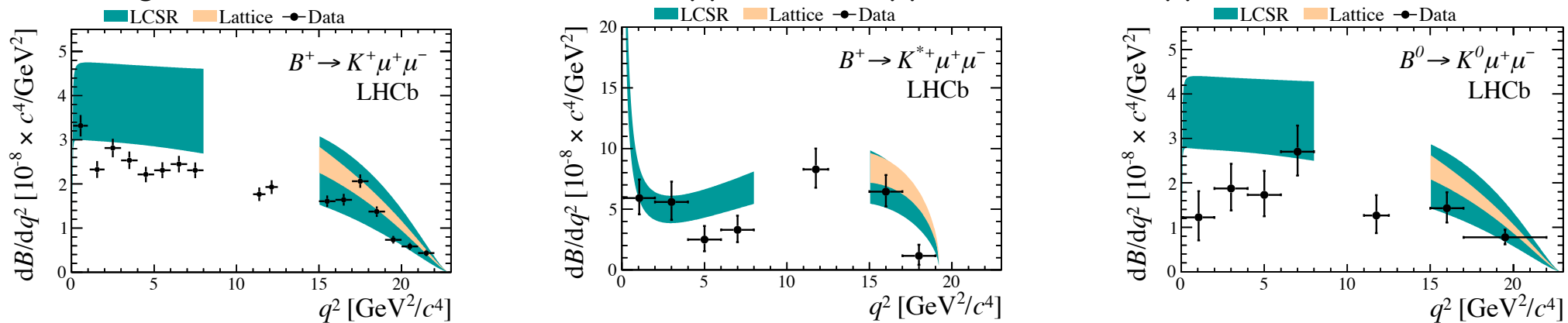
Ratio of branching fractions is probe of MFV hypothesis:

$$R = \frac{B(B^0 \rightarrow \mu \mu)}{B(B_s^0 \rightarrow \mu \mu)} = 0.14^{+0.08}_{-0.06}$$

→ measured for the first time

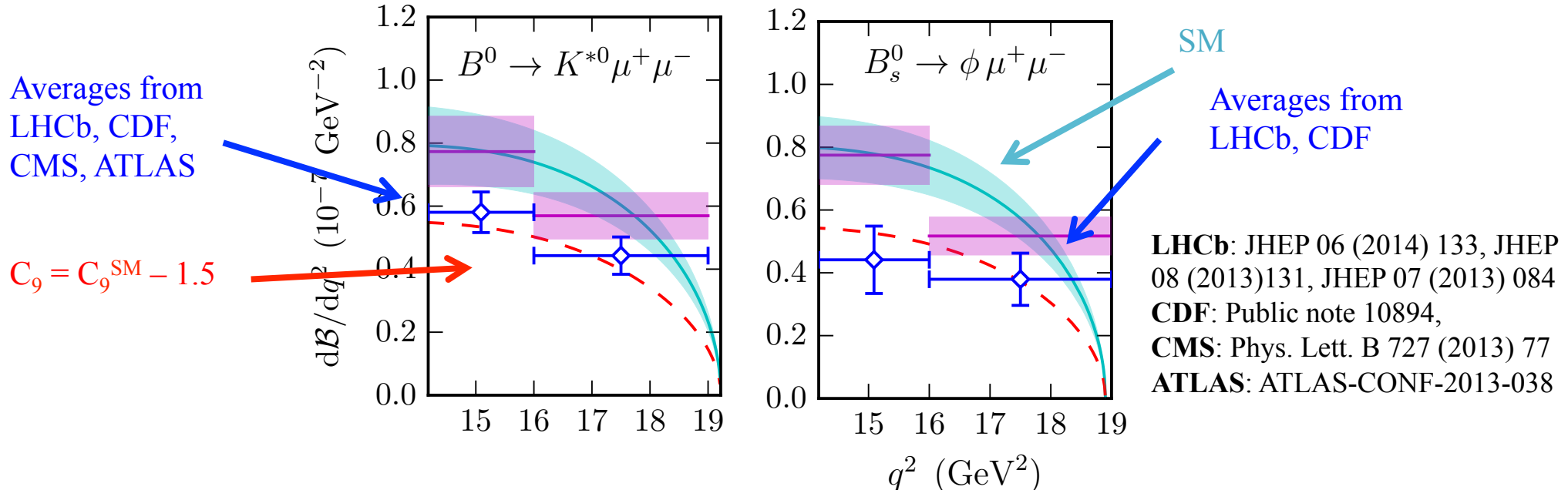
→ compatible with the SM prediction at the 2.3 σ level

Branching fraction measurement for $B^0 \rightarrow K^0 \mu\mu$, $B^+ \rightarrow K^+ \mu\mu$ and $B^+ \rightarrow K^{*+} \mu\mu$: JHEP 06 (2014) 133



SM predictions: JHEP 07 (2011) 067; JHEP 01 (2012) 107; Phys. Rev. Lett. 111 (2013) 162002

Average of the $B^0 \rightarrow K^{*0} \mu\mu$ and $B_s \rightarrow \phi \mu\mu$ decay in the high- q^2 range: Horgan et al., PRL 112, 212003



→ branching fractions tend to lie below SM predictions

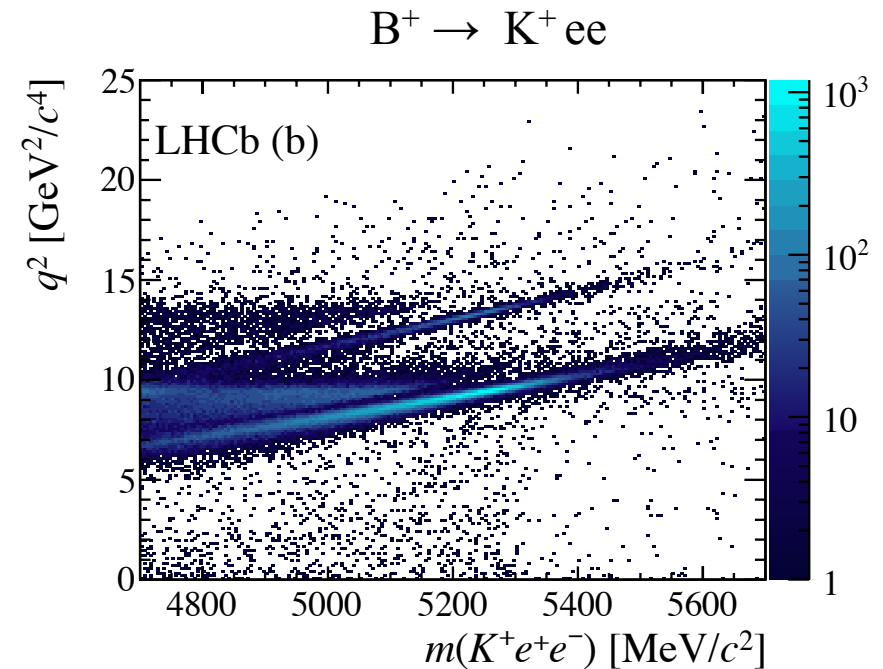
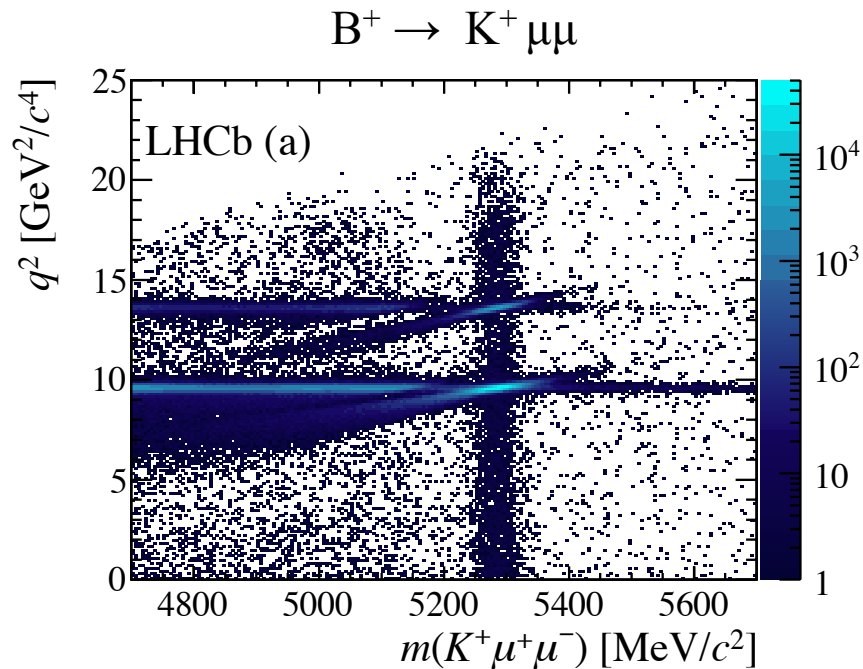
(see also: Altmannshofer et al., arxiv:1411.3161)

Ratio of branching fractions of
 $B^+ \rightarrow K^+ \mu\mu$ and $B^+ \rightarrow K^+ ee$:

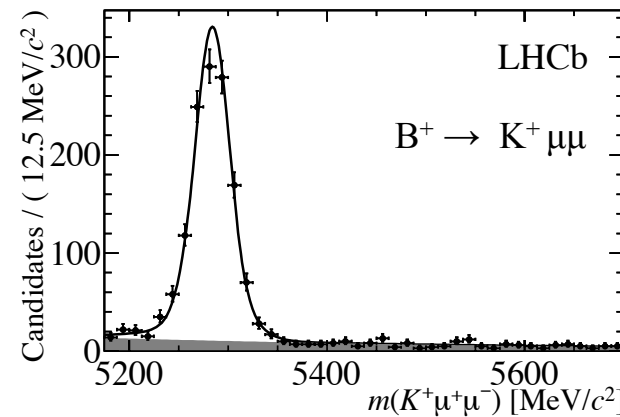
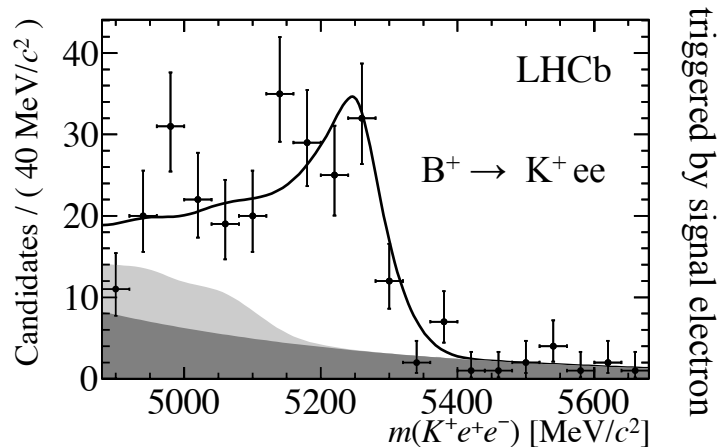
$$R_K = \frac{\Gamma(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\Gamma(B^+ \rightarrow K^+ e^+ e^-)}$$

- Lepton universality in SM $\rightarrow R_K$ predicted to be 1 in SM within $O(10^{-3})$
 JHEP 12 (2007) 040, Phys. Rev. Lett. 111 (2013) 162002
- Measurements from Babar (Phys. Rev. D86 (2012) 032012),
 Belle (Phys. Rev. Lett. 103 (2009) 171801) and LHCb (Phys. Rev. Lett. 113 (2014) 151601)

LHCb measurement uses full 3fb^{-1} dataset in $1 < q^2 < 6 \text{ GeV}^2/c^4$:



- $B^+ \rightarrow K^+ ee$ mass shape affected by bremsstrahlung, transverse momentum of electron and occupancy
→ sample divided in trigger categories / $B^+ \rightarrow J/\Psi K^+$ to investigate shape dependence
- Signal yield corrected for bin migration due to bremsstrahlung



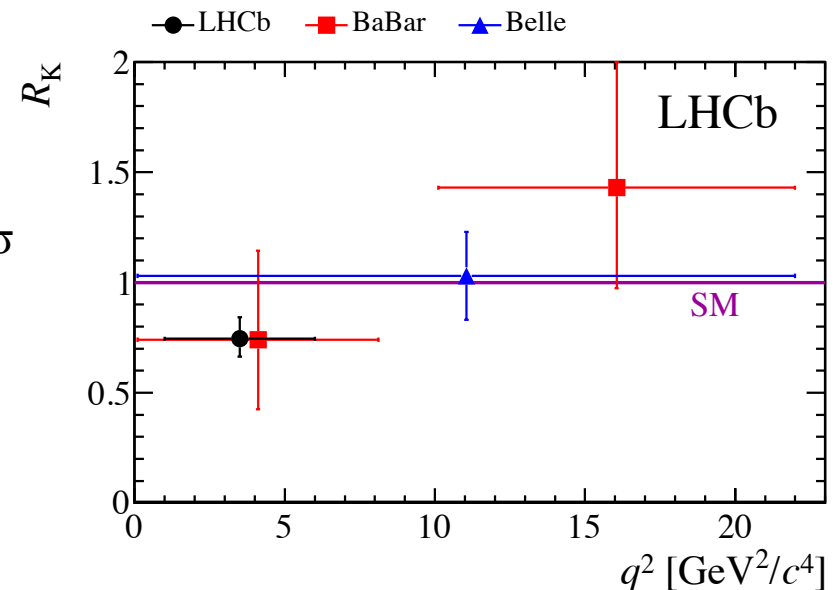
$$R_K = 0.745^{+0.090}_{-0.074}(\text{stat}) \pm 0.036(\text{syst})$$

→ most precise to date, compatible with SM within 2.6σ

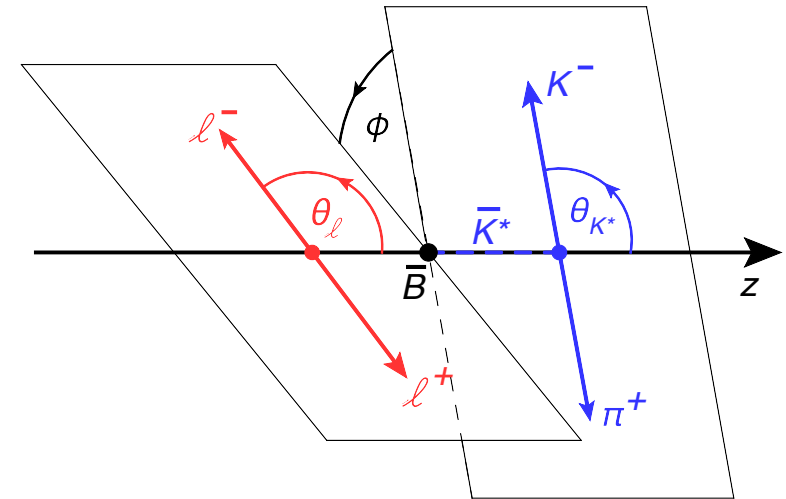
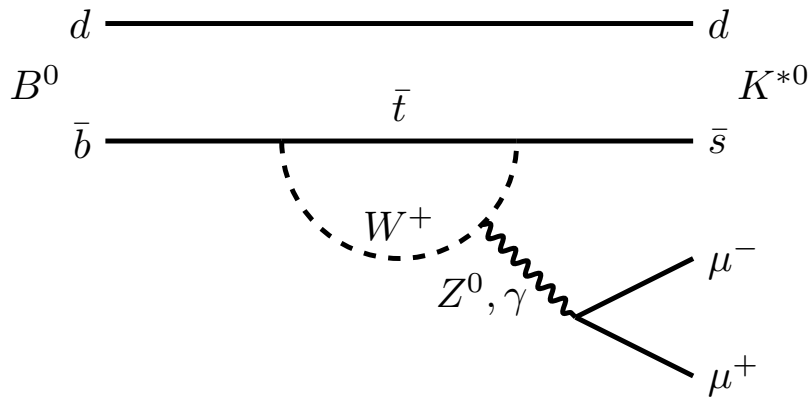
→ BR ($B^+ \rightarrow K^+ ee$) in agreement with SM

Consistent with branching fractions if possible NP only contributes to $b \rightarrow s \mu\mu$ and not to $b \rightarrow s ee$

Altmannshofer, Straub, arXiv:1503.06199v2



Angular observables of $B \rightarrow K^* l^+ l^-$



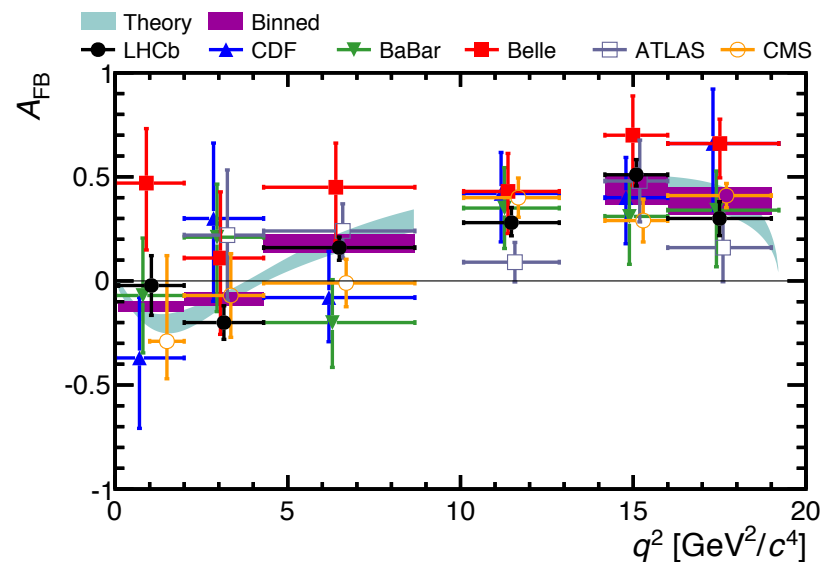
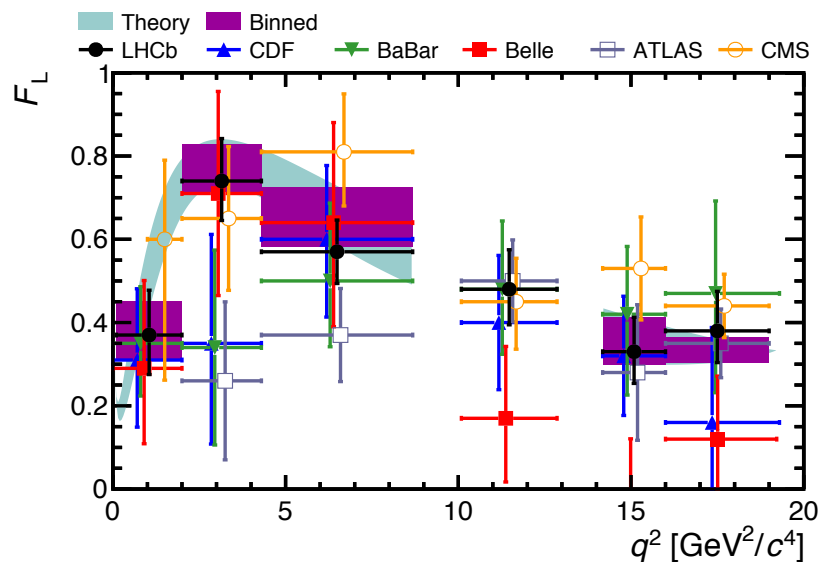
$B^0 \rightarrow K^{*0} l^+ l^-$ described by three angles (θ_K, θ_l, Φ) and di-muon mass squared, q^2 :

