



Belle status and Belle II prospect for $B \rightarrow D^{(*)} \tau \nu$ and related topics

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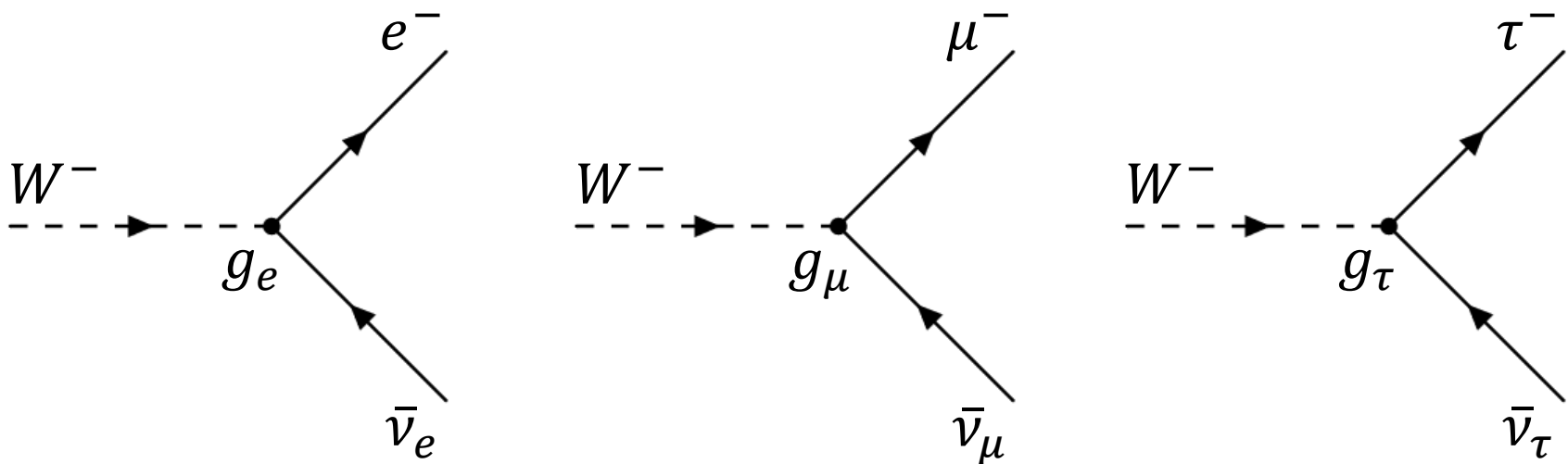


Nov. 15, 2018

WPI-next Mini-workshop
"Hints for New Physics in Heavy Flavors"

Lepton flavor universality

- In the Standard Model, the electroweak couplings between leptons and gauge bosons do not depend on the lepton flavor.
 - The difference of the branching fraction comes from the difference of the mass, i.e. helicity suppression and phase space.



$$g_e = g_\mu = g_\tau$$

Tests of lepton flavor universality

- Decays of W/Z bosons

- $\frac{\Gamma_{\mu\mu}}{\Gamma_{ee}} \equiv \frac{\mathcal{B}(Z \rightarrow \mu^+ \mu^-)}{\mathcal{B}(Z \rightarrow e^+ e^-)}, \frac{\Gamma_{\tau\tau}}{\Gamma_{ee}} \equiv \frac{\mathcal{B}(Z \rightarrow \tau^+ \tau^-)}{\mathcal{B}(Z \rightarrow e^+ e^-)}$ by LEP [Phys. Rep. 427 (2006) 257]
- $R_Z \equiv \frac{\sigma_Z \cdot \mathcal{B}(Z \rightarrow e^+ e^-)}{\sigma_Z \cdot \mathcal{B}(Z \rightarrow \mu^+ \mu^-)}, R_W \equiv \frac{\sigma_{W^\pm} \cdot \mathcal{B}(W^\pm \rightarrow e\nu)}{\sigma_{W^\pm} \cdot \mathcal{B}(W^\pm \rightarrow \mu\nu)}$ by ATLAS [Phys. Rev. D85, 072004 (2012)]
- $\mathcal{B}(W \rightarrow \ell\nu)$ ($\ell = e, \mu, \tau$) by LEP [Phys. Rep. 532 (2013) 119]
- $\frac{\mathcal{B}(W \rightarrow e\nu)}{\mathcal{B}(W \rightarrow \mu\nu)}$ by CDF, D0, LEP, ATLAS, LHCb [JHEP 10 (2016) 030]

- Decays of leptons

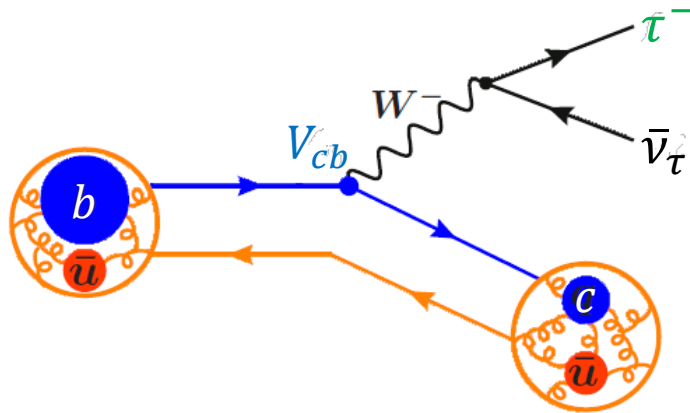
- $(g_\tau/g_\mu), (g_\tau/g_e), (g_\mu/g_e)$ from $\Gamma(\tau \rightarrow \mu\nu\nu), \Gamma(\tau \rightarrow e\nu\nu), \Gamma(\mu \rightarrow e\nu\nu)$
- $(g_\tau/g_\mu)_\pi, (g_\tau/g_\mu)_K$ from $\frac{\Gamma(\tau \rightarrow h\nu)}{\Gamma(h \rightarrow \mu\nu)}, \frac{\Gamma(\tau \rightarrow h\nu)}{\Gamma(h \rightarrow e\nu)}$

- Decays of light mesons

- $R_{e/\mu} = \frac{\Gamma(\pi \rightarrow e\nu(\gamma))}{\Gamma(\pi \rightarrow \mu\nu(\gamma))}$ by PIENU [Phys. Rev. Lett. 115, 071801 (2015)]
- $R_K = \frac{\Gamma(K \rightarrow e\nu)}{\Gamma(K \rightarrow \mu\nu)}$ by KLOE, NA62 [Phys. Lett. B719, 326 (2013)], et al.

All consistent with SM except for $\mathcal{B}(W \rightarrow \tau\nu_\tau)$

$$B \rightarrow D^{(*)} \tau \nu$$



Sensitive to new physics
because the massive 3rd generation
***b* quark** and ***\tau* lepton** are involved.

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{cb} \left\{ [\bar{c} \gamma^\mu (1 - \gamma_5) b] [\bar{\tau} \gamma_\mu (1 - \gamma_5) \nu_\tau] \quad \dots \text{SM } (W^\pm) \right. \\ \left. - \frac{m_b m_\tau}{m_B^2} \bar{c} [g_S + g_P \gamma_5] b [\bar{\tau} (1 - \gamma_5) \nu_\tau] \right\} \quad \dots \text{New Physics } (H^\pm) \\ + \text{h. c.}$$

Flavor-dependent coupling to the fermions

$$\frac{d\Gamma(B^- \rightarrow D^0 \ell^- \bar{\nu})}{dw} = \frac{G_F^2 m_D^3}{48\pi^3} (m_B + m_D)^2 (w^2 - 1)^{3/2} |\eta_{EW}|^2 |V_{cb}|^2 |\mathcal{G}(w)|^2$$

$$\frac{d\Gamma(B^- \rightarrow D^{*0} \ell^- \bar{\nu})}{dw} = \frac{G_F^2 m_{D^*}^3}{4\pi^3} (m_B - m_{D^*})^2 (w^2 - 1)^{1/2} |\eta_{EW}|^2 |V_{cb}|^2 \chi(w) |\mathcal{F}(w)|^2$$

