

XYZ mesons + some other stuff

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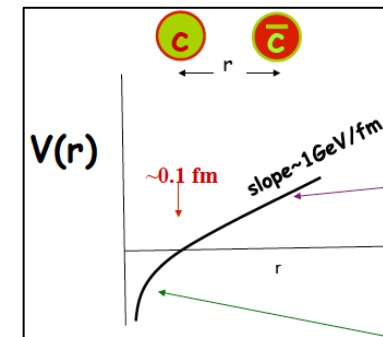
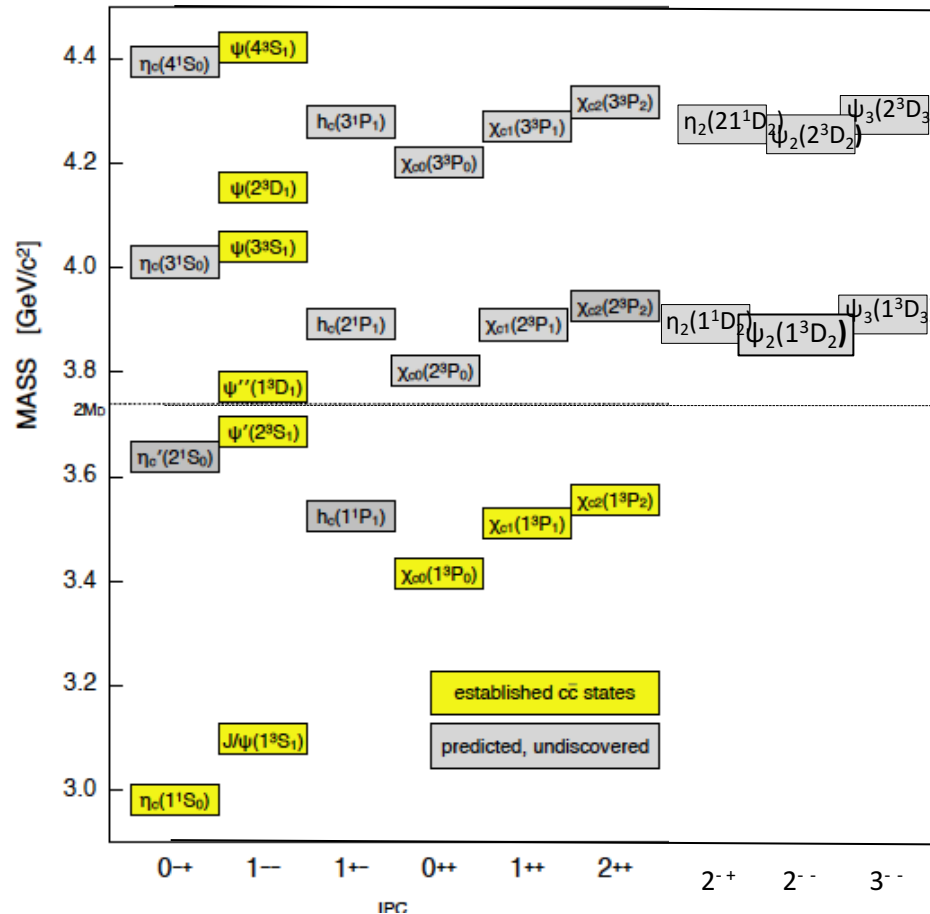
Daejeon, So KOREA

“Hints for New Physics in Heavy Flavors,” KMI, Nagoya, Nov. 16-18, 2018

charmonium: pre B-factory

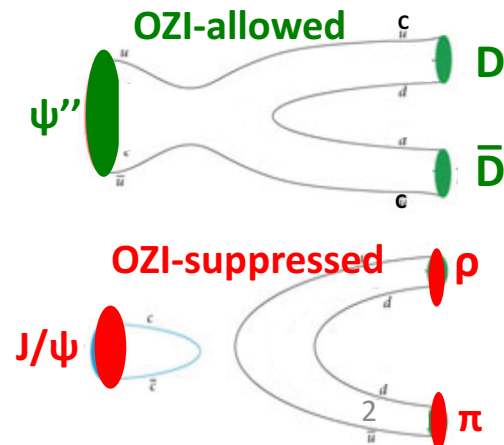
forty-plus years of work

potential model works well

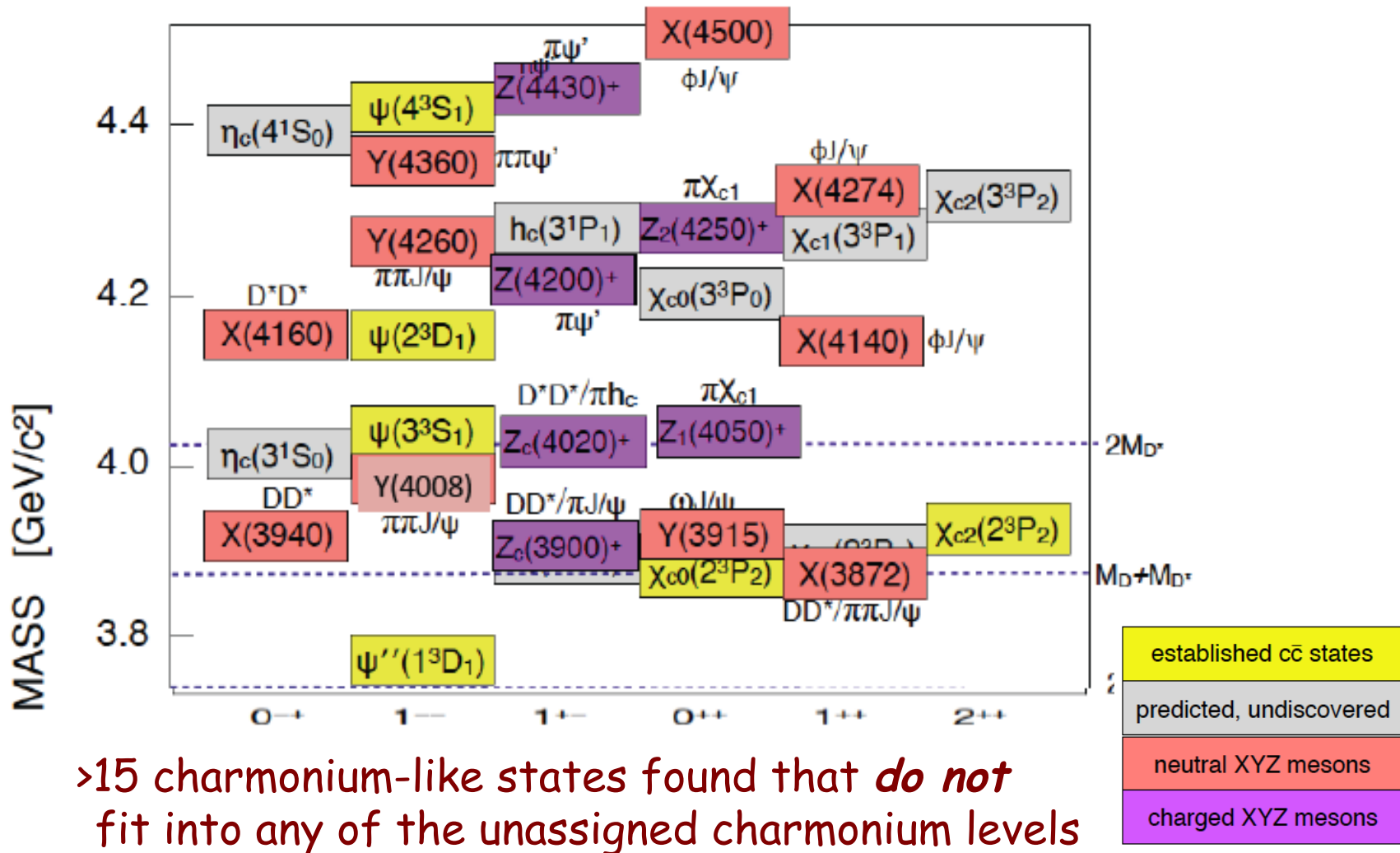


measured &
predicted masses agree

OZI-rule applies
no exceptions

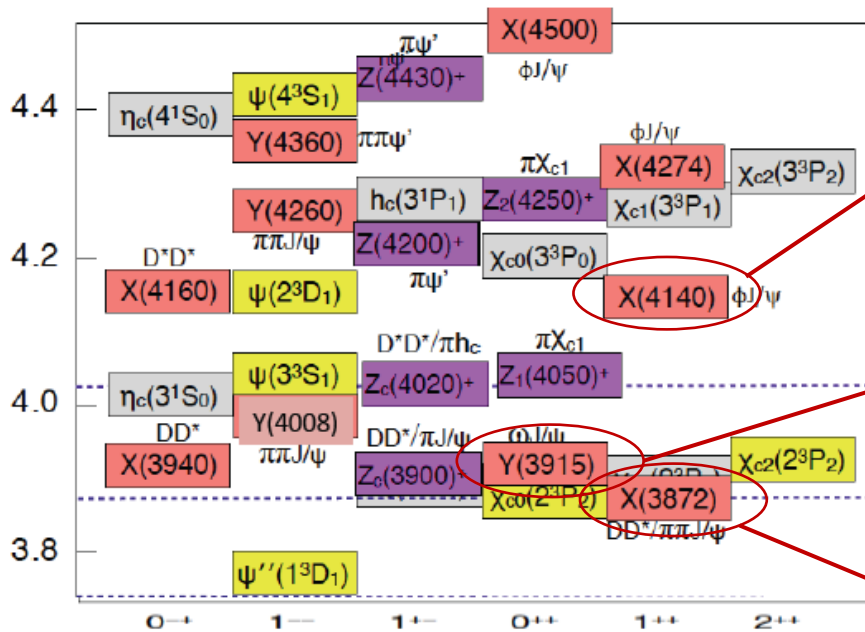


charmonium: post B-factory

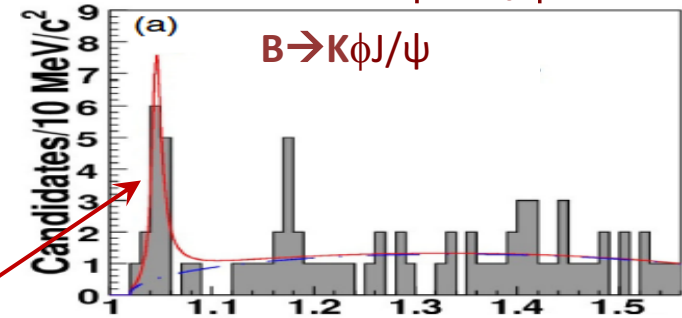


Are there patterns to the new particles?

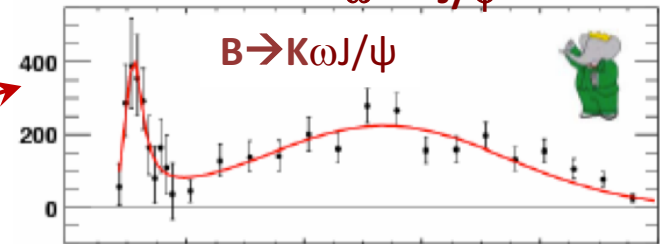
For example:



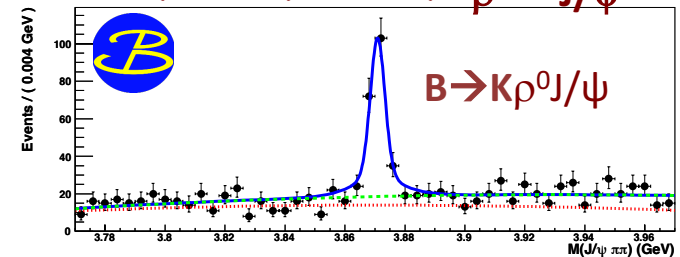
$X(4140): M \approx (m_{\phi} + m_{J/\psi}) + \sim 20 \text{ MeV}$



$X(3915): M \approx (m_{\omega} + m_{J/\psi}) + \sim 20 \text{ MeV}$

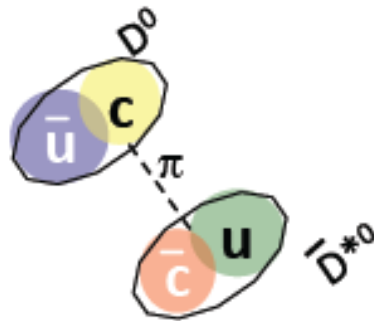


$X(3872): M \approx (m_{\rho} + m_{J/\psi})$

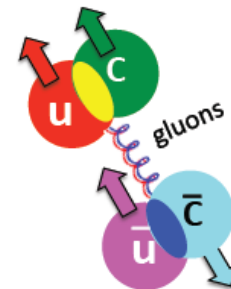


what are they?

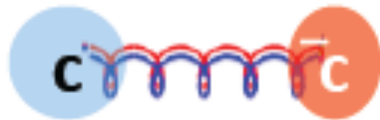
-- “standard slide” --



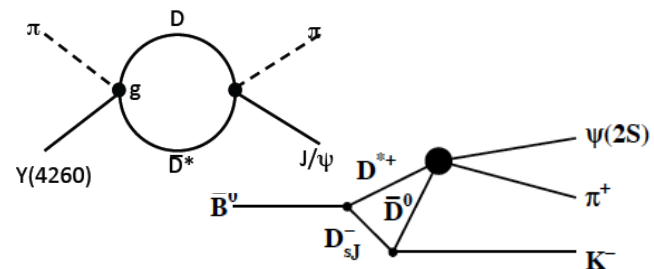
molecules?



QCD tetraquarks?



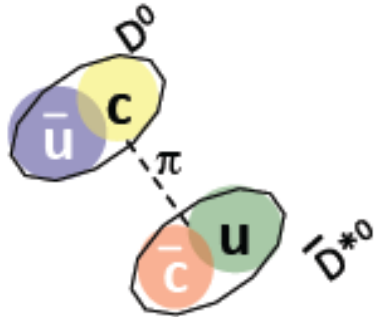
QCD hybrids?



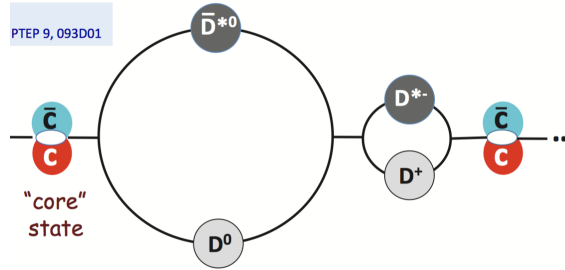
threshold effects?

what are they?

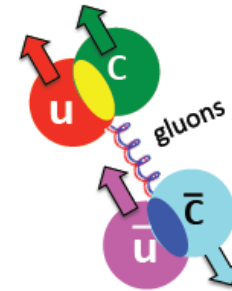
-- add one more possibility --



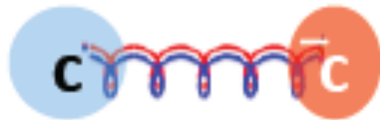
molecules?



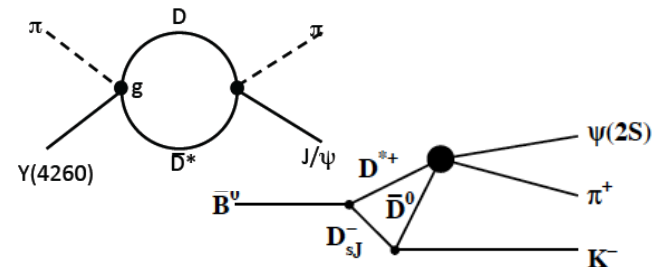
coupled channel system?



QCD tetraquarks?

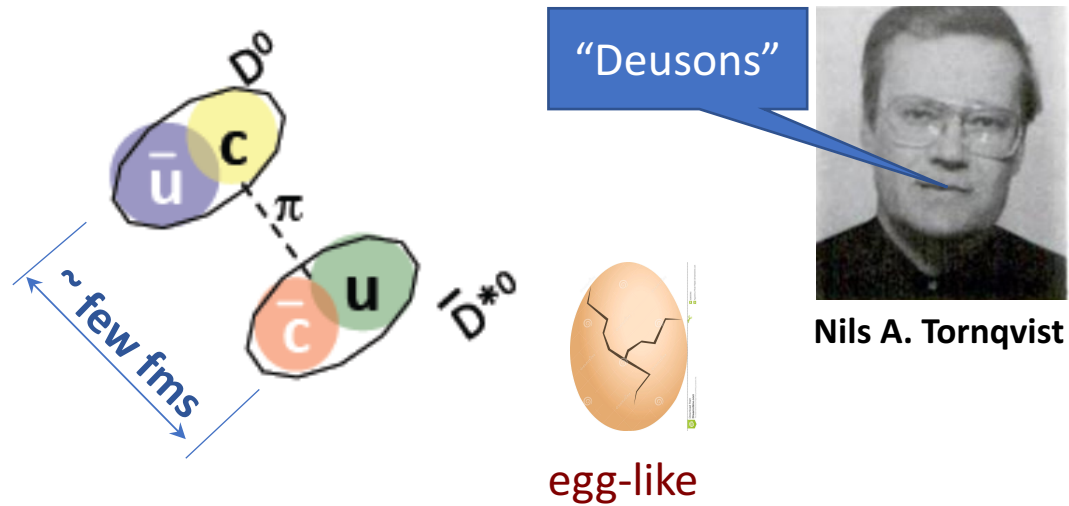


QCD hybrids?



threshold effects?

deuteron-like molecules



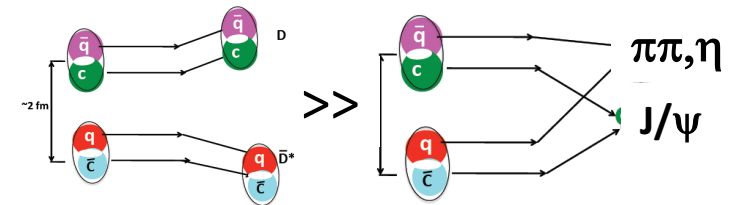
Karliner & Skwarnicki (PDG 2016):

masses near thresholds $d_{\text{rms}}^{-1} \approx a^{-1} = \sqrt{2\mu|BE|} < m_\pi \Rightarrow BE < \frac{m_\pi^2}{2\mu} \approx 10 \text{ MeV (for } 2\mu = m_D)$

Constituent mesons should be narrower than the molecule

J^{PC} consistent with S-wave *e.g.*, $J^{PC} = 1^{++}$ for $D\bar{D}^*$; $= 1^{--}$ for $D\bar{D}_1^{**}$

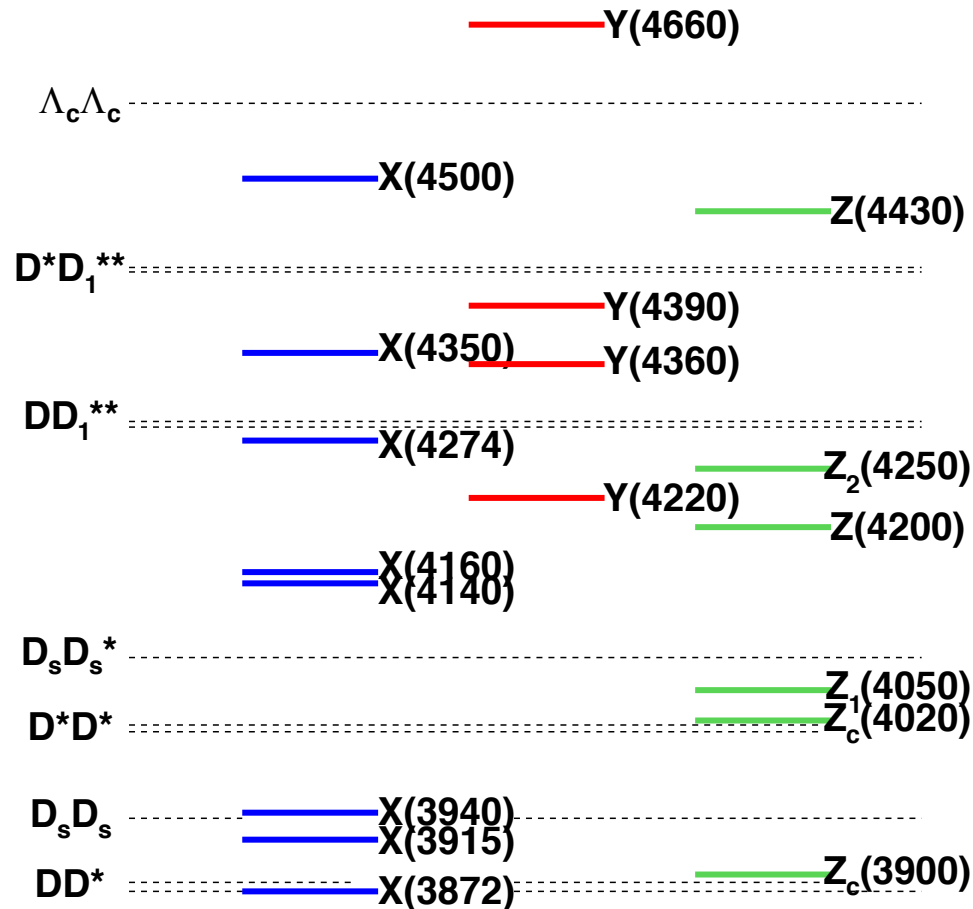
fall-apart decays $\gg$ hidden charm modes



no $0^- \oplus 0^-$ molecules (one π -exchange forbidden)

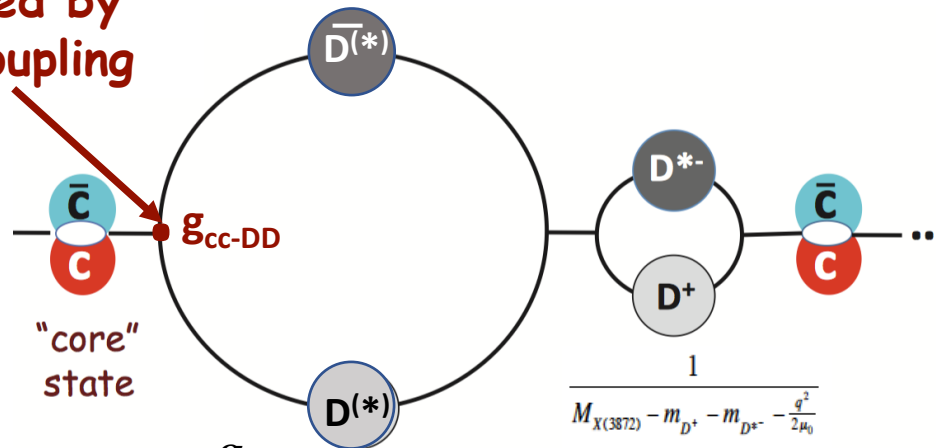
XYZ mesons vs open-charm thresholds

-- aside from the X(3872), no apparent correlation --



coupled-channel system

mass affected by $c\bar{c}-D^{(*)}\bar{D}^{(*)}$ coupling



$$\frac{g_{c\bar{c}-D\bar{D}}}{M_X - m_{D^{(*)}} - m_{\bar{D}^{(*)}} - \frac{q^2}{2\mu}}$$

If $M_X \rightarrow D^{(*)}\bar{D}^{(*)}$ threshold, propagator $\rightarrow$ divergent and the coupling is amplified