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} = \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi \right. \\ \left. + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi \right. \\ \left. + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

F_L, A_{FB} and S_i are determined in bins of q^2 and depend on Wilson coefficients C_7, C_9 and C_{10} and hadronic form factors

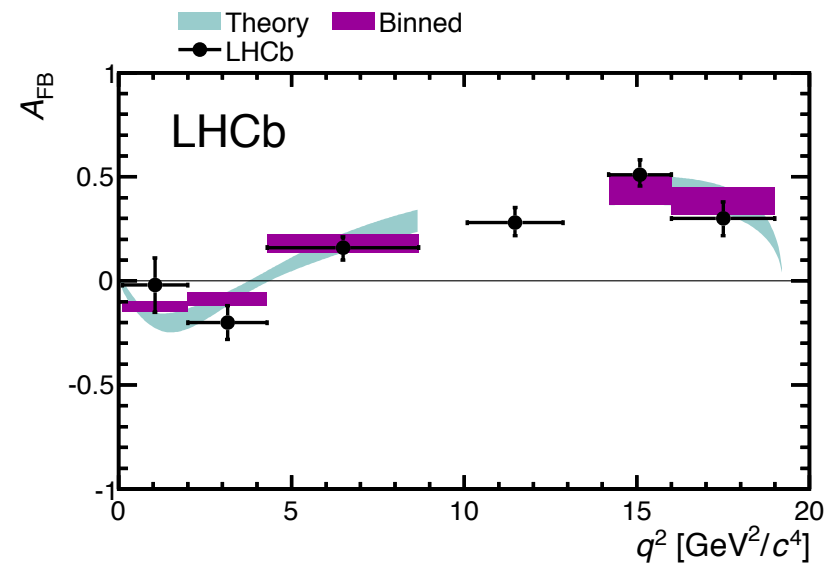
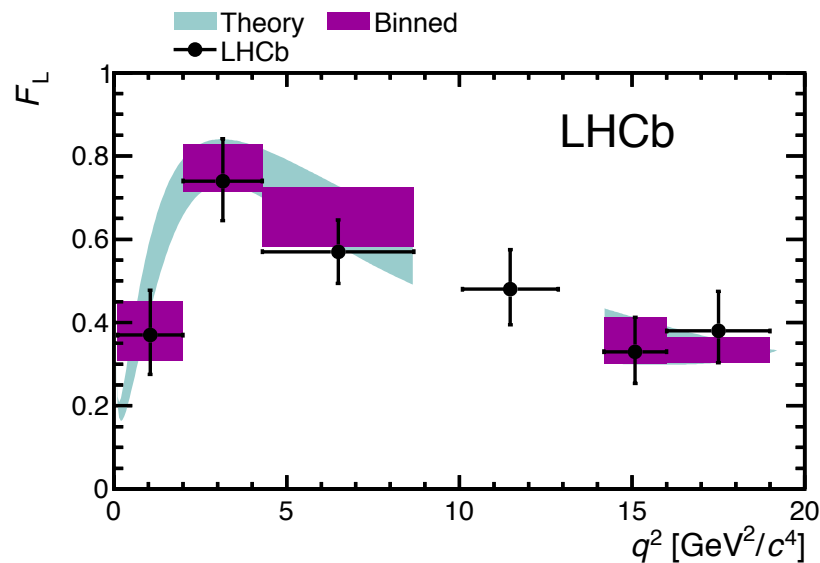
Long history of $B^0 \rightarrow K^{*0} \mu\mu$ measurements:

Belle: Phys. Rev. Lett. 103 (2009) 171801, **Babar:** Phys. Rev. D. 73. 092001, **CDF:** Phys. Rev. Lett. 108 081807, **CMS:** Phys. Lett. B 727 (2013) 77, **ATLAS:** ATLAS-CONF-2013-038, **LHCb** JHEP 08 (2013) 131



Long history of $B^0 \rightarrow K^{*0} \mu\mu$ measurements:

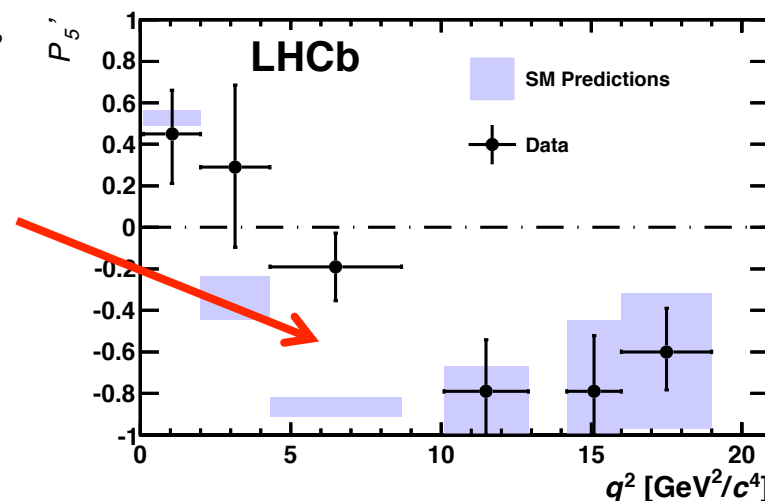
Belle: Phys. Rev. Lett. 103 (2009) 171801, **Babar**: Phys. Rev. D. 73. 092001, **CDF**: Phys. Rev. Lett. 108 081807, **CMS**: Phys. Lett. B 727 (2013) 77, **ATLAS**: ATLAS-CONF-2013-038, **LHCb** JHEP 08 (2013) 131



→ mostly compatible with SM,
but ...

3.7 σ local deviation from
SM prediction

PRL 111, 191801 (2013)

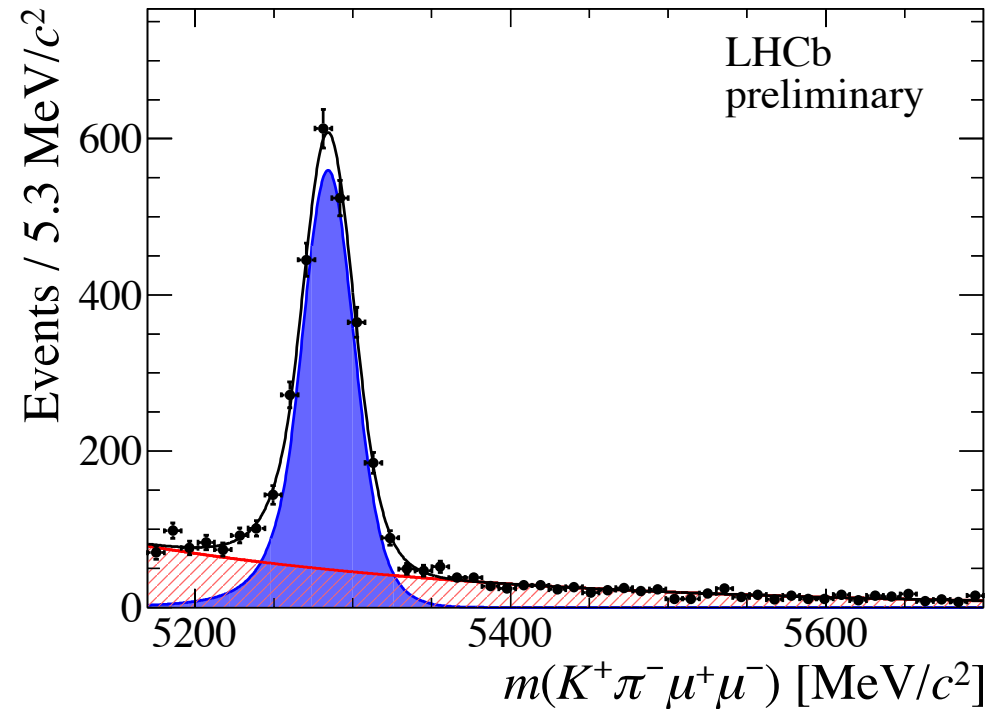


Less form-factor dependent
observable:

$$P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}}$$

Full Run1 analysis from LHCb (3 fb⁻¹) :

- update of 1 fb⁻¹ analysis, first presented at Moriond 2015
- total signal yield: $N_{\text{sig}} = 2398 \pm 57$

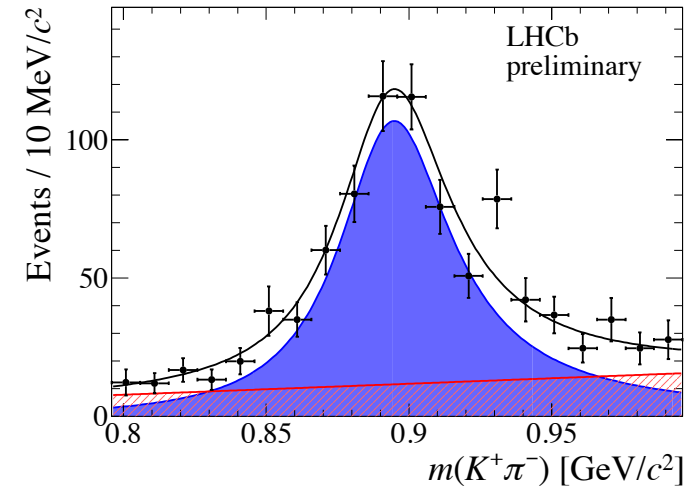


- first simultaneous determination of all eight CP-averaged observables in a single fit which allows to provide the full correlation matrix

extracted from likelihood fit in decay angles, $m_{K\pi\mu\mu}$ and q^2

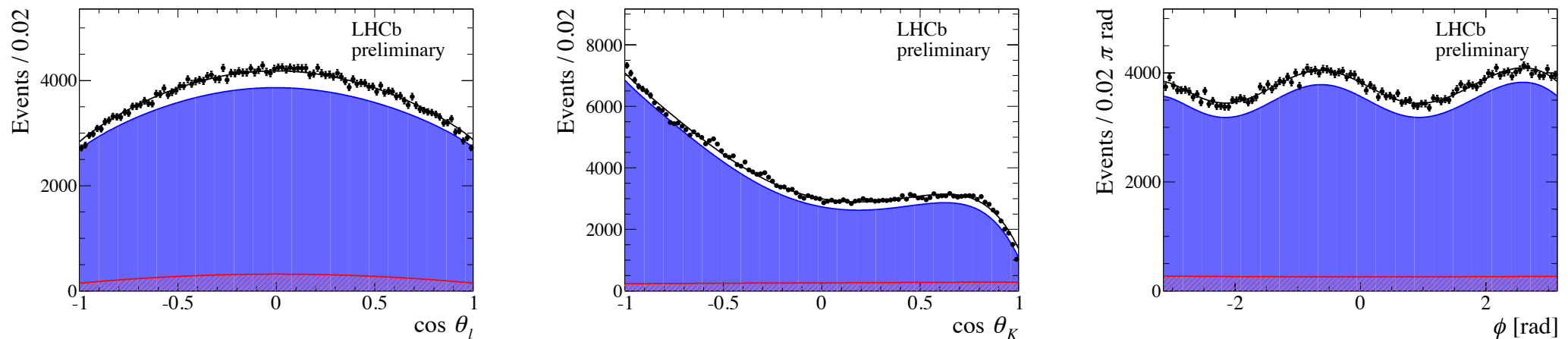
Simultaneously fitting $m_{K\pi}$ to constrain S-wave component F_S

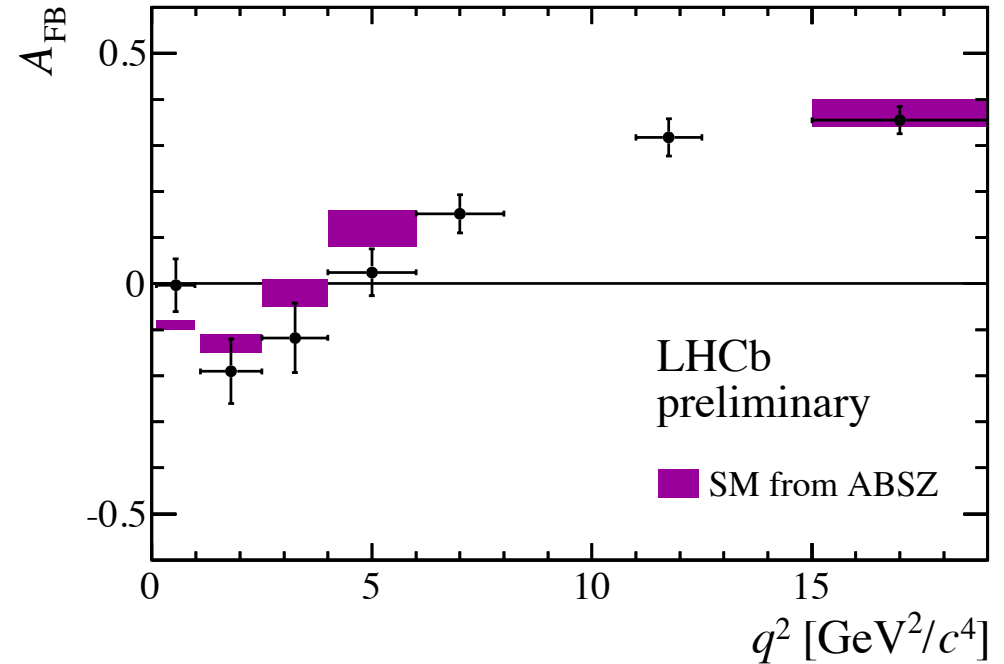
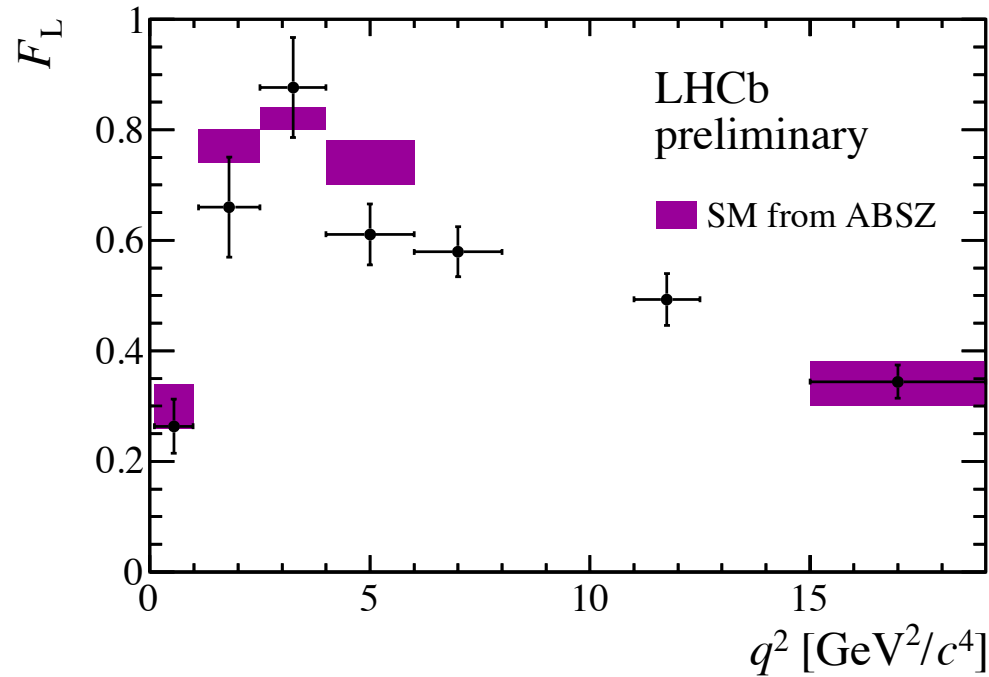
$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \Big|_{S+P} = (1 - F_S) \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \Big|_P + \frac{3}{16\pi} F_S \sin^2 \theta_\ell + \text{S-P interference}$$



Angular acceptances from simulation, 4D parameterization using Legendre polynomials

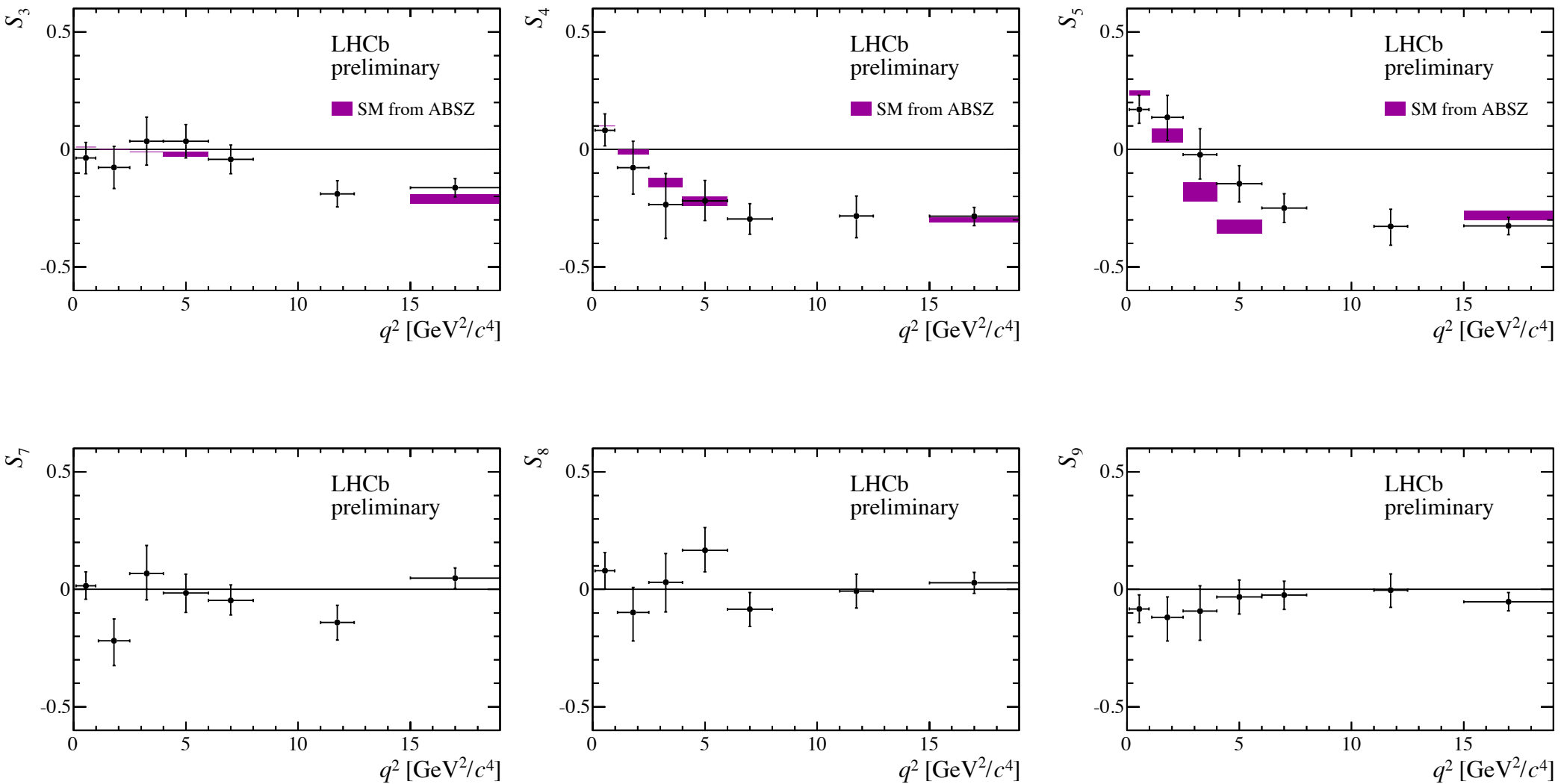
Fit cross-checked with $B^0 \rightarrow J/\Psi K^{*0}$: consistent with results in PRD 88, 052002 (2013)