Sizable uncertainties on $|V_{cb}|$ and the form factors

Hint of new physics in $b \rightarrow c\ell\nu$ tree decays

$$R(D^{(*)}) = \frac{\Gamma(B \rightarrow D^{(*)}\tau\nu)}{\Gamma(B \rightarrow D^{(*)}\ell\nu)}$$

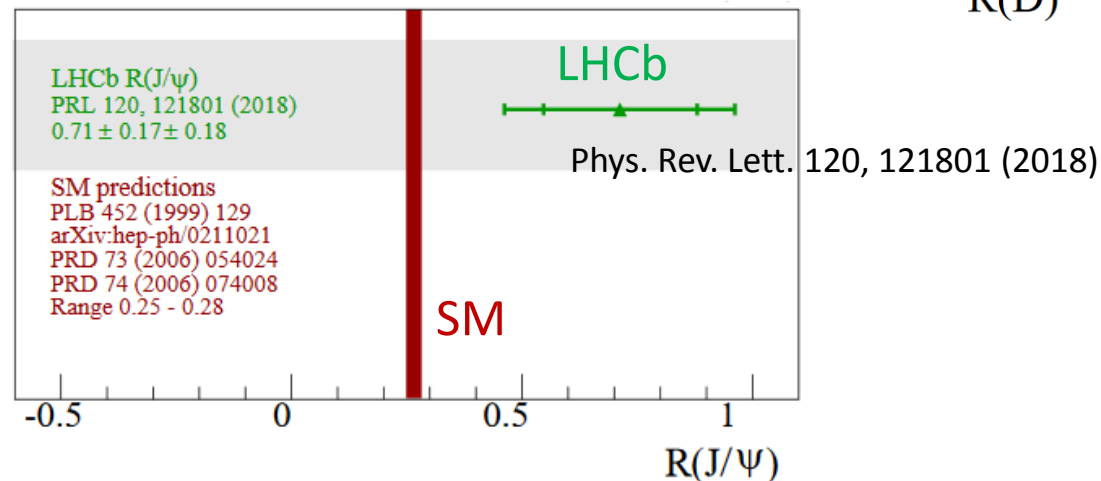
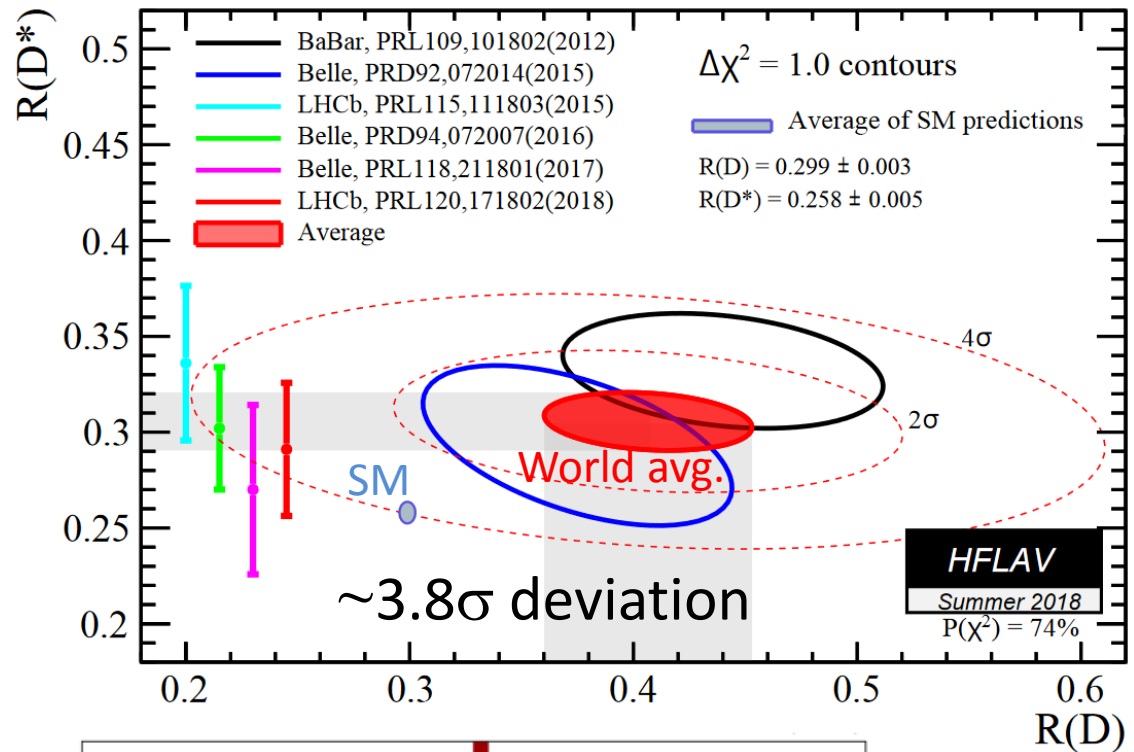
Useful observable to probe new physics since the uncertainties on $|V_{cb}|$ and the form factors as well as the experimental systematics cancel out

$$R(J/\Psi) = \frac{\Gamma(B_c \rightarrow J/\Psi\tau\nu)}{\Gamma(B_c \rightarrow J/\Psi\mu\nu)}$$

Deviation also in

$$R(K^{(*)}) = \frac{\Gamma(B \rightarrow K^{(*)}\mu\mu)}{\Gamma(B \rightarrow K^{(*)}ee)}$$

... $b \rightarrow s\ell\ell$ penguin decays

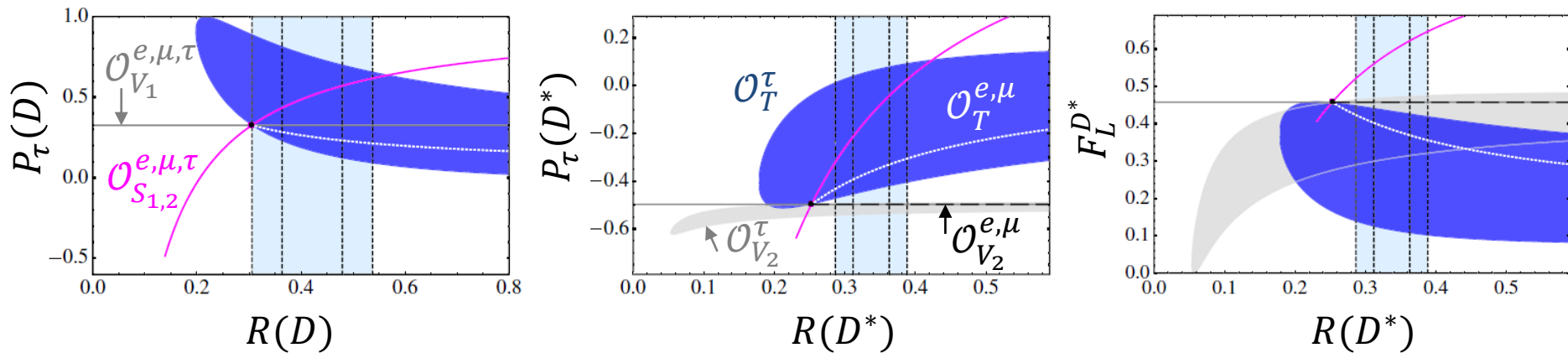


D^* and τ polarizations in $B \rightarrow D^* \tau \nu$

Observable which could distinguish the type of new physics:
Longitudinal polarizations

- $P_\tau(D^*) = \frac{\Gamma^+(D^*) - \Gamma^-(D^*)}{\Gamma^+(D^*) + \Gamma^-(D^*)}$ $\Gamma^\pm(D^*)$: decay rate with τ helicity $\lambda_\tau = \pm \frac{1}{2}$
- $F_L^{D^*} = \frac{\Gamma(D_L^*)}{\Gamma(D_L^*) + \Gamma(D_T^*)}$ $\Gamma(D_{L(T)}^*)$: decay rate of longitudinally (transversely) polarized D^*