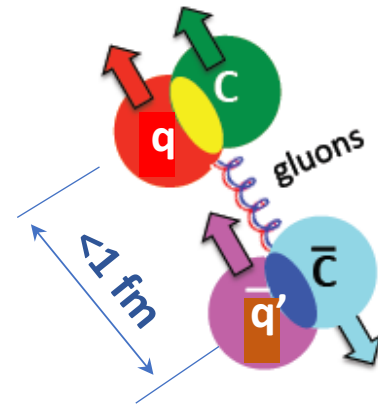
Specific model by
Takizawa & Takeuchi, PTEP 9, 093D01

$$|X(3872)\rangle = 0.94|D^0\bar{D}^{*0}\rangle + 0.23|D^+D^{*-}\rangle - 0.24|c\bar{c}\rangle$$

need a core $c\bar{c}$ state strongly coupled to an S-wave $D^{(*)}\bar{D}^{(*)}$ system

close to a $D^{(*)}\bar{D}^{(*)}$ mass threshold

QCD tetraquarks



ball bearing-like

Maiani et al., PRD 71, 014028 (2005)

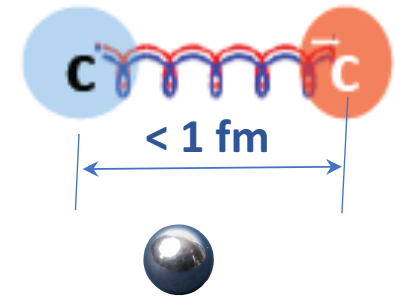
compact & tightly bound by the color force: BE = " ∞ "

since spin force $\sim 1/m_Q$, "bad" diquarks are not so bad

most masses and J^{PC} values are accessible for $[cq][\bar{c}\bar{q}']$

QCD is flavor blind ($q=u,d,s$) $\therefore$ tetraquark states should come in octets

charmonium hybrids

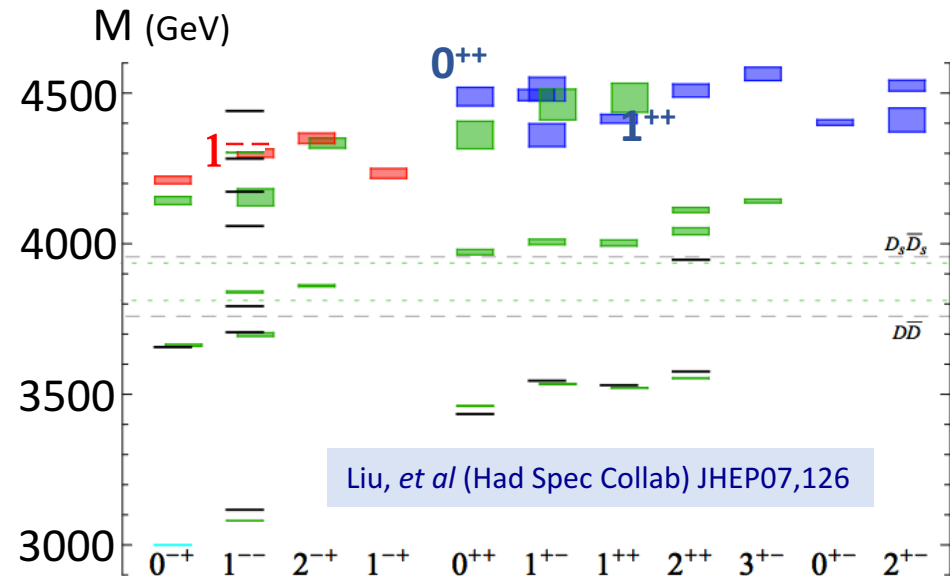
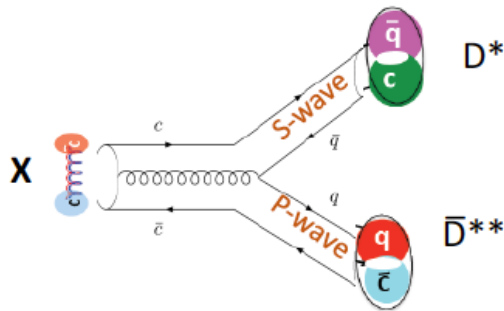


ball bearing-like

LQCD ($m_\pi=400$ MeV) predicts high masses
(e.g.: $1^{--} \approx 4.3$ GeV; $0^{++} \approx 4.5$ GeV; $1^{++} \approx 4.4$ GeV)

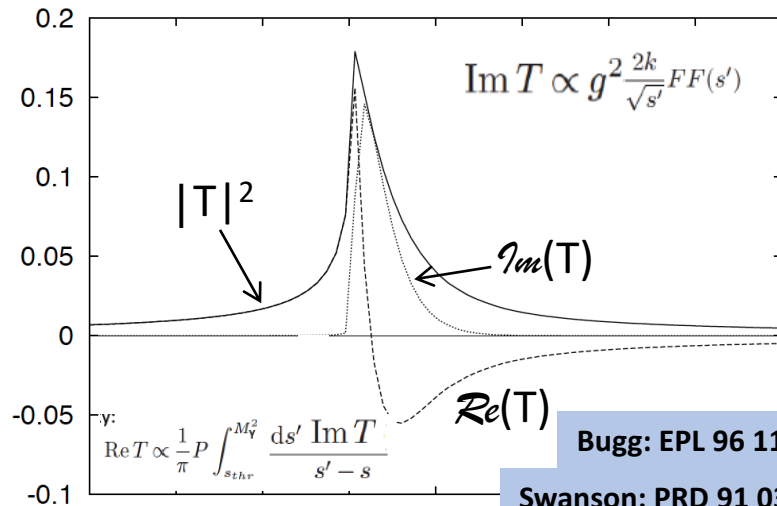
no charged states

decays to S-wave $\oplus$ P-wave preferred



Threshold effects

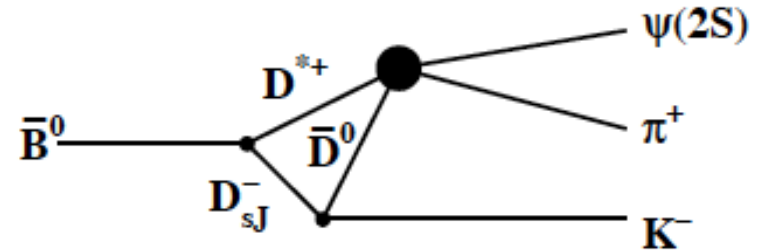
cusps



Bugg: EPL 96 11002 (2011)

Swanson: PRD 91 034009 (2015)

rescattering

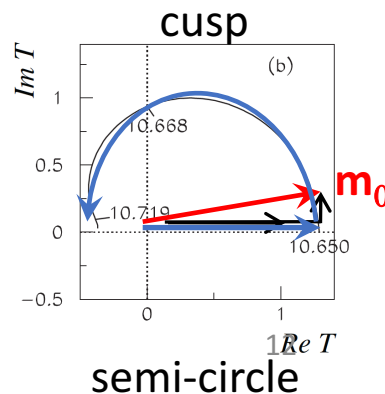


Landau: singular when loop particles are on the mass shell

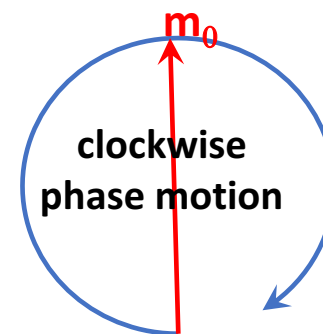
Pakhlov & Uglov, PLB748,183 (2015)

peaks just above threshold: $a^{-1} = \sqrt{2\mu\delta E} < m_\pi \Rightarrow \delta E < \frac{m_\pi^2}{2\mu} \approx 10 \text{ MeV (for } 2\mu = m_D)$

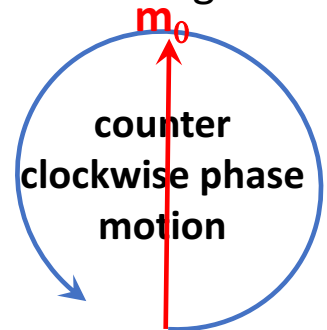
distinctive phase motion:



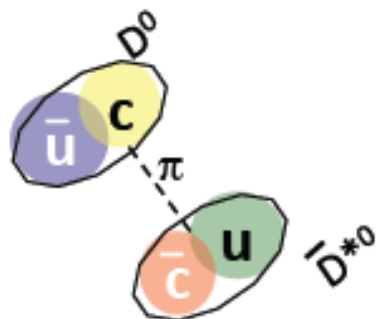
rescattering



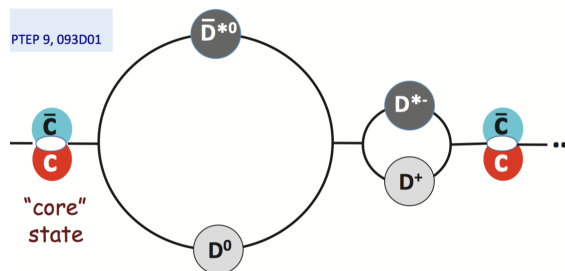
Breit Wigner



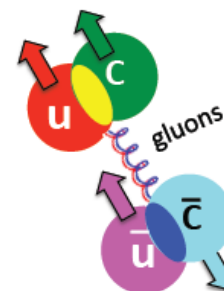
what are they?



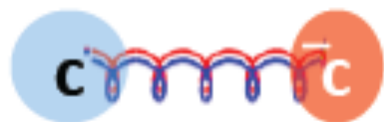
molecules?



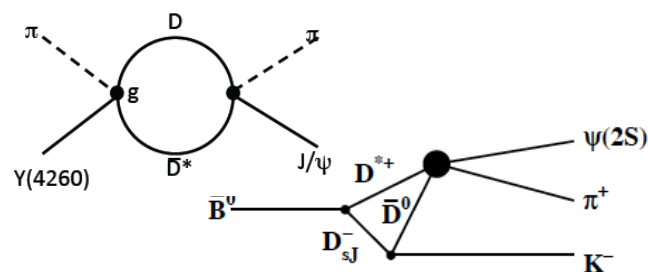
coupled channel system?



QCD tetraquarks?



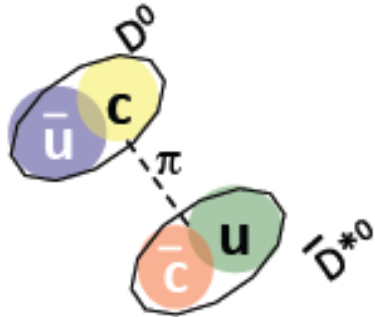
QCD hybrids?



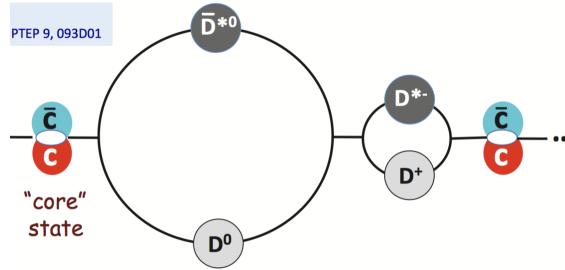
threshold effects?

~~what are they?~~

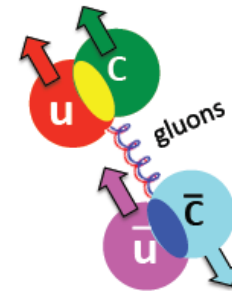
What aren't they?



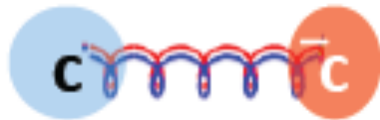
molecules?



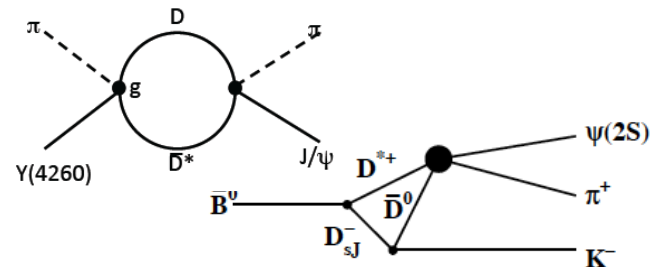
coupled channel system?



QCD tetraquarks?

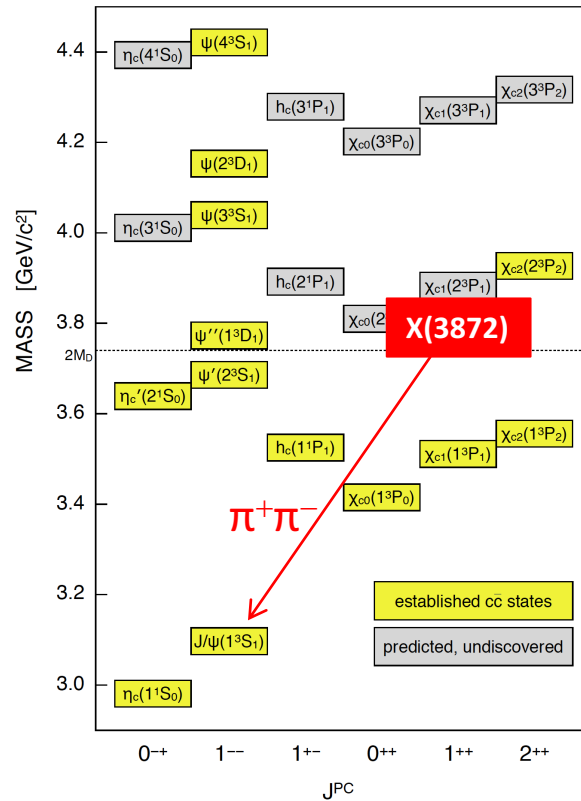


QCD hybrids?



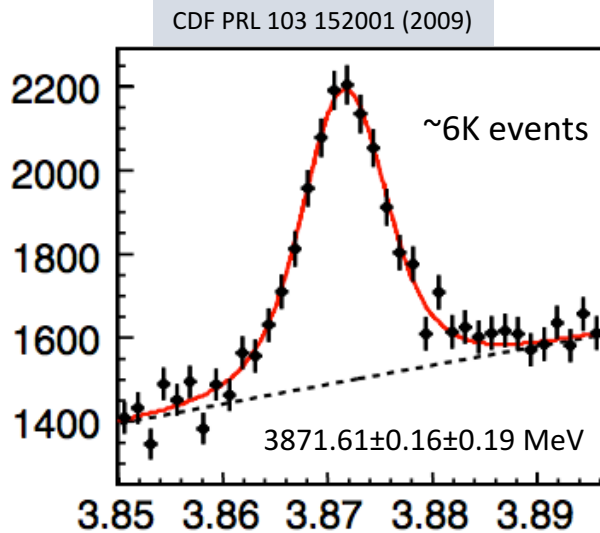
threshold effects?

X(3872)



X(3872) properties

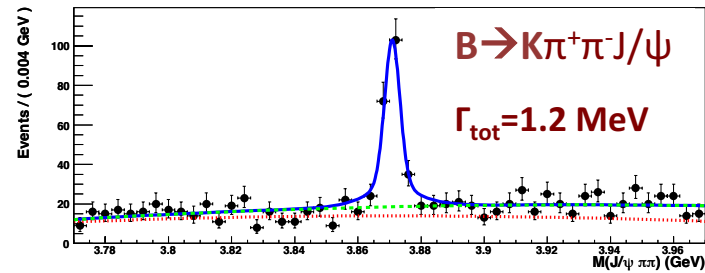
X(3872) & $m_{D^0} + m_{D^{*0}}$
are indistinguishable



PDG17: $M_{X(3872)} = 3871.69 \pm 0.17$
 $m_{D^0} + m_{D^{*0}} = 3871.85 \pm 0.11$

$$"BE" = (m_{D^0} + m_{D^{*0}}) - M_{X(3872)} = 0.16 \pm 0.20$$

narrow width: $\Gamma_{X(3872)} \lesssim \Gamma_{\chi_{c1}}$

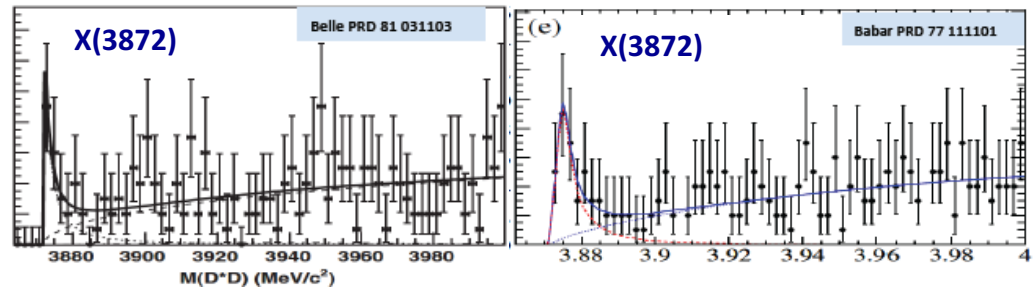


$M(\pi^+ \pi^- J/\psi)$

Belle PRD 84 052004 (2011)

Strongly coupled to $D^0 \bar{D}^{*0}$

$B \rightarrow K D^0 \bar{D}^{*0}$



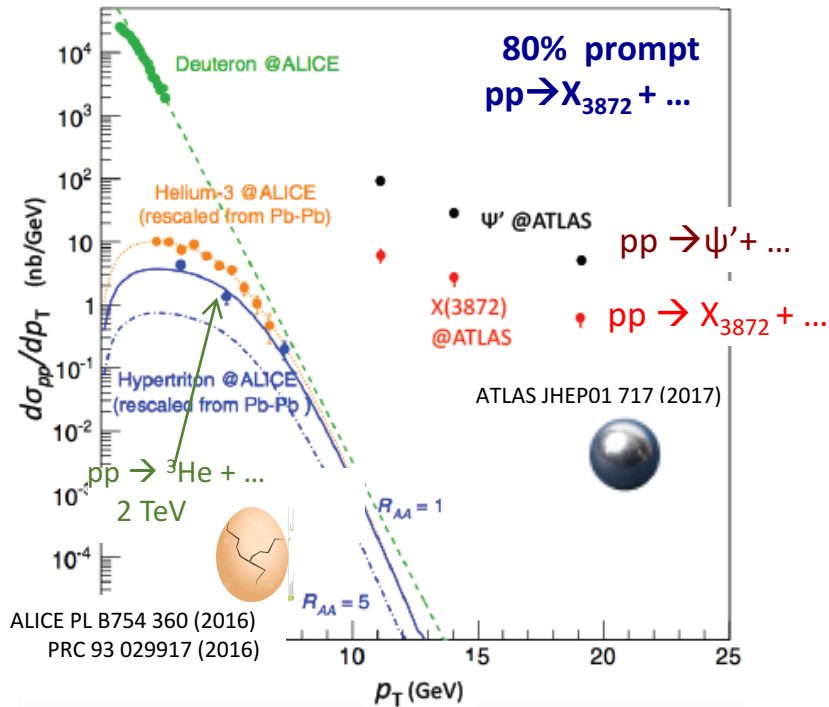
LHCb: $J^{PC} = 1^{++}$

LHCb PRD 92 011102

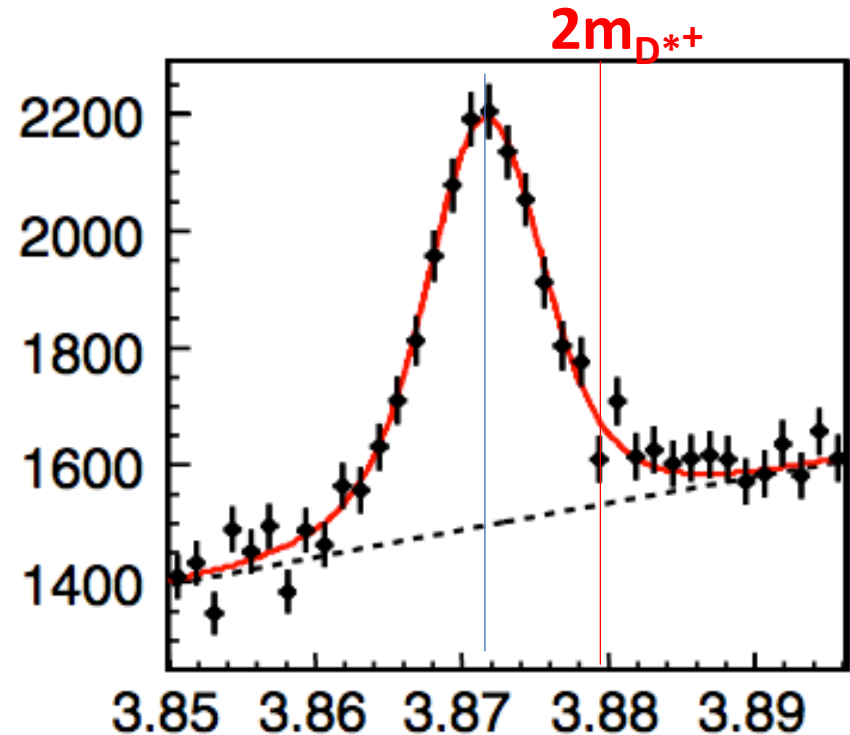
X(3872) = deuteron-like $D^0\bar{D}^{*0}$ molecule?

produced promptly in 7 TeV pp collisions

no sign of it in D^0/D^{*-} or D^+D^{*-}



See Esposito et al., PRD 92 034028 (2015)

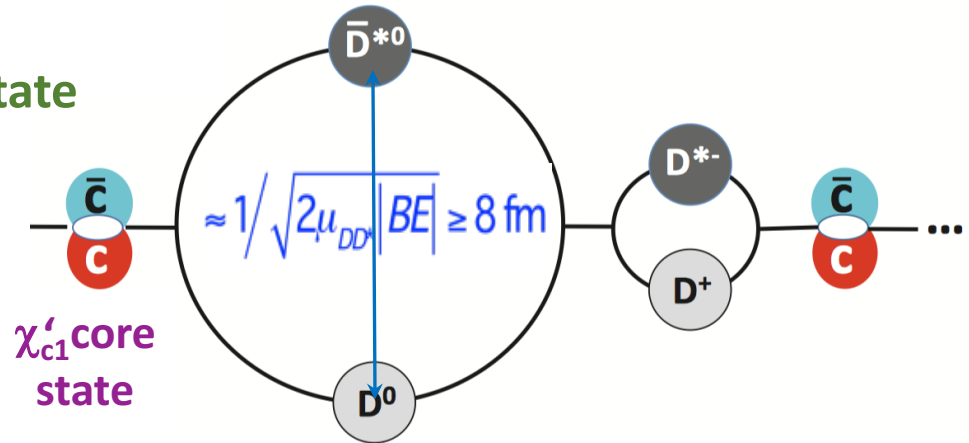


CDF PRL 103 152001 (2009)

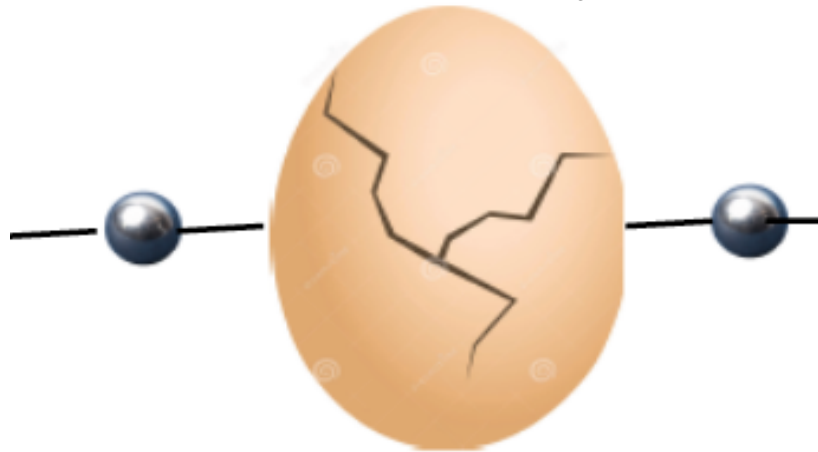
X(3872)=coupled channel state?