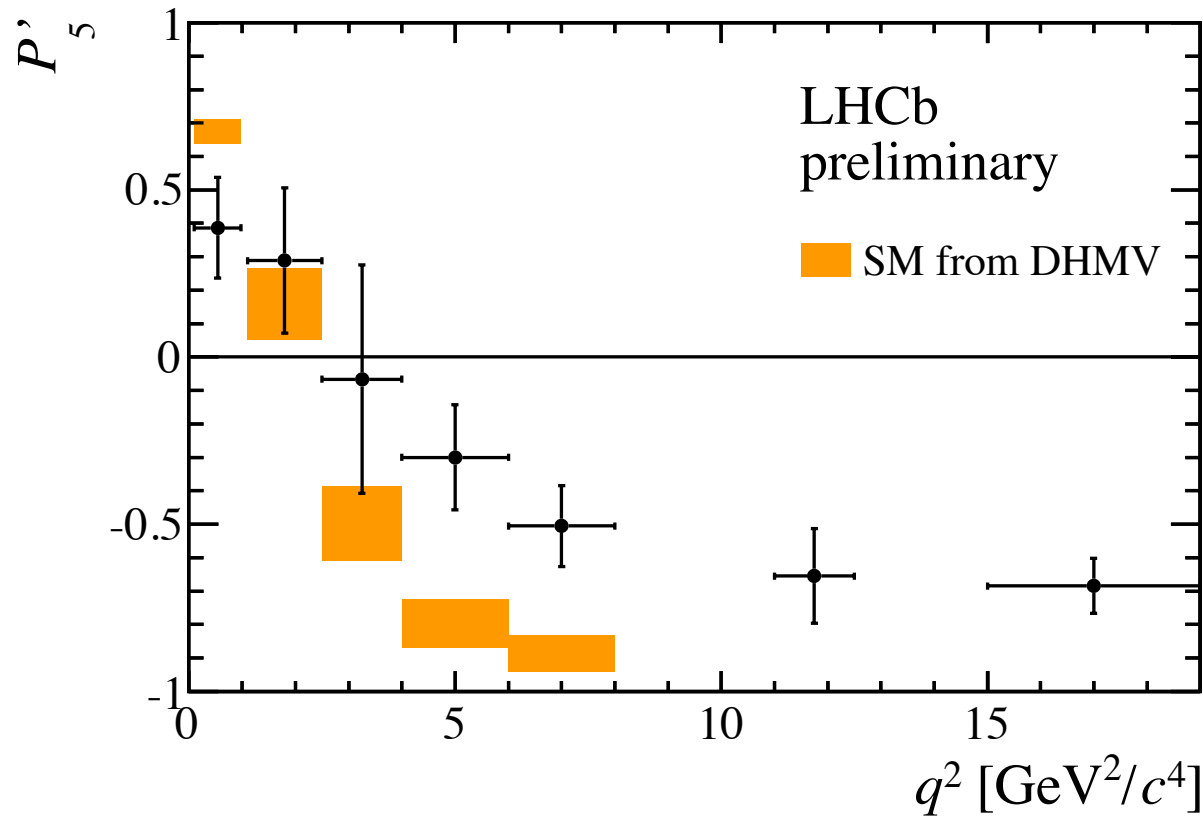
Theory prediction from arXiv:1503.05534, arXiv:1411.3161

- A_{FB} systematically below SM prediction
- Zero-crossing point evaluated as in JHEP 08 (2013) 131 and consistent with SM:
 $q^2_0 = 3.7^{+0.8}_{-1.1} \text{ GeV}^2$



Less form-factor dependent observable:
(smaller theoretical uncertainties)

$$P'_5 = \frac{S_5}{\sqrt{F_L(1 - F_L)}}$$



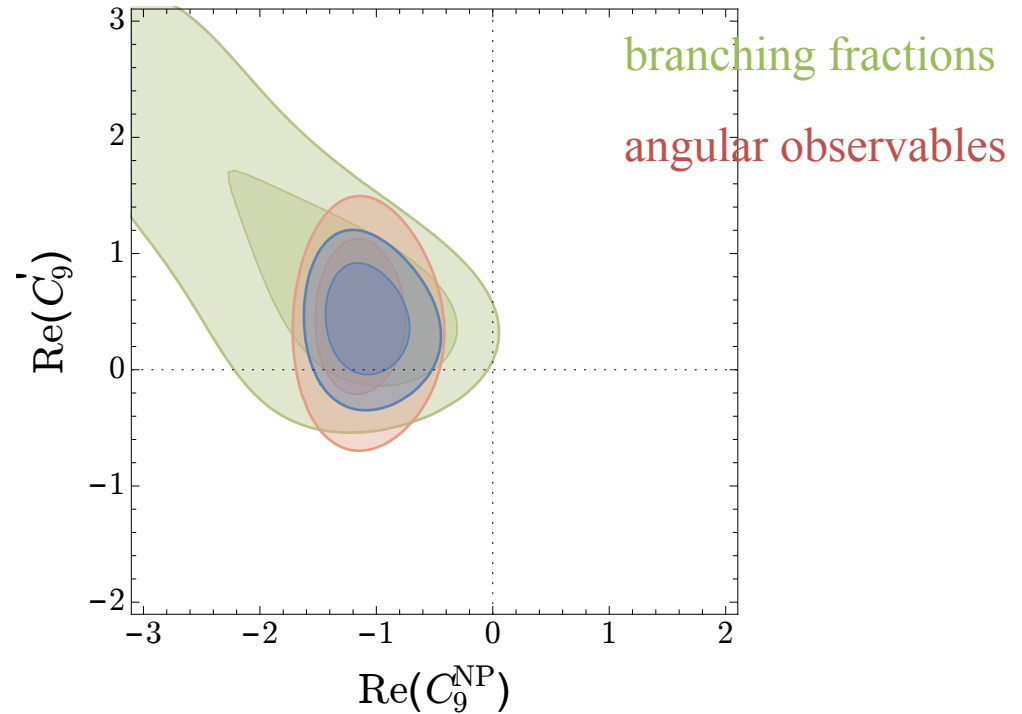
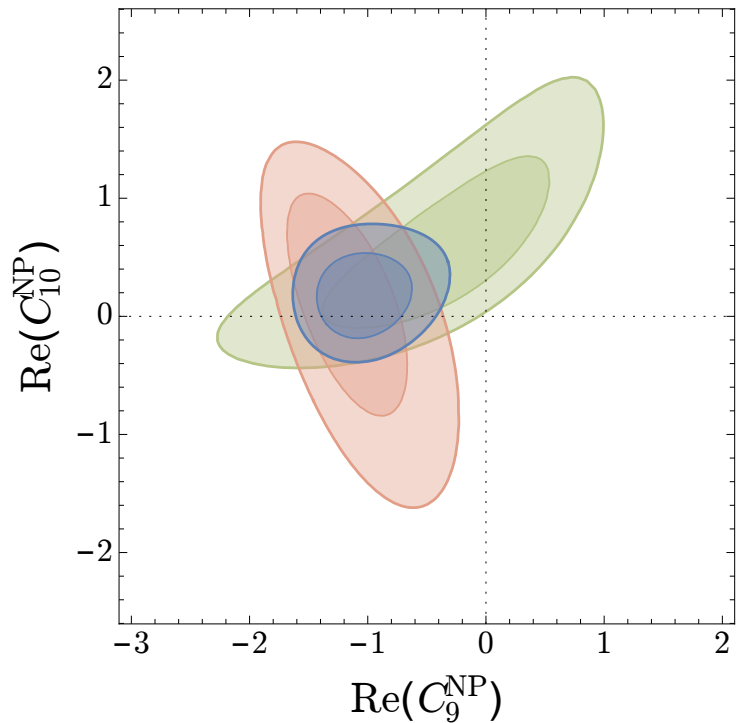
Consistent with 1 fb⁻¹ analysis and tension to SM prediction confirmed

Two bins each show local deviation of 2.9 σ , naïve χ^2 combination gives 3.7 σ

Wilson coefficients from $b \rightarrow s \mu\mu$ in global fit:

- 88 measurements are used as input for this fit (including results from ATLAS, CMS, LHCb)

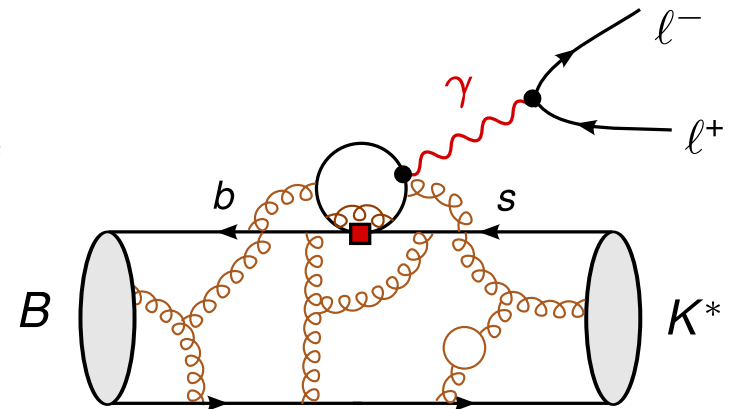
Altmannshofer, Straub, arXiv:1503.06199v2 [hep-ph]



- Fit prefers negative $C_9^{\text{NP}} \sim -1.1$ ($C_9 = C_9^{\text{SM}} + C_9^{\text{NP}}$)
- Constraints from angular observables and branching fractions compatible

Hadronic effects:

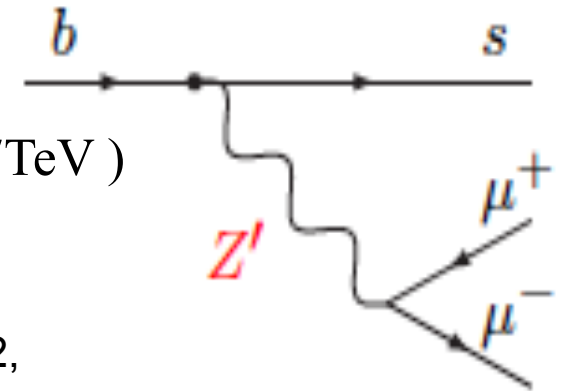
- Unexpectedly huge charm effects can mimic negative C_9^{NP} at intermediate q^2
- But: hadronic effects can not violate LFU
→ important to perform more measurements like R_K



Altmannshofer, Straub, arXiv:1503.06199v2 [hep-ph], Straub, Moriond EW, 2015

Possible New Physics interpretation:

- Data can be described with Z' with FV couplings and mass $O(7\text{TeV})$
→ can accommodate all present measurements

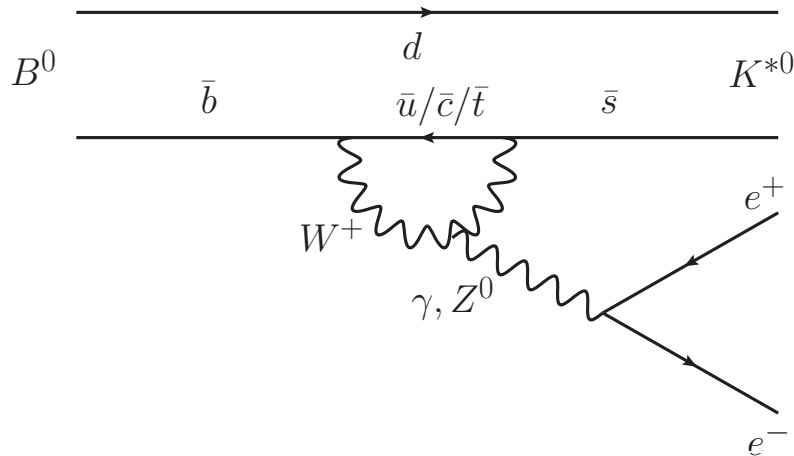


Gauld et al., JHEP 1401 (2014) 069, Buras et al., JHEP 1402 (2014) 112,
Altmannshofer et al. PRD 89 (2014) 095033

but also other models: Hiller et al., PRD 90, 054014 (2014) , Glashow et al., PRL 114, 091801 (2015) ,
Crivellin et al., Phys.Rev.Lett. 114 (2015) 151801

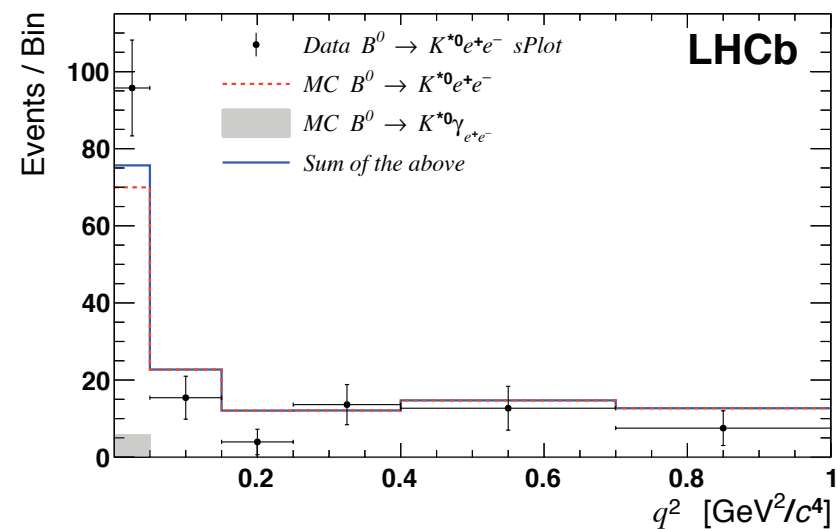
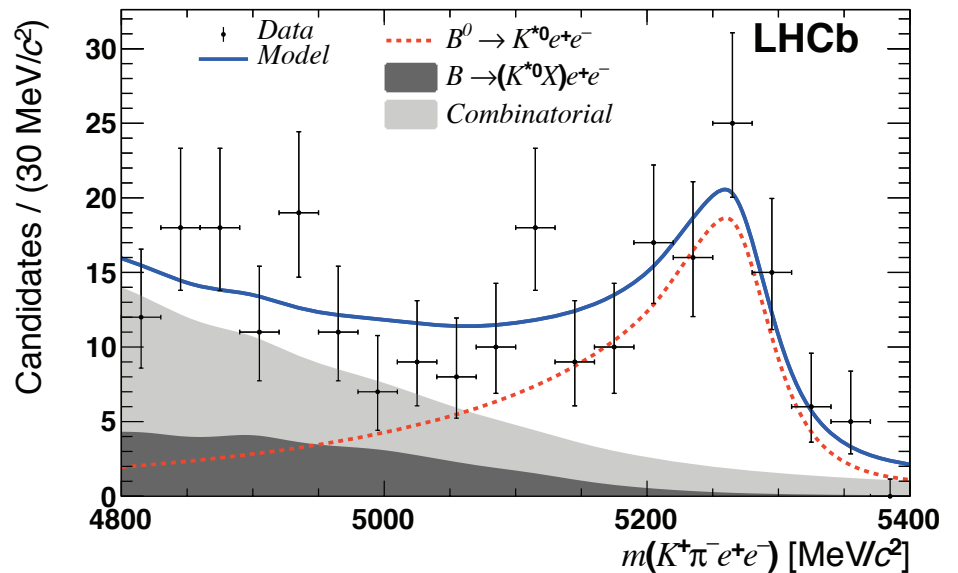
In SM photons from $b \rightarrow s \gamma$ are predominantly left-handed

Angular analysis of $B^0 \rightarrow K^{*0} e e$ is at small values of q^2 sensitive to photon polarization and therefore to C_7, C_7'



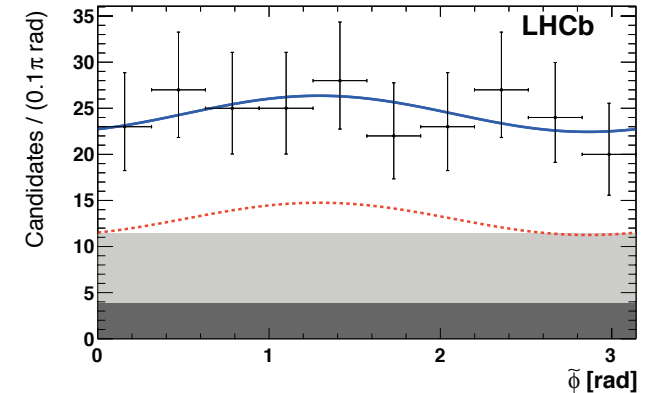
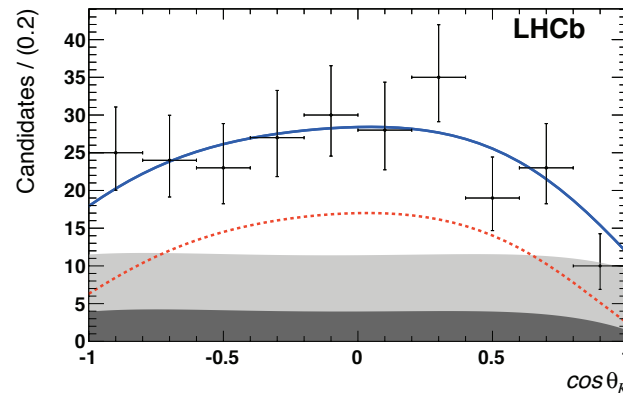
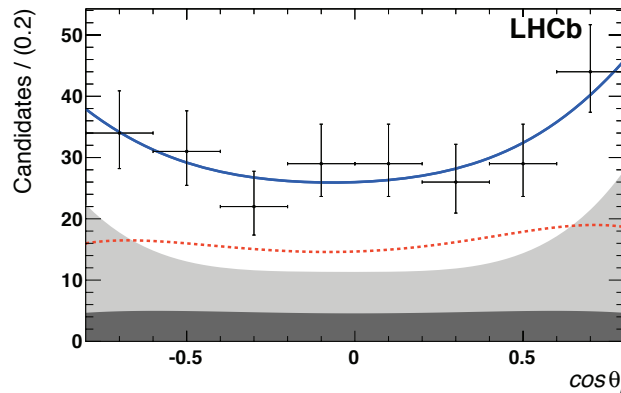
Virtual photon coupling dominates at low q^2
(photon pole):

Analysis is performed in q^2 [0.004 , 1.0] GeV^2



Fit to folded decay angle distribution: $\phi = \phi + \pi$ if $\phi < 0$

Measurement of F_L , $A_T^{(2)}$, $A_T^{(\text{Im})}$, $A_T^{(\text{Re})}$ with $A_T^{(2)}(q^2 \rightarrow 0) = \frac{2\text{Re}(\mathcal{C}_7 \mathcal{C}_7'^*)}{|\mathcal{C}_7|^2 + |\mathcal{C}_7'|^2}$ $A_T^{(\text{Im})}(q^2 \rightarrow 0) = \frac{2\text{Im}(\mathcal{C}_7 \mathcal{C}_7'^*)}{|\mathcal{C}_7|^2 + |\mathcal{C}_7'|^2}$