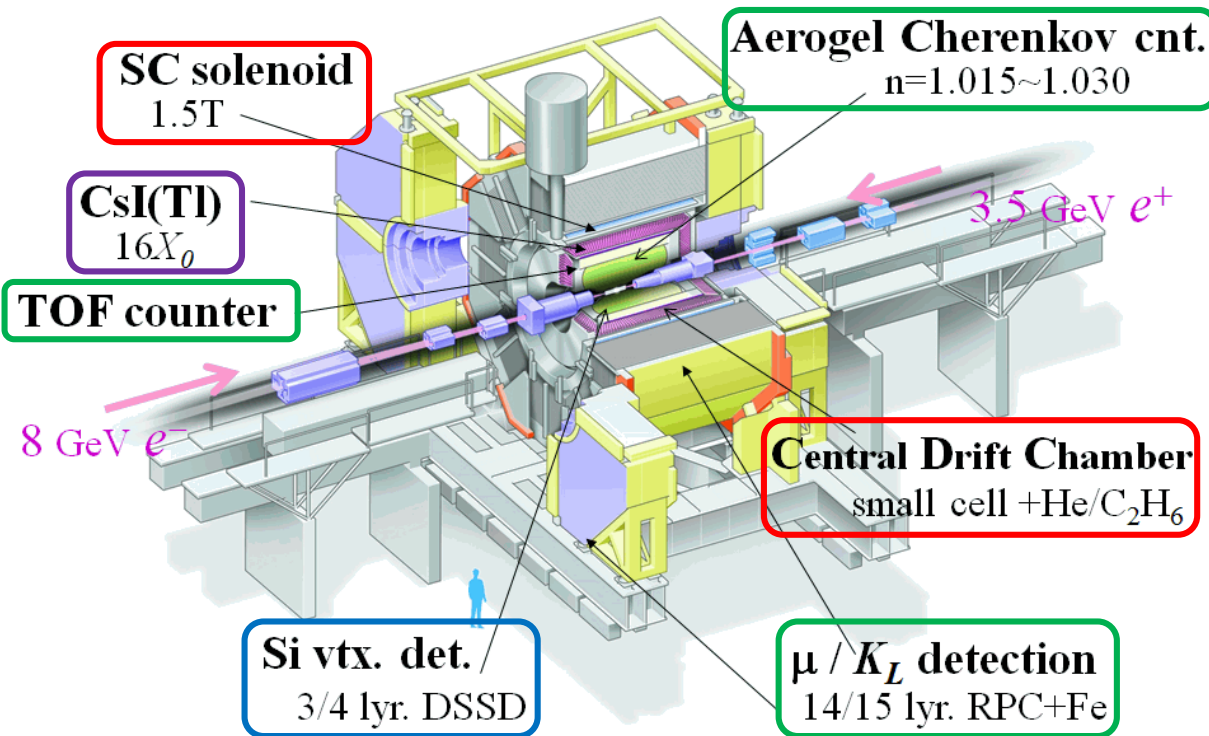
New physics scenarios [Phys. Rev. D 87, 034028 (2013)]



Belle measured $R(D)$, $R(D^*)$ and $P_\tau(D^*)$, and is still active in producing new results.

The Belle experiment

- Collected 772×10^6 $B\bar{B}$ events at KEKB factory (1998-2010), asymmetric e^+e^- collider at $\sqrt{s} = 10.58$ GeV, in Japan.
 - $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ (very clean and well-known initial state)



Hermetic spectrometer capable of

- Tracking and momentum meas. of charged tracks
- Vertex meas.
- Particle ID
- γ energy meas.

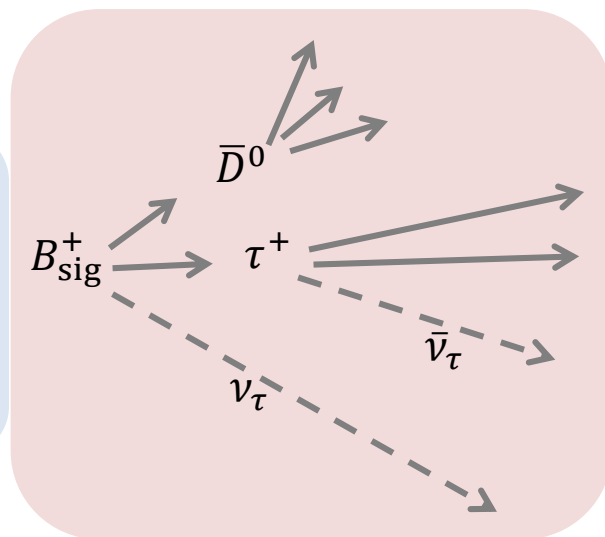
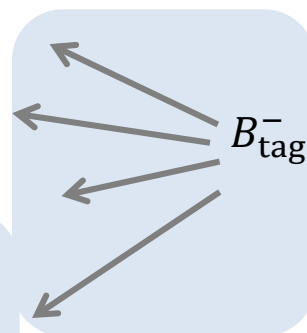
$B \rightarrow D^{(*)}\tau\nu$ reconstruction in Belle

- Not a rare decay
 - In SM, $\mathcal{B}(B^+ \rightarrow \bar{D}^0 \tau^+ \nu_\tau) = 0.66\%$ and $\mathcal{B}(B^+ \rightarrow \bar{D}^{*0} \tau^+ \nu_\tau) = 1.23\%$
- but reconstruction of τ is challenging due to multiple neutrinos and need a high statistics..
 - Need full reconstruction of the event
 - Suppress non- $B\bar{B}$ bkgd. and misreconstructed events
 - quite low efficiency

Reconstruct one of the B 's decaying

1. Hadronically ($\epsilon_{\text{sig}} \approx 0.2\%$)
2. Semileptonically ($\epsilon_{\text{sig}} \approx 0.5\%$)
3. Inclusively ($\epsilon_{\text{sig}} \approx \text{a few \%}$)