$D\bar{D}^* \oplus \chi_{c1}'$ coupled channel state

Specific model by
Takizawa & Takeuchi, PTEP 9, 093D01



produced promptly via χ_{c1}' component



X(3872)

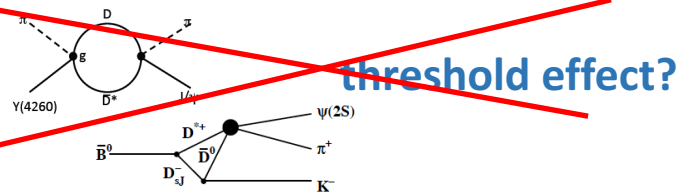
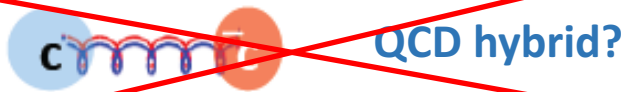
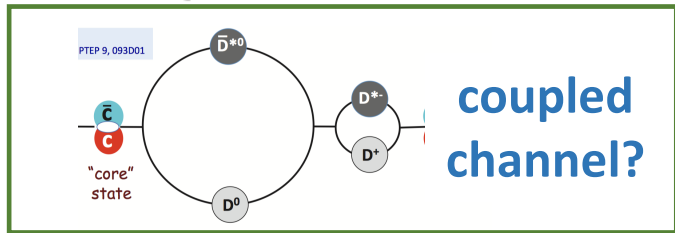
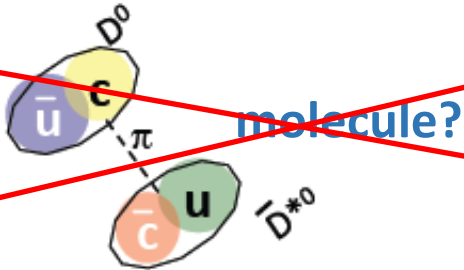
Produced promptly in HE pp collisions
no isospin-related states are seen

good description PTEP 9, 093D01 (2013)

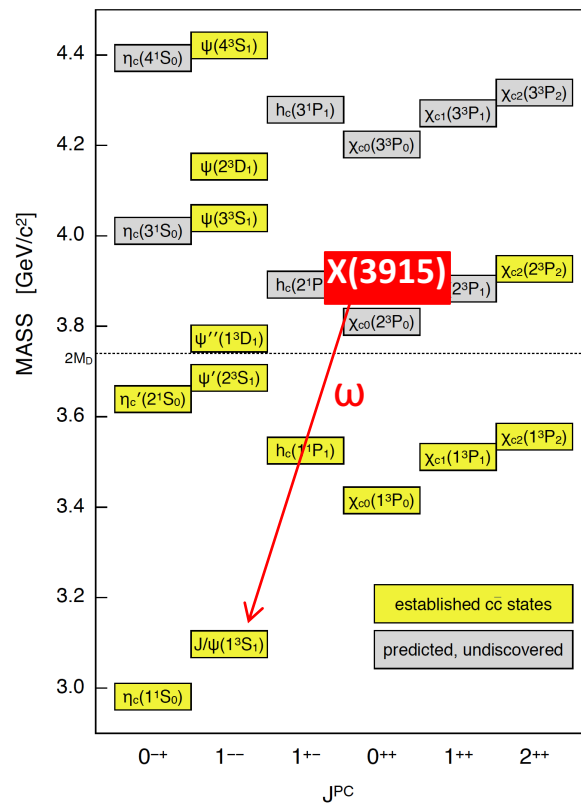
PRD 71 014028 (2005)
no 1^{++} partner states seen

mass is 500 MeV below
LQCD's lightest 1^{++} hybrid

width is too narrow; mass
too close to threshold



X(3915)



X(3915)

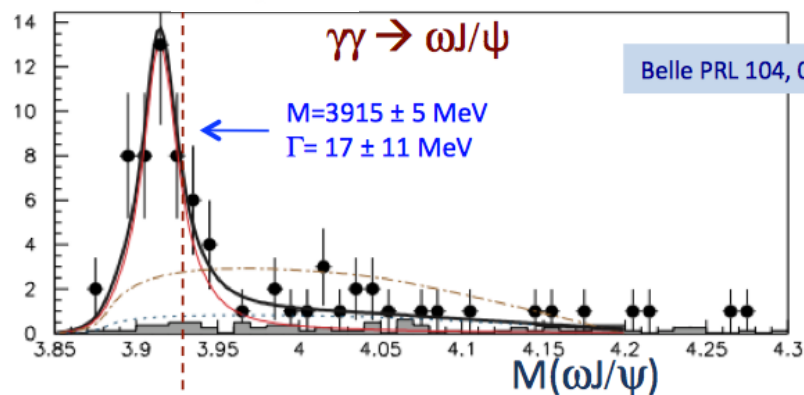
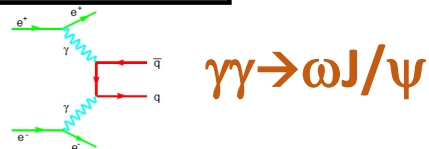
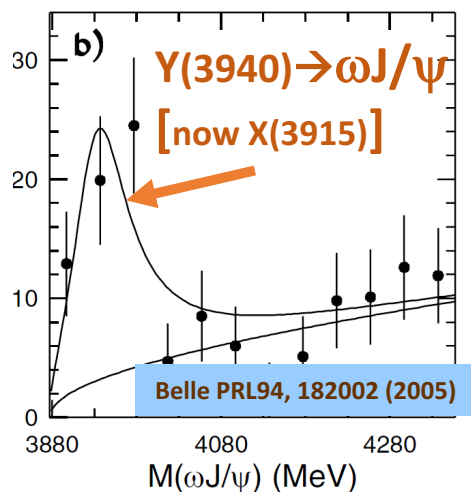
-- seen in 2 production channels by 2 experiments --

PDG 2018: $M_{X(3915)} = 3918 \pm 2 \text{ MeV}$

$\Gamma_{X(3915)} = 20 \pm 5 \text{ MeV}$

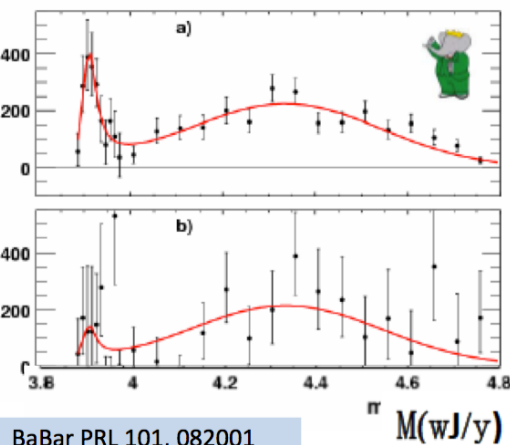
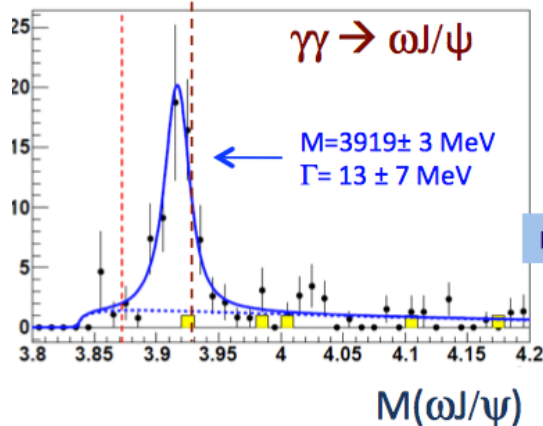
$M_{X(3915)} = 2m_{D^*} - 18 \text{ MeV}$

$B \rightarrow K \omega J/\psi$

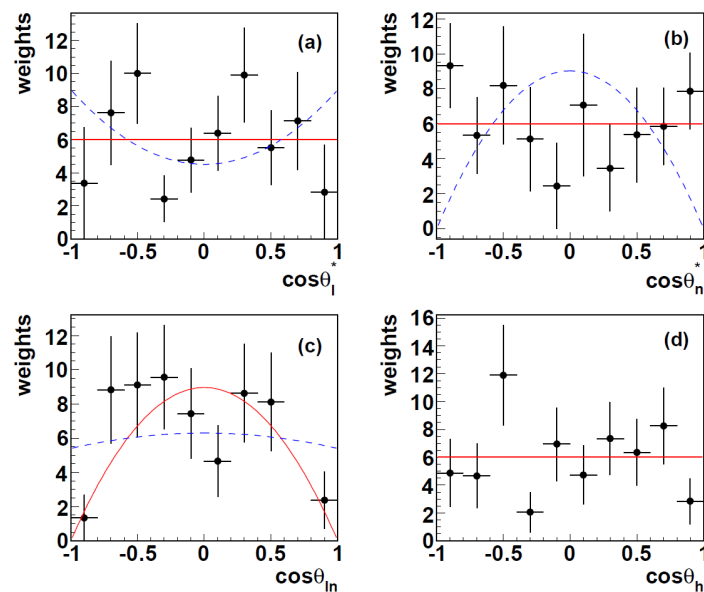
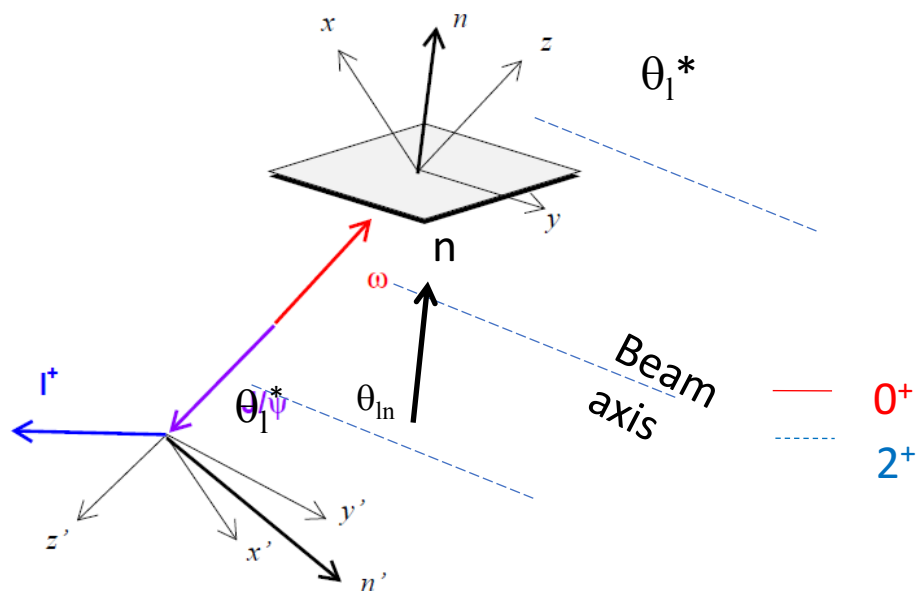


$B^\pm \rightarrow K^\pm \omega J/\psi$

$B^0 \rightarrow K_S \omega J/\psi$



BaBar measurements prefer $J^{PC}=0^{++}$

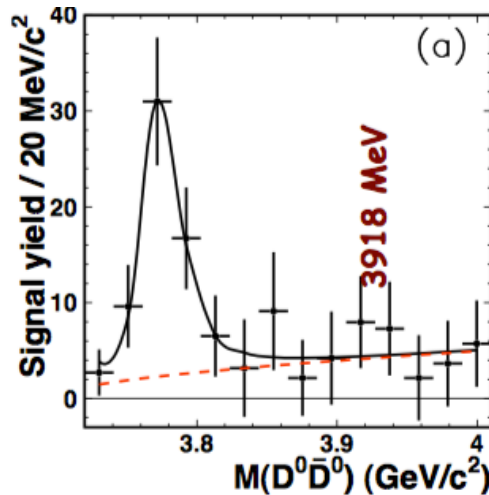


BaBar PRD 86, 072002 (2012)

no sign of $X(3915) \rightarrow D\bar{D}$

-- in either $B \rightarrow K D\bar{D}$ or $\gamma\gamma \rightarrow D\bar{D}$ --

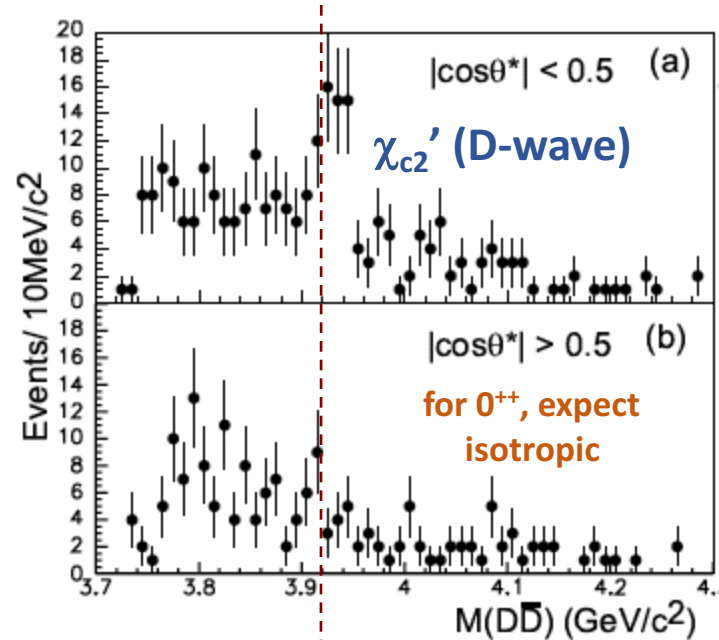
$B \rightarrow K D\bar{D}$ (Belle)



$\Gamma(X_{3915}) \rightarrow D\bar{D} < 1 \text{ MeV}$

J. Brodzicka et al. (Belle) PRD 100, 092001

$\gamma\gamma \rightarrow K D\bar{D}$ (Belle)



3918 MeV

Belle PRL 89, 102001 (2002)

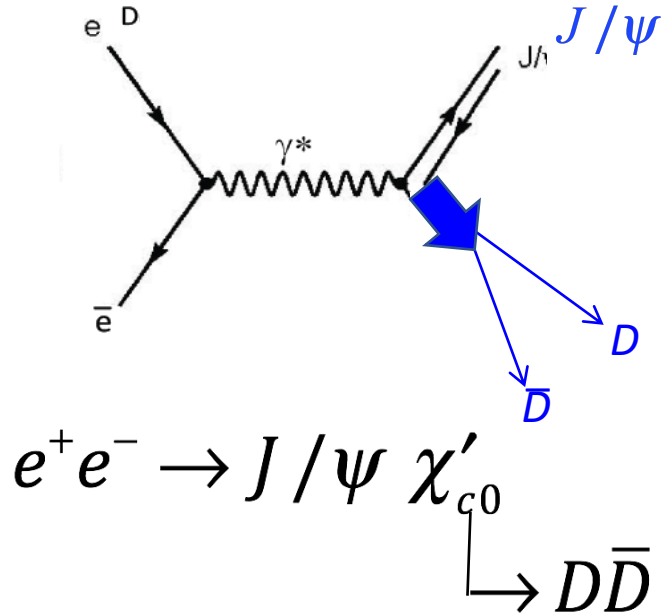
$X(3915) \rightarrow \omega J\psi /$ is
OZI-rule violating
for a $c\bar{c}$ meson

$$\frac{Bf(X(3915) \rightarrow D^0 \bar{D}^0)}{Bf(X(3915) \rightarrow \omega J / \psi)} < 1.2$$

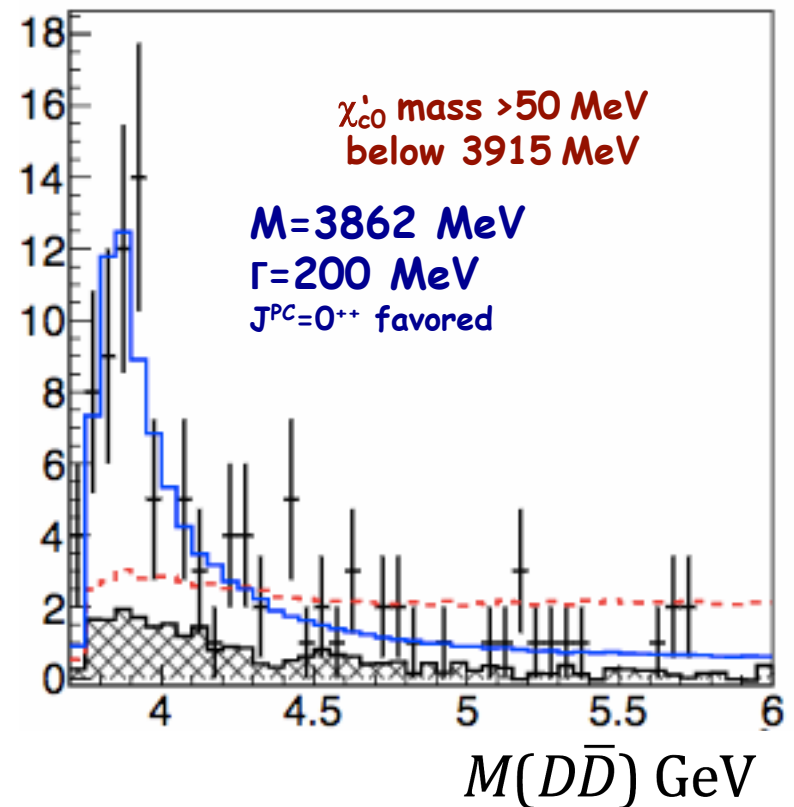
SLO PRD91, 057501 (2015)

& it isn't the χ'_{c0} charmonium state

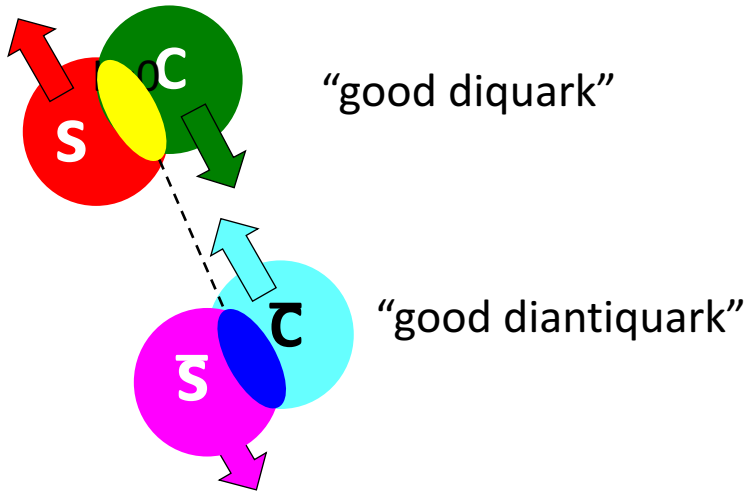
Belle found the “real” χ'_{c0} last year



K. Chilikin et al. (Belle) PRD 95, 092003c(2017)

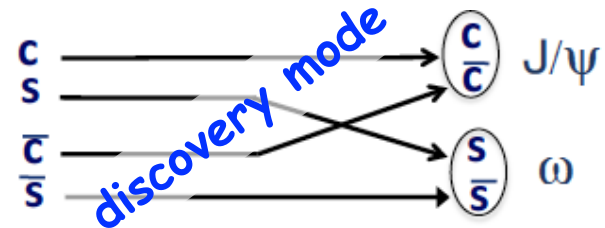


a $J^{PC}=0^{++}$ $cs\bar{c}\bar{s}$ tetraquark?

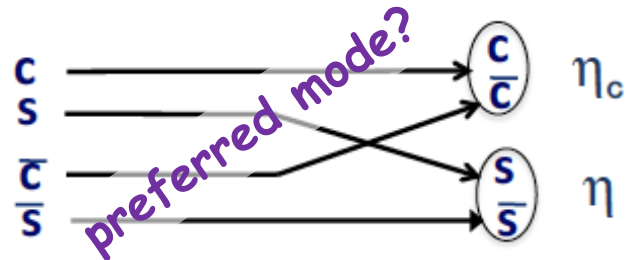


no "fall-apart" decays to $D\bar{D}$

OZI-allowed decay processes:



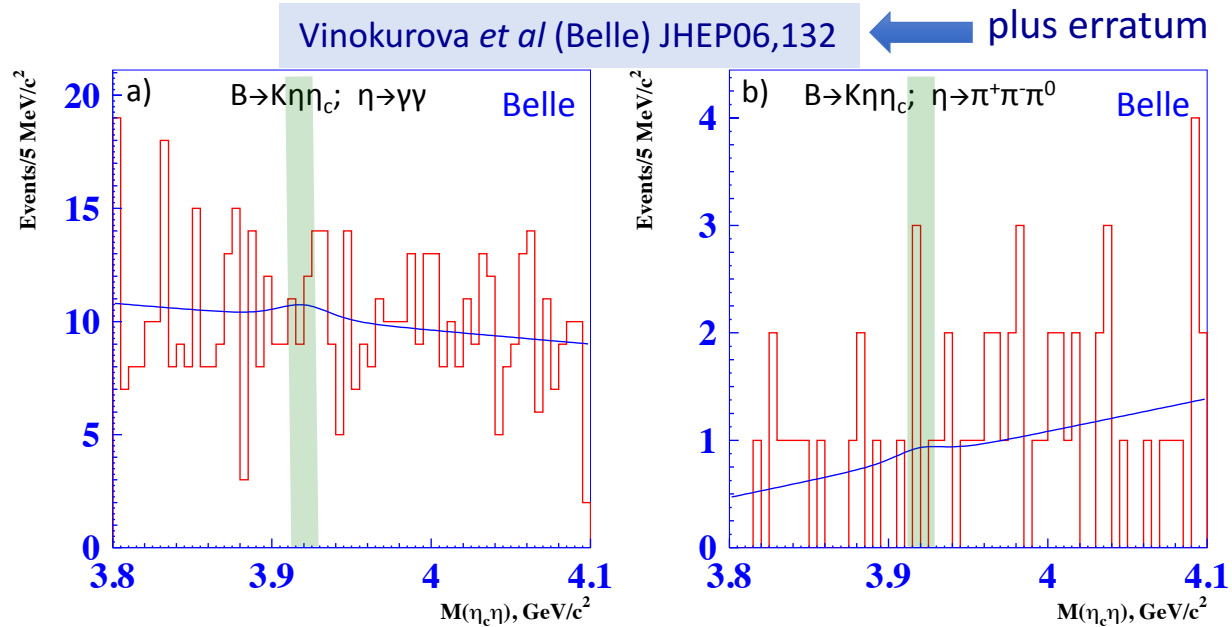
ω has a small ($\approx 3\%$) $s\bar{s}$ content



η has a large ($\approx 40\%$) $s\bar{s}$ content

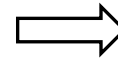
Expect:
$$\frac{Bf(X(3915)) \rightarrow \eta\eta_c}{Bf(X(S915)) \rightarrow \omega J/\psi} \gg 1$$

No sign of $X(3915) \rightarrow \eta_c \eta$



$$\mathcal{B}(B^+ \rightarrow K^+ X(3915)) \times \mathcal{B}(X \rightarrow \eta \eta_c) < 4.7 \times 10^{-5}$$

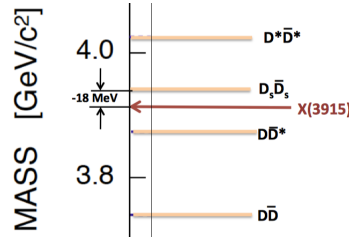
$$\mathcal{B}(B^+ \rightarrow K^+ X(3915)) \times \mathcal{B}(X \rightarrow \omega J/\psi) = 3.0_{-0.7}^{+0.9} \times 10^{-5}$$



$$\frac{Bf(X \rightarrow \eta_c \eta)}{Bf(X \rightarrow J/\psi \omega)} < 2$$

not good for a tetraquark interpretation

X(3915)



$D_s\bar{D}_s$ B.E. (≈ 18 MeV) large
 $D^*\bar{D}^*$ B.E. (≈ 100 MeV) *very* large
 π -exchange forbidden for $D_s\bar{D}_s$
 but see: PRD91 114014 (2015)

no nearby $D\bar{D}$ threshold
 no candidate $c\bar{c}$ core state

possible $[cs][\bar{c}\bar{s}]$ tetraquark PRD93, 094024 (2016)
 -- no sign of $X(3915) \rightarrow \eta\eta_c$ or partner states

mass is 500 MeV below
 LQCD's lightest 0^{++} hybrid

mass is *below* the only
 nearby threshold

molecule?