Result:

obs.	result
F_L	$+0.16 \pm 0.06 \pm 0.03$
$A_T^{(2)}$	$-0.23 \pm 0.23 \pm 0.05$
A_T^{Re}	$+0.10 \pm 0.18 \pm 0.05$
A_T^{Im}	$+0.14 \pm 0.22 \pm 0.05$

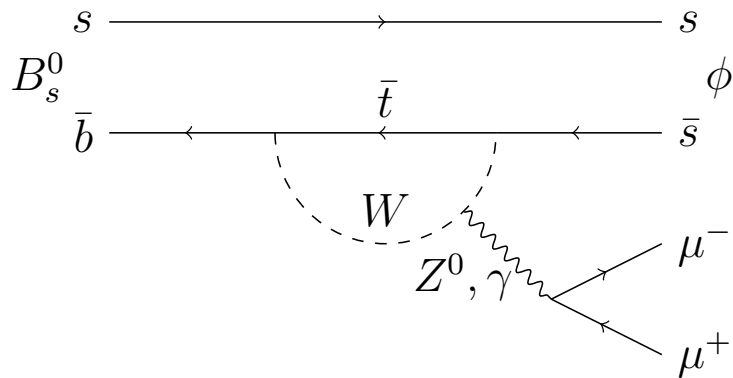
Jaeger et al. JHEP 05 (2013) 043

obs.	SM prediction
F_L	$+0.10^{+0.11}_{-0.05}$
$A_T^{(2)}$	$+0.03^{+0.05}_{-0.04}$
A_T^{Re}	$-0.15^{+0.04}_{-0.03}$
A_T^{Im}	$(-0.2^{+1.2}_{-1.2}) \times 10^{-4}$

Results consistent with SM, sensitivity to \mathcal{C}_7' comparable to sensitivity from $S_{K^*\gamma}$

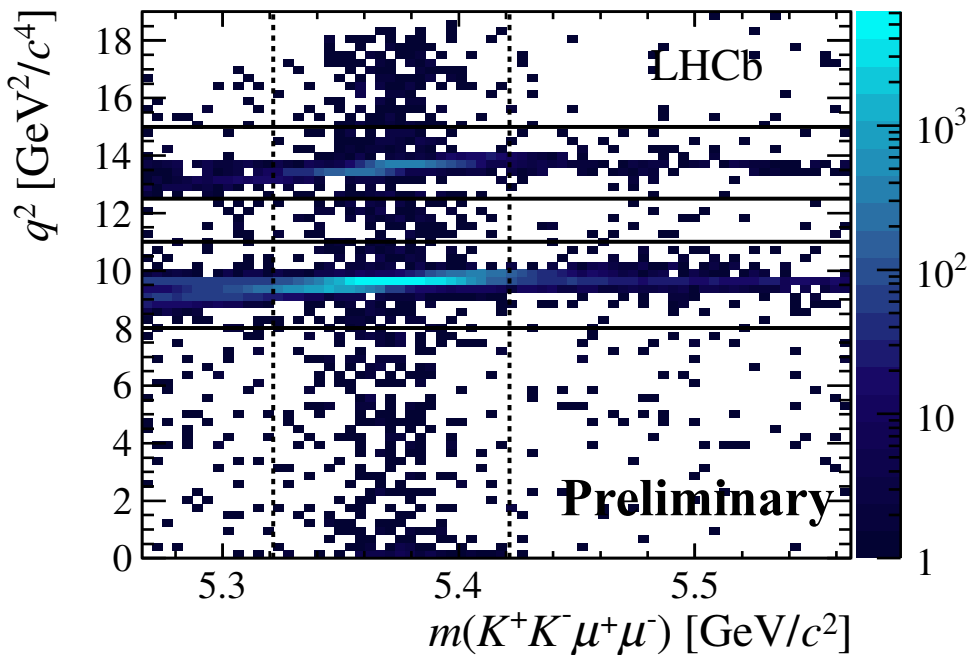
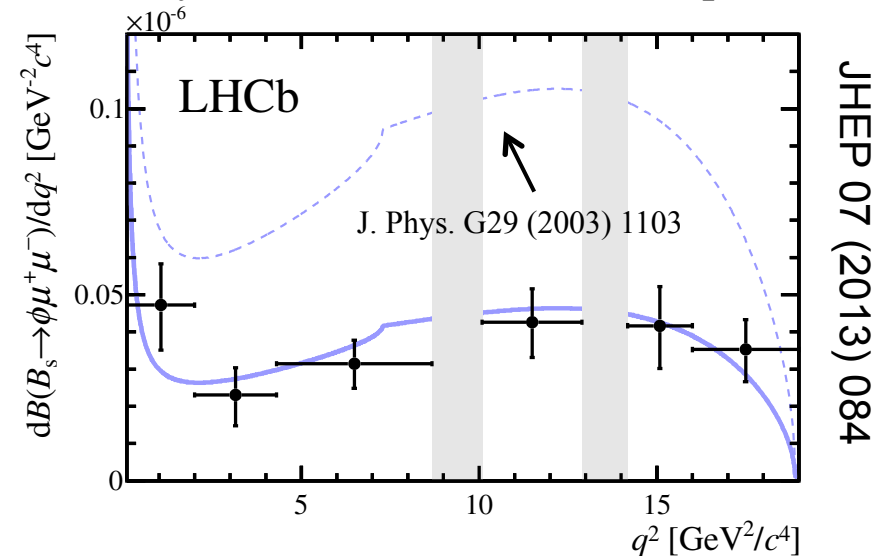
New results

Very similar to $B^0 \rightarrow K^{*0} \mu\mu$:



Today: update with full Run1 dataset (3fb⁻¹):

1fb⁻¹ analysis showed tension to SM predictions:

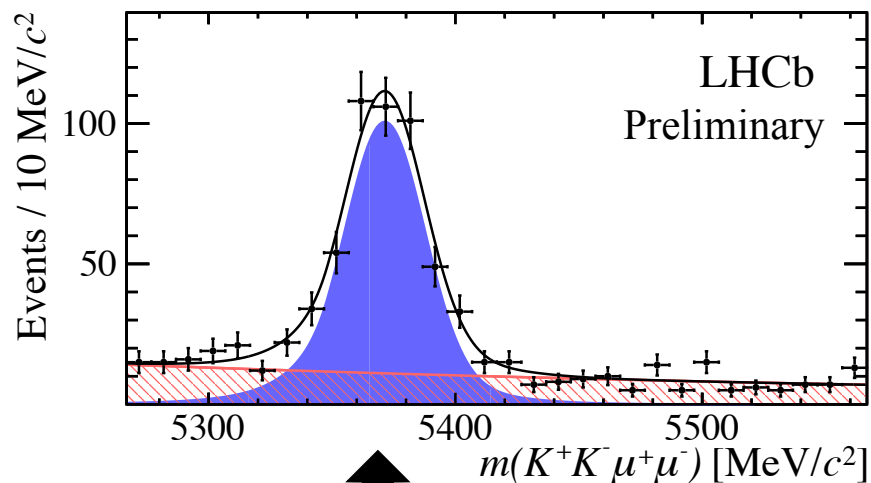


BDT to suppress combinatorial background

Veto of $B_s \rightarrow J/\Psi \phi$ and $B_s \rightarrow \Psi(2S) \phi$

Similar to $B^0 \rightarrow K^{*0} \mu\mu$ used PID to explicitly veto

- $B_s \rightarrow J/\Psi \phi$ with K – μ double misidentification
- $\Lambda_b \rightarrow \Lambda(1520) \mu\mu$ with p – K misidentification

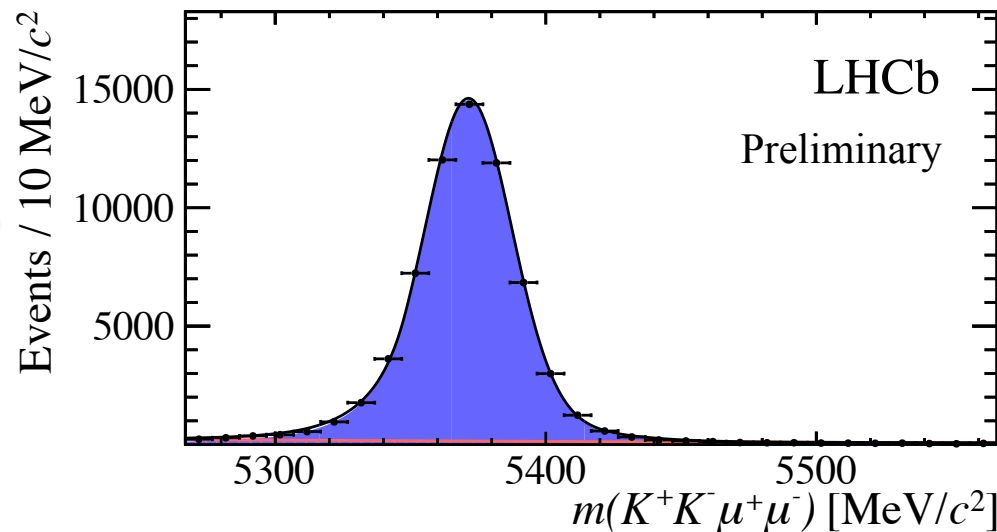
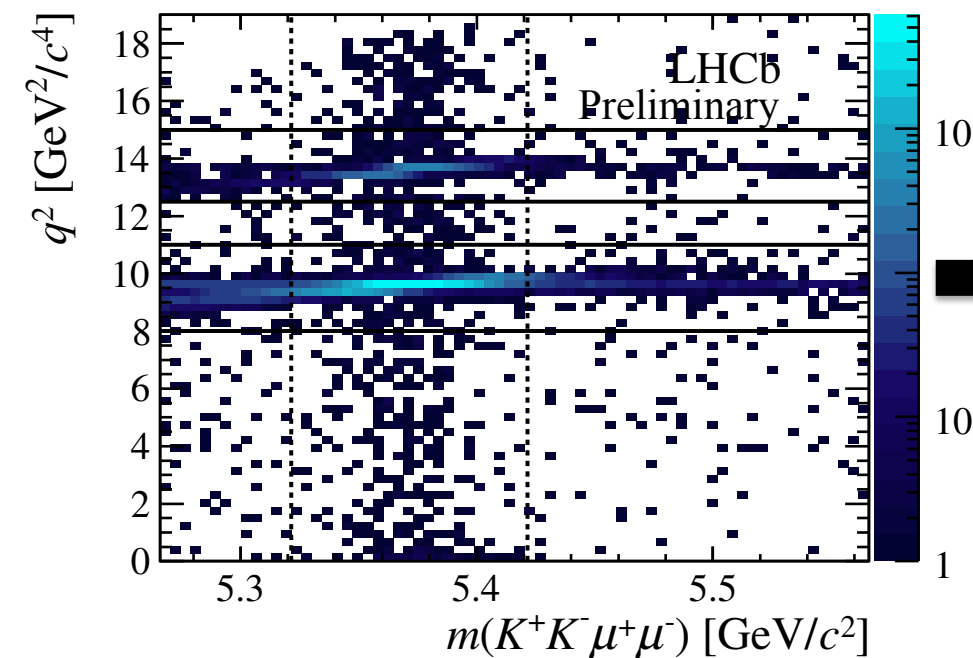


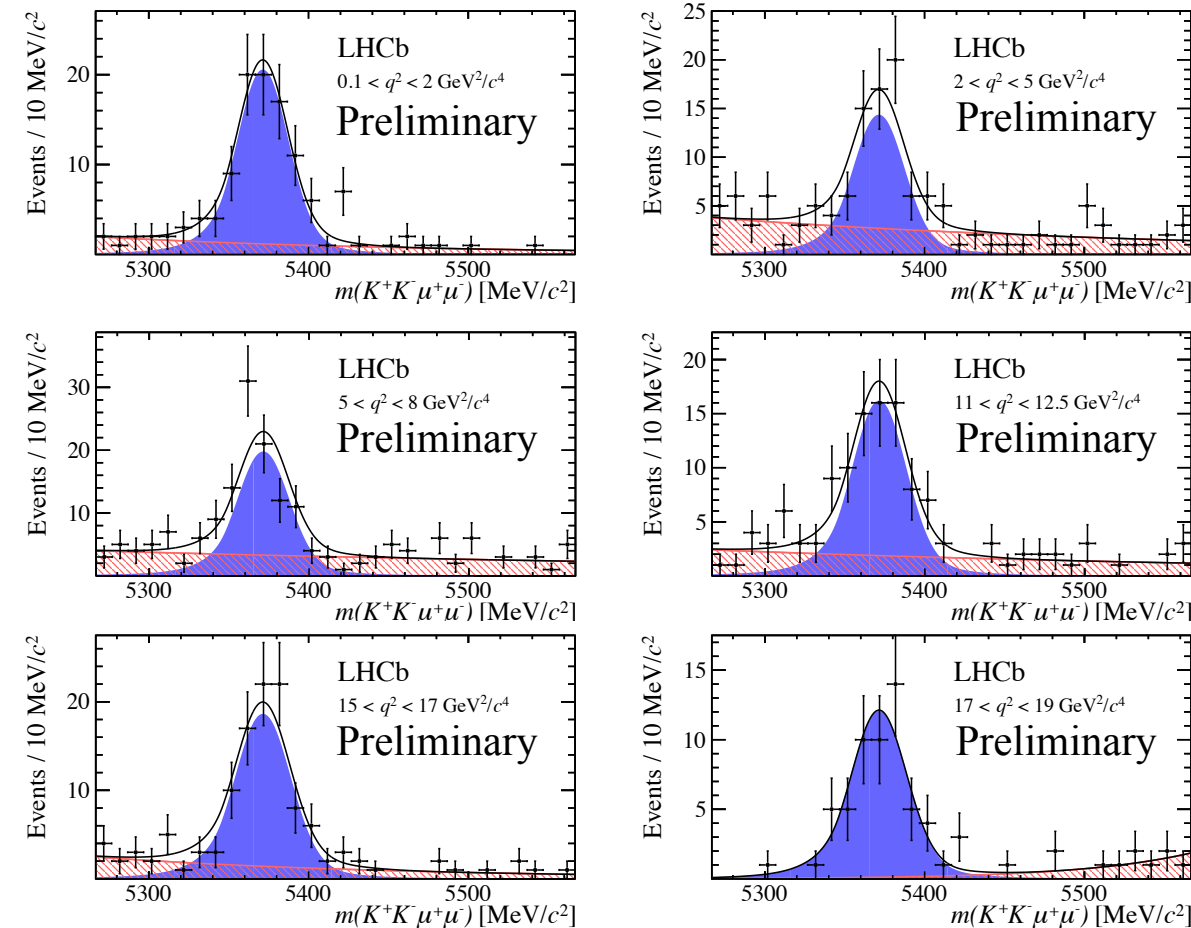
Total signal yield: $N_{\text{sig}} = 432 \pm 24$

$B_s \rightarrow J/\Psi \phi$ as normalisation channel for branching fraction measurement

Efficiencies determined from simulated signal samples

➤ corrected for differences to data





Branching fraction in bins of q^2 :

- Bins chosen such that signal yield is evenly distributed

Signal mass model:

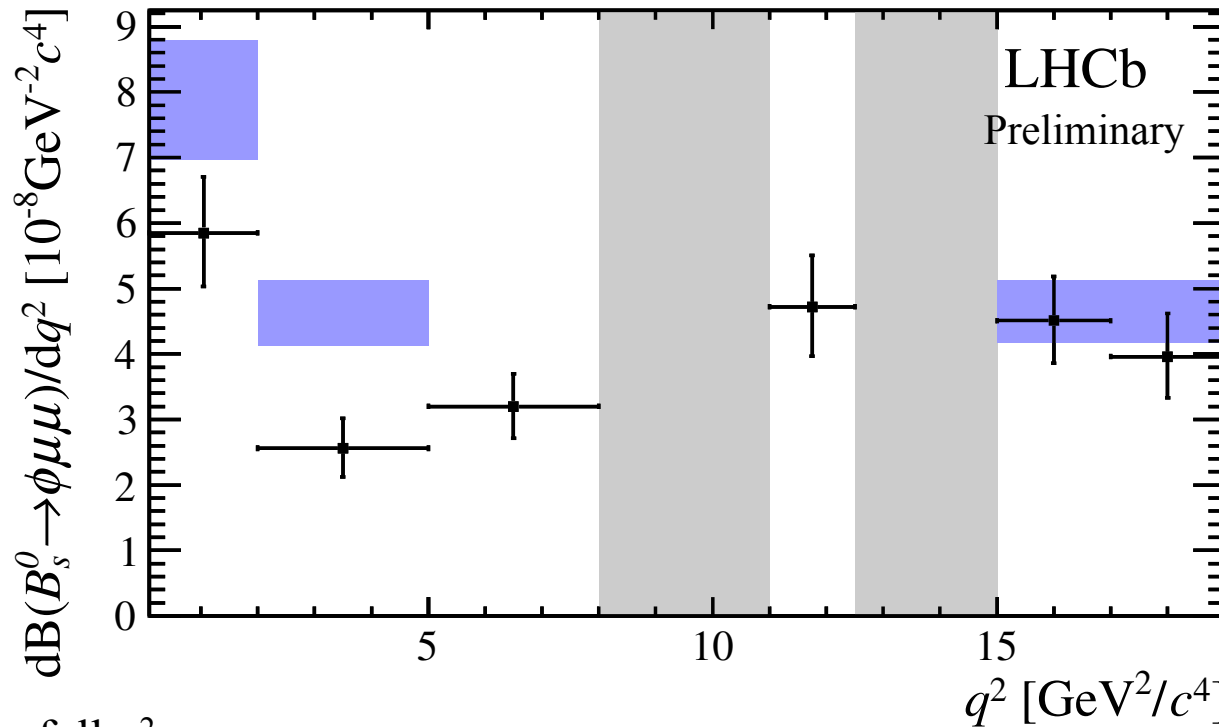
- Determined from $B_s \rightarrow J/\Psi \phi$ fit
- Allow for q^2 dependent width

Background model:

- exponential function

Systematic uncertainties:

- Dominated by the limited size of the simulated signal sample
- Angular acceptance effects estimated by varying Wilson coefficients in generation
- Mass model uncertainties estimated with pseudo-experiments



theory prediction:
arXiv:1411.3161,
arXiv:1503.05534

Extrapolation to full q^2 range:

(using WC and FF from Phys. Rev. D66 (2002) 034002, Phys. Rev. D 71 (2005) 014029)

$$\frac{\mathcal{B}(B_s^0 \rightarrow \phi \mu^+ \mu^-)}{\mathcal{B}(B_s^0 \rightarrow J/\psi \phi)} = (7.40_{-0.40}^{+0.42} \pm 0.20 \pm 0.21) \times 10^{-4},$$

$$\mathcal{B}(B_s^0 \rightarrow \phi \mu^+ \mu^-) = (7.97_{-0.43}^{+0.45} \pm 0.22 \pm 0.23 \pm 0.60) \times 10^{-7}$$

Most precise measurement to date, consistent with previous analysis
in $1 < q^2 < 6 \text{ GeV}^2$: 3.5σ tension to prediction based on SM