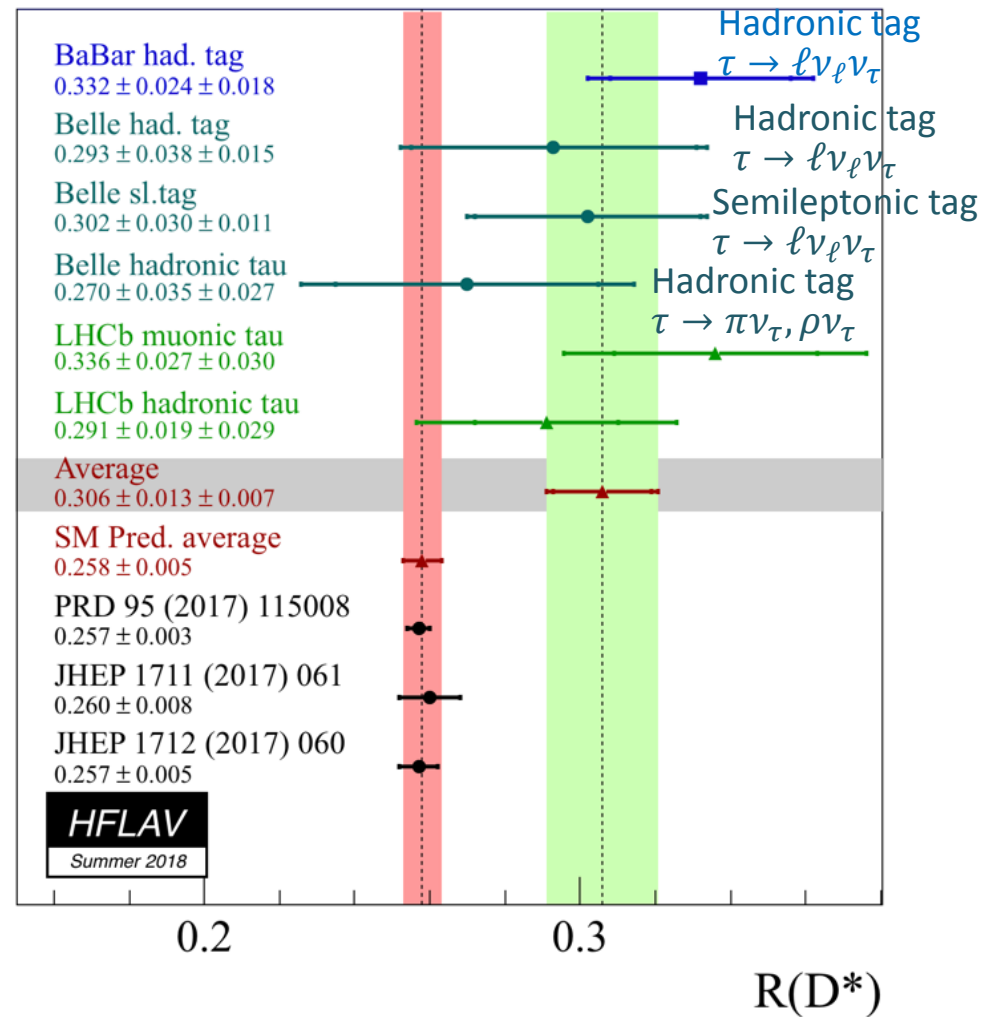
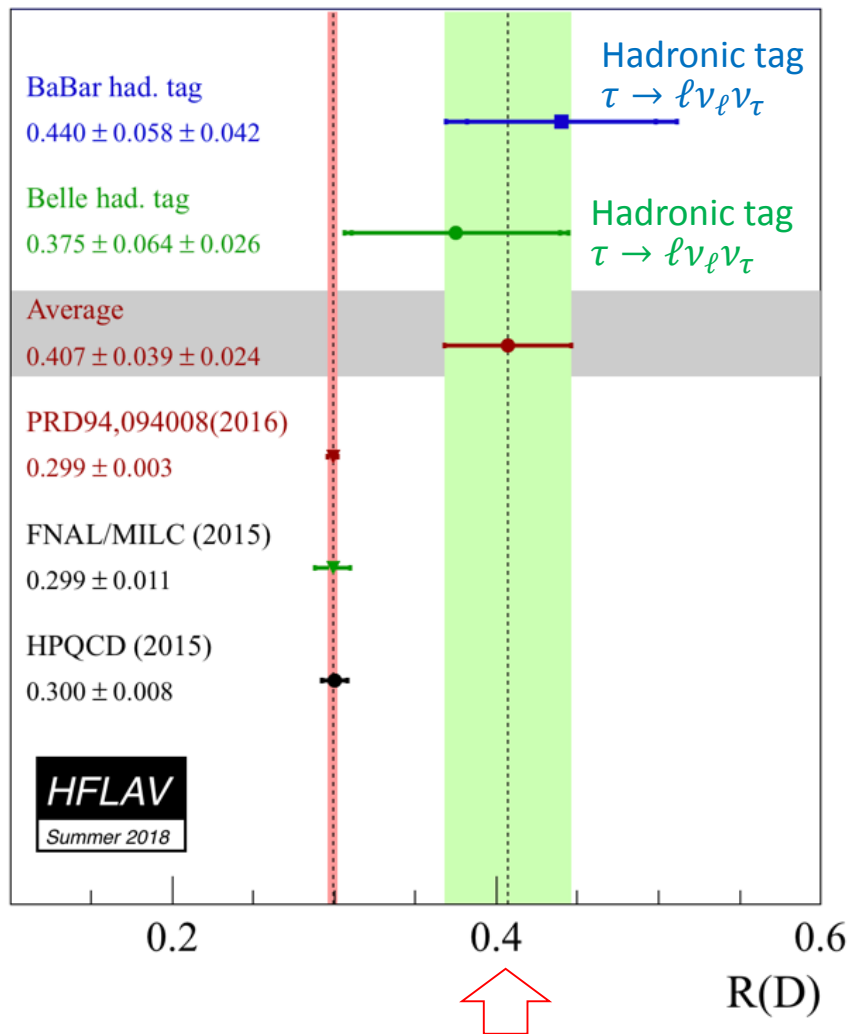
Efficiency ↑
Purity ↓



Select the other B of the signal decay with

- a $D^{(*)}$
- a charged daughter of τ
 1. Leptonic τ decay
 2. Hadronic τ decay

Previous results on $R(D)$ and $R(D^*)$



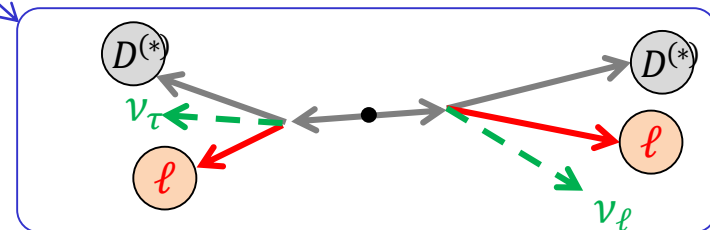
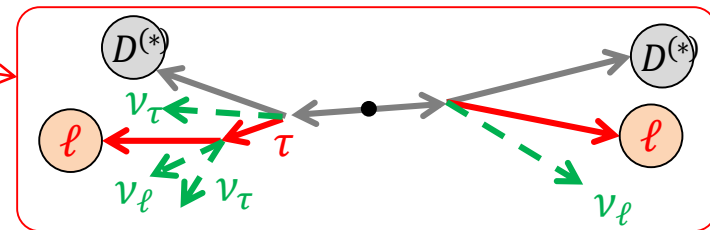
Only two (direct) measurements with hadronic tag
 $\rightarrow R(D)$ with semileptonic tag will be added.

$B \rightarrow D^{(*)}\tau\nu$ with semileptonic tag

- Simultaneous measurement of $R(D)$ and $R(D^*)$

$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu_\tau)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu_\ell)} = \frac{\text{signal}}{\text{normalization}}$$

- In the previous result only $B^0\bar{B}^0 \rightarrow (D^{*-}\ell^+)(D^{*+}\ell^-)$
- Add $B^0\bar{B}^0 \rightarrow (D^{(*)-}\ell^+)(D^{(*)+}\ell^-)$ and $B^+B^- \rightarrow (\bar{D}^{(*)0}\ell^+)(D^{(*)0}\ell^-)$



- Analysis with the Belle II software framework
 - To reconstruct B_{tag} we can exploit FEI (Full Event Interpretation; Multivariate analysis with Boosted-Decision Tree classifier)
 - higher efficiency

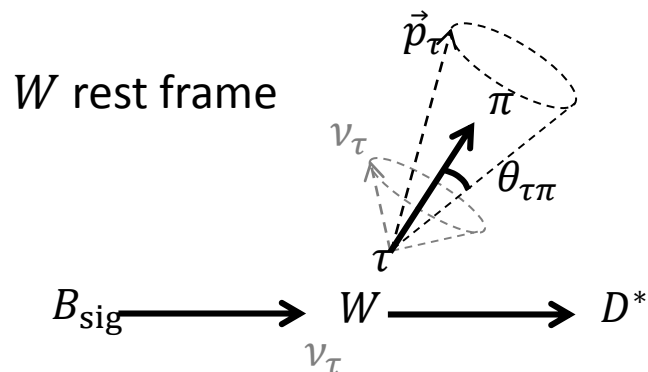
Close to opening the blinded signal box

Polarization measurements

Angular distribution of τ decay

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{1}{2} [1 + \alpha P_{\tau}(D^*) \cos \theta_{\text{hel}}]$$

$$\alpha = \begin{cases} 1 & \text{for } \tau \rightarrow \pi \nu \\ 0.45 & \text{for } \tau \rightarrow \rho \nu \end{cases}$$



\vec{p}_{τ} can be constrained to lie on the cone with a half apex angle $\theta_{\tau\pi}$:

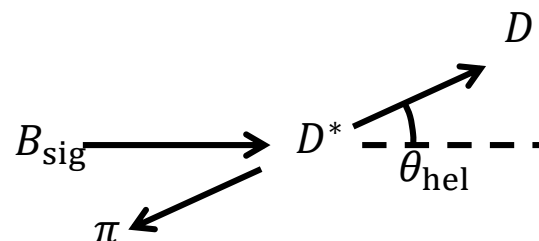
$$\cos \theta_{\tau\pi} = \frac{2E_{\tau}E_{\pi} - m_{\tau}^2 - m_{\pi}^2}{2|\vec{p}_{\tau}||\vec{p}_{\pi}|}$$

Boost in an arbitrary direction on the cone to translate $\cos \theta_{\tau\pi}$ to $\cos \theta_{\text{hel}}$ in the τ rest frame.