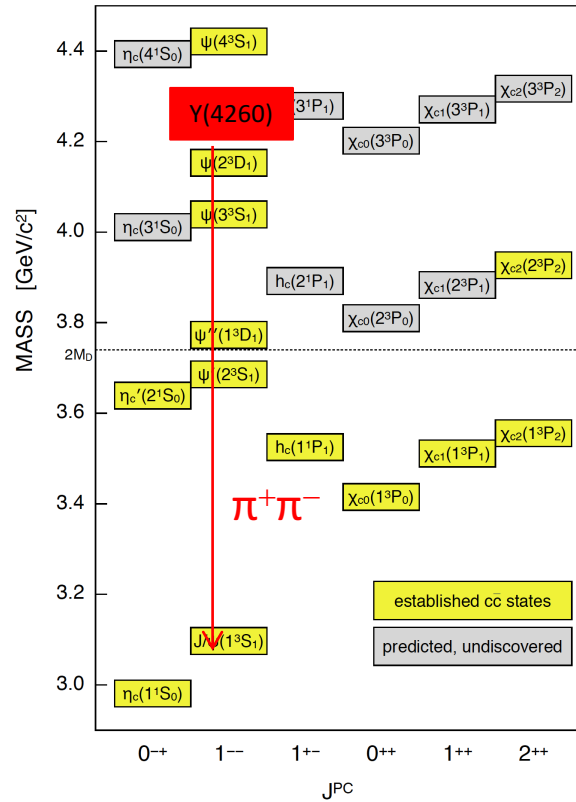
coupled
 channels?

QCD tetraquark?

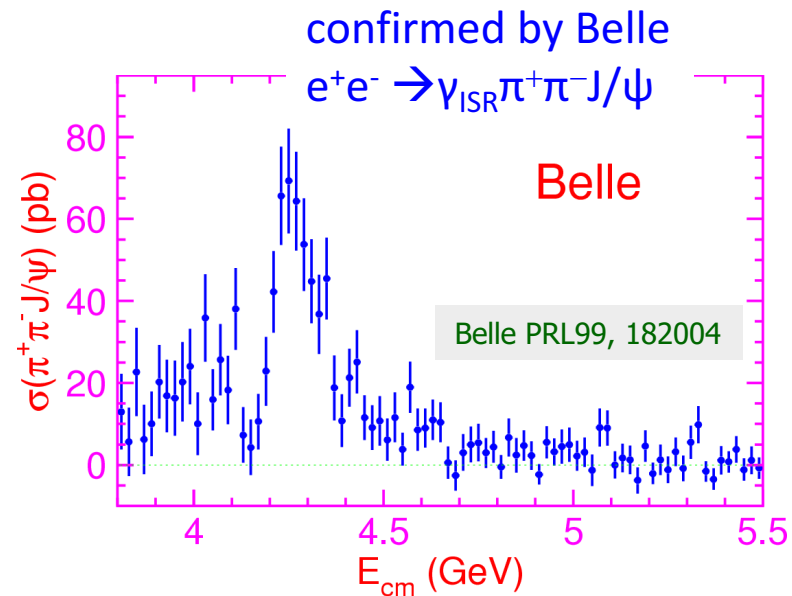
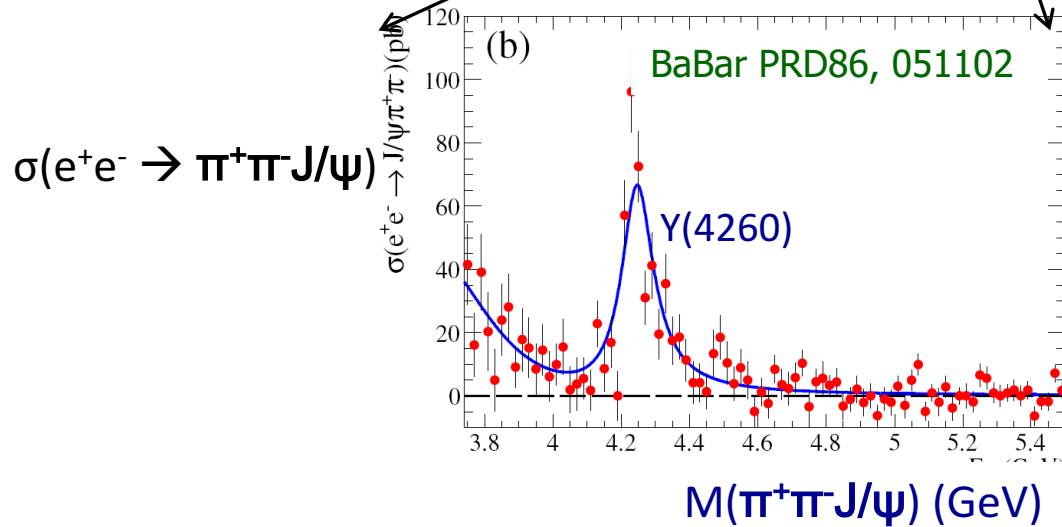
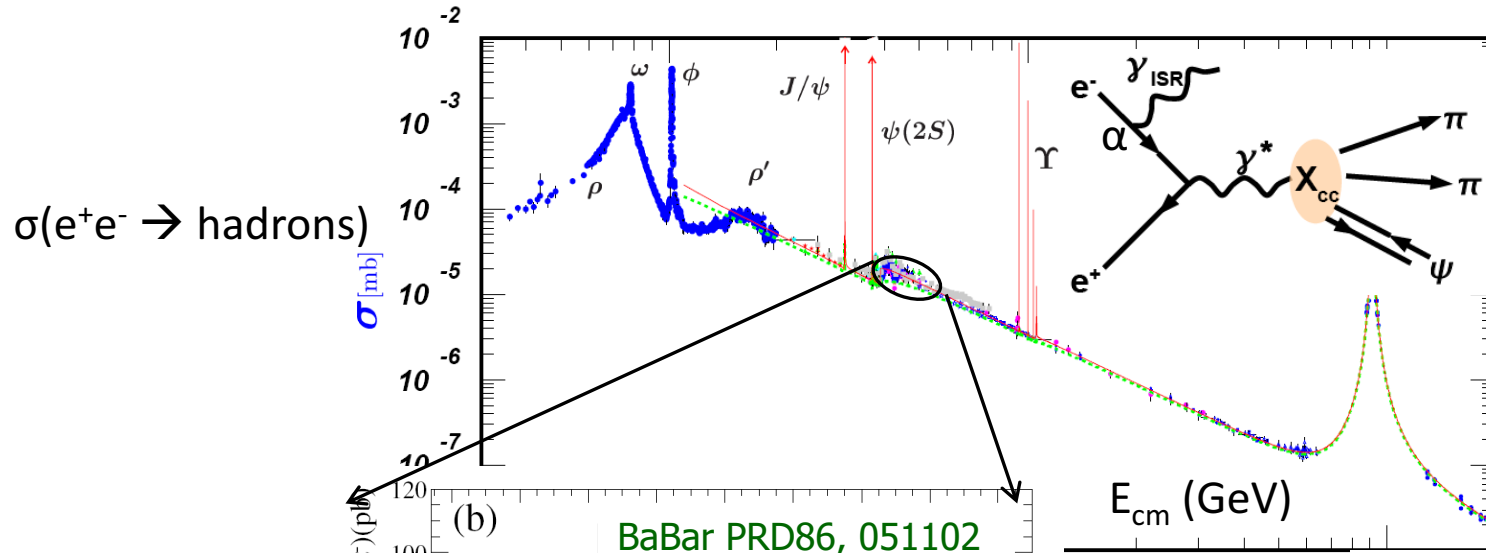
QCD hybrid?

threshold effect?

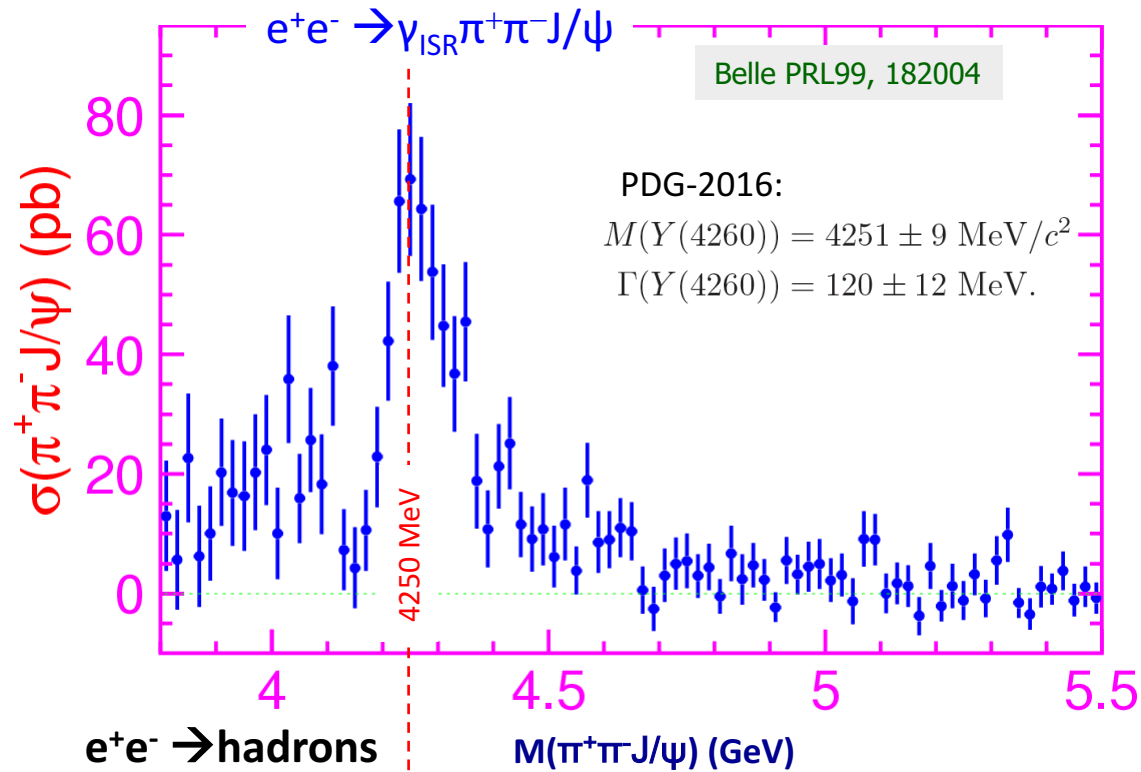
$\Upsilon(4260)$



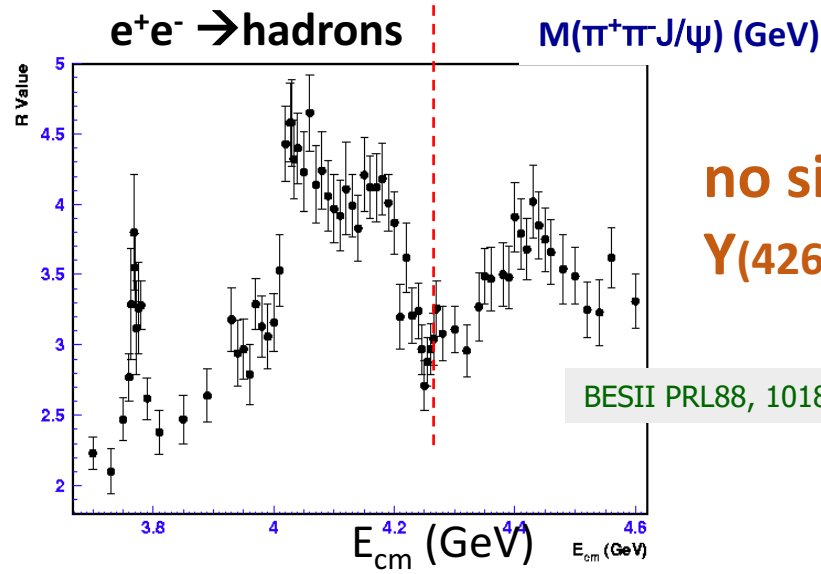
found by BaBar in $e^+e^- \rightarrow \gamma_{\text{ISR}}\pi^+\pi^-J/\psi$



peculiar fact 1: $\pi\pi J/\psi$ peak at a dip in R_{had}



$\Gamma(\pi^+\pi^- J/\psi)$ is large, but
should be OZI suppressed if $c\bar{c}$



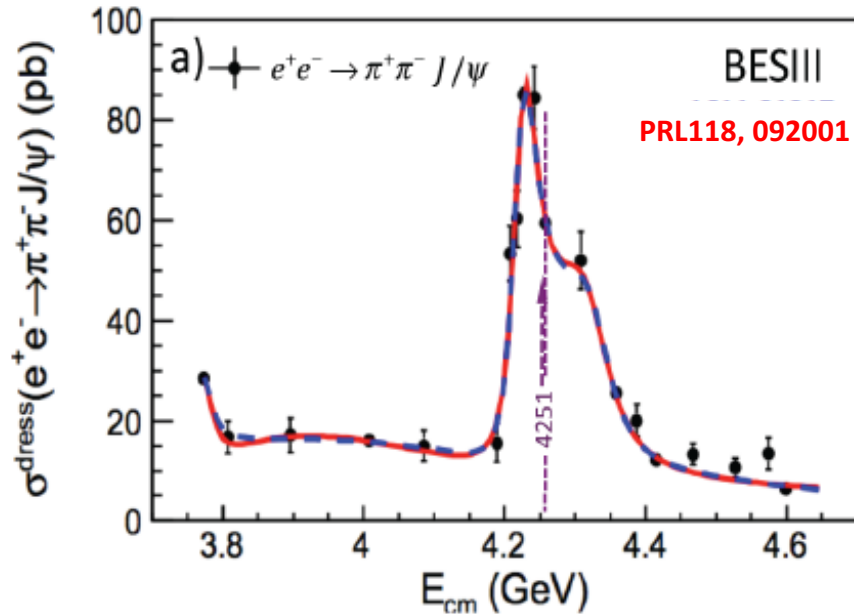
no sign of
 $Y(4260) \rightarrow D^{(*)} \bar{D}^{(*)}$

BESII PRL88, 101802

peculiar fact 2: $Y(4260) \rightarrow \pi\pi J/\psi$ is 2 peaks

-- one at ≈ 4220 MeV & one at ≈ 4320 MeV --

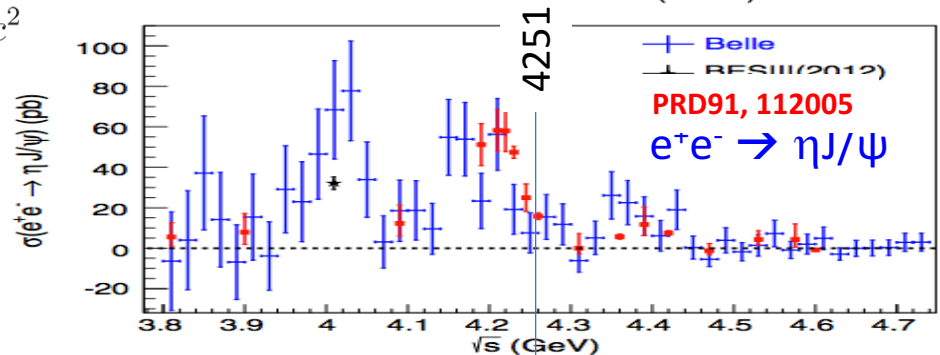
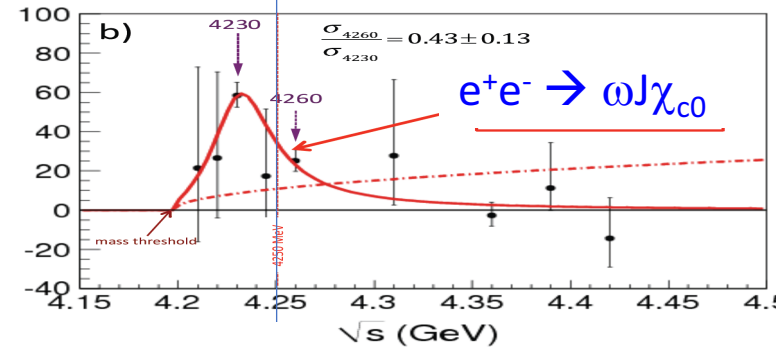
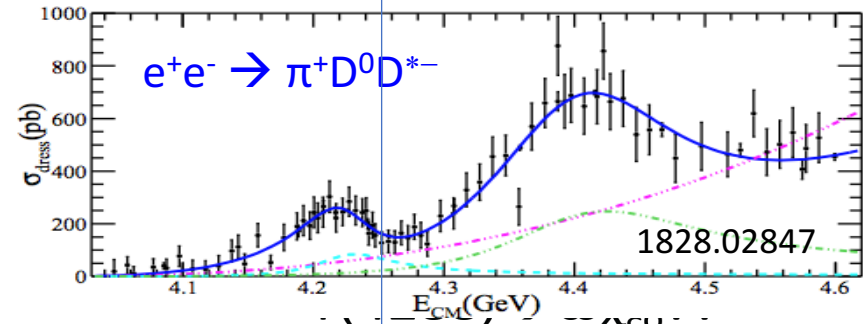
2 peaks in $e^+e^- \rightarrow \pi^+\pi^- J/\psi$



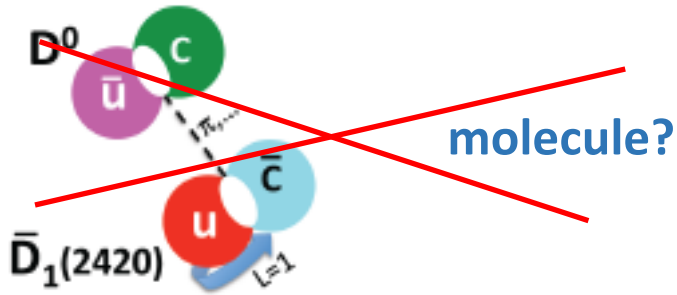
$$M_1 = 4220 \pm 4 \text{ MeV}/c^2 \quad M_2 = 4320 \pm 13 \text{ MeV}/c^2$$

$$\Gamma_1 = 44 \pm 5 \text{ MeV} \quad \Gamma_2 = 101^{+27}_{-22} \text{ MeV}$$

only the lower peak seen in other channels

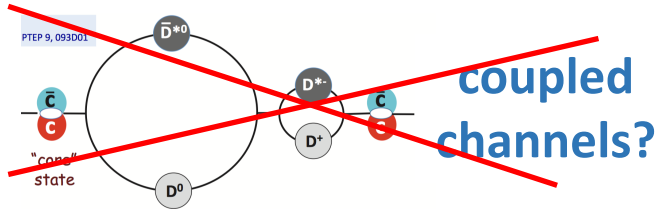


Y(4260)



DD₁(2460) BE (≈ 65 MeV) is very large

-- but see PRD 90, 074039



no candidate $c\bar{c}$ state or nearby $D\bar{D}$ threshold

-- but see PRD 94, 054035



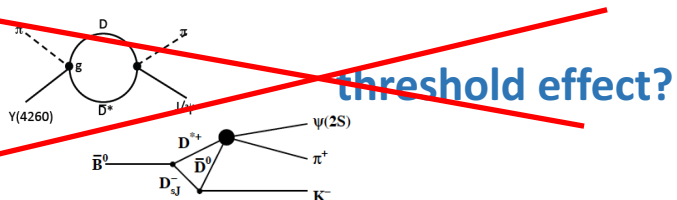
$[cq][\bar{c}\bar{q}]$ tetraquark

-- but no partner states have been identified



PLB 631 164 (2005)

≈ 80 MeV below LQCD's lightest 1^{--} hybrid

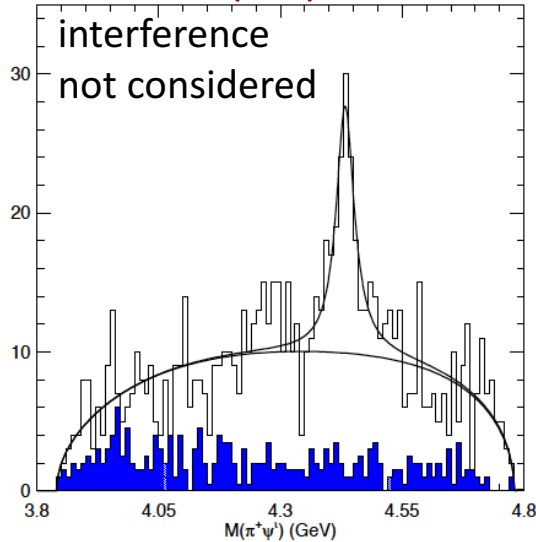


mass is *below* the only relevant threshold

What about the charged Z states?