Angular observables extracted from 4d unbinned maximum likelihood fit:

$$\begin{aligned} \frac{1}{d\Gamma/dq^2} \frac{d^3\Gamma}{d\cos\theta_l d\cos\theta_K d\phi} = & \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ & + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l - F_L \cos^2 \theta_K \cos 2\theta_l \\ & + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi \\ & + A_5 \sin 2\theta_K \sin \theta_l \cos \phi + A_6^s \sin^2 \theta_K \cos \theta_l \\ & + S_7 \sin 2\theta_K \sin \theta_l \sin \phi + A_8 \sin 2\theta_K \sin 2\theta_l \sin \phi \\ & \left. + A_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right]. \end{aligned}$$

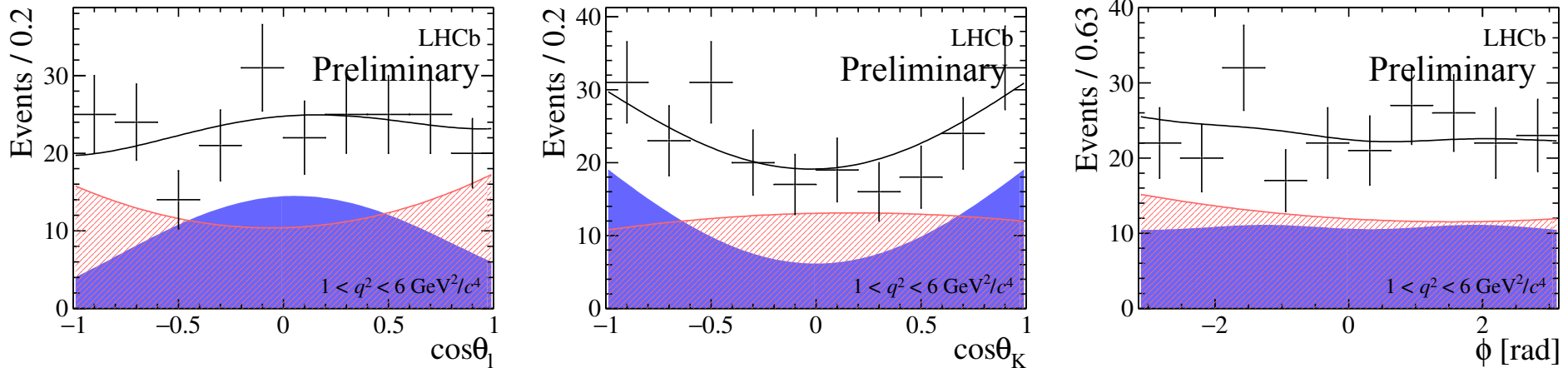
KK $\mu\mu$ is not a flavour-specific final state:
→ observables:

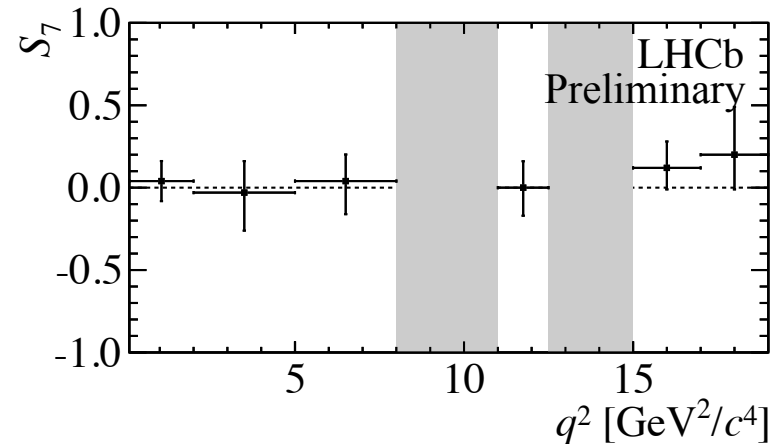
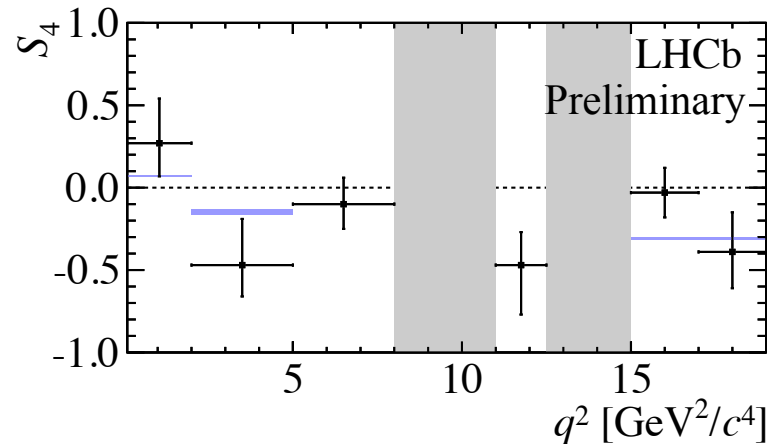
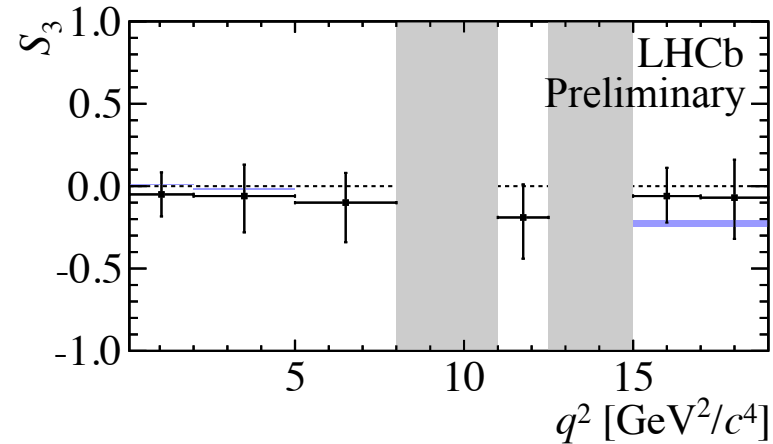
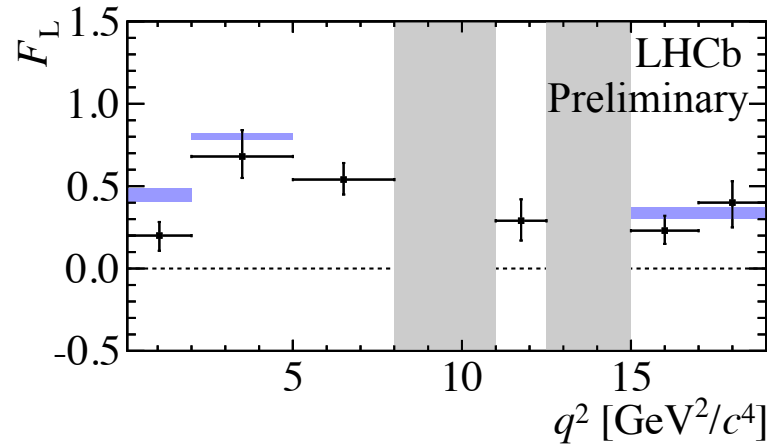
CP-averages and CP-asymmetries

angular acceptance parameterized in 4d using Legendre coefficients:

$$\epsilon(\cos\theta_l, \cos\theta_K, \phi, q^2) = \sum_{klmn} c_{klmn} P_k(\cos\theta_l) P_l(\cos\theta_K) P_m(\phi) P_n(q^2)$$

Feldman-Cousins method to ensure correct coverage with low statistics





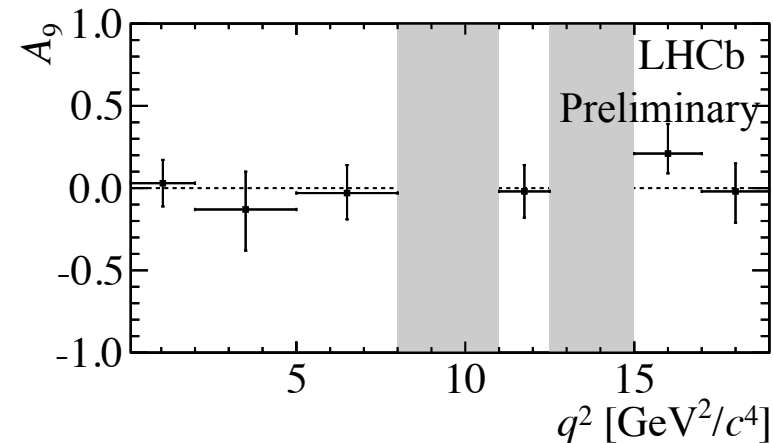
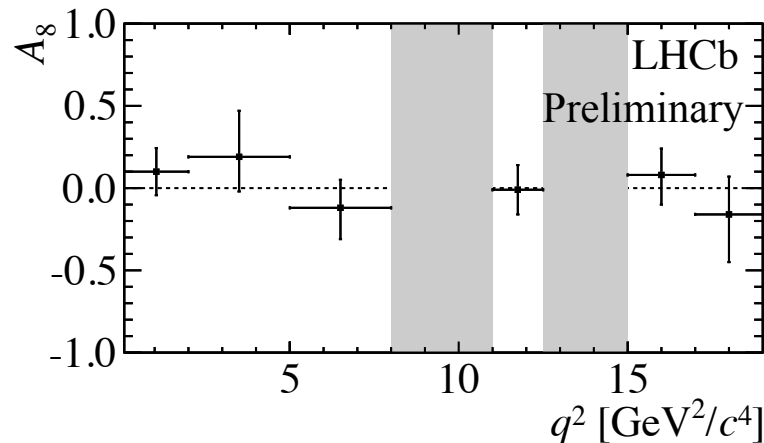
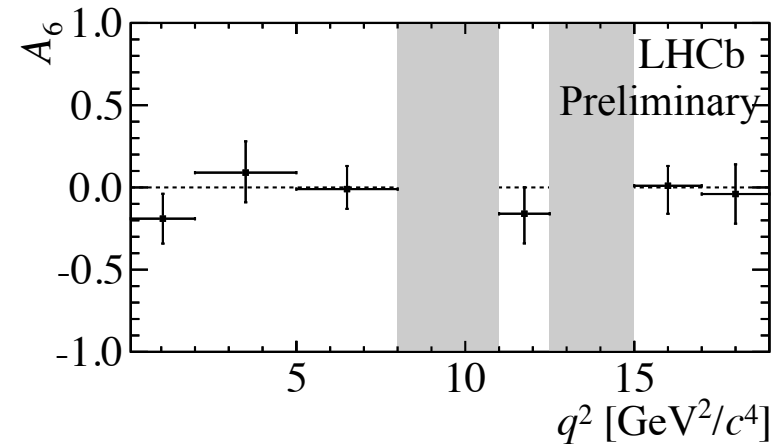
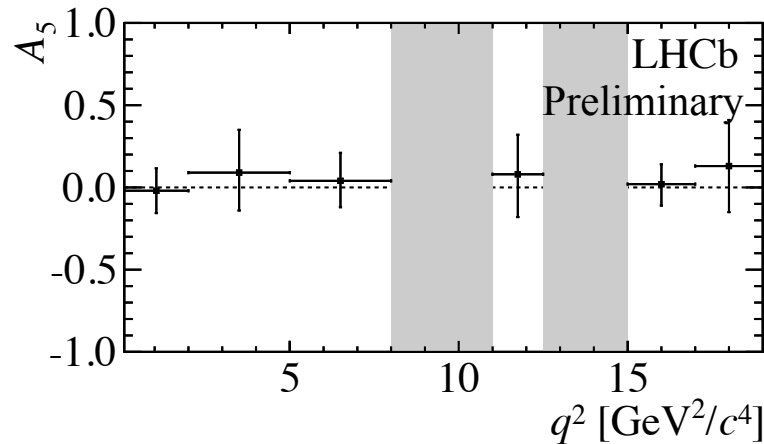
theory prediction: arXiv:1503.05534, S_7 zero in SM

Systematic uncertainties evaluated with pseudo-experiments:

- Dominated by background model choice
- Angular acceptance affected by limited statistics of simulated sample
- S-wave pollution estimated by simulating 1.1% S-wave component



In general measurement is dominated by statistical



all CP-asymmetries are zero in SM \rightarrow consistent with measurement

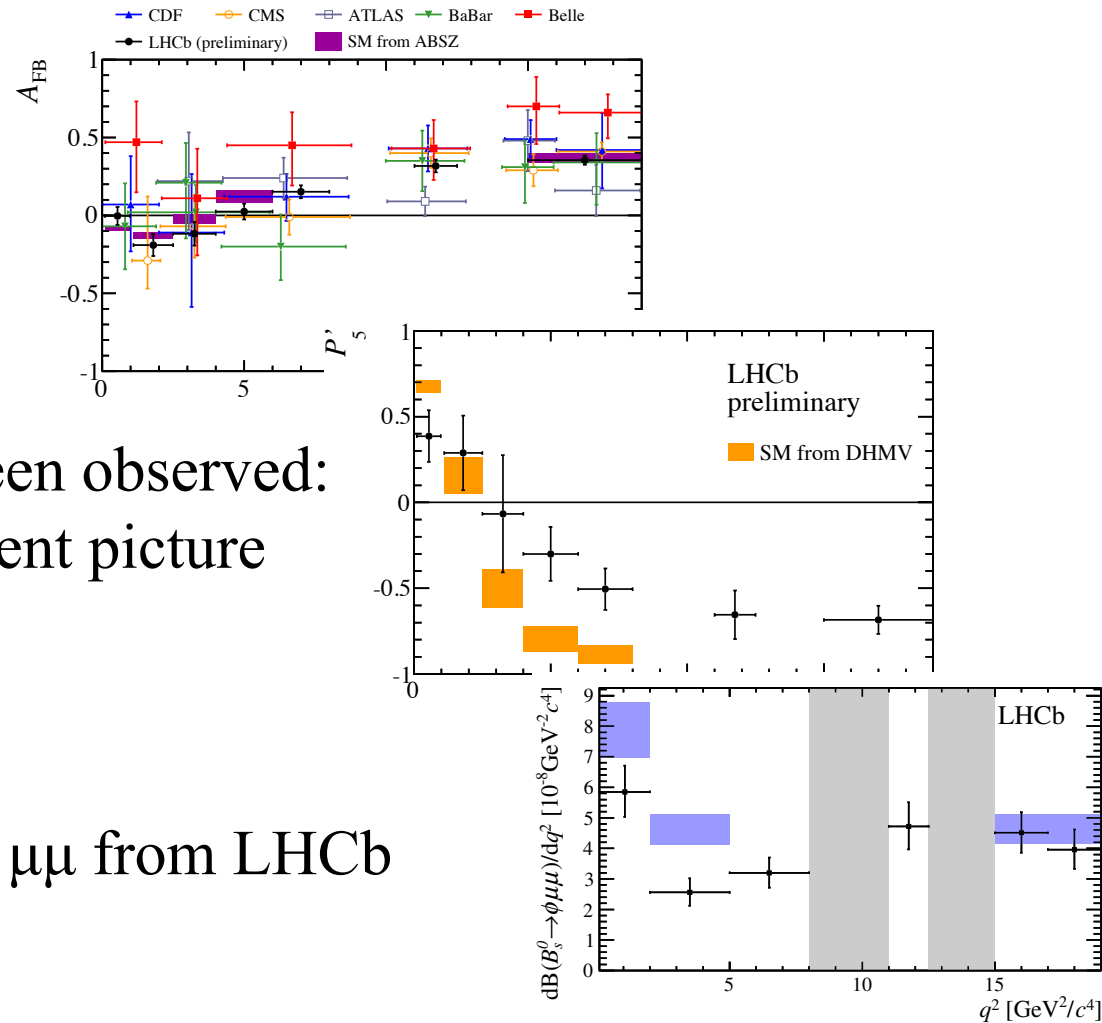
Systematic uncertainties evaluated with pseudo-experiments:

- Dominated by background model choice
- Angular acceptance affected by limited statistics of simulated sample
- S-wave pollution estimated by simulating 1.1% S-wave component

}

In general measurement is dominated by statistical

- Electroweak penguin decays are an interesting and promising probe for NP effects
- Results from many experiments, including LHCb, ATLAS, CMS
- Some tensions to the SM have been observed: global fit of WC provides consistent picture throughout all measurements
- Presented new results on $B_s \rightarrow \phi \mu\mu$ from LHCb



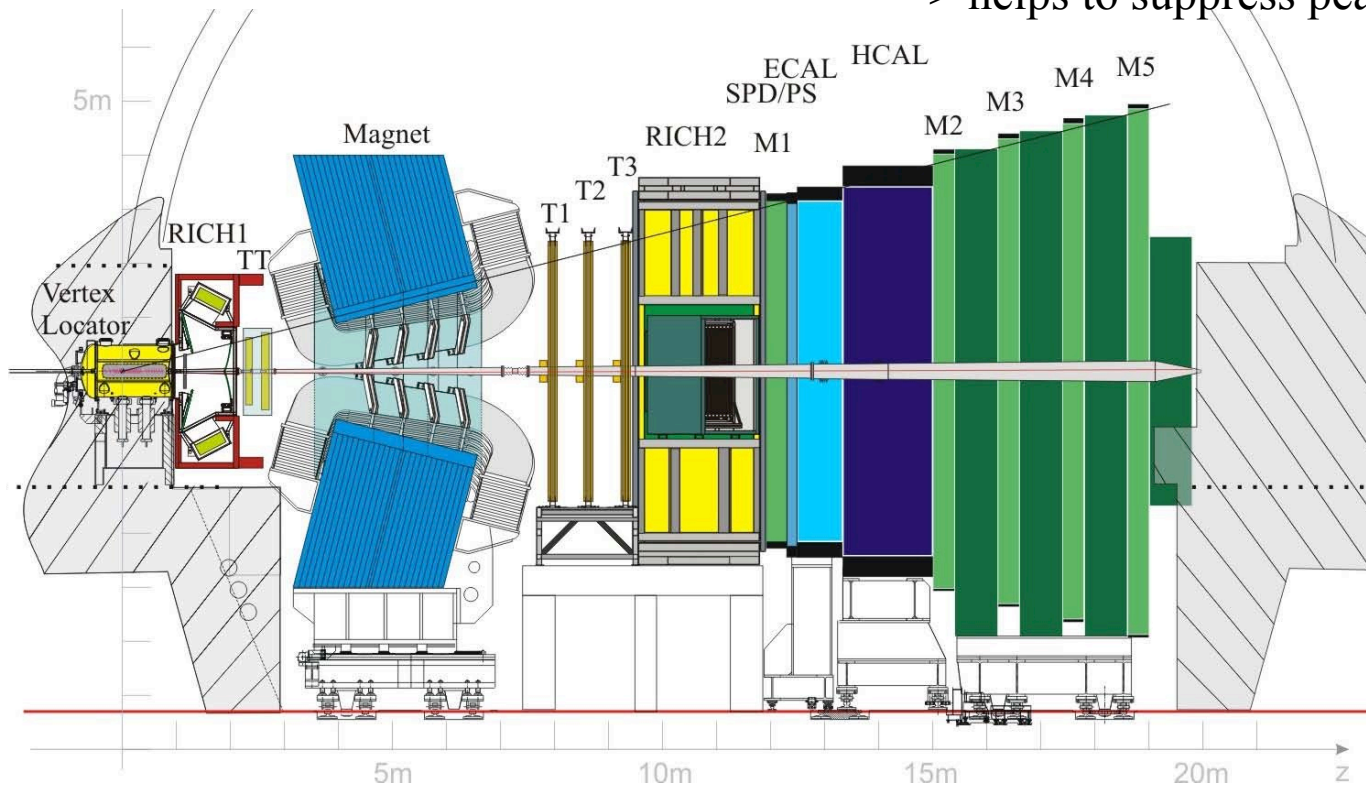
... many more interesting results in the pipeline and promising times ahead with LHC Run2