Angular distribution of D^* decay

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{3}{4} [2F_L^{D^*} \cos^2 \theta_{\text{hel}} + F_T^{D^*} \sin^2 \theta_{\text{hel}}] \\ (F_L^{D^*} + F_T^{D^*} = 1)$$

D^* rest frame



[Pros]

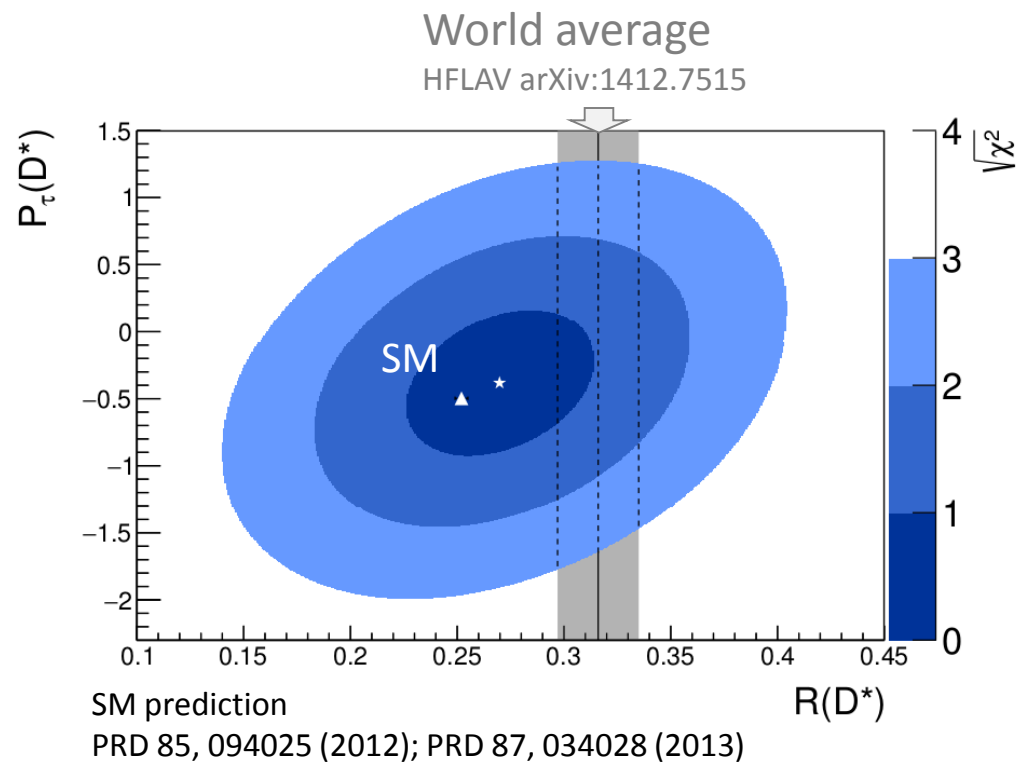
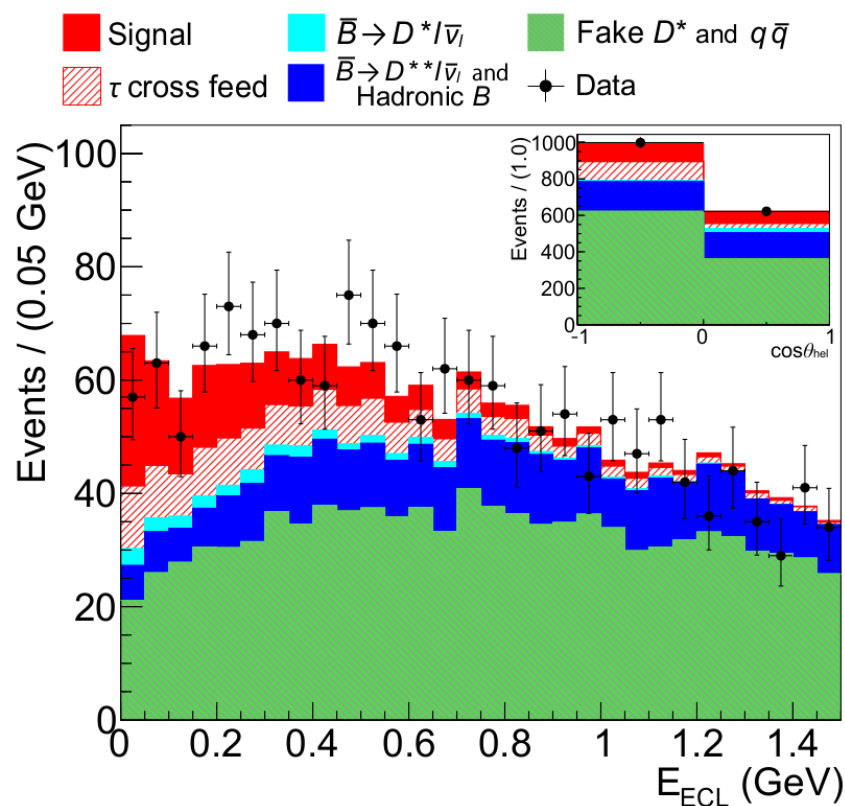
- All τ decays are useful.
- Not affected by cross-feeds of τ decays.

[Cons]

- Strong dependence of acceptance on $\cos \theta_{\text{hel}}$ and q^2 .

Result on $P_\tau(D^*)$

- Hadronic tag
- Two-body τ decays ($\tau \rightarrow \pi\nu_\tau, \rho\nu_\tau$)



$$P_\tau(D^*) = -0.38 \pm 0.51(\text{stat})_{-0.16}^{+0.21}(\text{syst})$$

$P_\tau(D^*)$ and $F_L^{D^*}$ with inclusive tag

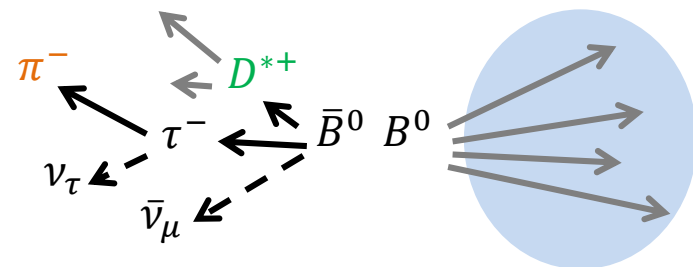
- Select candidates for B_{sig} daughters; $D^{*+} + (\ell^- \text{ or } \pi^-)$.

- $\bar{B}^0 \rightarrow D^{*+} \tau^- \bar{\nu}_\tau$

- $D^{*+} \rightarrow D^0 \pi^+$

- $D^0 \rightarrow K^- \pi^+, K^- \pi^+ \pi^0, K^- \pi^+ \pi^- \pi^+$

- $\tau^- \rightarrow \ell^- \nu_\tau \bar{\nu}_\tau, \pi^- \bar{\nu}_\tau$



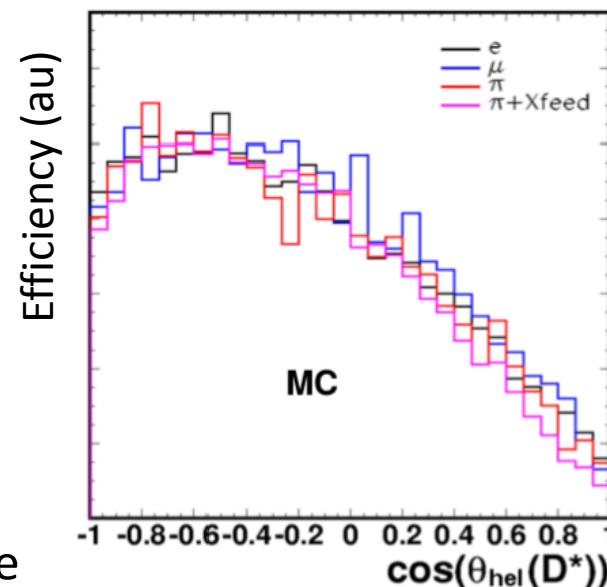
- Reconstruct B_{tag} inclusively from **all the remaining particles**.
 - Proper assignment of the particles without missing should lead to

$$M_{\text{tag}} \equiv \sqrt{E_{\text{beam}}^2 - |\vec{p}_{\text{tag}}|^2} \approx M_B$$

$$\Delta E_{\text{tag}} \equiv E_{\text{tag}} - E_{\text{beam}} \approx 0$$

- Use only $\cos \theta_{\text{hel}} < 0$ for $F_L^{D^*}$ meas.