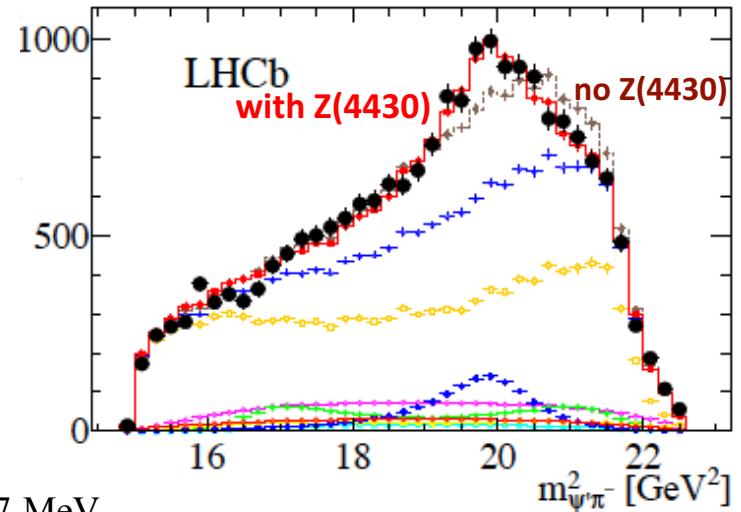
Z(4430) found by Belle; confirmed by LHCb

Belle: PRL 100 142001 (2007)



LHCb: PRL 112 222002 (2014)

no K^* vetoes

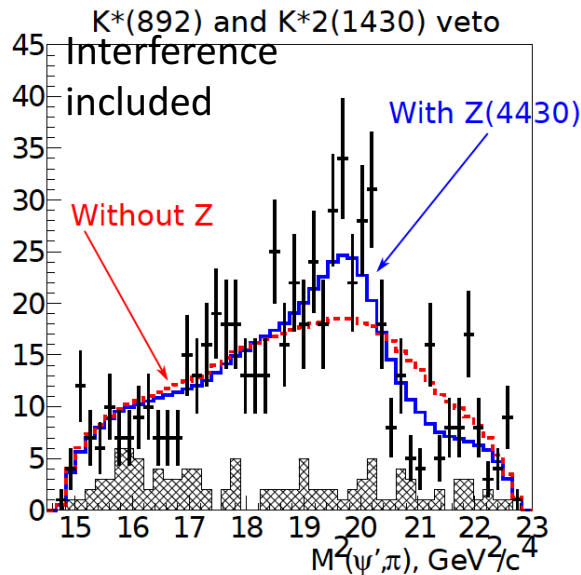


PDG 2018 average

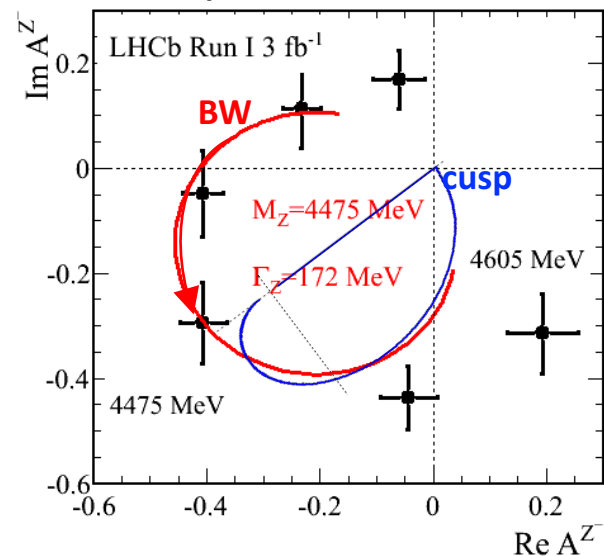
$$M(Z(4430)) = 4478 \pm 17 \text{ MeV}$$

$$\Gamma(Z(4430)) = 181 \pm 31 \text{ MeV}$$

Belle: PRD 88 074026 (2013)



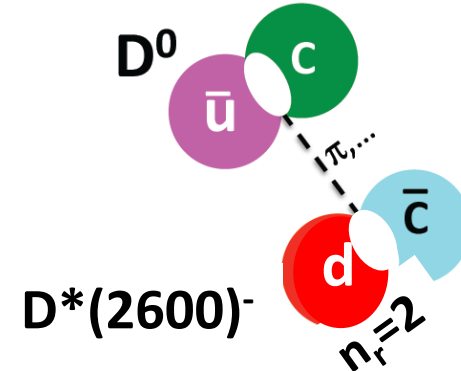
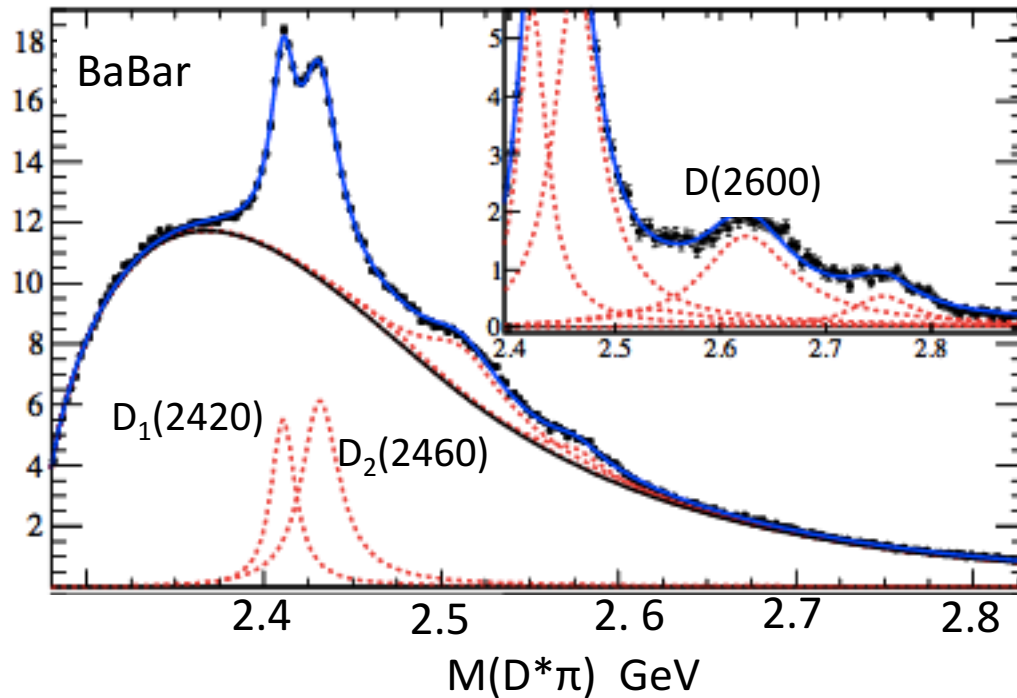
BW-like phase motion confirmed



$D\bar{D}^*(2S)$ molecule

-- ($D^*(2S)$ =radially excited D^* ?) --

BaBar: Phys. Rev. D82, 111101

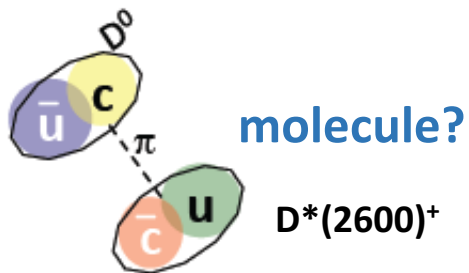


$$M(D(2600)) = 2609 \pm 4 \text{ MeV}$$

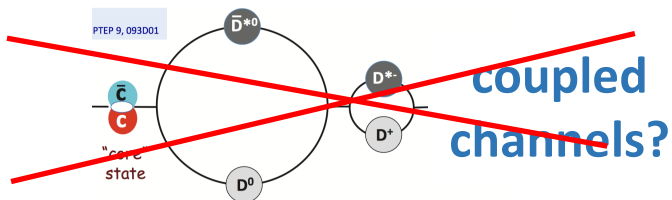
$$\Gamma(D(2600)) = 93 \pm 15 \text{ MeV}$$

$$\text{“B.E.”} = (m_{D^+} + m_{D^*(2S)}) - M_{Z(4430)} \approx 0 \pm 18 \text{ MeV}$$

Z(4430)



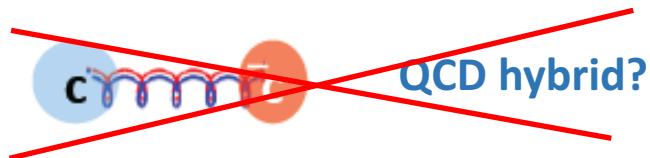
$\Gamma(Z(4430)) \approx 180 \text{ MeV}$ & $\Gamma(D^*(2600)) \approx 100 \text{ MeV}$
too short-lived for a molecule?



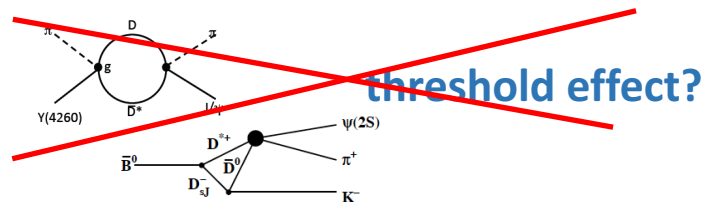
no charged cc core states



PRD 89 114010 (2012) / PRL 113, 112001 (2014)
no partner states seen



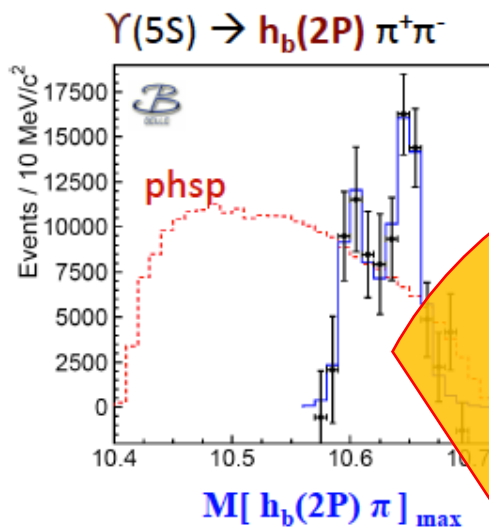
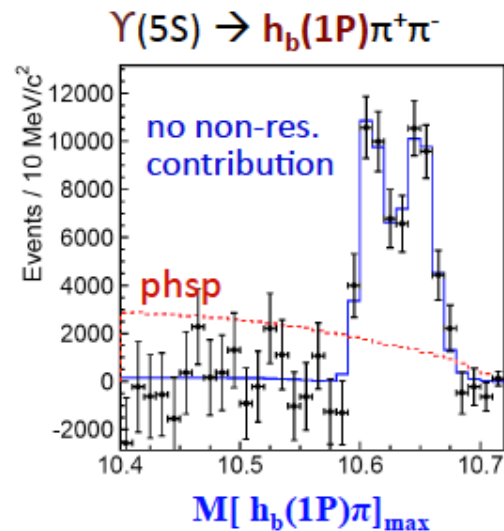
no charged cc-gluon states



Argand plot favors BW-like phase motion

Z_b states discovered by Belle

Belle: PRL108, 232001 (2012)

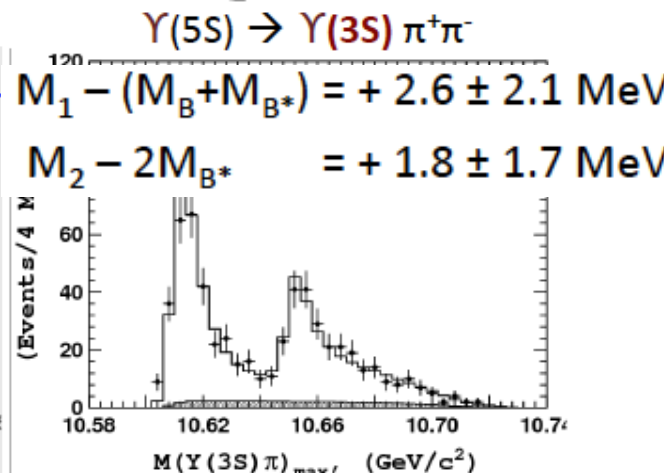
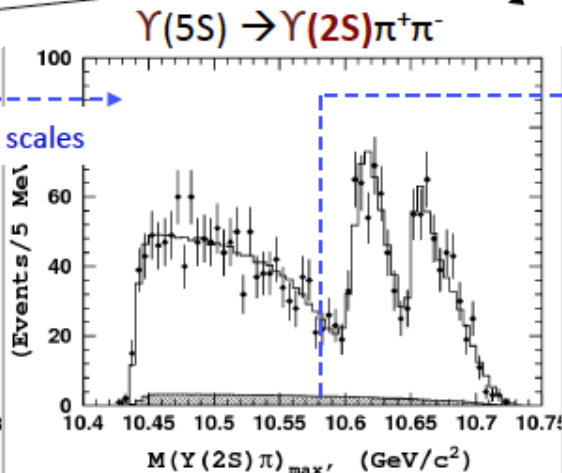
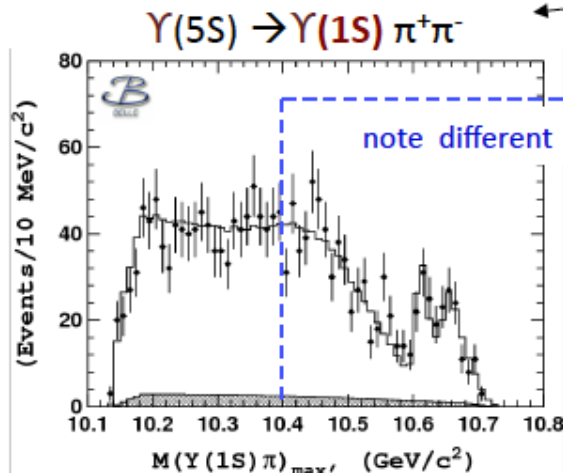


Z_1 & Z_2 are just above the BB^* & B^*B^* thresholds
 where CUSP-like states are expected

$$M_1 - (M_B + M_{B^*}) = +2.6 \pm 2.1 \text{ MeV}$$

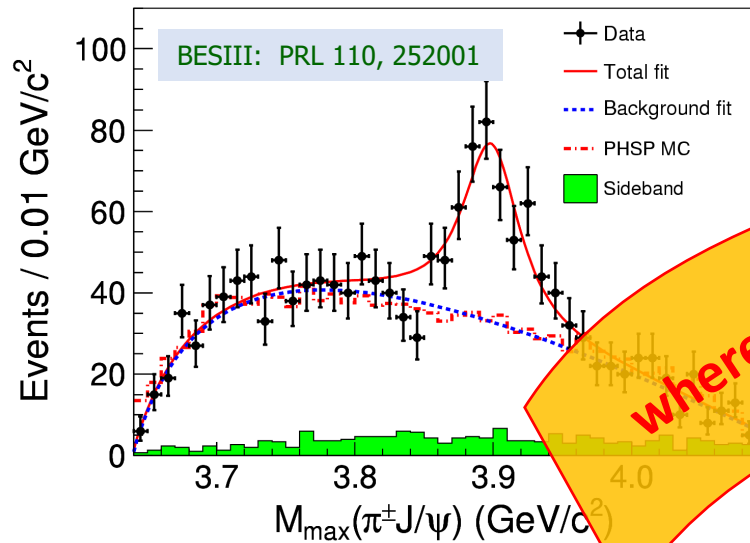
$$M_2 - 2M_{B^*} = +1.8 \pm 1.7 \text{ MeV}$$

Dalitz plot analysis



Z_c states discovered by BESIII & Belle

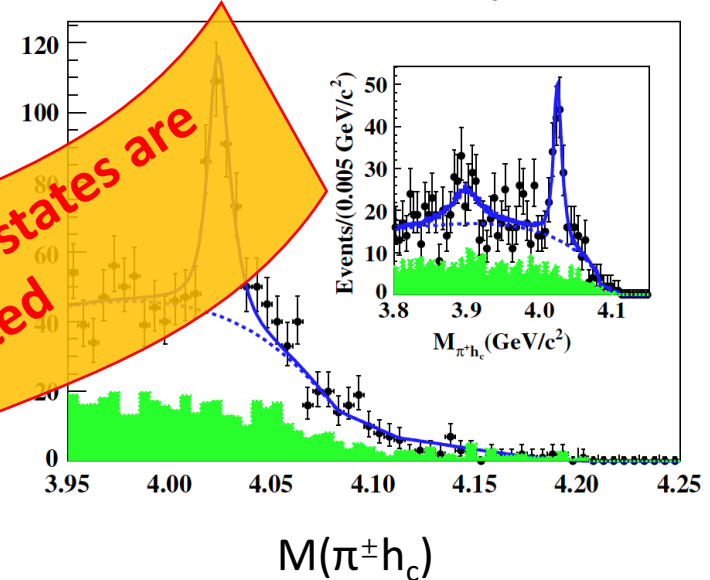
$\Upsilon(4260) \rightarrow \pi^+ \pi^- J/\psi$



$12 \pm 3 \text{ MeV}$ above $D^0 D^{*-}$ thresh.

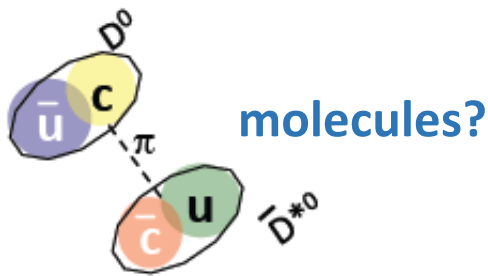
Also seen by Belle:
BESIII: PRL110, 252002

$\Upsilon(4260) \rightarrow \pi^+ \pi^- h_c$



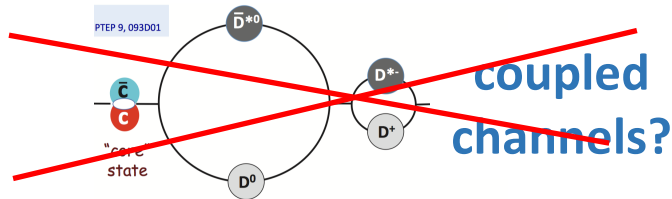
$5.6 \pm 2.8 \text{ MeV}$ above $D^{*0} D^{*-}$ thresh.

$Z_c(3900)/Z_c(4020)$ & $Z_1(10610)/Z_2(10650)$



molecules?

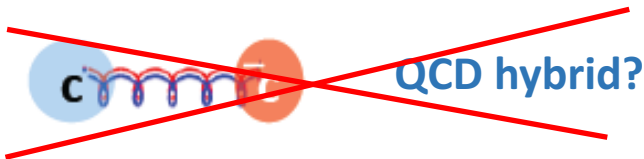
just above DD^*/D^*D^* (BB^*/B^*B^*) thresholds
-- but no phase motion measurements



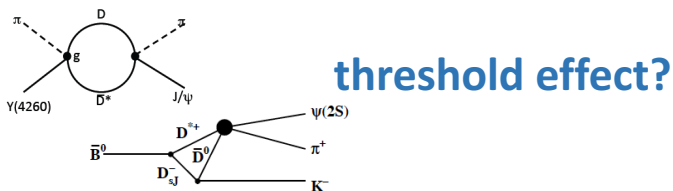
no charged cc core states



PRD87 111102 (2013)
no partner states seen



no charged cc-gluon states



similar to expectations for cusps
EPL 96 11002 (2011) / PRD 91 034009 (2015)

-- Argand plots are needed

Scorecard

state	Molecule?	Coupled-channel	Tetraquark?	Hybrid?	Threshold effect?
X(3872)	problem with pp production	Yes	partners not seen	$m \approx 500$ MeV too low	narrow/ at threshold
X(3915)	no $1-\pi$ exchange allowed	no $c\bar{c}$ core or $D\bar{D}$ thresh.	partners not seen	$m \approx 500$ MeV too low	below threshold
Y(4260) (Y(4220))?	$D \oplus \bar{D}_1(2420)$? B.E. ≈ 65 MeV	no $c\bar{c}$ core or $D\bar{D}$ thresh.	partner not seen	$m \approx 65$ MeV too low	no nearby threshold
Z(4430)	$D \oplus \bar{D}^*(2S)$? short lifetimes	no $c\bar{c}$ core state	partner not seen	electrically charged	below threshold
$Z_c(3900)$ $Z_c(4020)$	≈ 7 MeV above DD^* (D^*D^*) threshold	no $c\bar{c}$ core state	partner not seen	electrically charged	need Argand plot
$Z_1(10610)$ $Z_2(10650)$	≈ 2 MeV above BB^* (B^*B^*) threshold	no $c\bar{c}$ core state	partner not seen	electrically charged	need Argand plot

only the X(3872) has a clear assignment

Comments:

the X(3872) seems unique & not closely related to the other XYZ states

QCD-tetraquark model can account for everything & predict nothing

A “deuson-like” bound molecule has not yet been seen

Y(4220) is the only XYZ hybrid possibility, but this assignment is not compelling

Comments:

the $X(3872)$ seems unique & not closely related to the other XYZ states

QCD-tetraquark model can account for everything & predict nothing

A “deuson’-like bound molecule has not yet been seen

$Y(4220)$ is the only XYZ hybrid possibility, but this assignment is not compelling

We need a new idea

to do list for experimenters:

are $X(3915)$ seen in $B \rightarrow K\omega J/\psi$ & $X(3915)$ seen in $\gamma\gamma \rightarrow \omega J/\psi$ the same state?
-- need separate J^{PC} measurements

is $Bf(X(3915) \rightarrow \eta\eta_c) < Bf(X(3915) \rightarrow \omega J/\psi)$?
-- If so, it's bad for the QCD-tetraquark model

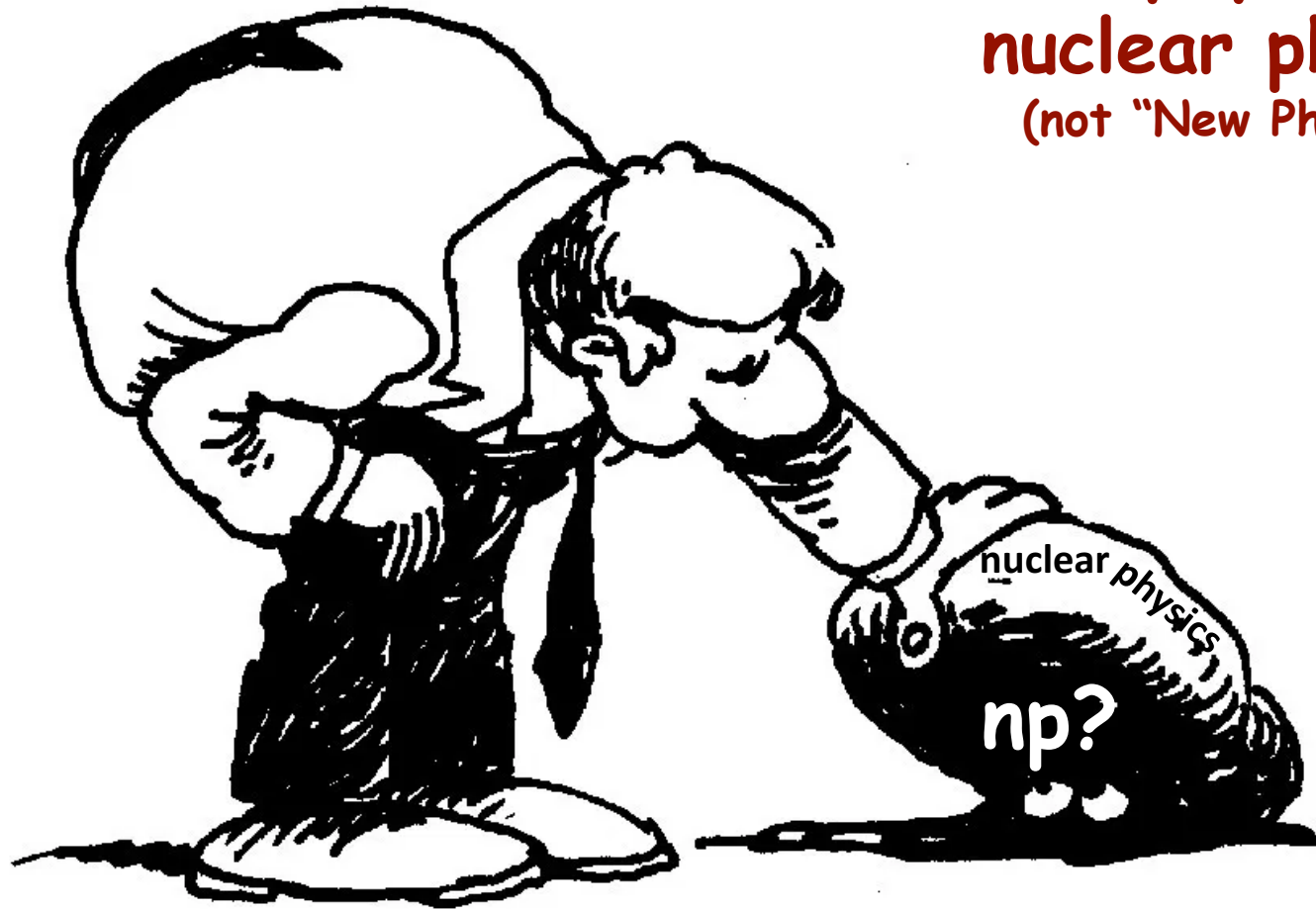
Argand plots for the Z_c ($Z_{1,2}$) states are desperately needed