Backup

Forward spectrometer with acceptance optimized for b-hadrons: $2 < \eta < 5$

decay time resolution ~ 45 fs
 \rightarrow good separation of B vertices

excellent K - π separation
 (~ 95 % for ~ 5 % $\pi \rightarrow K$ mis-id probability)
 \rightarrow helps to suppress peaking background

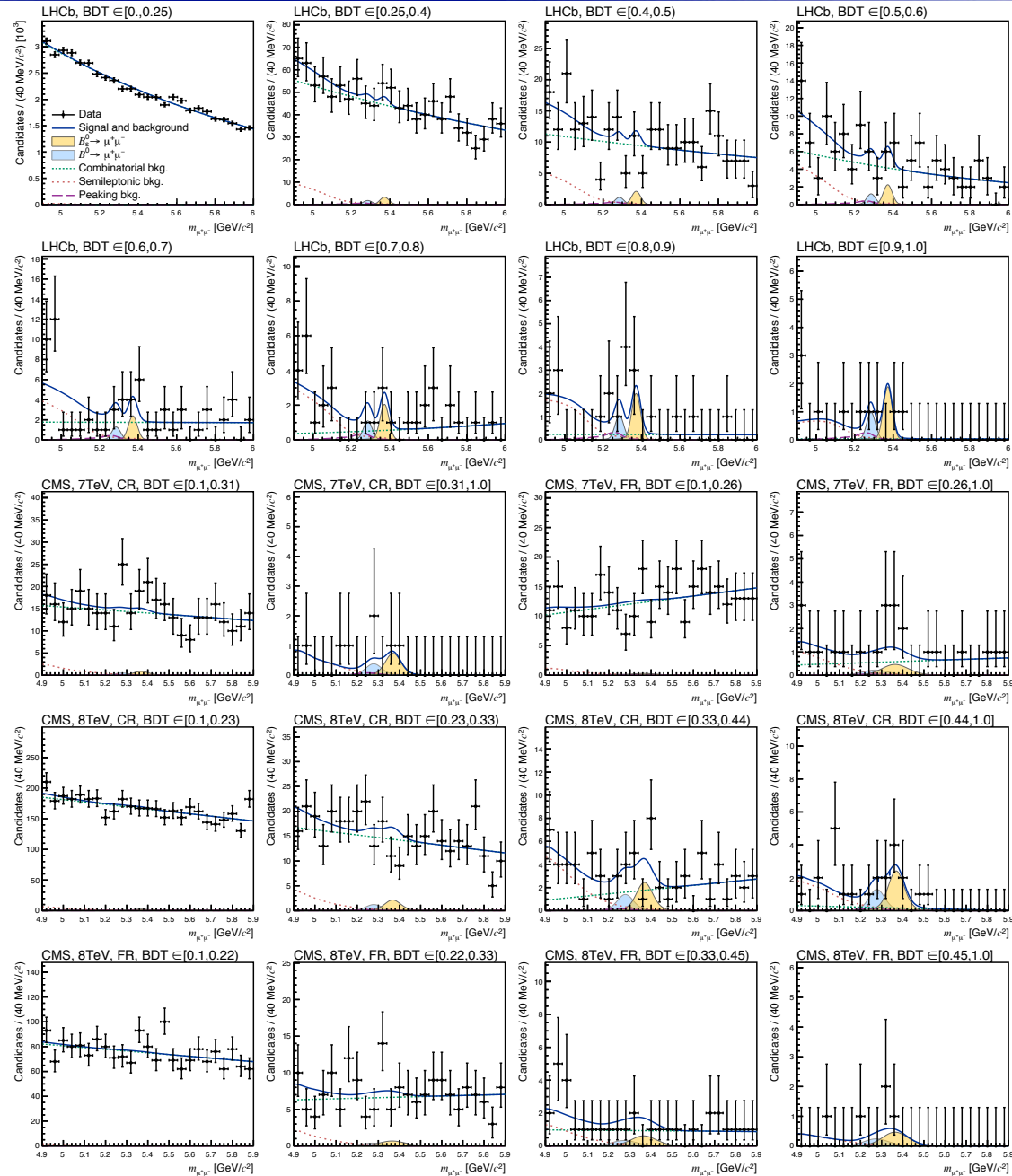


good momentum ($\Delta p / p = 0.4 - 0.6$ %)
 and mass resolution

excellent muon identification
 (~ 97 % for 1-3 % $\pi \rightarrow \mu$ mis-id probability)

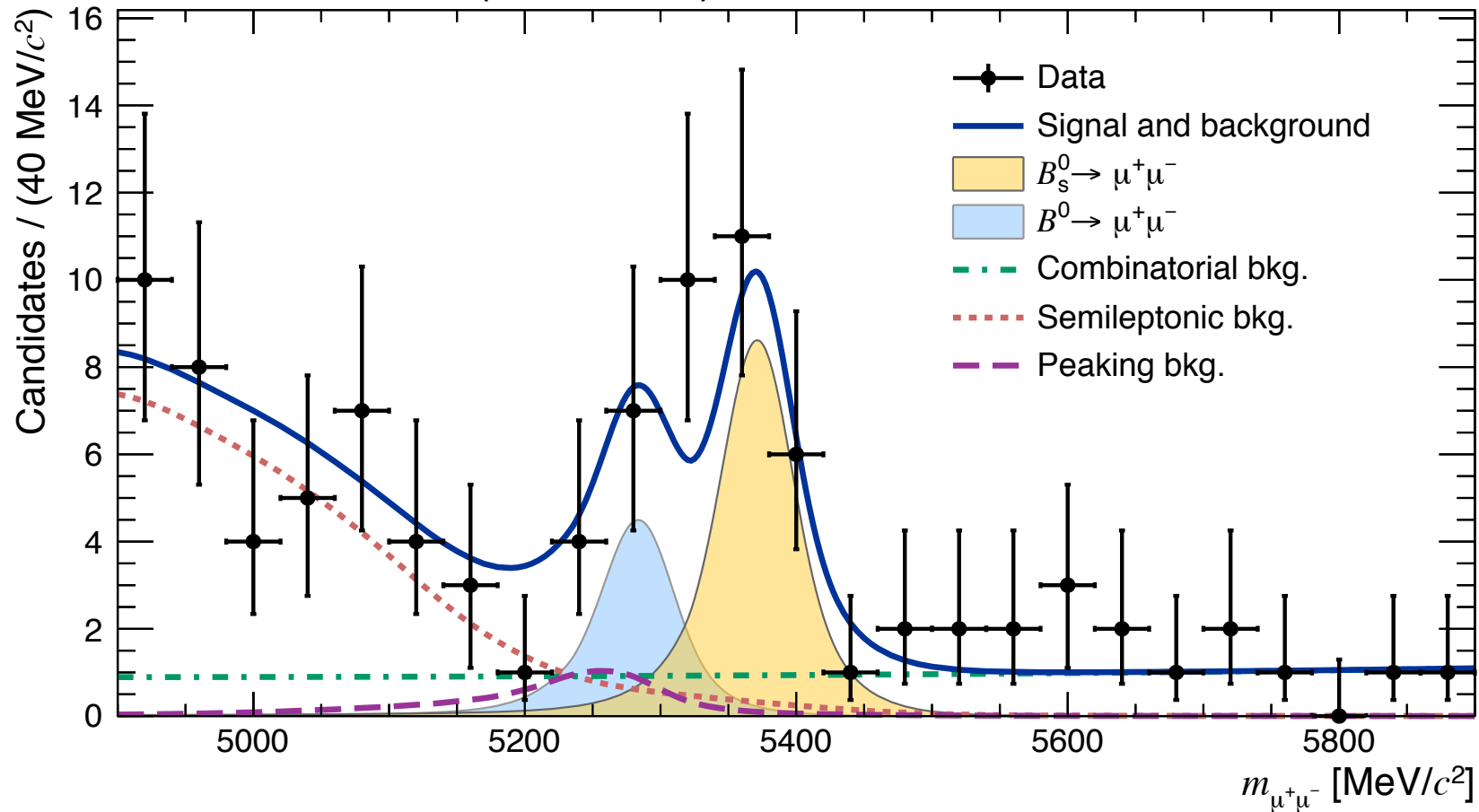
+ very efficient trigger for di-muon channels $\varepsilon \approx 90$ %

Invariant di-muon mass
in each of the 20 fit
categories:



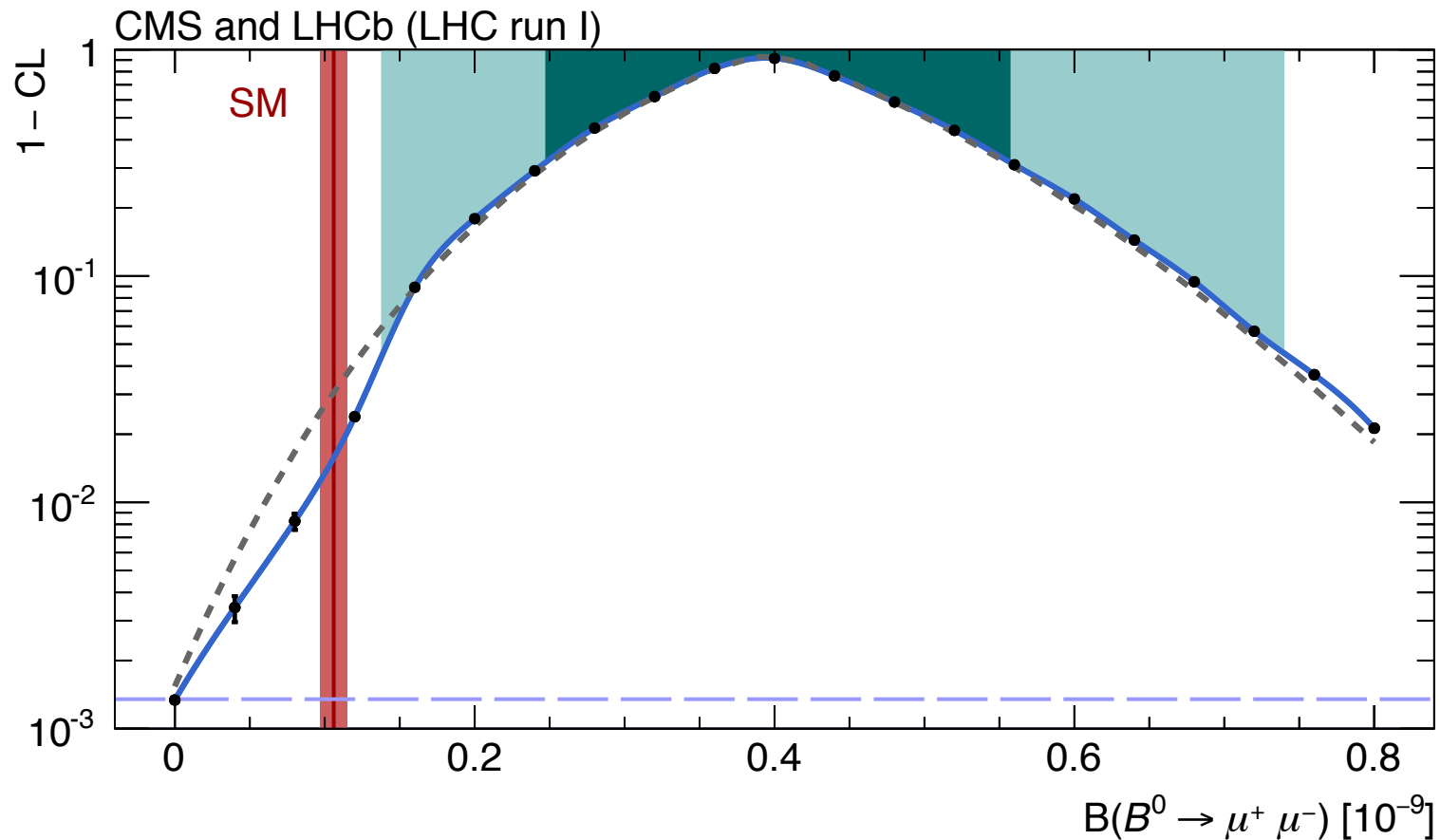
Invariant di-muon mass for the best 6 categories:

CMS and LHCb (LHC run I)

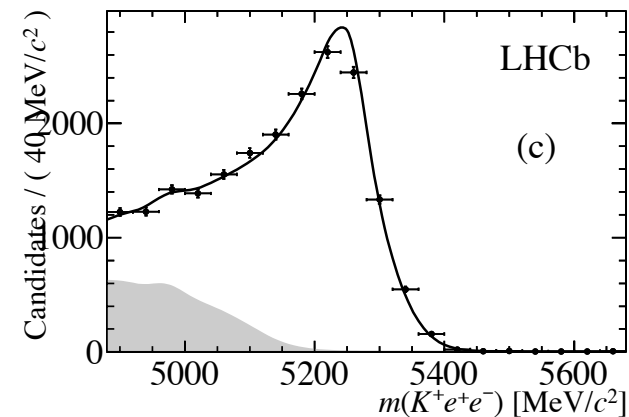
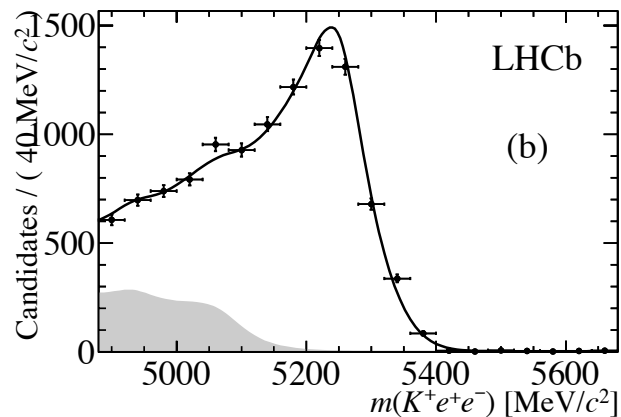
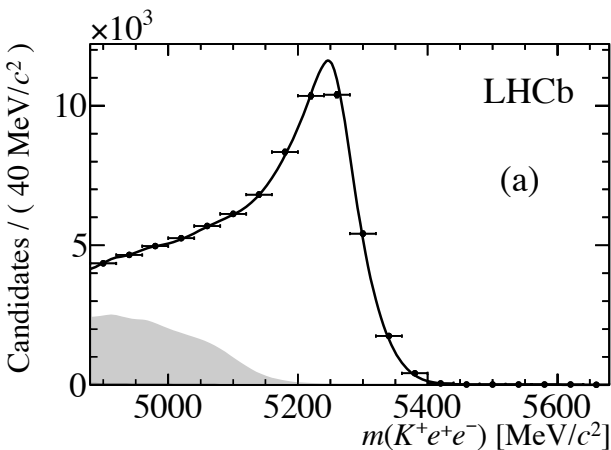


$B \rightarrow \mu^+ \mu^-$ combination

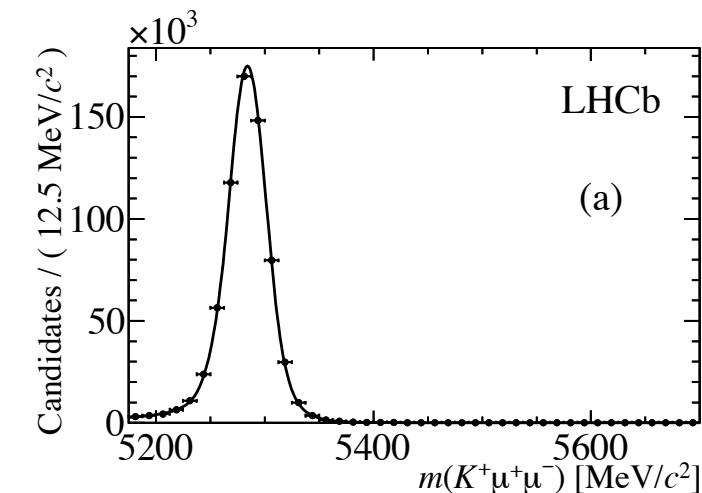
Confidence level obtained with the Feldman-Cousins method for $B^0 \rightarrow \mu\mu$:



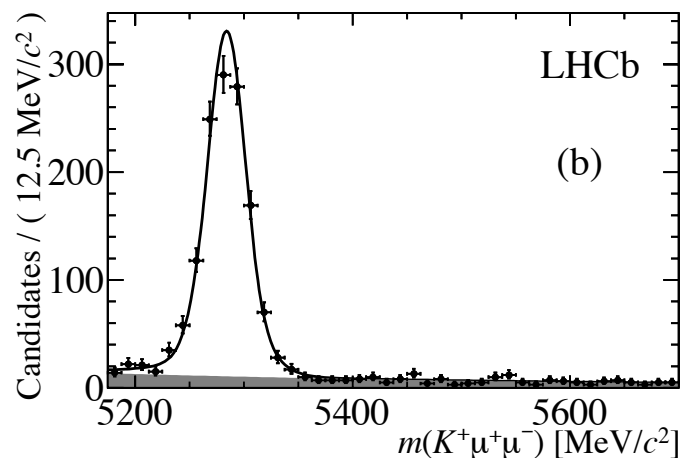
$B^+ \rightarrow J/\Psi (\rightarrow e e) K^+$ mass fits:



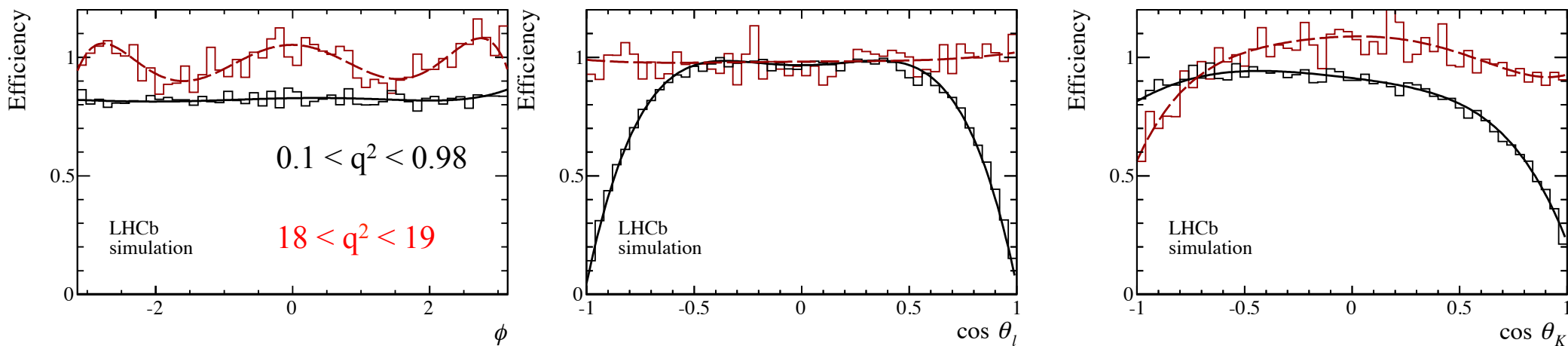
$B^+ \rightarrow J/\Psi (\rightarrow \mu \mu) K^+$:



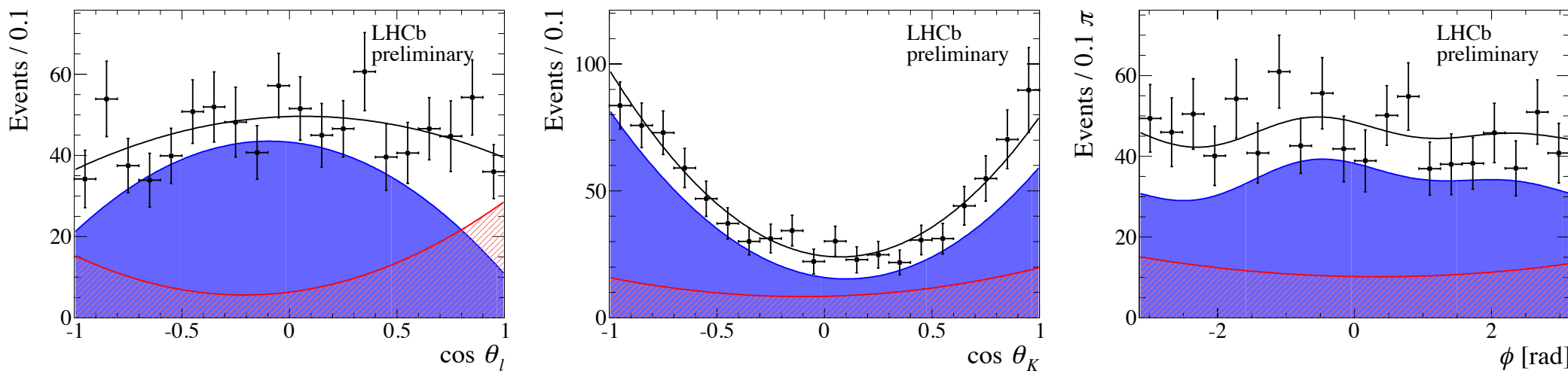
$B^+ \rightarrow K^+ \mu \mu$:



Angular efficiency determined from a principal moment analysis using simulated events:



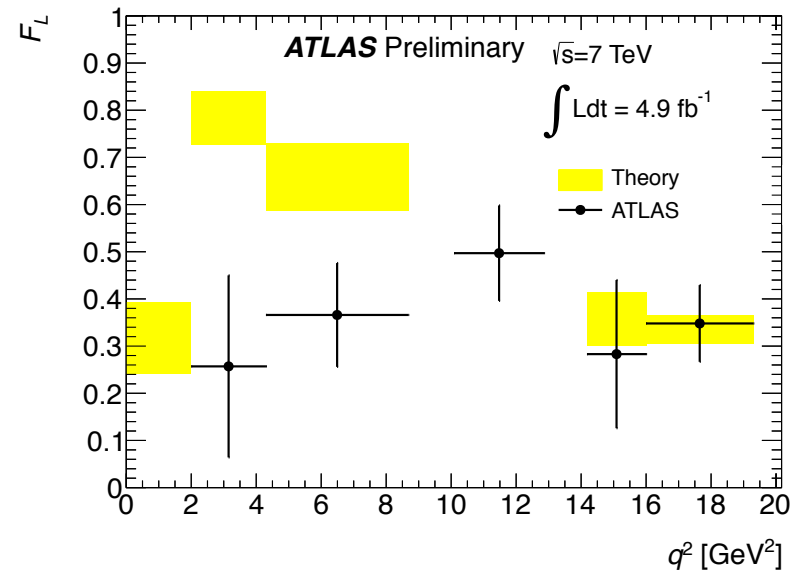
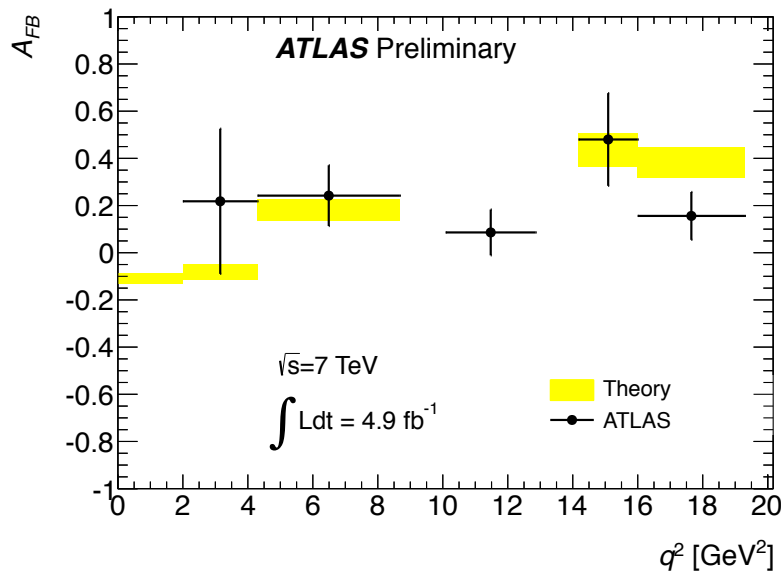
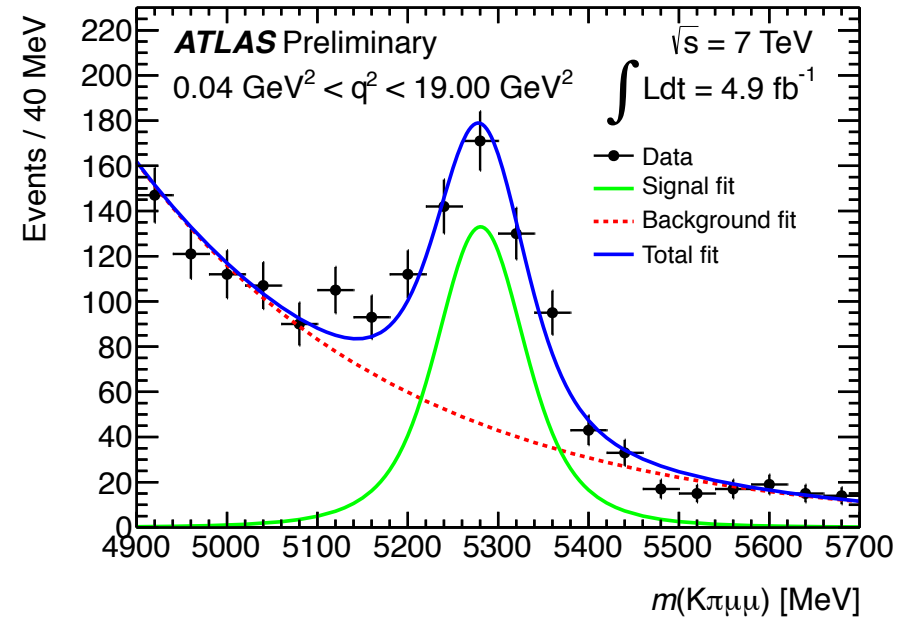
Fit projections in $1.1 < q^2 < 6.0$:

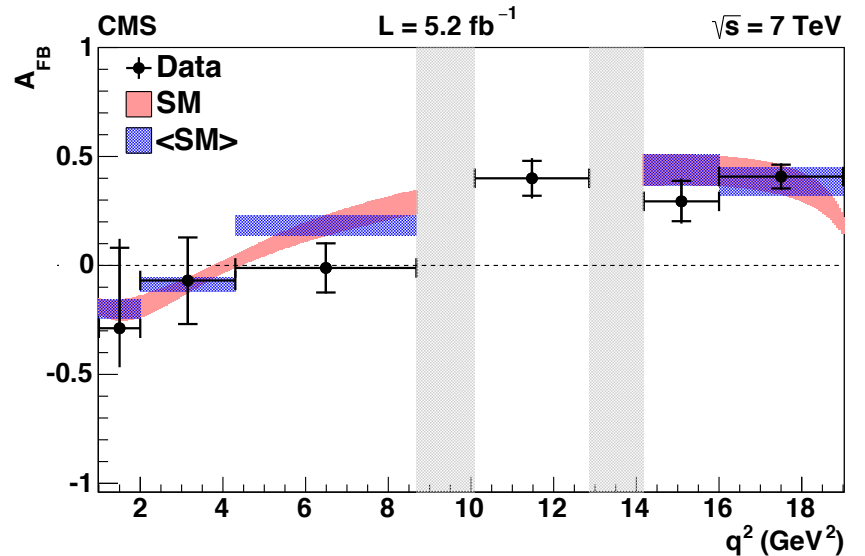
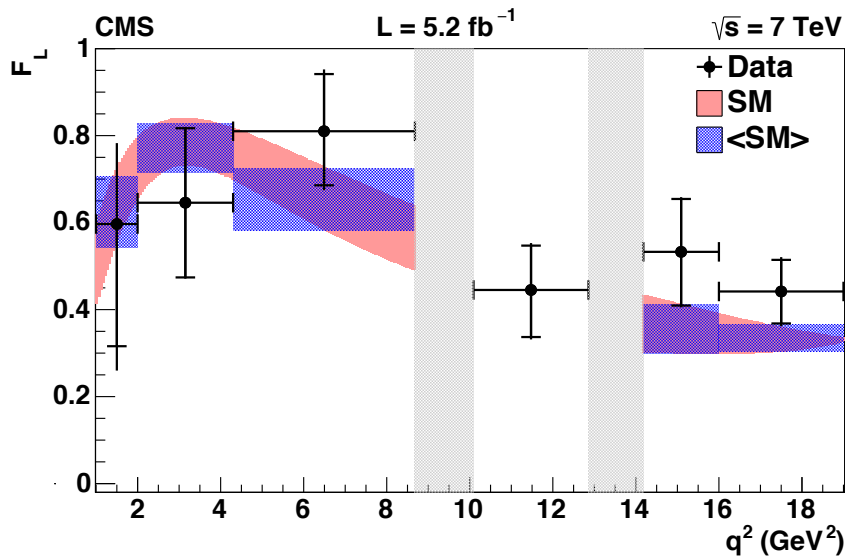
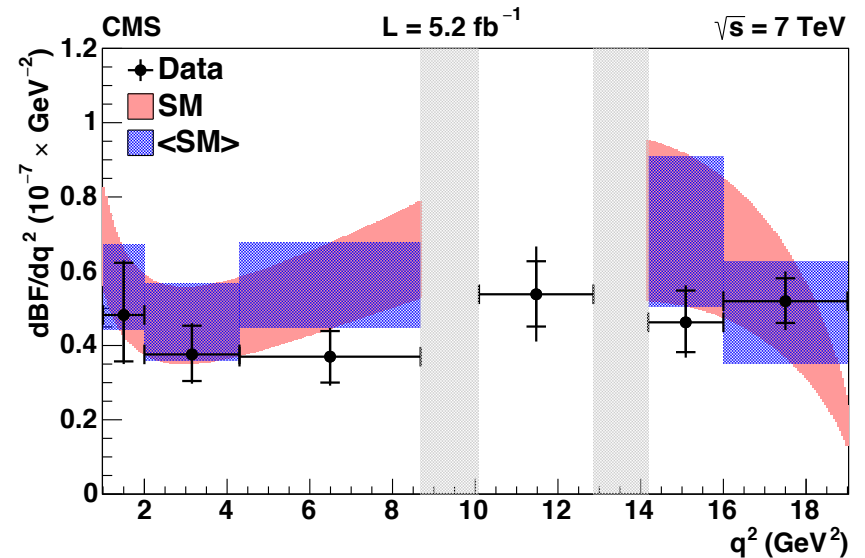
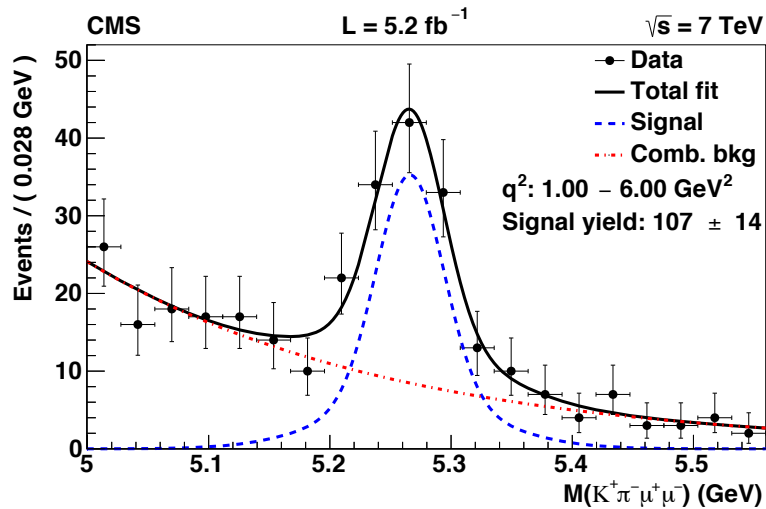


F_L and A_{FB} extracted from product of 1d decay rates:

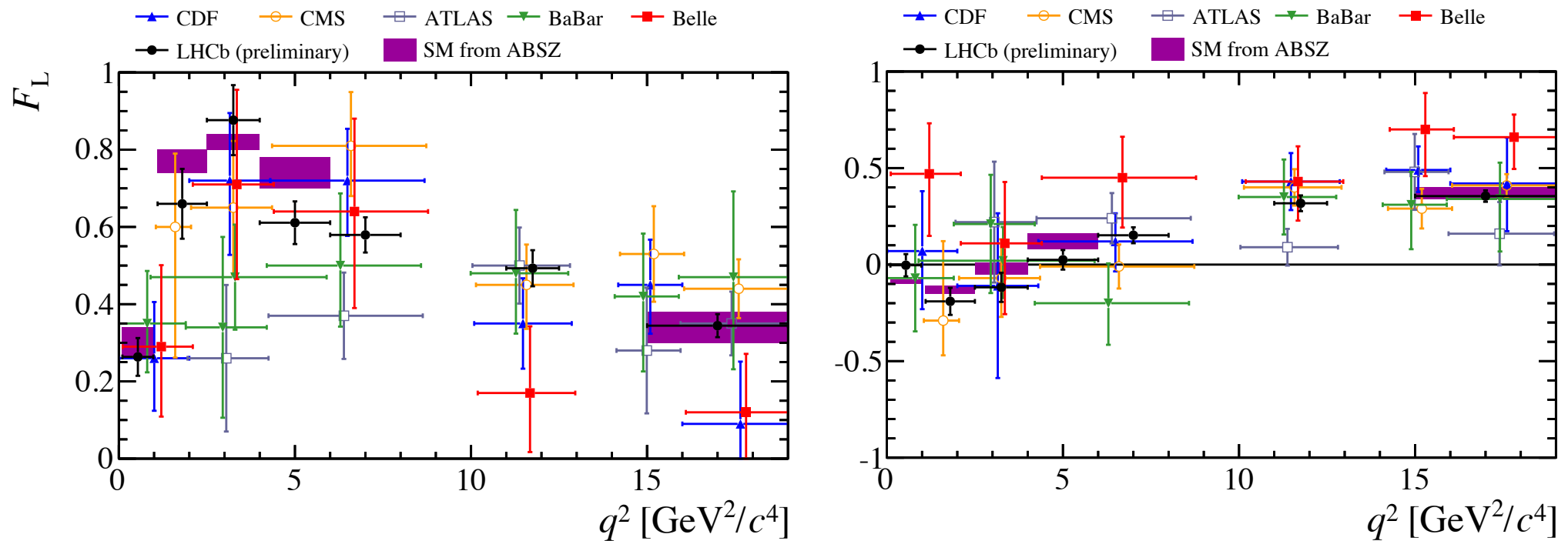
$$\frac{1}{\Gamma} \frac{d^2\Gamma}{dq^2 d\cos\theta_L} = \frac{3}{4} F_L(q^2) (1 - \cos^2\theta_L) + \frac{3}{8} (1 - F_L(q^2)) (1 + \cos^2\theta_L) + A_{FB}(q^2) \cos\theta_L$$

$$\frac{1}{\Gamma} \frac{d^2\Gamma}{dq^2 d\cos\theta_K} = \frac{3}{2} F_L(q^2) \cos^2\theta_K + \frac{3}{4} (1 - F_L(q^2)) (1 - \cos^2\theta_K)$$





Belle: Phys. Rev. Lett. 103 (2009) 171801, **Babar:** Phys. Rev. D. 73. 092001, **CDF:** Phys. Rev. Lett. 108 081807, **CMS:** Phys. Lett. B 727 (2013) 77, **ATLAS:** ATLAS-CONF-2013-038, **LHCb:** LHCb-CONF-2015-002

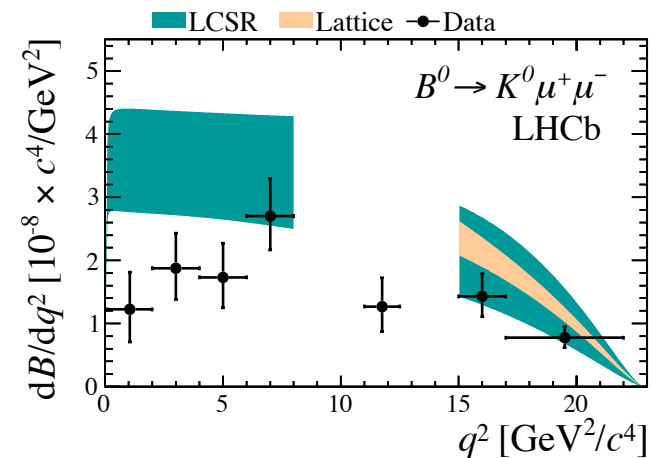
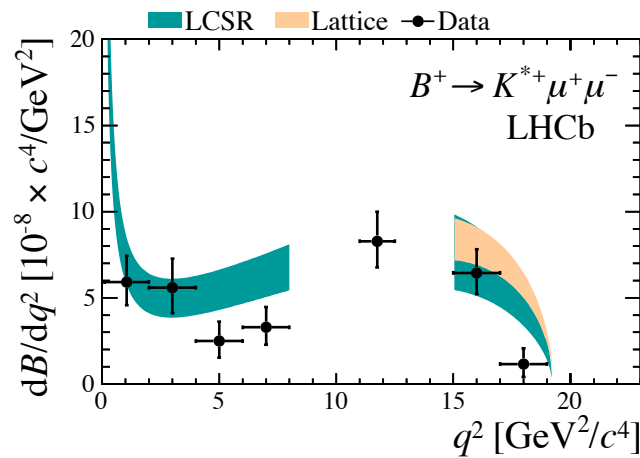
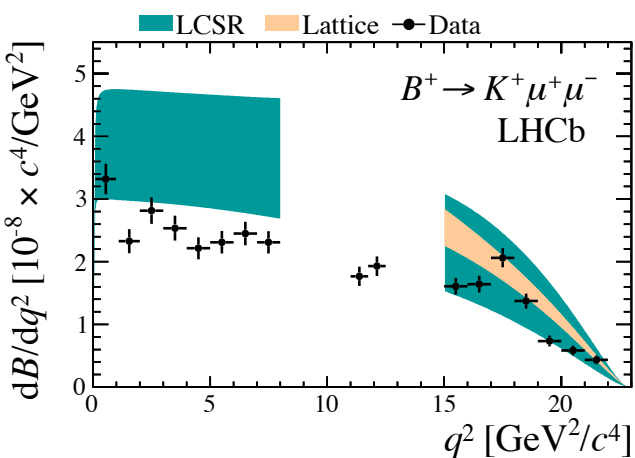