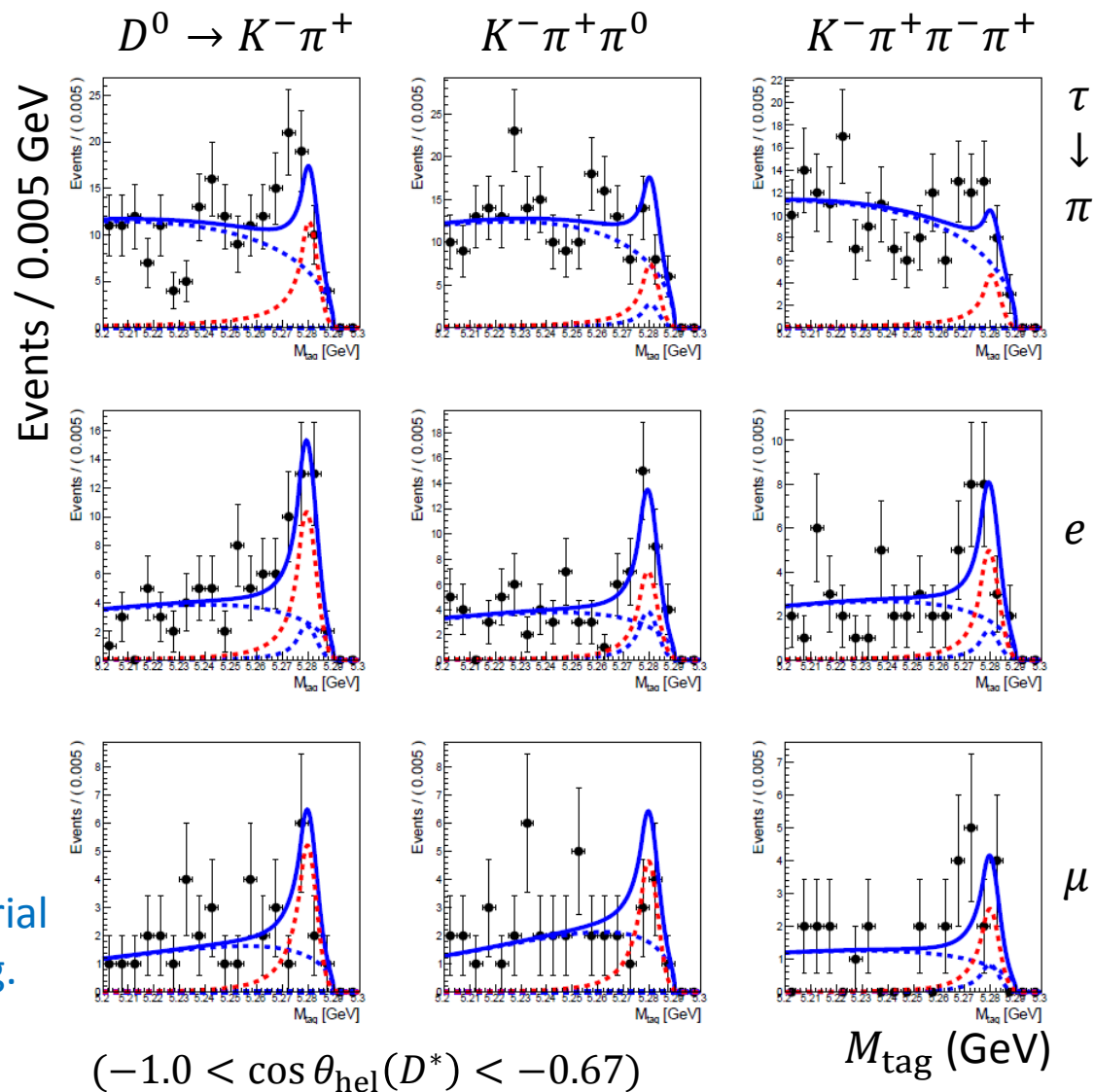
- Strong dependence of the efficiency on $\cos \theta_{\text{hel}}$ due to the slow π from D^* , which is softer at a larger $\cos \theta_{\text{hel}}$.
 - Correct signal yield for the efficiency/acceptance



Signal extraction for $F_L^{D^*}$ measurement

Simultaneous extended unbinned max likelihood fit to all 9 sub-channels in the M_{tag} distributions for each of 3 bins of $\cos \theta_{\text{hel}}$

Signal
Combinatorial
Peaking bkg.



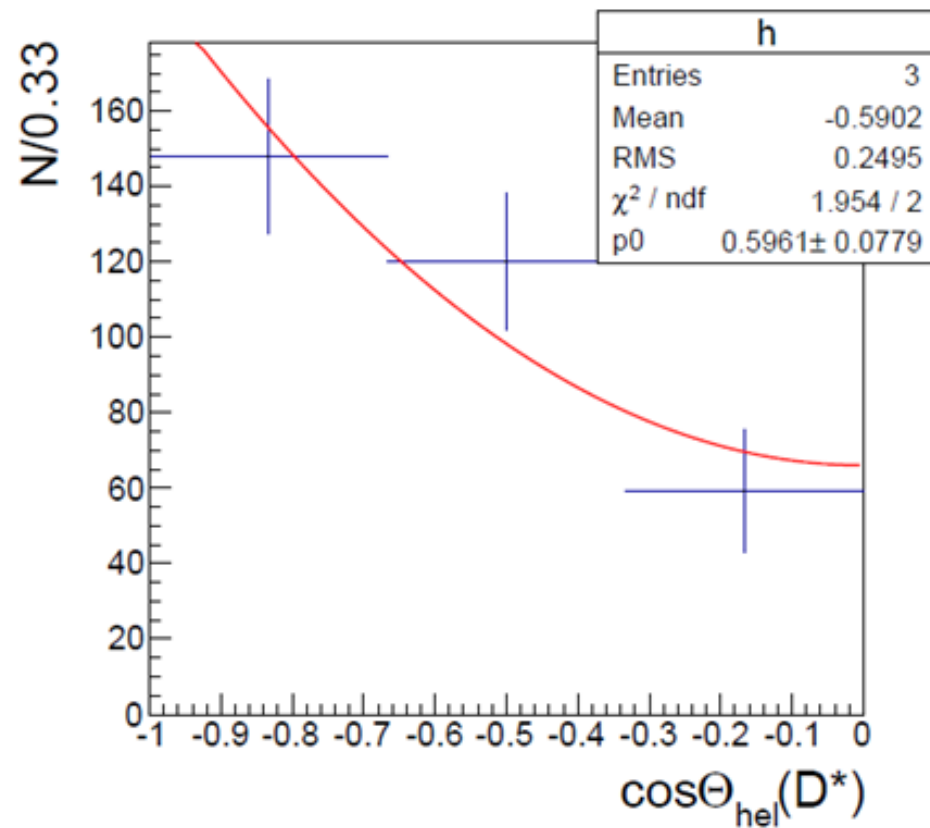
Result on $F_L^{D^*}$ presented at CKM2018

$$F_L^{D^*} = 0.60 \pm 0.08(\text{stat}) \pm 0.035(\text{syst})$$

cf. in SM

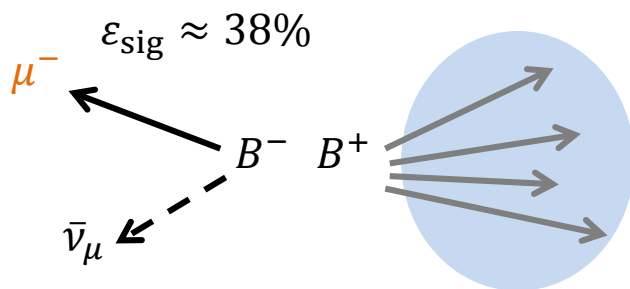
- $F_L^{D^*} = 0.46 \pm 0.03$ [Phys. Rev. D 95, 115038 (2017)]
- $F_L^{D^*} = 0.441 \pm 0.006$ [arXiv:1808.03565]