$Bf(B \rightarrow KZ_c(3900/4020))=?$; $Bf(B \rightarrow KY(4220))=?$

time-like baryon form-factors from BaBar, CMD3 and BESIII

time-like baryon form-factors from BaBar, CMD3 and BESIII

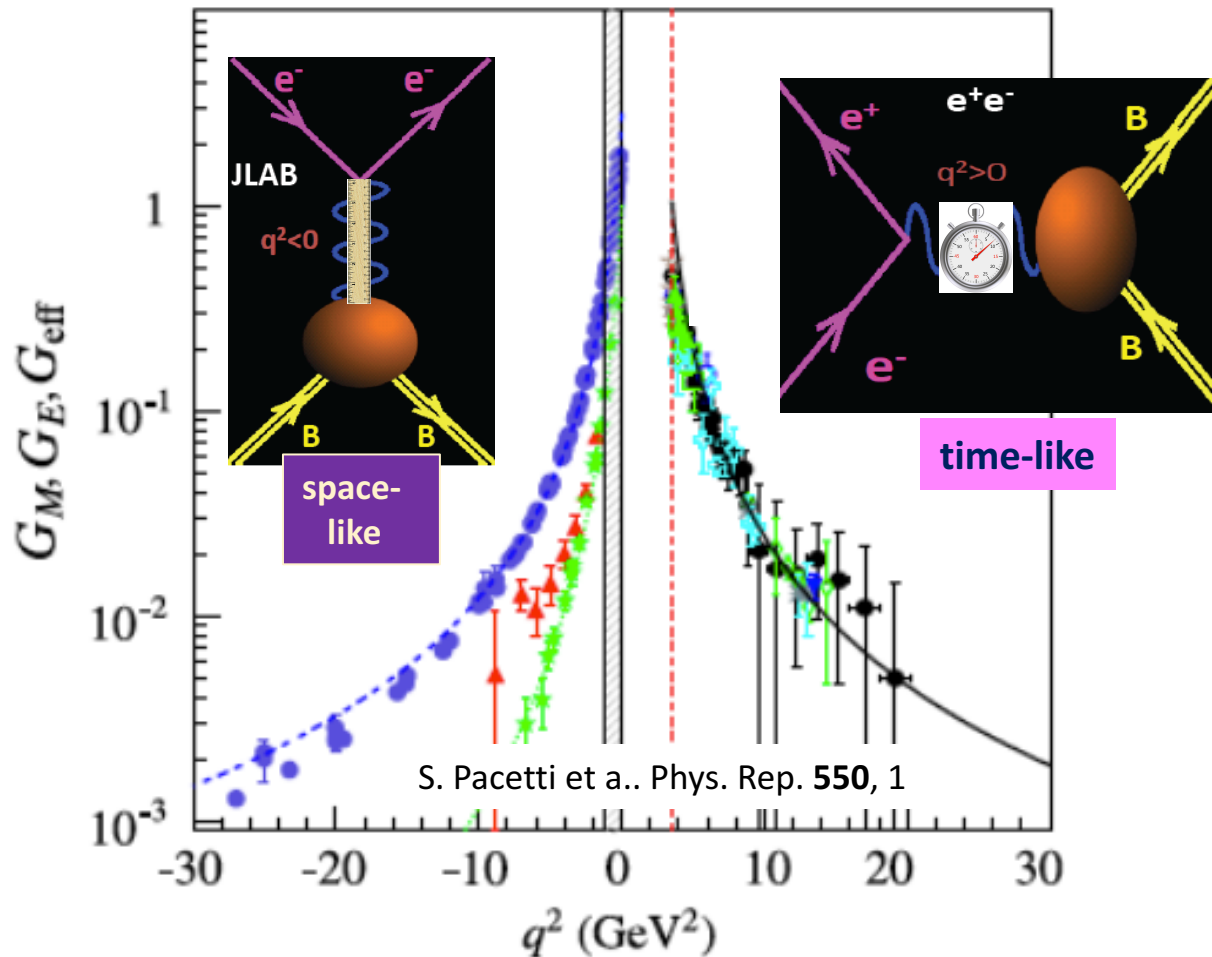
new physics in
nuclear physics?
(not "New Physics")



Time-like & space-like form-factors

Crossing symmetry:

$$\langle N(p') | j^\mu | N(p) \rangle \rightarrow \langle \bar{N}(p') N(p) | j^\mu | 0 \rangle$$



$e^+e^- \rightarrow B\bar{B}$

-- formulae & definitions --

Sachs form factors

$$G_E = F_1 + \frac{q^2}{4M^2} F_2$$

$$G_M = F_1 + F_2$$

$$G_E(0) = Q_N$$

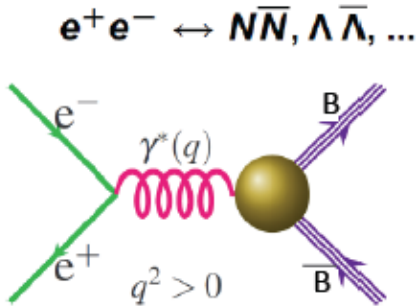
$$G_M(0) = \mu_N$$

Born cross section:

time-like "Sachs" form-factors

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4m_{B\bar{B}}^2} \left[(1 + \cos^2 \theta) |G_M(m_{B\bar{B}})|^2 + \frac{1}{\tau} \sin^2 \theta |G_E(m_{B\bar{B}})|^2 \right]$$

$$\tau = \frac{m_{B\bar{B}}^2}{4M_B^2} \quad \beta = \sqrt{1 - \frac{1}{\tau}}$$



$e^+e^- \rightarrow B\bar{B}$

Sachs form factors

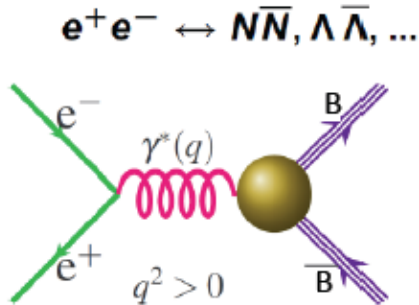
$$G_E = F_1 + \frac{q^2}{4M^2} F_2$$

$$G_M = F_1 + F_2$$

$$\begin{aligned} G_E(0) &= Q_N \\ G_M(0) &= \mu_N \end{aligned}$$

-- formulae & definitions --

Born cross section:



time-like "Sachs" form-factors

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4m_{B\bar{B}}^2} \left[(1 + \cos^2 \theta) |G_M(m_{B\bar{B}})|^2 + \frac{1}{\tau} \sin^2 \theta |G_E(m_{B\bar{B}})|^2 \right]$$

$$\tau = \frac{m_{B\bar{B}}^2}{4M_B^2} \quad \beta = \sqrt{1 - \frac{1}{\tau}}$$

Coulomb enhancement factor

$$C_{\text{charged}} = \frac{\pi\alpha / \beta}{1 - \exp(-\pi\alpha / \beta)} \xrightarrow{(\beta \rightarrow 0)} \pi\alpha / \beta$$

$$C_{\text{neutral}} = 1$$

in point-like approx

$e^+e^- \rightarrow B\bar{B}$

Sachs form factors

$$G_E = F_1 + \frac{q^2}{4M^2} F_2$$

$$G_M = F_1 + F_2$$

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-- formulae & definitions --

Born cross section:

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$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4m_{B\bar{B}}^2} \left[(1 + \cos^2 \theta) |G_M(m_{B\bar{B}})|^2 + \frac{1}{\tau} \sin^2 \theta |G_E(m_{B\bar{B}})|^2 \right]$$

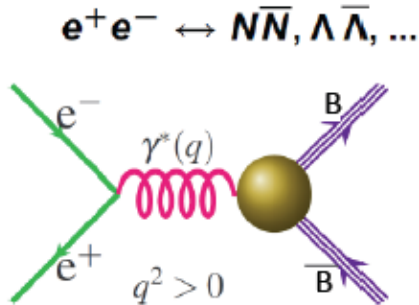
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in point-like approx



integrated cross section:

$$\sigma_{e\bar{e}}(m_{e\bar{e}}) = \frac{4\pi\alpha^2\beta C}{3m^2} \left[|G_M(m_{e\bar{e}})|^2 + \frac{1}{2\tau} |G_E(m_{e\bar{e}})|^2 \right] = \frac{4\pi\alpha^2\beta C}{3m^2} |G_{\text{eff}}(m_{e\bar{e}})|^2 (1 + 1/2\tau)$$

"effective" form factor

$e^+e^- \rightarrow B\bar{B}$

Sachs form factors

$$G_E = F_1 + \frac{q^2}{4M^2} F_2$$

$$G_M = F_1 + F_2$$

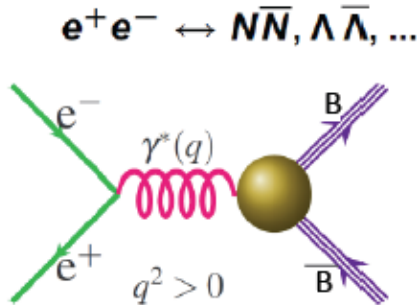
$$G_E(0) = Q_N$$

$$G_M(0) = \mu_N$$

-- formulae & definitions --

Born cross section:

time-like "Sachs" form-factors



$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4m_{B\bar{B}}^2} \left[(1 + \cos^2 \theta) |G_M(m_{B\bar{B}})|^2 + \frac{1}{\tau} \sin^2 \theta |G_E(m_{B\bar{B}})|^2 \right]$$

$$\tau = \frac{m_{B\bar{B}}^2}{4M_B^2} \quad \beta = \sqrt{1 - \frac{1}{\tau}}$$

Coulomb enhancement factor

$$C_{\text{charged}} = \frac{\pi\alpha / \beta}{1 - \exp(-\pi\alpha / \beta)} \xrightarrow{(\beta \rightarrow 0)} \pi\alpha / \beta$$

$$C_{\text{neutral}} = 1$$

in point-like approx

integrated cross section:

$$\sigma_{e\bar{e}}(m_{e\bar{e}}) = \frac{4\pi\alpha^2\beta C}{3m^2} \left[|G_M(m_{e\bar{e}})|^2 + \frac{1}{2\tau} |G_E(m_{e\bar{e}})|^2 \right] = \frac{4\pi\alpha^2\beta C}{3m^2} |G_{\text{eff}}(m_{e\bar{e}})|^2 (1 + 1/2\tau)$$

"effective" form factor

effective form factor:

$$|G_{\text{eff}}|^2 = \frac{|G_M|^2 + \frac{1}{2\tau} |G_E|^2}{1 + \frac{1}{2\tau}} \sigma_{B\bar{B}}(m_{B\bar{B}}) \Rightarrow |G_{\text{eff}}| = \left(\frac{3m_{B\bar{B}}^2}{\pi\alpha^2\beta C (1 + \frac{1}{2\tau})} \right)^{\frac{1}{2}} \sqrt{\sigma_{B\bar{B}}}$$

$e^+e^- \rightarrow B\bar{B}$

Sachs form factors

$$G_E = F_1 + \frac{q^2}{4M^2} F_2$$

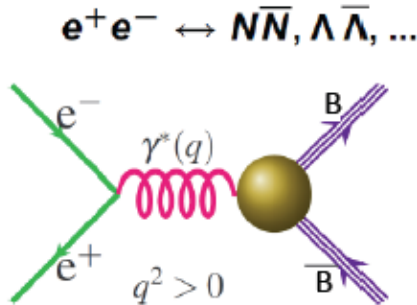
$$G_M = F_1 + F_2$$

$$G_E(0) = Q_N$$

$$G_M(0) = \mu_N$$

-- formulae & definitions --

Born cross section:



time-like "Sachs" form-factors

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4m_{B\bar{B}}^2} \left[(1 + \cos^2 \theta) |G_M(m_{B\bar{B}})|^2 + \frac{1}{\tau} \sin^2 \theta |G_E(m_{B\bar{B}})|^2 \right]$$

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$$C_{\text{charged}} = \frac{\pi\alpha / \beta}{1 - \exp(-\pi\alpha / \beta)} \xrightarrow{(\beta \rightarrow 0)} \pi\alpha / \beta$$

$$C_{\text{neutral}} = 1$$

in point-like approx

integrated cross section:

$$\sigma_{\text{int}}(m_{\text{int}}) = \frac{4\pi\alpha^2\beta C}{3m^2} \left[|G_M(m_{\text{int}})|^2 + \frac{1}{2\tau} |G_E(m_{\text{int}})|^2 \right] = \frac{4\pi\alpha^2\beta C}{3m^2} |G_{\text{eff}}(m_{\text{int}})|^2 (1 + 1/2\tau)$$

"effective" form factor

effective form factor:

$$|G_{\text{eff}}|^2 = \frac{|G_M|^2 + \frac{1}{2\tau} |G_E|^2}{1 + \frac{1}{2\tau}} \sigma_{B\bar{B}}(m_{B\bar{B}}) \Rightarrow |G_{\text{eff}}| = \left(\frac{3m_{B\bar{B}}^2}{\pi\alpha^2\beta C (1 + \frac{1}{2\tau})} \right)^{\frac{1}{2}} \sqrt{\sigma_{B\bar{B}}}$$

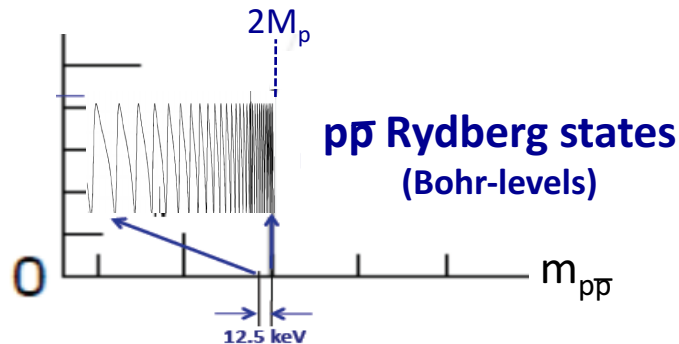
analyticity:

$$G_M(4M_B^2) = G_E(4M_B^2) \Rightarrow G_{\text{eff}}(4M_B^2) = G_M(4M_B^2)$$

$e^+e^- \rightarrow p\bar{p}$ at threshold

Integrated cross section:

$$\sigma_{p\bar{p}} = \frac{4\pi\alpha^2 \beta C}{3m^2} \left| G_{eff}(m_{p\bar{p}}) \right|^2 \left(1 + 1/2\tau \right)$$



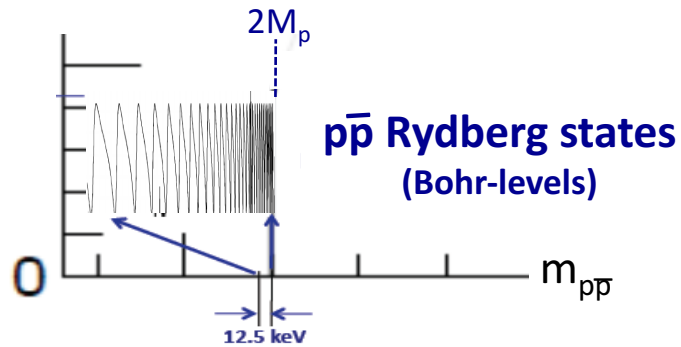
$$\text{for } p\bar{p}: C = \frac{\pi\alpha / \beta}{1 - \exp(-\pi\alpha / \beta)} \rightarrow \frac{\pi\alpha}{\beta}$$

Sommerfeld resummation factor

$e^+e^- \rightarrow p\bar{p}$ at threshold

Integrated cross section:

$$\sigma_{p\bar{p}} = \frac{4\pi\alpha^2 \beta C}{3m^2} \left| G_{eff}(m_{p\bar{p}}) \right|^2 \left(1 + 1/2\tau \right)$$



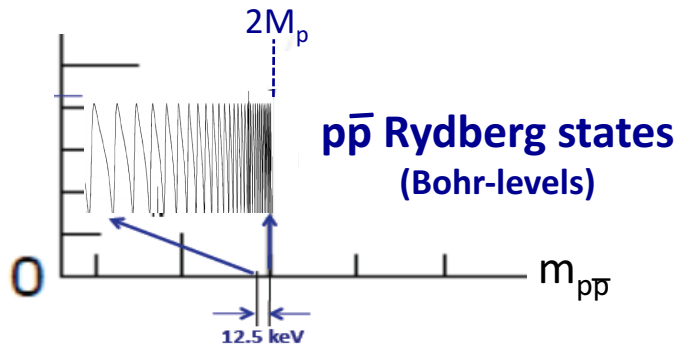
$$\text{for } p\bar{p}: C = \frac{\pi\alpha / \beta}{1 - \exp(-\pi\alpha / \beta)} \rightarrow \frac{\pi\alpha}{\beta}$$

Sommerfeld resummation factor

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Integrated cross section:

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$$\text{for } p\bar{p}: C = \frac{\pi\alpha / \beta}{1 - \exp(-\pi\alpha / \beta)} \rightarrow \frac{\pi\alpha}{\beta}$$

Sommerfeld resummation factor

in point-like approx:

$$\sigma_0 = \frac{\pi^2 \alpha^3}{2M_p^2} \left| G_{eff}(2M_p) \right|^2$$

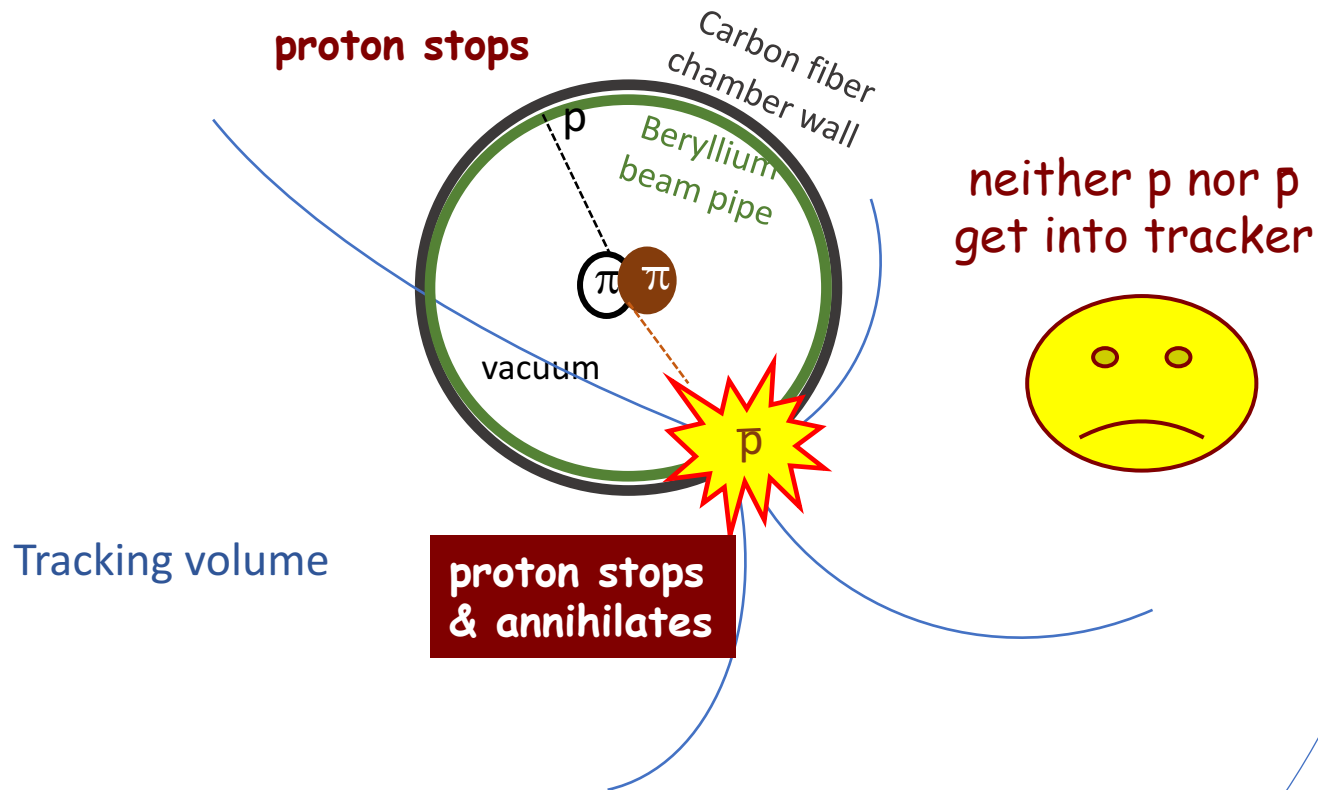
$$\approx 0.85 \text{ nb} \left| G_{eff}(2M_p) \right|^2 \rightarrow$$

The graph shows the cross section σ as a function of $m_{p\bar{p}} - 2M_p$. The curve starts at a non-zero value on the vertical axis and increases monotonically. The label $p\bar{p}$ is placed near the curve.