- Branching fraction measurement for $B^0 \rightarrow K^0 \mu\mu$, $B^+ \rightarrow K^+ \mu\mu$ and $B^+ \rightarrow K^{*+} \mu\mu$
($B^0 \rightarrow K^{*0} \mu\mu$ to be updated soon with detailed study of s-wave contribution)

- Full Run-2 dataset (3fb^{-1})

- normalized to resonant $B \rightarrow J/\Psi K$ channels

Decay mode	Signal yield
$B^+ \rightarrow K^+ \mu^+ \mu^-$	4746 ± 81
$B^0 \rightarrow K_s^0 \mu^+ \mu^-$	176 ± 17
$B^+ \rightarrow K^{*+} (\rightarrow K_s^0 \pi^+) \mu^+ \mu^-$	162 ± 16
$B^0 \rightarrow K^{*0} (\rightarrow K^+ \pi^-) \mu^+ \mu^-$	2361 ± 56



extrapolated to full q^2 range:

$$\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-) = (4.29 \pm 0.07(\text{stat}) \pm 0.21(\text{syst})) \cdot 10^{-7}$$

$$\mathcal{B}(B^0 \rightarrow K^0 \mu^+ \mu^-) = (3.27 \pm 0.34(\text{stat}) \pm 0.17(\text{syst})) \cdot 10^{-7}$$

$$\mathcal{B}(B^+ \rightarrow K^{*+} \mu^+ \mu^-) = (39.24 \pm 0.93(\text{stat}) \pm 0.67(\text{syst})) \cdot 10^{-7}$$

→ more precise than world average
→ consistent with predictions but favors lower values

main systematic uncertainty: $B \rightarrow J/\Psi K$ branching fraction

q^2 bin [GeV^2/c^4]	$N_{\phi\mu\mu}$	$\frac{d\mathcal{B}(B_s^0 \rightarrow \phi\mu\mu)}{\mathcal{B}(B_s^0 \rightarrow J/\psi\phi)dq^2}$ [$10^{-5} \text{ GeV}^{-2} c^4$]	$\frac{d\mathcal{B}(B_s^0 \rightarrow \phi\mu^+\mu^-)}{dq^2}$ [$10^{-8} \text{ GeV}^{-2} c^4$]
$0.1 < q^2 < 2.0$	$85.1^{+10.6}_{-10.0}$	$5.43^{+0.68}_{-0.64} \pm 0.13$	$5.85^{+0.73}_{-0.69} \pm 0.14 \pm 0.44$
$2.0 < q^2 < 5.0$	$59.5^{+9.8}_{-9.2}$	$2.38^{+0.39}_{-0.37} \pm 0.06$	$2.56^{+0.42}_{-0.39} \pm 0.06 \pm 0.19$
$5.0 < q^2 < 8.0$	$82.6^{+11.5}_{-10.9}$	$2.98^{+0.41}_{-0.39} \pm 0.07$	$3.20^{+0.44}_{-0.42} \pm 0.08 \pm 0.24$
$11.0 < q^2 < 12.5$	$70.5^{+10.4}_{-9.8}$	$4.38^{+0.64}_{-0.61} \pm 0.14$	$4.72^{+0.69}_{-0.65} \pm 0.15 \pm 0.36$
$15.0 < q^2 < 17.0$	$83.0^{+10.4}_{-9.9}$	$4.19^{+0.53}_{-0.50} \pm 0.11$	$4.51^{+0.57}_{-0.54} \pm 0.12 \pm 0.34$
$17.0 < q^2 < 19.0$	$54.2^{+7.8}_{-7.4}$	$3.68^{+0.53}_{-0.50} \pm 0.13$	$3.96^{+0.57}_{-0.54} \pm 0.14 \pm 0.30$
$1.0 < q^2 < 6.0$	$100.9^{+12.8}_{-12.2}$	$2.40^{+0.30}_{-0.29} \pm 0.07$	$2.58^{+0.33}_{-0.31} \pm 0.08 \pm 0.19$
$15.0 < q^2 < 19.0$	$135.4^{+13.2}_{-12.7}$	$3.75^{+0.37}_{-0.35} \pm 0.12$	$4.04^{+0.39}_{-0.38} \pm 0.13 \pm 0.30$

Systematic	Uncertainty [$10^{-5} \text{ GeV}^{-2} c^4$]							
	[0.1, 2]	[2, 5]	[5, 8]	[11, 12.5]	[15, 17]	[17, 19]	[1, 6]	[15, 17]
Peaking bkg.	0.03	0.02	0.02	0.10	0.02	0.01	0.02	0.01
Simulation corr.	0.01	0.01	0.01	0.01	0.05	0.04	0.00	0.04
Angular model	0.04	0.00	0.01	0.00	0.01	0.06	0.00	0.01
Efficiency ratio	0.06	0.03	0.03	0.06	0.06	0.07	0.02	0.04
$\mathcal{B} (J/\psi \rightarrow \mu^+ \mu^-)$	0.03	0.01	0.02	0.02	0.02	0.02	0.01	0.02
Signal mass model	0.02	0.01	0.03	0.03	0.03	0.00	0.05	0.05
Bkg. mass model	0.02	0.02	0.02	0.02	0.03	0.05	0.01	0.06
Quadratic sum	0.09	0.04	0.06	0.12	0.09	0.11	0.06	0.10

Efficiency related uncertainties:

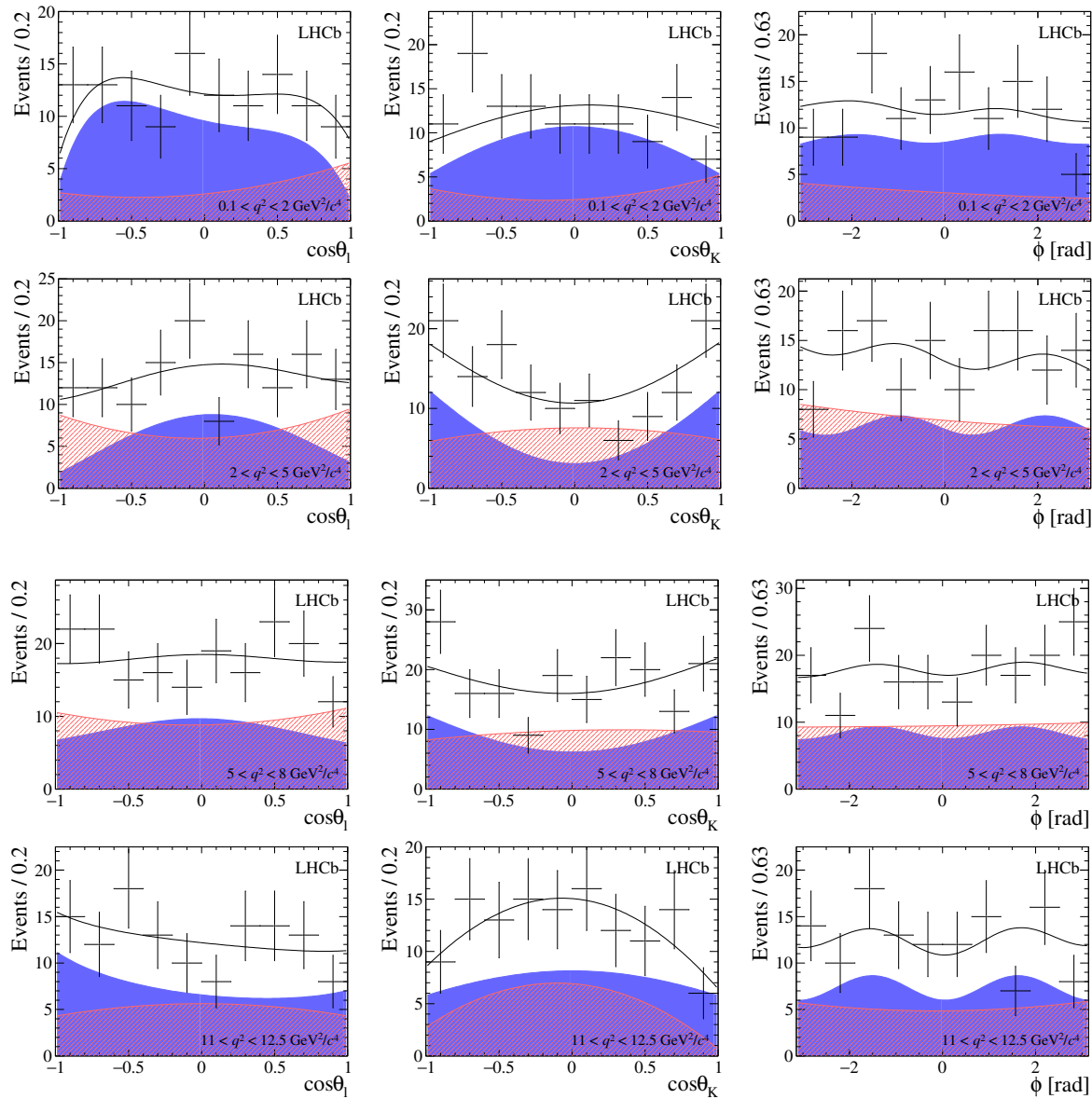
- Dominated by the limited size of the simulated signal sample
- Angular acceptance effects estimated by varying Wilson coefficients in generation
- Effect of corrections of simulated sample in general small

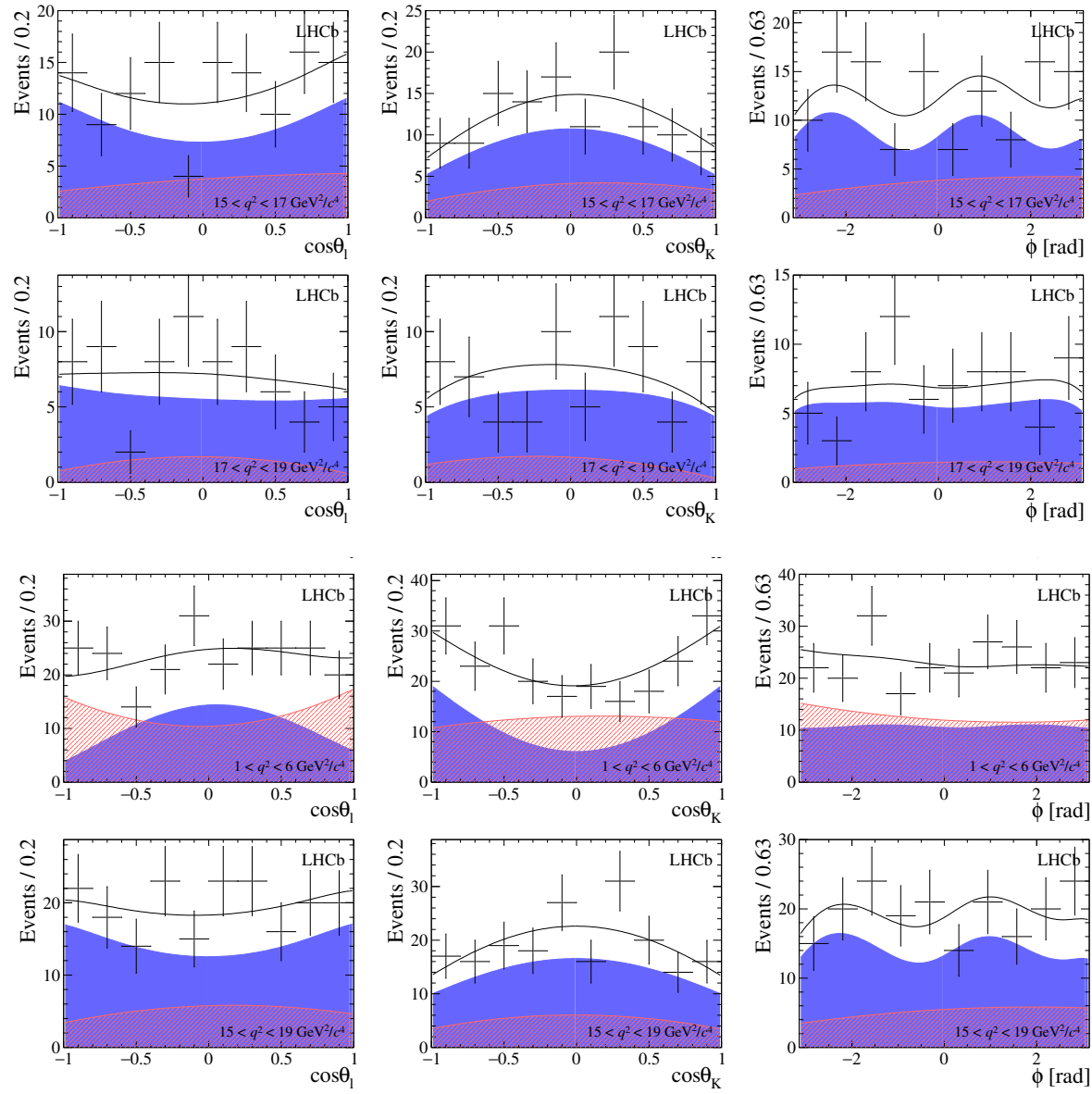
Mass model uncertainties:

- Estimated with pseudo-experiments

Dominant uncertainty for total branching fraction:

- Branching fraction of $B_s \rightarrow J/\Psi \phi$ normalization channel: 7.5%





Systematic uncertainties evaluated with pseudo-experiments:

Mostly related to angular acceptance:

- Data-driven corrections of simulated signal sample: < 0.01
- Limited statistics of simulated sample: < 0.02

Remaining peaking background:

- Estimated by injecting simulated $\Lambda_b \rightarrow \Lambda(1520) \mu\mu$ and $B \rightarrow K^* \mu\mu$ events: < 0.01

S-wave pollution:

- Expected to be similar to $B_s \rightarrow J/\Psi \phi$, estimated by simulating a 1.1% S-wave: < 0.01

Background parameterization:

- Dominant uncertainty from model choice: < 0.04

q^2 bin [GeV ² /c ⁴]	F_L	S_3	S_4	S_7
$0.1 < q^2 < 2.0$	$0.20^{+0.08}_{-0.09} \pm 0.02$	$-0.05^{+0.13}_{-0.13} \pm 0.01$	$0.27^{+0.28}_{-0.18} \pm 0.01$	$0.04^{+0.12}_{-0.12} \pm 0.00$
$2.0 < q^2 < 5.0$	$0.68^{+0.16}_{-0.13} \pm 0.03$	$-0.06^{+0.19}_{-0.23} \pm 0.01$	$-0.47^{+0.30}_{-0.44} \pm 0.01$	$-0.03^{+0.18}_{-0.23} \pm 0.01$
$5.0 < q^2 < 8.0$	$0.54^{+0.10}_{-0.09} \pm 0.02$	$-0.10^{+0.20}_{-0.29} \pm 0.01$	$-0.10^{+0.15}_{-0.18} \pm 0.01$	$0.04^{+0.16}_{-0.20} \pm 0.01$
$11.0 < q^2 < 12.5$	$0.29^{+0.11}_{-0.11} \pm 0.04$	$-0.19^{+0.20}_{-0.23} \pm 0.01$	$-0.47^{+0.21}_{-0.29} \pm 0.01$	$0.00^{+0.15}_{-0.17} \pm 0.01$
$15.0 < q^2 < 17.0$	$0.23^{+0.09}_{-0.08} \pm 0.02$	$-0.06^{+0.16}_{-0.19} \pm 0.01$	$-0.03^{+0.15}_{-0.15} \pm 0.01$	$0.12^{+0.16}_{-0.13} \pm 0.01$
$17.0 < q^2 < 19.0$	$0.40^{+0.13}_{-0.15} \pm 0.02$	$-0.07^{+0.23}_{-0.27} \pm 0.02$	$-0.39^{+0.25}_{-0.34} \pm 0.02$	$0.20^{+0.29}_{-0.22} \pm 0.01$
$1.0 < q^2 < 6.0$	$0.63^{+0.09}_{-0.09} \pm 0.03$	$-0.02^{+0.12}_{-0.13} \pm 0.01$	$-0.19^{+0.14}_{-0.13} \pm 0.01$	$-0.03^{+0.14}_{-0.14} \pm 0.00$
$15.0 < q^2 < 19.0$	$0.29^{+0.07}_{-0.06} \pm 0.02$	$-0.09^{+0.11}_{-0.12} \pm 0.01$	$-0.14^{+0.11}_{-0.11} \pm 0.01$	$0.13^{+0.11}_{-0.11} \pm 0.01$

q^2 bin [GeV ² /c ⁴]	A_5	A_6	A_8	A_9
$0.1 < q^2 < 2.0$	$-0.02^{+0.13}_{-0.13} \pm 0.00$	$-0.19^{+0.15}_{-0.15} \pm 0.01$	$0.10^{+0.14}_{-0.14} \pm 0.00$	$0.03^{+0.14}_{-0.14} \pm 0.01$
$2.0 < q^2 < 5.0$	$0.09^{+0.28}_{-0.22} \pm 0.01$	$0.09^{+0.20}_{-0.19} \pm 0.02$	$0.19^{+0.26}_{-0.21} \pm 0.01$	$-0.13^{+0.24}_{-0.30} \pm 0.01$
$5.0 < q^2 < 8.0$	$0.04^{+0.17}_{-0.17} \pm 0.01$	$-0.01^{+0.14}_{-0.12} \pm 0.01$	$-0.12^{+0.17}_{-0.19} \pm 0.01$	$-0.03^{+0.17}_{-0.16} \pm 0.01$
$11.0 < q^2 < 12.5$	$0.08^{+0.21}_{-0.21} \pm 0.01$	$-0.16^{+0.16}_{-0.18} \pm 0.01$	$-0.01^{+0.15}_{-0.15} \pm 0.01$	$-0.02^{+0.16}_{-0.15} \pm 0.01$
$15.0 < q^2 < 17.0$	$0.02^{+0.13}_{-0.14} \pm 0.01$	$0.01^{+0.12}_{-0.17} \pm 0.01$	$0.08^{+0.16}_{-0.18} \pm 0.01$	$0.21^{+0.18}_{-0.12} \pm 0.01$
$17.0 < q^2 < 19.0$	$0.13^{+0.29}_{-0.27} \pm 0.01$	$-0.04^{+0.18}_{-0.19} \pm 0.01$	$-0.16^{+0.24}_{-0.29} \pm 0.01$	$-0.02^{+0.19}_{-0.19} \pm 0.01$
$1.0 < q^2 < 6.0$	$0.20^{+0.13}_{-0.13} \pm 0.00$	$0.08^{+0.12}_{-0.11} \pm 0.01$	$-0.00^{+0.15}_{-0.17} \pm 0.00$	$-0.01^{+0.13}_{-0.13} \pm 0.01$
$15.0 < q^2 < 19.0$	$0.11^{+0.10}_{-0.10} \pm 0.00$	$0.00^{+0.10}_{-0.11} \pm 0.01$	$0.03^{+0.12}_{-0.12} \pm 0.00$	$0.12^{+0.11}_{-0.09} \pm 0.00$