Consistent with SM within 2σ



Search for $B \rightarrow \mu \nu_\mu$

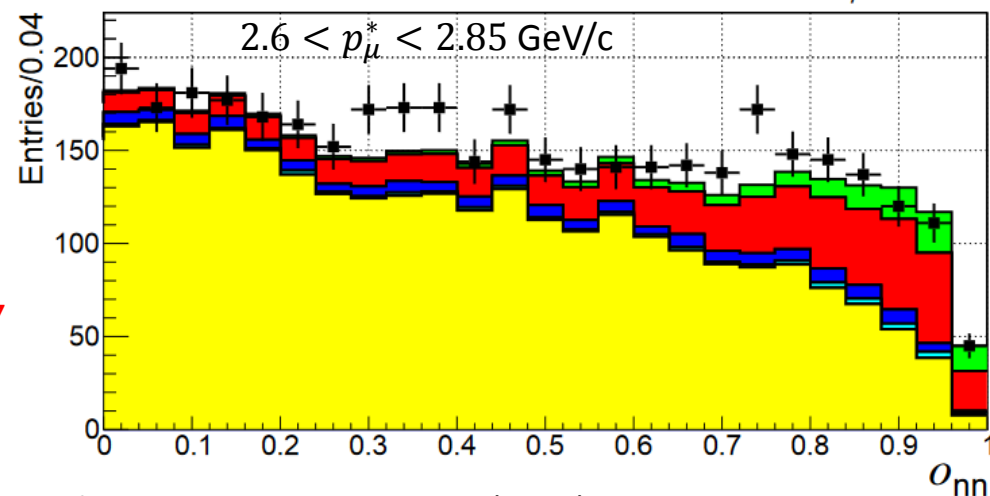
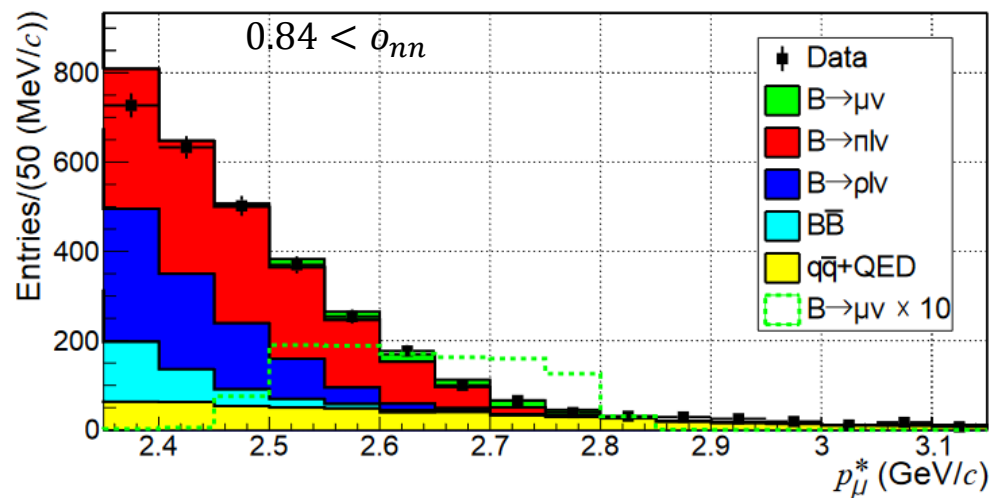
- In SM $\mathcal{B}(B^- \rightarrow \mu^- \bar{\nu}_\mu) = \frac{G_F^2 m_B m_\mu^2}{8\pi} \left(1 - \frac{m_\mu^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2 \tau_B = (3.80 \pm 0.31) \times 10^{-7}$
- More precise SM prediction of $\frac{\mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}_\tau)}{\mathcal{B}(B^- \rightarrow \mu^- \bar{\nu}_\mu)}$ than $R(D^{(*)})$
- Untagged (inclusive) method
 - Select a muon and check that the rest of event resembles B



$$\mathcal{B}(B^- \rightarrow \mu^- \bar{\nu}_\mu) = (6.46 \pm 2.22 \pm 1.60) \times 10^{-7}$$

Significance: 2.4σ

$[2.9, 10.7] \times 10^{-7}$ at 90% CL



Prospects for $B \rightarrow D^{(*)}\tau\nu$ at Belle II

Composition of the systematic uncertainties in each Belle analysis

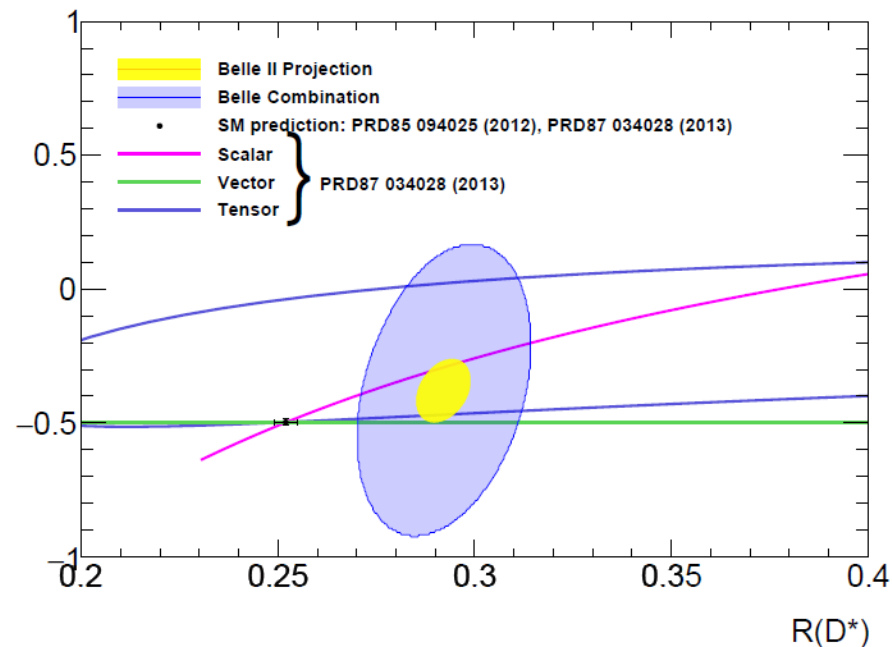
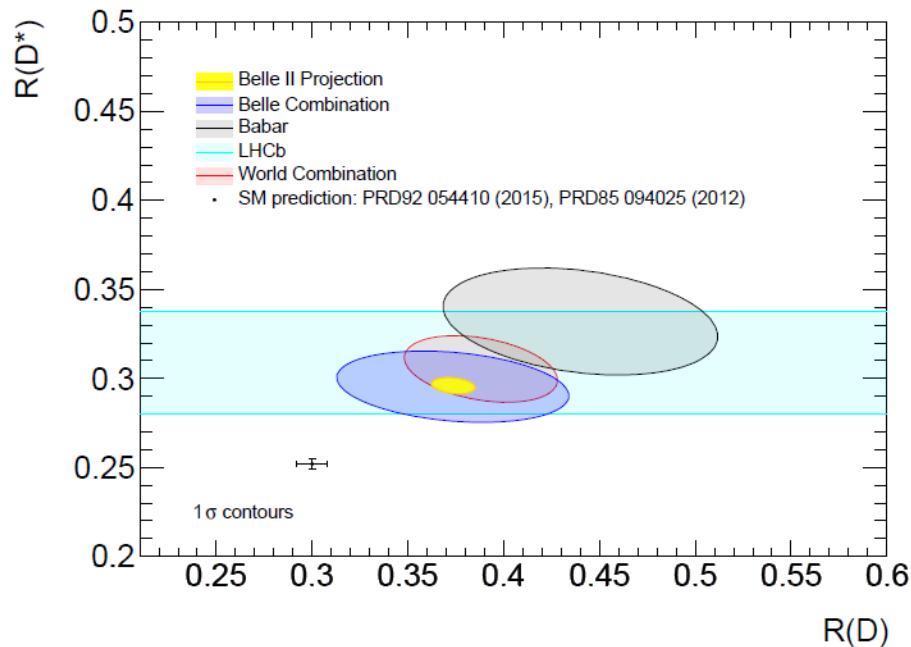
Source	Belle (Had, ℓ^-) R_D	Belle (Had, ℓ^-) R_{D^*}	Belle (SL, ℓ^-) R_{D^*}	Belle (Had, h^-) R_{D^*}
MC statistics	4.4%	3.6%	2.5%	$+4.0\%$ -2.9%
$B \rightarrow D^{**}\ell\nu_\ell$	4.4%	3.4%	$+1.0\%$ -1.7%	2.3%
Hadronic B	0.1%	0.1%	1.1%	$+7.3\%$ -6.5%
Other sources	3.4%	1.6%	$+1.8\%$ -1.4%	5.0%
Total	7.1%	5.2%	$+3.4\%$ -3.5%	$+10.0\%$ -9.0%