$e^+e^- \rightarrow p\bar{p}$ near threshold for $E_{\text{cm}} < 1.9 \text{ GeV}$

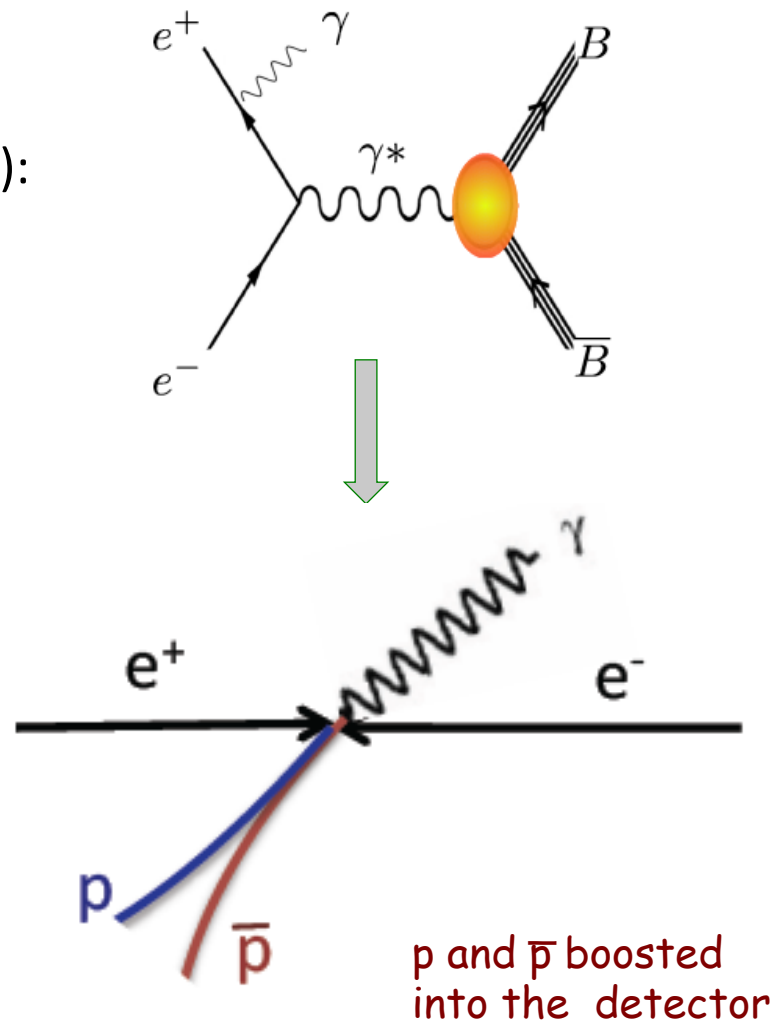
-- experimental issues --

$KE_p < 11 \text{ MeV}$
range $< 0.5 \text{ mm Be} + \text{C}$

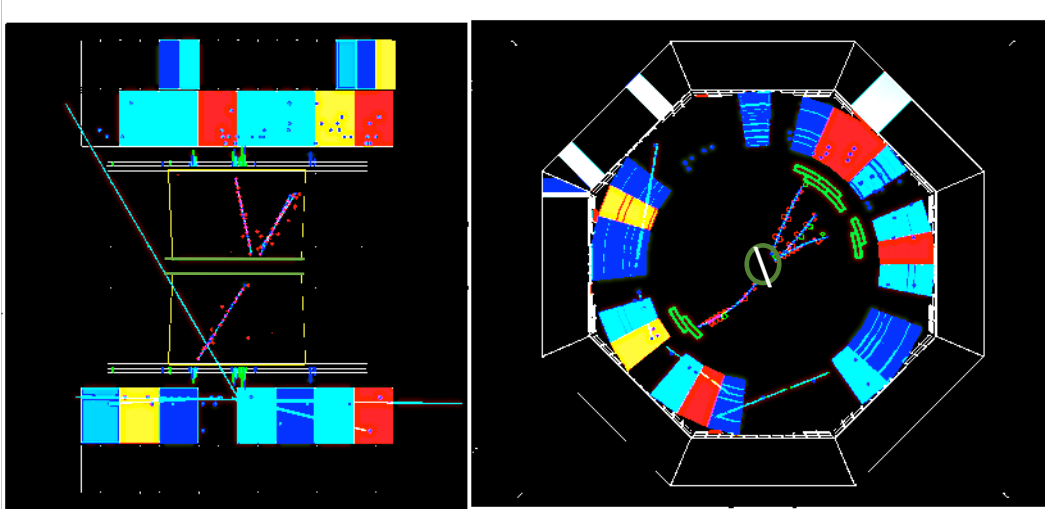


BaBar: produce boosted $p\bar{p}$ pairs via isr

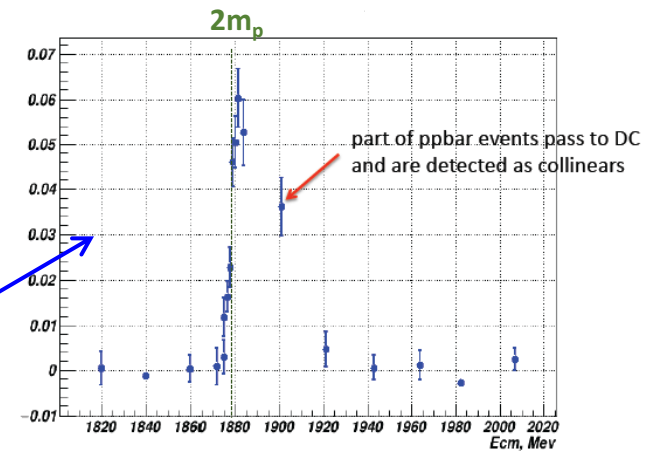
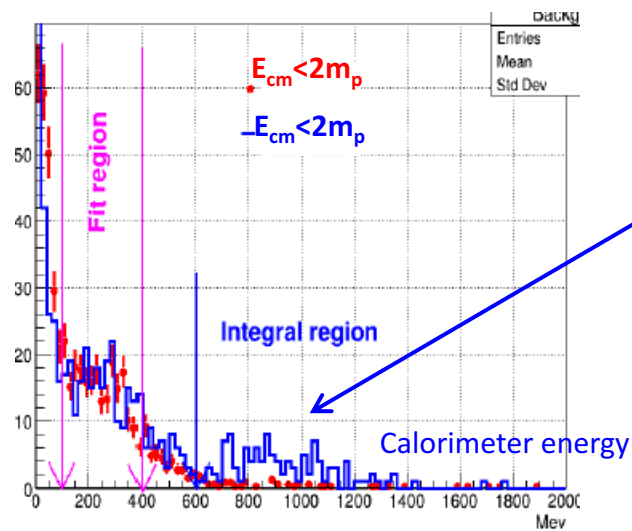
large angle initial state radiation (isr):



CMD3: Detect $\bar{p}$ annihilations in beam pipe



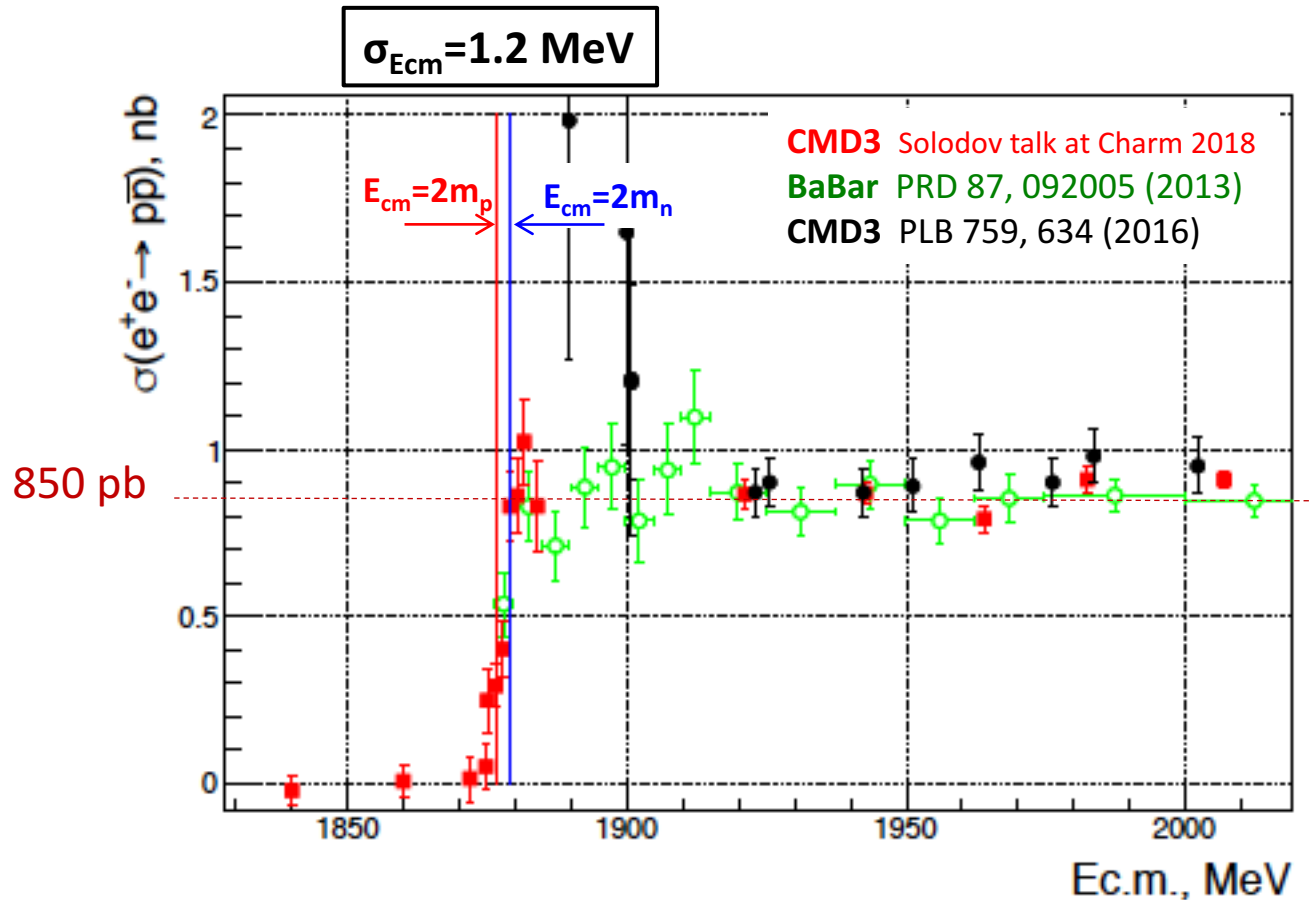
Solodov talk at Bad Honnef 2018



490 events have been found

$e^+e^- \rightarrow p\bar{p}$ at $E_{\text{cm}}=2m_p$ threshold

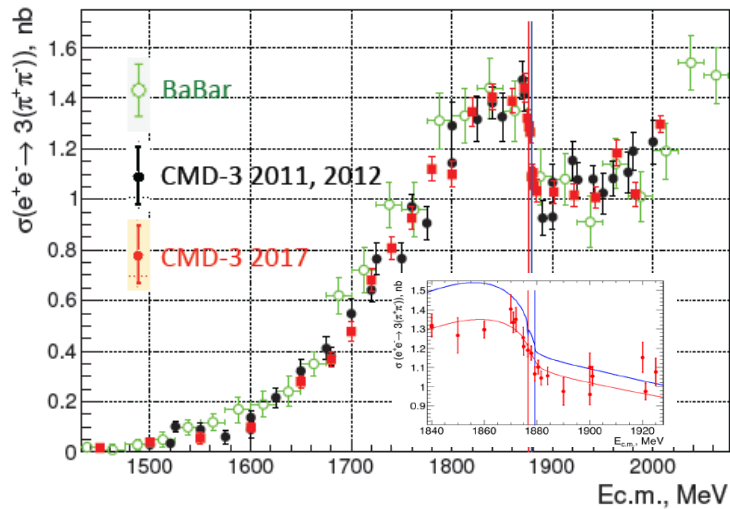
-- fast ($\delta E_{\text{cm}} \lesssim 1$ MeV) cross section jump at threshold --



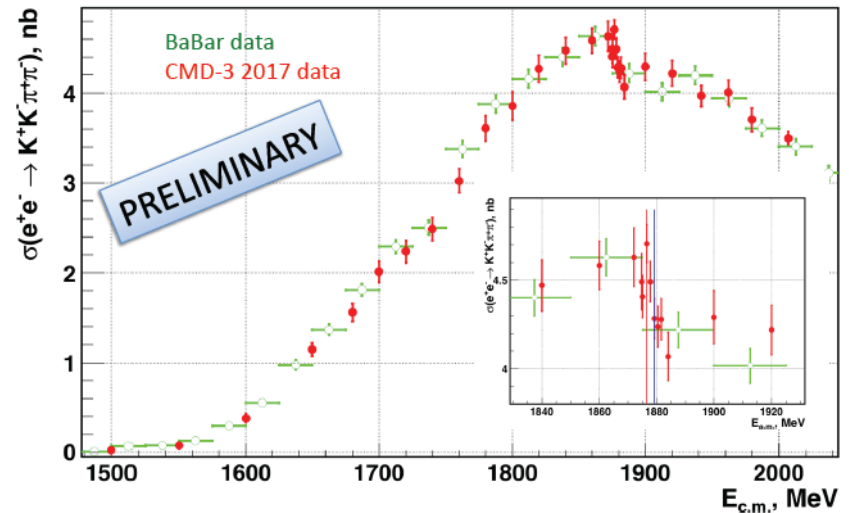
point-like approx. works well

look at other channels

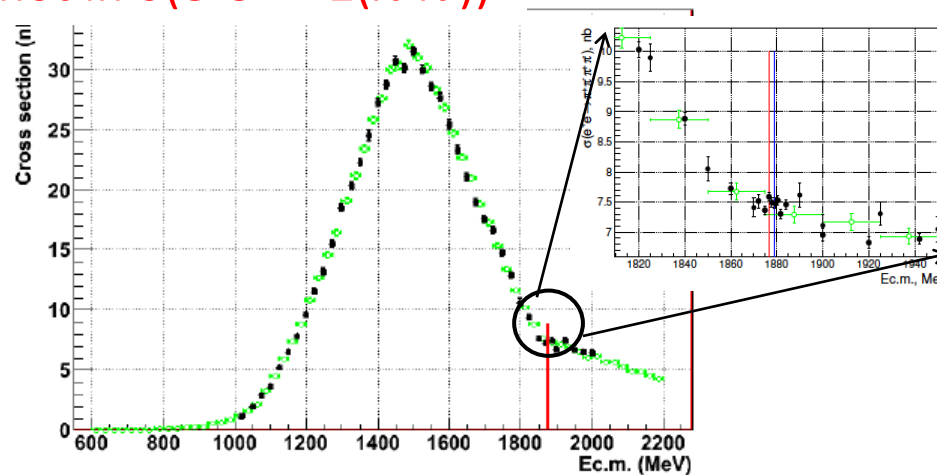
rapid dips in $\sigma(e^+e^- \rightarrow 3(\pi^+\pi^-))$



and $\sigma(e^+e^- \rightarrow K^+K^-\pi^+\pi^-)$

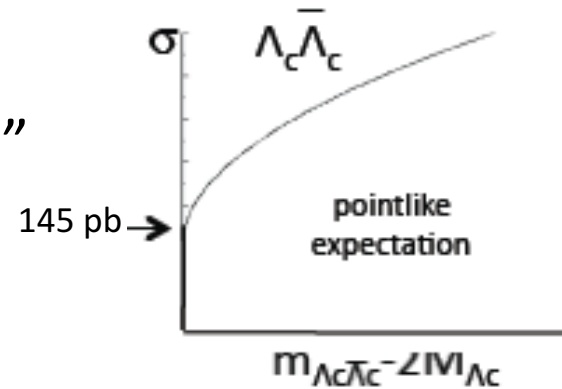


but not in $\sigma(e^+e^- \rightarrow 2(\pi^+\pi^-))$



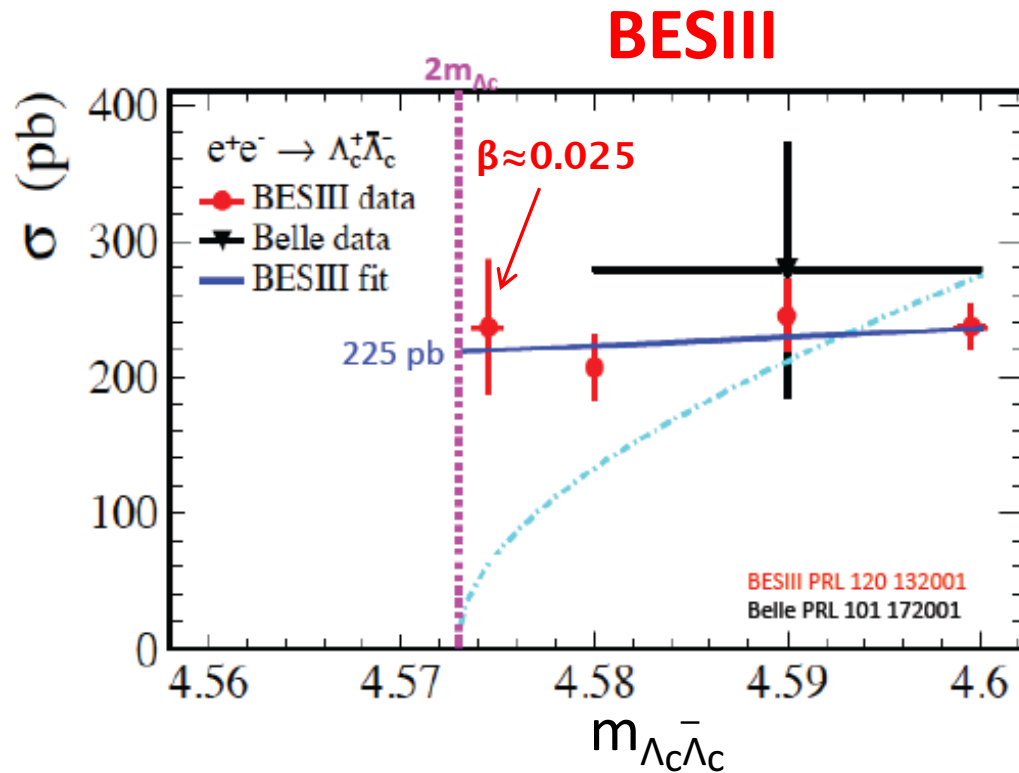
$$e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-$$

Λ_c is charged, expect $\approx 145\text{pb}$ “jump”
in point-like approximation

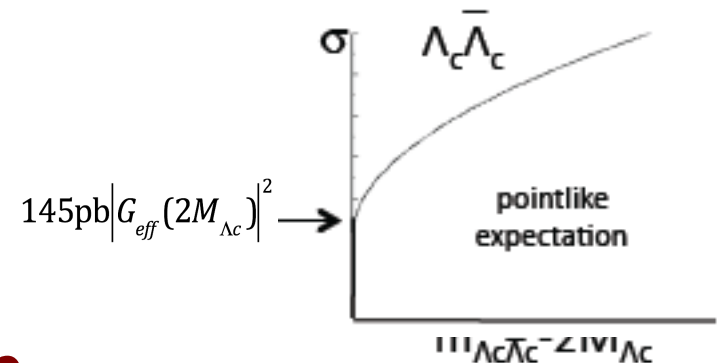


Λ_c is an Isospin singlet, no π -exchange
no Λ_c - Λ_c moleculelike states expected

$\sigma(e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-) @ \text{threshold}$



≈ 225 pb “jump” at threshold
 $\approx$ consistent with $\delta\sigma \approx 145$ pb
 $|G_{eff}|=1$ pointlike jump
 but $\approx$ flat after that (like pp)



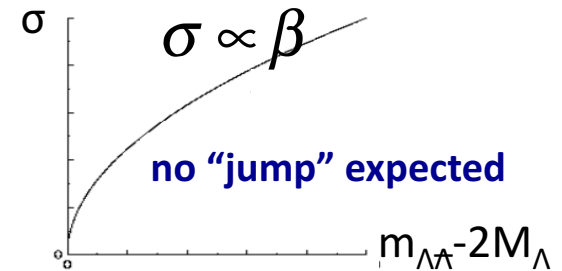
point-like approx. works here too

$$e^+e^- \rightarrow \Lambda\bar{\Lambda}$$

in point-like approx:

Electrically neutral $\rightarrow$ no Ryberg states

- no Coulomb enhancement

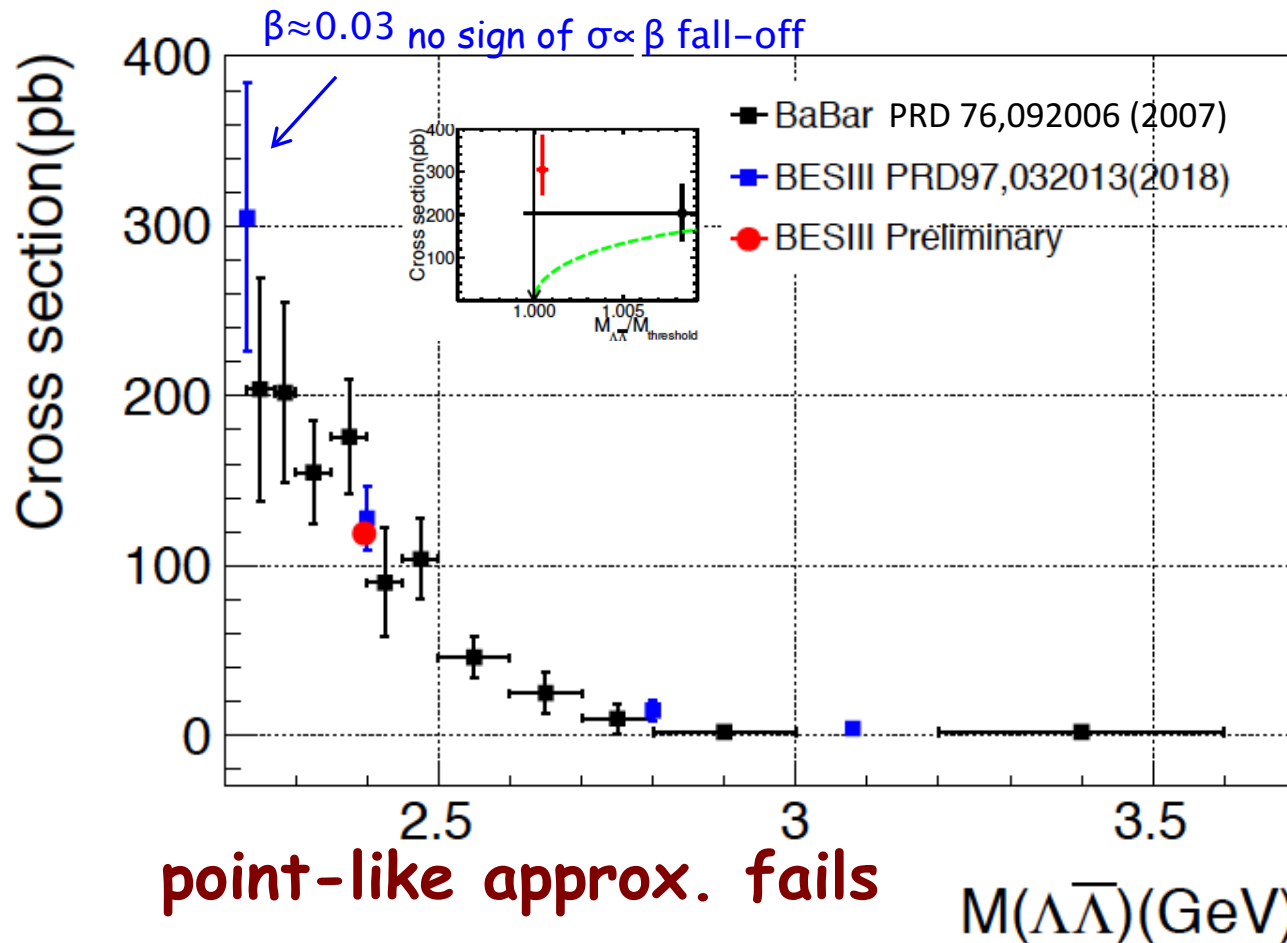


Isospin singlet, π -exchange not allowed

- $\Lambda\bar{\Lambda}$ molecule is unlikely

$\sigma(e^+e^- \rightarrow \Lambda\bar{\Lambda})$ at $E_{\text{cm}} \approx 2m_\Lambda$ threshold

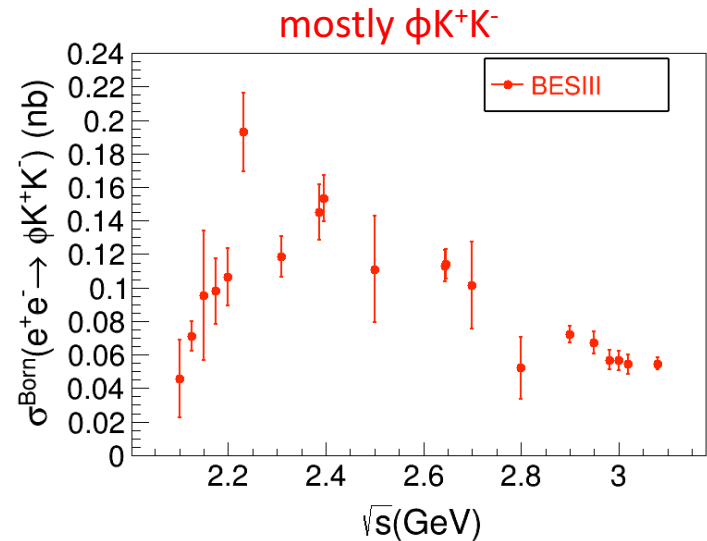
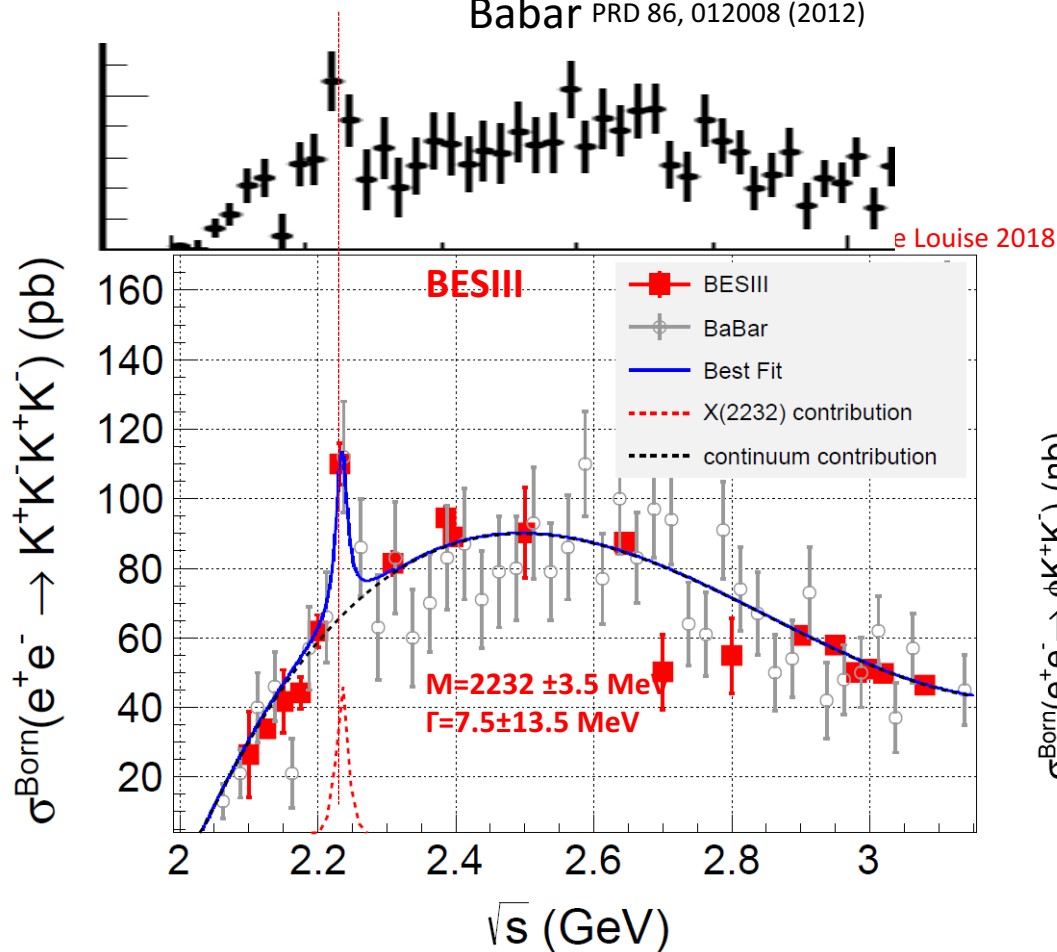
$$\sigma_{\Lambda\bar{\Lambda}}(m) = \frac{4\pi\alpha^2 \beta}{3m^2} |G_{\text{eff}}(m)|^2 \left(1 + \frac{1}{2\tau}\right)$$



$\sigma(e^+e^- \rightarrow K^+K^- K^+K^-)$ peak @ $2m_\Lambda$?

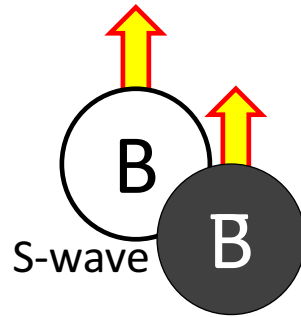
-- seen by both BaBar and BESIII --

Babar PRD 86, 012008 (2012)



baryonium?

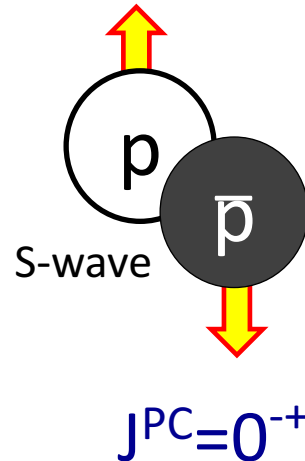
-- sub-threshold $B\bar{B}$ QCD S-wave bound states --



$$J^{PC}=1^{--}$$

$$e^+e^- \rightarrow B\bar{B}$$

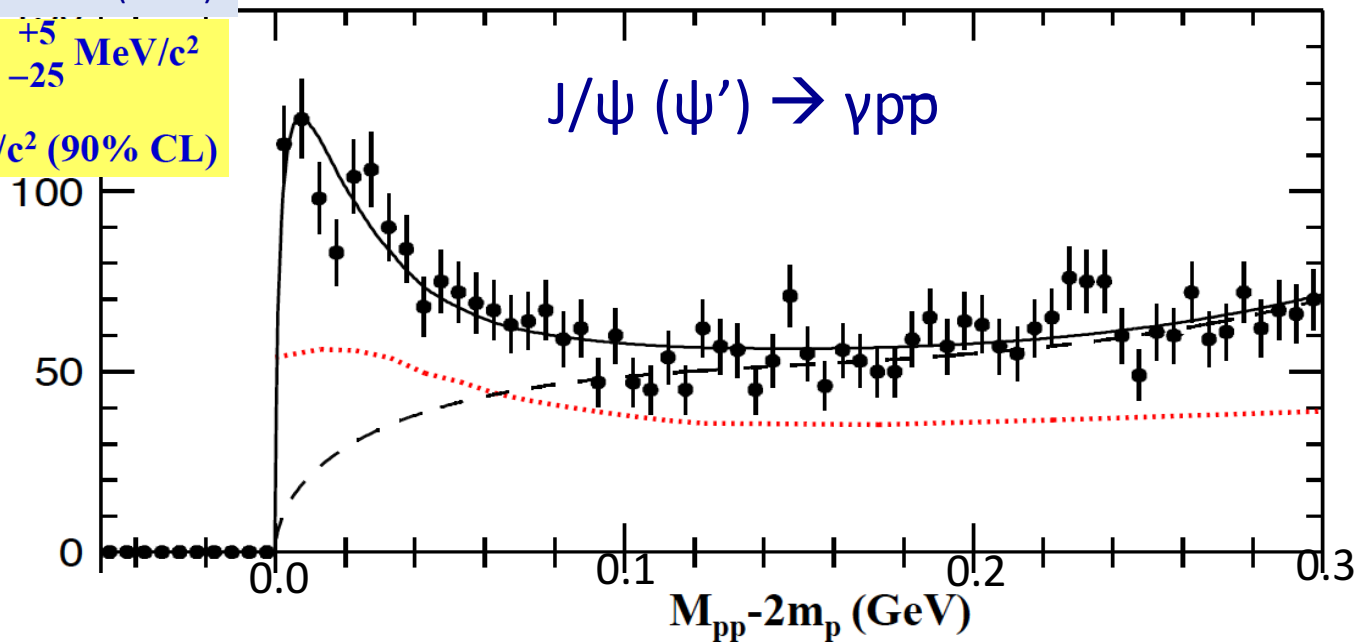
a 0^{-+} $p\bar{p}$ bound state is well established



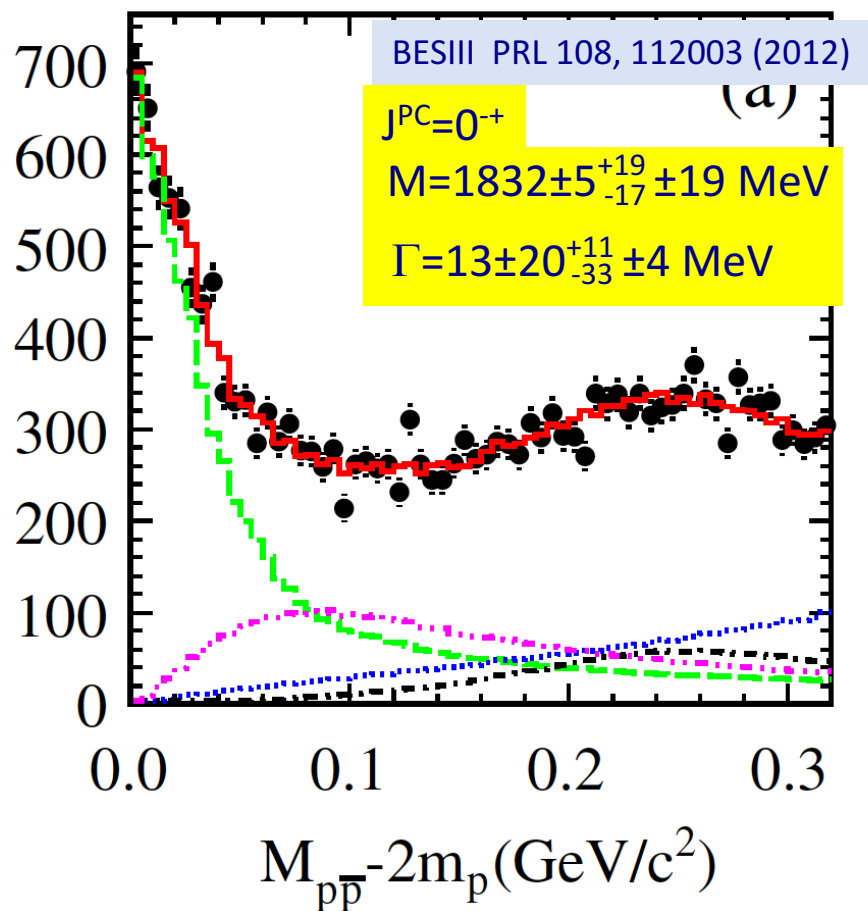
BESII PRL 91, 02001 (2003)

$M=1859^{+3+5}_{-10-25} \text{ MeV}/c^2$

$\Gamma < 30 \text{ MeV}/c^2$ (90% CL)

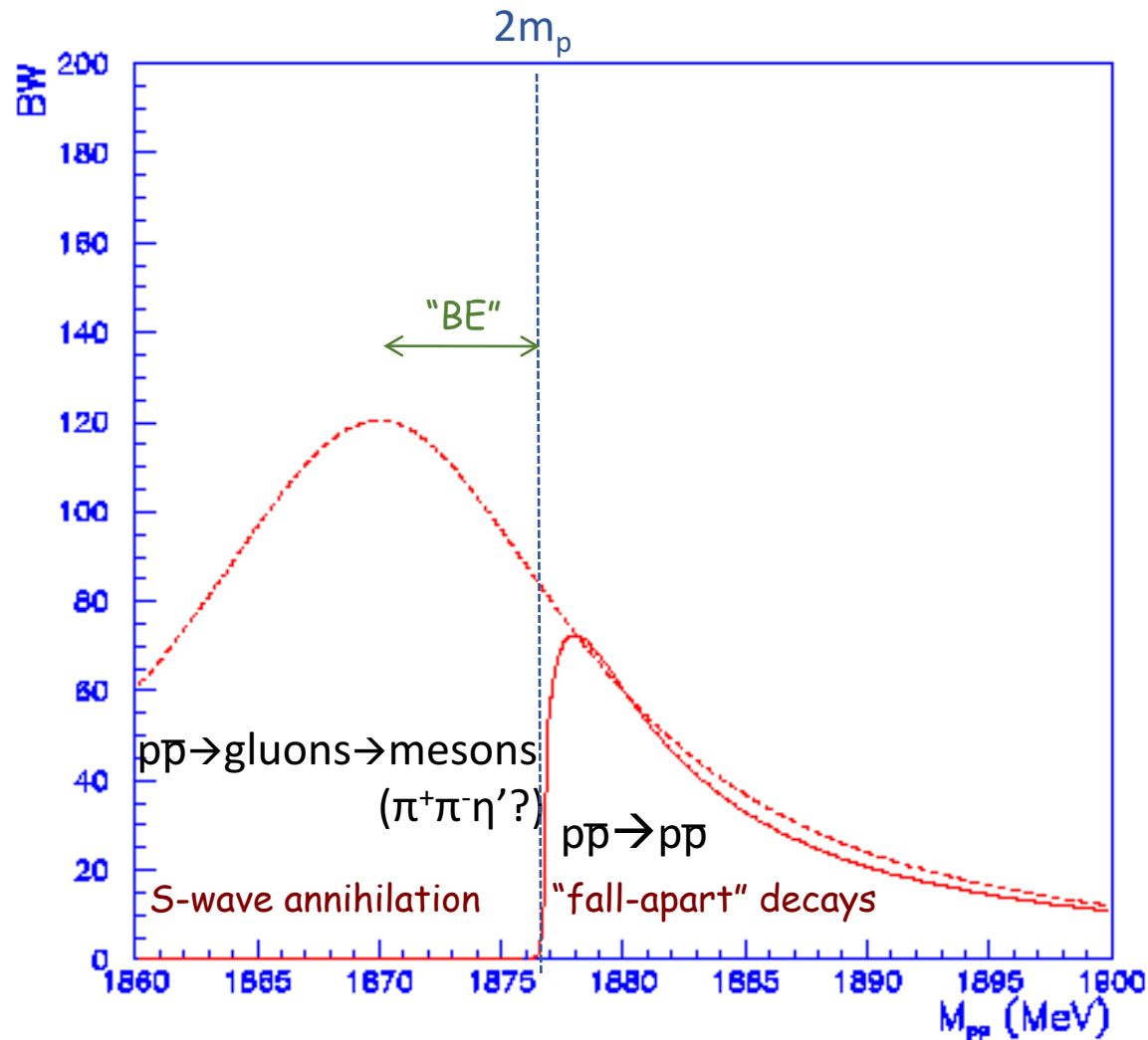


$J/\psi \rightarrow \gamma p \bar{p}$ at BESIII (PWA)



FSI included: A. Sibirtsev et al, PRD71, 054010 (2005)

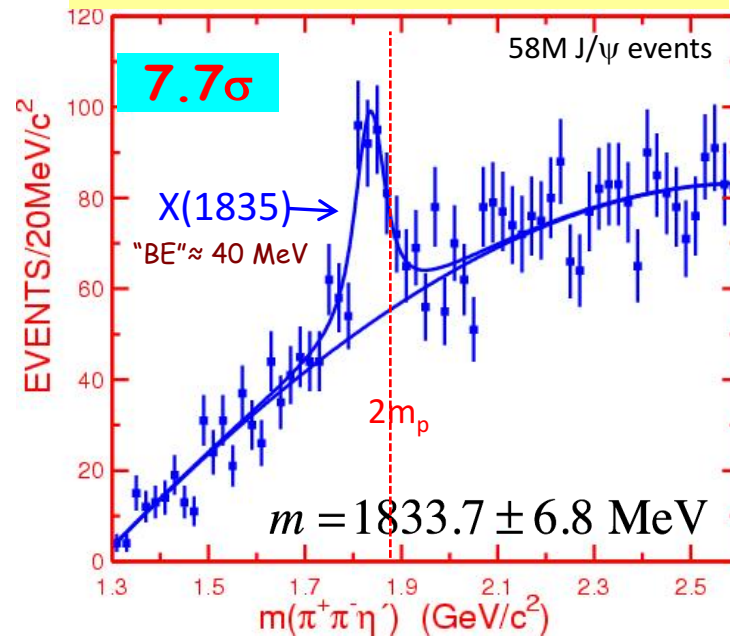
“protononium:” a $p\bar{p}$ bound state?



$X(1835) \rightarrow \pi^+ \pi^- \eta'$ with 58M J/ψ decays (BESII)

BESII observation of $X(1835)$ in

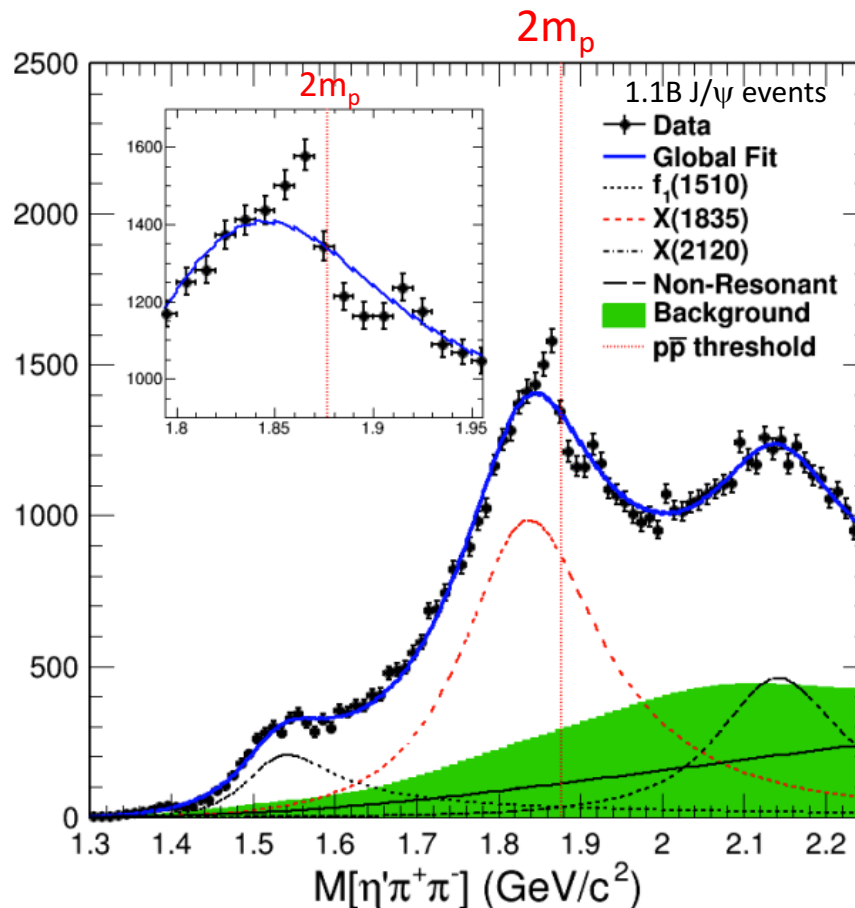
$$J/\psi \rightarrow \gamma \pi^+ \pi^- \eta'$$



BESII PRL 95, 262001 (2005)

$X(1835) \rightarrow \pi^+ \pi^- \eta'$ with 1.1B J/ψ decays (BESIII)

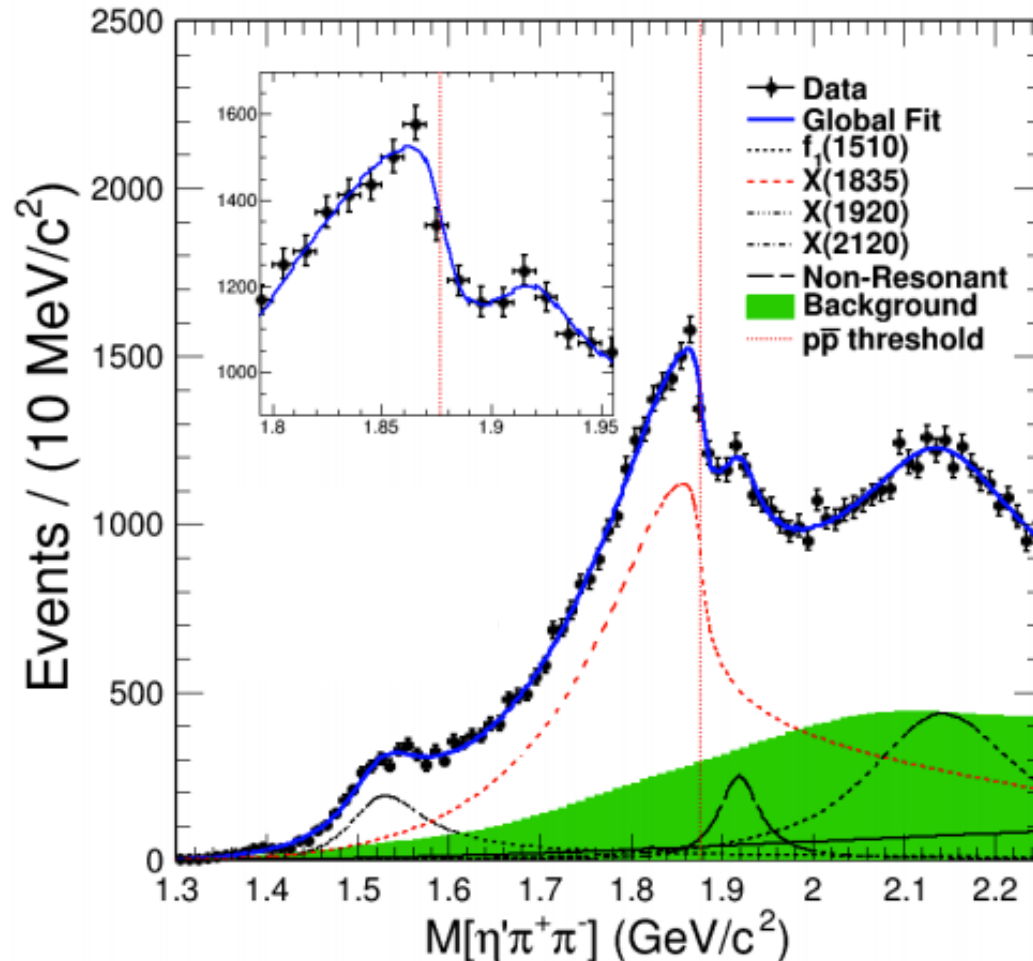
$$J/\psi \rightarrow \gamma \pi^+ \pi^- \eta'$$



Flatté formula fit:

$$T = \frac{\sqrt{\rho_{out}}}{\mathcal{M}^2 - s - i \sum_k g_k^2 \rho_k}, \quad \sum_k g_k^2 \rho_k \simeq g_0^2 (\rho_0 + \frac{g_{p\bar{p}}^2}{g_0^2} \rho_{p\bar{p}})$$

S.M. Flatté PLB 63, 224 (1976)



Fit results:

$$\frac{g_{p\bar{p}}^2}{g_0^2} = 2.31 \pm 0.37$$

X coupling to $p\bar{p}$

X coupling to everything else

summary

Cross section threshold jumps see for $e^+e^- \rightarrow B\bar{B}$

- both for charged ($p\bar{p}$ & $\Lambda_c\bar{\Lambda}_c$) and neutral ($n\bar{n}$ & $\Lambda\bar{\Lambda}$) pairs
- jump times < 1 ns (much faster than phase space)
- consistent with expectations for pointlike, **charged** particles
- above threshold behavior is decidedly non-pointlike

Accompanying structures seen in other channels

- dips in $\sigma(e^+e^- \rightarrow 3(\pi^+\pi^-) \text{ & } K^+K^-\pi^+\pi^-)$ at $E_{\text{cm}}=2m_p$ (but not $2(\pi^+\pi^-)$)
- peak in $e^+e^- \rightarrow \varphi K^+K^-$ at $E_{\text{cm}}=2m_\Lambda$

A subthreshold 0^{++} $p\bar{p}$ state seen in $J/\psi \rightarrow \gamma p\bar{p}$

- associated structure seen in $e^+e^- \rightarrow \pi^+\pi^-\eta'$

More results expected soon

- $e^+e^- \rightarrow \Sigma\bar{\Sigma}$ and $\Xi\bar{\Xi}$ at threshold from BESIII
- more $e^+e^- \rightarrow p\bar{p}$ and $n\bar{n}$ from CMDS, SND & BESIII

**There is lots still to be learned about
the "well known" stable baryons**

Thank You

どうも ありがとう

謝謝

감사합니다