“The Belle II Physics Book”, arXiv:1808.10567

- The uncertainty due to the MC statistics is reducible.
 - MC stat affects the estimation of the reconstruction efficiency, understanding of small cross-feed components and PDFs for the fit.
- The uncertainties from $\mathcal{B}(B \rightarrow D^{**}\ell\nu_\ell)$, D^{**} decays and hadronic B decays have to be reduced.
 - Need dedicated measurements of $B \rightarrow D^{**}\ell\nu_\ell$ and hadronic B decays with a large data sample.

Prospects for $B \rightarrow D^{(*)}\tau\nu$ at Belle II

- Belle $0.772 \times 10^9 B\bar{B} \rightarrow$ Belle II $\sim 50 \times 10^9 B\bar{B}$ (50 ab^{-1} in 6 yrs)



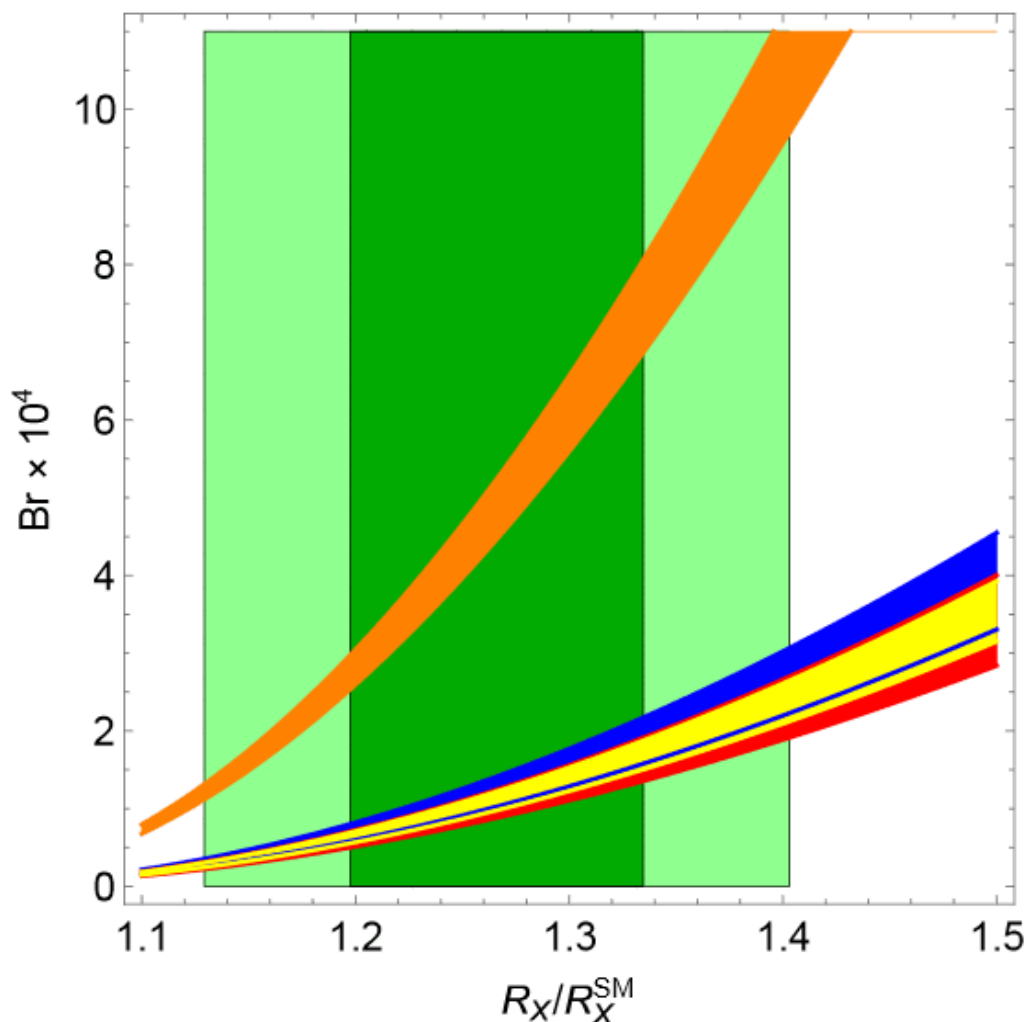
Expected precision (stat and syst)

	5 ab^{-1}	50 ab^{-1}
R_D	$(\pm 6.0 \pm 3.9)\%$	$(\pm 2.0 \pm 2.5)\%$
R_{D^*}	$(\pm 3.0 \pm 2.5)\%$	$(\pm 1.0 \pm 2.0)\%$
$P_\tau(D^*)$	$\pm 0.18 \pm 0.08$	$\pm 0.06 \pm 0.04$

In addition, q^2 and other distributions of kinematic observables to discriminate the new physics scenarios.

Search for $b \rightarrow s\tau^+\tau^-$ at Belle II

Phys. Rev. Lett. 120, 181802 (2018)



- $R_{D^{(*)}} \& R_{J/\psi} \ 2\sigma$
- $R_{D^{(*)}} \& R_{J/\psi} \ 1\sigma$
- $\text{Br}[B_s \rightarrow \tau\tau]$
- $\text{Br}[B \rightarrow K^* \tau\tau]$
- $\text{Br}[B \rightarrow K \tau\tau]$
- $\text{Br}[B_s \rightarrow \phi \tau\tau]$

The anomalies seen in $R(D^{(*)})$, $R(J/\psi)$, $R(K^{(*)})$ and $b \rightarrow s\mu^+\mu^-$ suggest a possibility of huge effects of lepton flavor universality violation in $b \rightarrow s\tau^+\tau^-$ (FCNC penguin).

$O(10^4)$ enhancement of the branching fractions

Summary

- The anomalies in the semileptonic B decays could be a hint for new physics.
- $R(D^{(*)}) = \frac{\Gamma(B \rightarrow D^{(*)} \tau \nu)}{\Gamma(B \rightarrow D^{(*)} \ell \nu)}$ and the polarizations of D^* and τ in $B \rightarrow D^{(*)} \tau \nu$ are useful observable to probe new physics.
- Belle measured those observables with different tagging methods, and the following new results will come out soon:
 - $R(D)$ and $R(D^*)$ with semileptonic tag
 - $P_\tau(D^*)$ with inclusive tag
- Belle II will also play an important role on the $B \rightarrow D^{(*)} \tau \nu$ measurements with x50 data.